Pollack in ICES Divisions 89a

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Background information

Pollack.27.89a is a stock in ICES Category 5. Currently, the management advice is based on commercial landings.

Pollack is a bentopelagic species. Main commercial fleets included gillnetters and longliners from France (80% landings) and gillnetters and longliners from Spain (17% landings). Recreational landings are supposed to be high (at the same level as commercial landings, they have been estimated.

Available data

- 1. Annual commercial landings (in tonnes): 1986-2018.
- 2. Abundance Index "France gillneters mesh > 90 mm, operating in div 8a, 2nd semester" (tonnes/fishing sequence): 2005-2018.

Fitting SPICT model

Starting session and download libraries

```
# Package from github: devtools::install_github('mawp/spict/spict')
# library(remotes) install_github('DTUAqua/spict/spict')

rm(list = ls(all = TRUE))

# Download libraries
library(spict)
library(icesAdvice)
library(ellipse)
library(formatR)
```

Creating data object

```
# Catch data: Only Commercial Landings. *Year 1999: mean of 1998 and 2000 as

# French landings were missing

pol89aC <- data.frame(obsC = c(2806, 2918, 2582, 1973, 1900, 2168, 1958, 1513, 1955,

1679, 1354, 1378, 1165, 1322, 1479, 1746, 1972, 1663, 1726, 1986, 2126, 1847,
```

```
2313, 1812, 1682, 2032, 1520, 1811, 1959, 1610, 1661, 1481, 1512), timeC = 1986:2018)

# Index data: Commercial index FR-GNS>90mm-8a-2s (tonnes/fishing sequence)

pol89aI <- data.frame(obsI = c(0.1151, 0.0663, 0.1292, 0.1289, 0.1244, 0.1079, 0.1966, 0.1743, 0.1565, 0.15, 0.1438, 0.1205, 0.1222, 0.1117), timeI = c(2005:2018) + 0.5)

# Create a list for input data

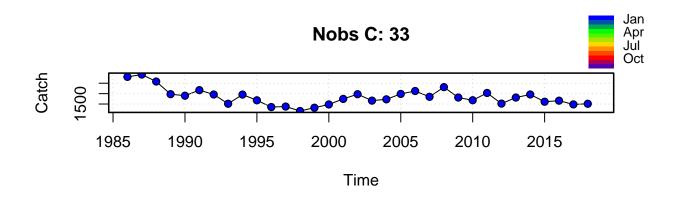
pol89a <- list(timeC = pol89aC$timeC, obsC = pol89aC$obsC, timeI = list(pol89aI$timeI), obsI = list(pol89aI$obsI))

# Check list

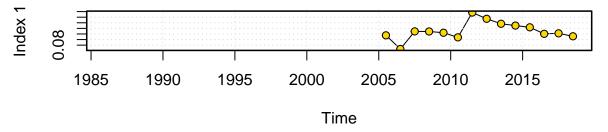
pol89a <- check.inp(pol89a)
```

Plot Raw data:

plotspict.data(pol89a)



Nobs I: 14



spict_v1.2.8@d9ece0a31623f1a26d3cb4328499f16136822d14

Figure 1: Raw data

To highlight:

- Catch and abundance series are overlapped only for a short period of time (14 years).
- There is not contrast in catch series during 2005-2018.

plotspict.ci(pol89a)

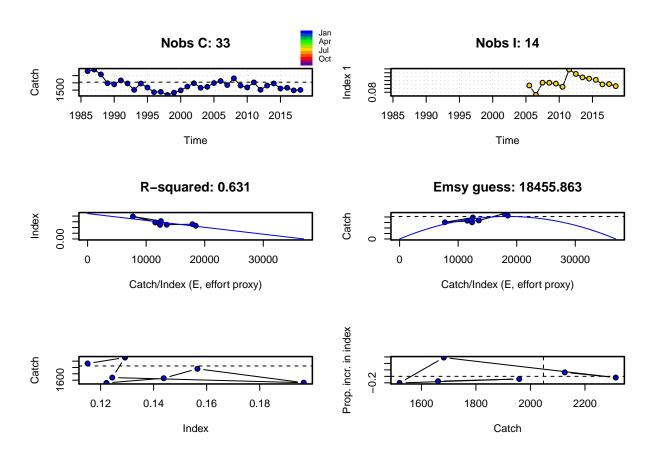


Figure 2: Fitting linear regression

Model Fitting

Run 1. Default priors and all parameters estimated

Not converged. Model did not obtain proper convergence!

```
res_pol89aDefault <- fit.spict(pol89a)
```

Run 2. Shorten Catch series to 2005-2018, overlapping with abundance index.

