

10. Single-agent Search

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Moving On...

- Two-player adversary search is nice, but not all interesting problems can be mapped to games
- Large class of optimization problems that all have the same search properties
- Find the best search value from the perspective of a single player
- Single-agent search

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Applications

- Pathfinding
- Dynamic programming
- Job shop scheduling
- DNA sequence alignment
- Scheduling
- Planning
- Constraint satisfaction
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Why Alpha-Beta First?

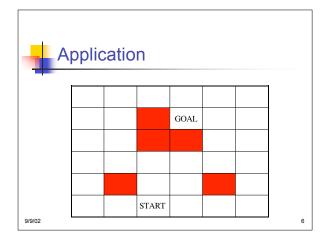
- Many of the performance enhancements we saw in alpha-beta translate to single-agent search
- Most originated with alpha-beta, and were adopted by other classes of search algorithms



Application: Pathfinding

- Consider a sample application
- Find a minimal cost path from a start node to a goal node
- Can move one square horizontally or vertically, each with a cost of one
 - Can be generalized to include diagonals
 - Can be generalized to include variable costs

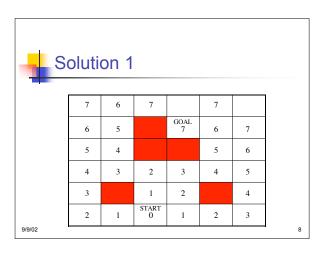
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Solution 1

- Trivial solution