Not converged. Shorten series gave totally unrealistic estimates, testing different configurations:

```
pol89aShorten = shorten.inp(pol89a, 2005, 2018)
res_pol89aShorten <- fit.spict(pol89aShorten)</pre>
```

Run 3. Fix parameter to Schaefer production curve (initial parameter). Symmetric productive curve (BMSY/K=0.5)

No converged:

Fmsys

0.3552445

 ${\tt NaN}$

```
pol89aSchaefer <- pol89a
pol89aSchaefer$ini$logn <- log(2)
pol89aSchaefer$phases$logn <- -1
res_pol89aSchaefer <- fit.spict(pol89aSchaefer)
res_pol89aSchaefer
## Convergence: 1 MSG: false convergence (8)
## WARNING: Model did not obtain proper convergence! Estimates and uncertainties are most likely invali-
## Gradient at current parameter vector
##
                      logK
                                           logsdb
                                                       logsdf
                                                                   logsdi
                                                                              logsdc
          logm
                                  logq
                                                                            14537482
##
     243530990 -114100200 -103330547
                                        -45350665
                                                      3185902
                                                                 19201573
##
## Objective function: -4.8534143
## Euler time step (years): 1/16 or 0.0625
## Nobs C: 33, Nobs I1: 14
##
## Priors
##
        logn \sim dnorm[log(2), 2^2]
##
    logalpha ~
                 dnorm[log(1), 2^2]
     logbeta ~ dnorm[log(1), 2^2]
##
##
## Fixed parameters
##
      fixed.value
##
##
## Model parameter estimates w 95% CI
##
                             cilow
                                                   log.est
               estimate
                                        ciupp
##
    alpha 1.724414e+00 1.5535251 1.9141018
                                                0.5448875
##
    beta
           8.661552e-01 0.7702417 0.9740122 -0.1436912
##
   r
           7.180673e-01
                               NaN
                                          NaN -0.3311920
##
   rc
           7.180673e-01
                               {\tt NaN}
                                          {\tt NaN}
                                               -0.3311920
##
    rold
           7.180673e-01
                               {\tt NaN}
                                          {\tt NaN}
                                               -0.3311920
##
           2.065420e+03
                               {\tt NaN}
                                          {\tt NaN}
   m
                                                7.6330889
##
   K
           1.150544e+04
                               {\tt NaN}
                                          NaN
                                                9.3505753
           1.590000e-05
##
                               {\tt NaN}
                                          NaN -11.0479791
   q
##
    sdb
           1.261693e-01
                               \mathtt{NaN}
                                          {\tt NaN}
                                               -2.0701308
           8.675190e-02 0.0858679 0.0876449 -2.4447030
##
    sdf
##
    sdi
           2.175681e-01 0.2011795 0.2352918 -1.5252433
           7.514060e-02 0.0674759 0.0836760 -2.5883942
##
    sdc
##
##
  Deterministic reference points (Drp)
##
              estimate cilow ciupp
                                       log.est
    Bmsyd 5752.7201188
                                NaN 8.657428
##
                          \mathtt{NaN}
##
    Fmsyd
             0.3590336
                          {\tt NaN}
                                NaN -1.024339
  MSYd 2065.4199636
                                NaN 7.633089
##
                          {\tt NaN}
## Stochastic reference points (Srp)
##
              estimate cilow ciupp
                                       log.est rel.diff.Drp
## Bmsys 5657.9991900 NaN
                                NaN 8.640826 -0.01674106
```

NaN -1.034949 -0.01066625

```
MSYs 2009.6139816
                         NaN
                               NaN 7.605698 -0.02776950
##
## States w 95% CI (inp$msytype: s)
##
                       estimate
                                       cilow
                                                    ciupp
                                                              log.est
##
   B 2018.50
                   7701.8620853 6427.3964547 9229.0369824
                                                           8.9492174
  F 2018.50
##
                      0.1958824
                                   0.1600968
                                                0.2396669 -1.6302408
   B 2018.50/Bmsy
                      1.3612342
                                   1.0824193
                                                1.7118677 0.3083918
##
   F_2018.50/Fmsy
                      0.5514017
                                   0.4300376
                                                0.7070168 -0.5952918
##
## Predictions w 95% CI (inp$msytype: s)
                     prediction
                                       cilow
                                                    ciupp
                                                              log.est
  B_2019.00
                   7817.7345592 6338.2962452 9642.4924420
##
                                                           8.9641501
##
  F_2019.00
                                                0.2456922 -1.6303410
                      0.1958628
                                   0.1561393
## B_2019.00/Bmsy
                      1.3817136
                                   1.0757361
                                                1.7747220 0.3233245
## F_2019.00/Fmsy
                      0.5513464
                                   0.4213261
                                                0.7214908 -0.5953919
## Catch_2019.00
                  1547.7675977 1219.5329747 1964.3458489
                                                           7.3445689
## E(B_inf)
                   8075.9135370
                                          NA
                                                        NA 8.9966413
```

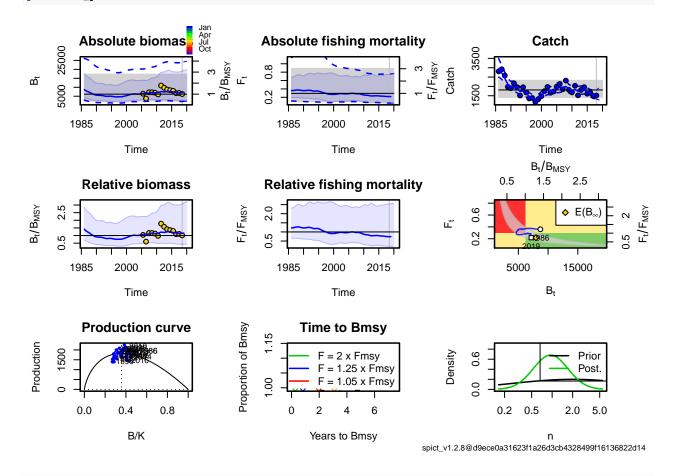
Run 4. Set priors for the ratio between biomass in the initial year relative to K, mean of log(0.5) and sd of 0.2

```
pol89aBkfrac <- pol89a
pol89aBkfracpriors logbkfrac \leftarrow c(log(0.5), 0.2, 1)
res_pol89aBkfrac <- fit.spict(pol89aBkfrac)</pre>
res_pol89aBkfrac
## Convergence: 0 MSG: relative convergence (4)
## Objective function at optimum: -4.5509311
## Euler time step (years): 1/16 or 0.0625
## Nobs C: 33, Nobs I1: 14
##
## Priors
##
                  dnorm[log(2), 2^2]
         logn
##
                  dnorm[log(1), 2^2]
     logalpha
##
      logbeta
                  dnorm[log(1), 2^2]
##
                  dnorm[log(0.5), 0.2^2]
    logbkfrac
##
## Model parameter estimates w 95% CI
##
               estimate
                                cilow
                                                       log.est
                                             ciupp
##
    alpha 2.697054e+00
                           0.7705388 9.440279e+00
                                                     0.9921602
##
    beta
           1.234193e+00
                           0.2062127 7.386703e+00
                                                     0.2104172
##
    r
           2.788867e-01
                           0.0617423 1.259716e+00
                                                    -1.2769498
##
           5.878453e-01
                           0.1943692 1.777865e+00
                                                    -0.5312914
    rc
##
    rold
           5.451653e+00
                           0.0000000 2.726796e+10
                                                     1.6959189
##
           1.823525e+03 1418.6280869 2.343986e+03
                                                     7.5085269
   m
##
   K
           1.731712e+04 6004.6937680 4.994137e+04
                                                     9.7594509
##
           1.790000e-05
                           0.0000057 5.610000e-05 -10.9286187
   q
##
           9.488437e-01
                           0.3013288 2.987780e+00
                                                    -0.0525112
                           0.0301167 2.419125e-01
                                                    -2.4609280
##
  sdb
           8.535570e-02
##
    sdf
           7.710060e-02
                           0.0164420 3.615431e-01
                                                    -2.5626445
##
  sdi
           2.302090e-01
                           0.1398924 3.788352e-01
                                                    -1.4687678
           9.515700e-02
                           0.0604641 1.497558e-01 -2.3522273
##
    sdc
##
```

```
## Deterministic reference points (Drp)
##
             estimate
                             cilow
                                          ciupp
                                                  log.est
   Bmsyd 6204.0989196 2202.4784482 1.747615e+04 8.732966
            0.2939227
                        0.0971846 8.889323e-01 -1.224439
   MSYd 1823.5252595 1418.6280869 2.343986e+03 7.508527
## Stochastic reference points (Srp)
             estimate
                            cilow
                                         ciupp
                                                 log.est rel.diff.Drp
##
   Bmsys 6159.4267006 2187.651388 1.734213e+04 8.725739 -0.0072526586
                       0.097157 8.897324e-01 -1.224131 0.0003076041
##
            0.2940131
   MSYs 1810.9559985 1410.495313 2.325113e+03 7.501610 -0.0069406772
##
## States w 95% CI (inp$msytype: s)
##
                       estimate
                                      cilow
                                                   ciupp
                                                            log.est
  B_2018.50
##
                   7053.0819195 2077.6339581 2.394357e+04 8.8612200
## F_2018.50
                                  0.0627155 7.566943e-01 -1.5239715
                     0.2178450
   B_2018.50/Bmsy
                     1.1450874
                                  0.4284152 3.060641e+00 0.1354810
                                  0.2165474 2.535181e+00 -0.2998405
##
  F_2018.50/Fmsy
                     0.7409364
##
## Predictions w 95% CI (inp$msytype: s)
##
                    prediction
                                      cilow
                                                   ciupp
                                                            log.est
## B 2019.00
                  7159.6995777 2122.3017467 2.415363e+04 8.8762233
## F 2019.00
                                  0.0623706 7.589069e-01 -1.5252689
                     0.2175625
## B_2019.00/Bmsy
                                  0.4323251 3.125349e+00 0.1504843
                     1.1623971
                                  0.2151627 2.544884e+00 -0.3011379
## F 2019.00/Fmsy
                     0.7399758
## Catch 2019.00 1578.5293427 1271.2707568 1.960051e+03 7.3642489
  E(B inf)
                  7964.4879541
                                         NA
                                                      NA 8.9827479
# Summary of estimates
round(sumspict.parest(res pol89aBkfrac), 2)
                                 ciupp log.est
##
          estimate
                    cilow
## alpha
             2.70
                     0.77 9.440000e+00
                                          0.99
## beta
             1.23
                     0.21 7.390000e+00
                                          0.21
## r
             0.28
                     0.06 1.260000e+00
                                         -1.28
## rc
             0.59
                     0.19 1.780000e+00
                                         -0.53
## rold
             5.45
                     0.00 2.726796e+10
                                          1.70
## m
         1823.53 1418.63 2.343990e+03
                                          7.51
## K
         17317.12 6004.69 4.994137e+04
                                          9.76
## q
             0.00
                     0.00 0.000000e+00 -10.93
             0.95
## n
                     0.30 2.990000e+00
                                        -0.05
## sdb
             0.09
                     0.03 2.400000e-01
                                         -2.46
## sdf
             0.08
                     0.02 3.600000e-01
                                         -2.56
## sdi
             0.23
                     0.14 3.800000e-01
                                         -1.47
## sdc
             0.10
                     0.06 1.500000e-01
                                         -2.35
# Reference points
sumspict.drefpoints(res_pol89aBkfrac)
            estimate
                            cilow
                                         ciupp
                                                 log.est
## Bmsyd 6204.0989196 2202.4784482 1.747615e+04 8.732965
## Fmsvd
            0.2939227
                        0.0971846 8.889323e-01 -1.224439
## MSYd 1823.5252595 1418.6280869 2.343986e+03 7.508527
```

Basic plotting of the results

plot(res_pol89aBkfrac)



Convergence checks

Convergence

res_pol89aBkfrac\$opt\$convergence

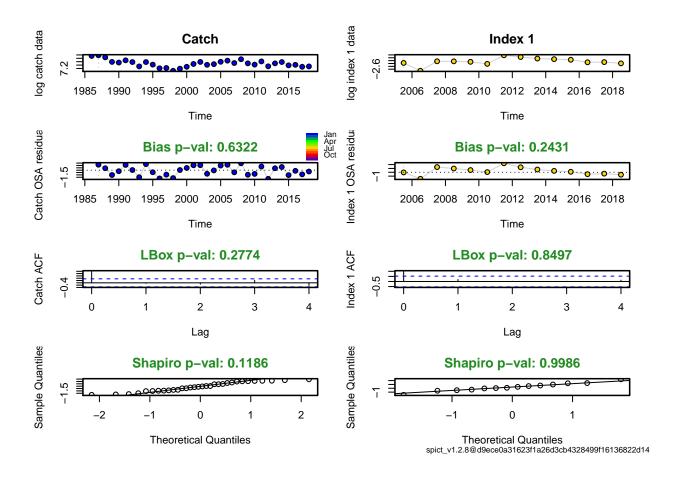
[1] 0

All the sd were estimated

all(is.finite(res_pol89aBkfrac\$sd))

[1] TRUE

No violation of assumptions: bias, correlation and normality:
res_pol89aBkfrac <- calc.osa.resid(res_pol89aBkfrac)
plotspict.diagnostic(res_pol89aBkfrac)</pre>



Retrospective: no trends and all runs inside the confidence intervals

Problems of convergence:

```
rep <- retro(res_pol89aBkfrac, nretroyear = 5)

## Error in calc.osa.resid(rep) :
## Could not calculate OSA residuals because estimation did not converge.</pre>
```

Run 5:

- \bullet Fix parameter to Schaefer production curve (initial parameter). Symmetric productive curve (BMSY/K=0.5)
- Set priors for the ratio between biomass in the initial year relative to K, mean of log(0.5) and sd of 0.2

```
pol89aSchaefBkfrac <- pol89a
# Set priors for B/K
pol89aSchaefBkfrac$priors$logbkfrac <- c(log(0.5), 0.2, 1)
# Fixing n at 2
pol89aSchaefBkfrac$ini$logn <- log(2)
pol89aSchaefBkfrac$phases$logn <- -1
# Fit the model</pre>
```

```
res_pol89aSchaefBkfrac <- fit.spict(pol89aSchaefBkfrac)

# Results
res_pol89aSchaefBkfrac

## Convergence: 0 MSG: relative convergence (4)

## Objective function at entirem, -4 0203638
```

```
## Objective function at optimum: -4.0203638
## Euler time step (years): 1/16 or 0.0625
## Nobs C: 33, Nobs I1: 14
##
## Priors
         logn ~ dnorm[log(2), 2^2]
##
##
     logalpha ~
                  dnorm[log(1), 2^2]
##
      logbeta ~
                  dnorm[log(1), 2^2]
   logbkfrac ~
                  dnorm[log(0.5), 0.2^2]
##
##
## Fixed parameters
##
     fixed.value
##
##
## Model parameter estimates w 95% CI
##
               estimate
                               cilow
                                            ciupp
                                                      log.est
##
   alpha 2.812626e+00
                           0.7084745 1.116606e+01
                                                    1.0341187
##
   beta
           1.076296e+00
                           0.3701895 3.129247e+00
                                                    0.0735260
##
   r
           5.874390e-01
                           0.1286586 2.682171e+00
                                                  -0.5319829
           5.874390e-01
                           0.1286586 2.682171e+00
                                                   -0.5319829
##
##
   rold
           5.874390e-01
                           0.1286586 2.682171e+00
                                                   -0.5319829
##
           1.986494e+03 1581.8809432 2.494598e+03
                                                    7.5941264
           1.352647e+04 3354.5637616 5.454221e+04
##
                                                    9.5124036
##
           1.620000e-05
                           0.0000044 5.990000e-05 -11.0278153
   q
##
   sdb
           7.838730e-02
                           0.0245496 2.502915e-01
                                                   -2.5460940
##
   sdf
           8.671620e-02
                           0.0366904 2.049499e-01
                                                   -2.4451146
##
   sdi
           2.204741e-01
                           0.1376418 3.531544e-01 -1.5119753
##
   sdc
           9.333230e-02
                           0.0608191 1.432268e-01 -2.3715886
##
## Deterministic reference points (Drp)
##
              estimate
                              cilow
                                           ciupp
                                                   log.est
##
   Bmsyd 6763.2340197 1677.2818808 27271.107456 8.819256
   Fmsyd
##
             0.2937195
                          0.0643293
                                        1.341086 -1.225130
   MSYd 1986.4936495 1581.8809432 2494.597989
                                                  7.594126
## Stochastic reference points (Srp)
##
              estimate
                              cilow
                                           ciupp
                                                   log.est rel.diff.Drp
   Bmsys 6714.6367749 1668.7061176 27018.746166 8.812045 -0.007237509
##
   Fmsys
             0.2922289
                          0.0636834
                                        1.340974 -1.230218 -0.005100763
   MSYs 1962.1382732 1548.5980763 2486.110930 7.581790 -0.012412671
##
##
## States w 95% CI (inp$msytype: s)
##
                       estimate
                                                             log.est
                                       cilow
                                                    ciupp
  B_2018.50
##
                   8139.8643740 2369.9006831 2.795788e+04 9.0045288
## F_2018.50
                      0.1890012
                                   0.0541582 6.595765e-01 -1.6660020
  B 2018.50/Bmsy
                      1.2122568
                                   0.7340462 2.002008e+00 0.1924838
   F_2018.50/Fmsy
                                   0.3156222 1.325303e+00 -0.4357840
##
                      0.6467574
##
## Predictions w 95% CI (inp$msytype: s)
```

```
prediction
##
                                      cilow
                                                  ciupp
                                                           log.est
## B 2019.00
                  8288.8393687 2458.2527164 2.794866e+04 9.0226652
                                 0.0539088 6.601503e-01 -1.6678744
## F 2019.00
                     0.1886476
## B_2019.00/Bmsy
                                  0.7446432 2.046417e+00 0.2106202
                     1.2344434
## F_2019.00/Fmsy
                     0.6455475
                                  0.3121745 1.334931e+00 -0.4376565
## Catch 2019.00 1587.5324336 1269.3603387 1.985456e+03 7.3699362
## E(B inf)
                  9018.2679948
                                        NA
                                                     NA 9.1070076
```

Summary of estimates

round(sumspict.parest(res_pol89aSchaefBkfrac), 2)

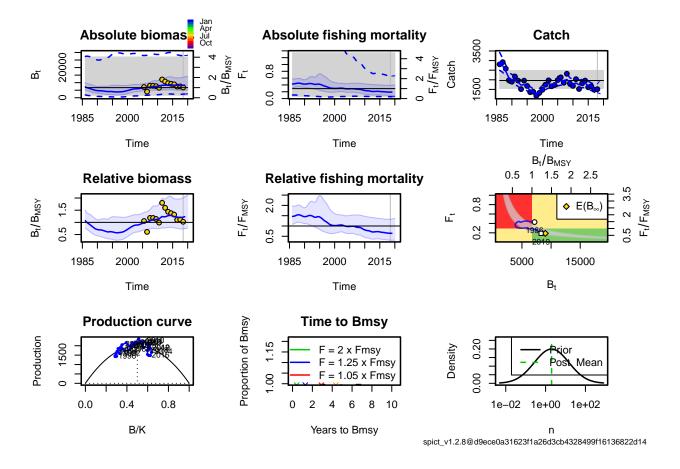
```
##
          estimate
                    cilow
                             ciupp log.est
## alpha
             2.81
                     0.71
                             11.17
                                      1.03
                                      0.07
## beta
             1.08
                     0.37
                              3.13
## r
             0.59
                     0.13
                              2.68
                                    -0.53
## rc
             0.59
                     0.13
                              2.68
                                     -0.53
             0.59
                     0.13
                              2.68
                                    -0.53
## rold
## m
          1986.49 1581.88 2494.60
                                    7.59
## K
         13526.47 3354.56 54542.21
                                      9.51
             0.00
                     0.00
                              0.00 -11.03
## q
             0.08
                     0.02
                              0.25
## sdb
                                    -2.55
## sdf
             0.09
                     0.04
                              0.20
                                    -2.45
## sdi
             0.22
                     0.14
                              0.35
                                     -1.51
             0.09
                     0.06
                                     -2.37
## sdc
                              0.14
```

Reference points

sumspict.drefpoints(res_pol89aSchaefBkfrac)

```
## estimate cilow ciupp log.est
## Bmsyd 6763.2340197 1.677282e+03 27271.107456 8.819256
## Fmsyd 0.2937195 6.432932e-02 1.341086 -1.225130
## MSYd 1986.4936495 1.581881e+03 2494.597989 7.594126
```

Basic plotting of the results plot(res_pol89aSchaefBkfrac)



Convergence checks

Convergence

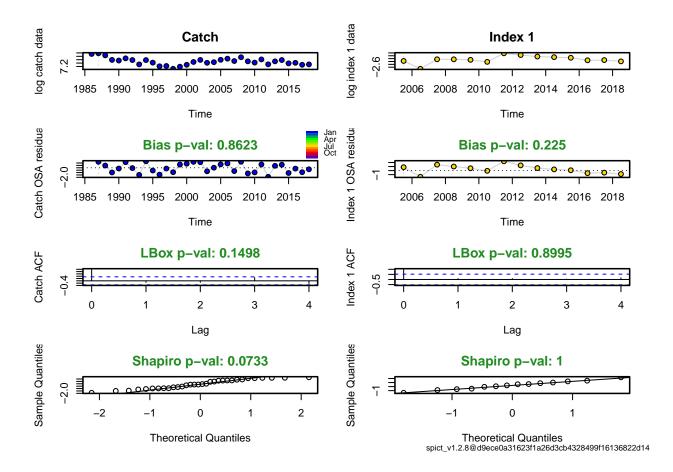
res_pol89aSchaefBkfrac\$opt\$convergence

[1] 0

All the sd were estimated
all(is.finite(res_pol89aSchaefBkfrac\$sd))

[1] TRUE

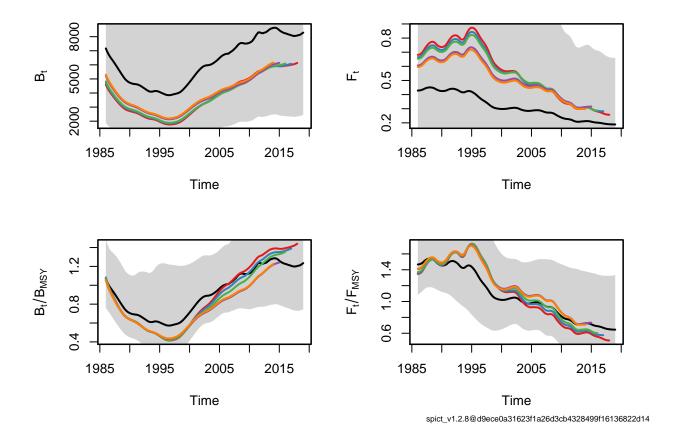
No violation of assumptions: bias, correlation and normality:
res_pol89aSchaefBkfrac <- calc.osa.resid(res_pol89aSchaefBkfrac)
plotspict.diagnostic(res_pol89aSchaefBkfrac)</pre>



Retrospective: no trends and all runs inside the confidence intervals

All runs converge and estimates are inside the confidence intervals. Problem with last year?. Trend changed relative to previous runs.

```
rep <- retro(res_pol89aSchaefBkfrac, nretroyear = 5)
plotspict.retro(rep)</pre>
```



Checking robustness to initial parameter values

All runs converged. It seems that there are two optima (see \$resmat). 18 runs with the same realistic estimates; but 12 converged models with unrealistic estimates.

```
check.ini(pol89aSchaefBkfrac, ntrials = 30)
## Checking sensitivity of fit to initial parameter values...
##
    Trial 1 ... model fitted!
##
    Trial 2 ... model fitted!
##
    Trial 3 ... model fitted!
    Trial 4 ... model fitted!
##
##
    Trial 5 ... model fitted!
    Trial 6 ... model fitted!
##
##
    Trial 7 ... model fitted!
```

Trial 12 ... model fitted!
Trial 13 ... model fitted!
Trial 14 ... model fitted!
Trial 15 ... model fitted!
Trial 16 ... model fitted!

Trial 8 ... model fitted!
Trial 9 ... model fitted!
Trial 10 ... model fitted!

Trial 11 ... model fitted!

set.seed(123)

##

##

```
Trial 17 ... model fitted!
##
   Trial 18 ... model fitted!
  Trial 19 ... model fitted!
## Trial 20 ... model fitted!
   Trial 21 ... model fitted!
## Trial 22 ... model fitted!
  Trial 23 ... model fitted!
   Trial 24 ... model fitted!
##
##
   Trial 25 ... model fitted!
##
  Trial 26 ... model fitted!
## Trial 27 ... model fitted!
## Trial 28 ... model fitted!
## Trial 29 ... model fitted!
## Trial 30 ... model fitted!
## $propchng
##
             logm logK logq logsdb logsdf logsdi logsdc
           -0.10 0.17 0.04 -1.10 -1.26
## Trial 1
                                              1.30
                                                   -0.08
## Trial 2
            0.19 0.03 0.02 -1.31
                                       0.13
                                             -0.51
                                                    -0.21
## Trial 3
           -0.20 0.24 0.11
                                             -1.30
                                1.31
                                       0.49
                                                    -1.11
## Trial 4
            0.09 0.08 -0.21
                              -0.45
                                      -0.60
                                             -0.13
                                                    -0.27
## Trial 5
           -0.10 -0.21 -0.19
                              -1.15
                                      -0.55
                                             -0.85
                                                     1.36
           -0.01 0.16
                        0.12
                                0.52
## Trial 6
                                       0.77
                                              1.02
                                                     0.24
## Trial 7
           -0.04 -0.08
                        0.15
                                1.03
                                       0.76
                                              0.10
                                                     0.67
            0.18 - 0.27
                              -0.86
## Trial 8
                        0.02
                                       1.08
                                             -0.17
                                                     0.84
## Trial 9 -0.18 0.15 -0.17
                                0.36
                                      -0.47
                                              1.16
                                                     0.33
## Trial 10 -0.11 0.19 0.02
                               -0.89
                                      -0.89
                                             -0.84
                                                     0.17
## Trial 11 0.13 0.08 -0.09
                                1.43
                                              0.80
                                       0.07
                                                     0.34
## Trial 12 0.06 -0.09 0.16
                                0.73
                                      -0.48
                                              0.24
                                                    -0.82
## Trial 13 -0.20 -0.04 -0.20
                                              0.93
                              -1.12
                                      -1.11
                                                     1.06
## Trial 14 0.08 -0.09 -0.07
                                0.51
                                       0.89
                                             -0.81
                                                     1.16
## Trial 15 -0.02 0.01 -0.04
                                0.48
                                       0.03
                                             -1.30
                                                     0.05
## Trial 16 0.19
                  0.25 - 0.05
                                0.26
                                       1.01
                                             -1.25
                                                     0.57
## Trial 17 -0.22 0.27 -0.09
                                1.02
                                      -0.14
                                             -1.30
                                                    -0.24
## Trial 18 -0.05 0.09 0.08
                                0.55
                                       0.80
                                              0.37
                                                    -1.39
## Trial 19 -0.17 -0.25
                        0.15
                               -0.54
                                      -0.34
                                             -1.12
                                                    -0.50
## Trial 20 0.12 0.01 -0.07
                               -0.92
                                      -0.82
                                             -1.37
                                                     0.17
## Trial 21 -0.09 -0.05 0.21
                                0.90
                                      -0.98
                                              0.77
                                                     0.75
## Trial 22 -0.21 -0.15 -0.10
                              -0.99
                                       0.01
                                              0.32
                                                     0.73
## Trial 23 -0.19 -0.07 -0.03
                                0.81
                                       0.16
                                              0.81
                                                    -0.01
## Trial 24 -0.07 0.09 0.05
                                0.41
                                      -0.10
                                             -0.69
                                                     0.80
## Trial 25 -0.04 -0.14 -0.05
                                0.90
                                      -1.04
                                             -0.71
                                                    -0.48
## Trial 26 0.06 -0.08 -0.01
                              -1.07
                                      -0.23
                                             -0.97
                                                     0.54
## Trial 27
            0.10 -0.14 -0.04
                                0.05
                                       0.67
                                             -0.18
                                                    -1.18
## Trial 28
           0.20 -0.14 0.07
                              -1.39
                                      -0.34
                                             -1.25
                                                     0.10
## Trial 29 -0.05 0.10 0.15
                              -0.21
                                       0.75
                                             -1.32
                                                    -0.29
## Trial 30 0.01 -0.06 -0.16
                                0.39
                                       0.61
                                              0.94
                                                     0.94
##
## $inimat
            Distance logK logm
                                  logq logsdb logsdf logsdi logsdc
                0.00 9.36 7.62 -10.99
                                       -1.61 -1.61
                                                      -1.61
## Basevec
                                         0.15
                                                             -1.48
## Trial 1
                3.81 8.39 8.95 -11.41
                                               0.42
                                                      -3.70
## Trial 2
                2.94 11.17 7.86 -11.19
                                         0.49 - 1.82
                                                      -0.79
                                                             -1.27
## Trial 3
                4.56 7.54 9.47 -12.16 -3.72 -2.40
                                                       0.48
                                                              0.18
                2.84 10.25 8.27 -8.72 -0.89 -0.65 -1.41 -1.18
## Trial 4
```

```
-3.80
## Trial 5
               4.36 8.39 6.00 -8.86
                                       0.24 - 0.73 - 0.25
## Trial 6
               2.87 9.26 8.81 -12.30
                                      -2.45 -2.85
                                                     -3.25
                                                            -2.00
## Trial 7
               2.92 8.97 7.02 -12.59
                                       -3.27 -2.84
                                                            -2.69
                                                     -1.77
## Trial 8
               3.74 11.01 5.53 -11.26
                                      -0.23 -3.35
                                                     -1.33
                                                            -2.96
                                                     -3.48
## Trial 9
               3.51 7.65 8.79 -9.17
                                       -2.19 -0.85
                                                            -2.14
## Trial 10
               3.04 8.33 9.07 -11.23
                                      -0.18 -0.17
                                                     -0.25
                                                            -1.89
               3.15 10.54 8.22 -10.02 -3.91 -1.72 -2.90
## Trial 11
                                                     -1.99
## Trial 12
               2.80 9.88 6.94 -12.78 -2.79 -0.84
                                                            -0.28
## Trial 13
               4.47 7.54 7.32 -8.76
                                        0.20
                                              0.17
                                                     -3.11
                                                            -3.31
               3.08 10.07 6.90 -10.27
                                       -2.44 - 3.05
## Trial 14
                                                     -0.31
                                                            -3.48
## Trial 15
               2.28 9.21 7.68 -10.53
                                      -2.38 -1.66
                                                      0.48 - 1.69
## Trial 16
               3.85 11.16 9.53 -10.49
                                       -2.02 -3.23
                                                            -2.52
                                                      0.40
## Trial 17
               4.08 7.34 9.69 -9.98
                                       -3.26 - 1.38
                                                      0.48
                                                            -1.22
## Trial 18
               3.02 8.93 8.31 -11.82
                                       -2.49 - 2.90
                                                     -2.21
                                                             0.62
## Trial 19
               3.71 7.77 5.74 -12.64
                                       -0.73 -1.06
                                                      0.19
                                                            -0.81
## Trial 20
               3.26 10.46 7.72 -10.26
                                       -0.13 -0.29
                                                      0.60
                                                            -1.89
## Trial 21
               3.69 8.50 7.21 -13.25
                                       -3.07 -0.03
                                                     -2.85
                                                            -2.81
## Trial 22
               3.24 7.42 6.45 -9.92
                                      -0.01 -1.62
                                                     -2.13
                                                            -2.78
## Trial 23
               2.65 7.57 7.12 -10.66
                                      -2.91 -1.86
                                                     -2.91
                                                            -1.60
## Trial 24
               2.15 8.69 8.32 -11.57
                                       -2.28 -1.45
                                                     -0.50
                                                            -2.89
## Trial 25
               2.92 8.96 6.55 -10.39
                                      -3.07
                                               0.07
                                                     -0.47
                                                            -0.83
## Trial 26
               2.64 9.91 7.04 -10.85
                                       0.12 - 1.23
                                                     -0.04
                                                            -2.47
## Trial 27
               2.68 10.32 6.54 -10.56 -1.70 -2.69
                                                     -1.31
                                                             0.29
## Trial 28
               3.82 11.22 6.58 -11.81
                                        0.63 - 1.06
                                                      0.40
                                                            -1.76
               3.10 8.94 8.36 -12.59 -1.27 -2.81
## Trial 29
                                                      0.52 - 1.14
## Trial 30
               3.03 9.43 7.18 -9.24 -2.24 -2.58 -3.13 -3.12
##
## $resmat
                                   K q sdb sdf sdi sdc
##
           Distance
               0.00 1986.49 13526.47 0 0.08 0.09 0.22 0.09
## Basevec
## Trial 1
               0.00 1986.49 13526.46 0 0.08 0.09 0.22 0.09
## Trial 2
               0.12 1986.49 13526.59 0 0.08 0.09 0.22 0.09
## Trial 3
           13108.71 3358.30
                              489.74 0 0.23 0.13 0.23 0.09
               0.03 1986.49 13526.50 0 0.08 0.09 0.22 0.09
## Trial 4
## Trial 5
               0.05 1986.49 13526.51 0 0.08 0.09 0.22 0.09
## Trial 6
               0.06 1986.49 13526.53 0 0.08 0.09 0.22 0.09
## Trial 7
               0.12 1986.49 13526.59 0 0.08 0.09 0.22 0.09
## Trial 8
               0.00 1986.49 13526.47 0 0.08 0.09 0.22 0.09
## Trial 9 13108.71 3358.30
                            489.74 0 0.23 0.13 0.23 0.09
## Trial 10 13108.71 3358.30
                              489.74 0 0.23 0.13 0.23 0.09
               0.01 1986.49 13526.48 0 0.08 0.09 0.22 0.09
## Trial 11
## Trial 12
               0.03 1986.49 13526.43 0 0.08 0.09 0.22 0.09
                              489.74 0 0.23 0.13 0.23 0.09
## Trial 13 13108.71 3358.30
               0.04 1986.49 13526.50 0 0.08 0.09 0.22 0.09
## Trial 14
## Trial 15
               0.01 1986.49 13526.45 0 0.08 0.09 0.22 0.09
                              489.73 0 0.23 0.13 0.23 0.09
## Trial 16 13108.71 3358.29
## Trial 17 13108.71 3358.29
                              489.73 0 0.23 0.13 0.23 0.09
## Trial 18 13108.71 3358.30
                              489.74 0 0.23 0.13 0.23 0.09
## Trial 19
               0.00 1986.49 13526.47 0 0.08 0.09 0.22 0.09
## Trial 20
               0.01 1986.49 13526.47 0 0.08 0.09 0.22 0.09
## Trial 21 13108.71 3358.30
                             489.74 0 0.23 0.13 0.23 0.09
## Trial 22 13108.71 3358.30
                             489.74 0 0.23 0.13 0.23 0.09
## Trial 23 13108.71 3358.30 489.74 0 0.23 0.13 0.23 0.09
## Trial 24 13108.71 3358.30 489.74 0 0.23 0.13 0.23 0.09
```

```
## Trial 25 13108.71 3358.30
                               489.74 0 0.23 0.13 0.23 0.09
## Trial 26
               0.03 1986.49 13526.50 0 0.08 0.09 0.22 0.09
                0.09 1986.49 13526.38 0 0.08 0.09 0.22 0.09
## Trial 27
## Trial 28
                0.11 1986.49 13526.58 0 0.08 0.09 0.22 0.09
## Trial 29 13108.71 3358.30
                               489.74 0 0.23 0.13 0.23 0.09
## Trial 30
                0.04 1986.49 13526.43 0 0.08 0.09 0.22 0.09
## Catch observations:
   [1] 1986 1987 1988 1989 1990 1991 1992 1993 1994 1995 1996 1997 1998 1999 2000
## [16] 2001 2002 2003 2004 2005 2006 2007 2008 2009 2010 2011 2012 2013 2014 2015
## [31] 2016 2017 2018
  [1] 2806 2918 2582 1973 1900 2168 1958 1513 1955 1679 1354 1378 1165 1322 1479
## [16] 1746 1972 1663 1726 1986 2126 1847 2313 1812 1682 2032 1520 1811 1959 1610
## [31] 1661 1481 1512
## Index observations:
## [[1]]
   [1] 2005.5 2006.5 2007.5 2008.5 2009.5 2010.5 2011.5 2012.5 2013.5 2014.5
## [11] 2015.5 2016.5 2017.5 2018.5
##
## [[1]]
## [1] 0.1151 0.0663 0.1292 0.1289 0.1244 0.1079 0.1966 0.1743 0.1565 0.1500
## [11] 0.1438 0.1205 0.1222 0.1117
```

Questions for Workshop - September 2020:

Run 5, that fixes n of productive curve (BMSY/K=0.5) and uses priors for B1/K, converged well and the output estimates are realistic. However, the model is sensitive to initial values and the confidence intervals are quite wide.

- 1. How the robustness can be improved?. To address the sensitivity to initial values.
- 2. Acting (fixing, set priors) on alfa and/or beta could help to narrow the confidence intervals?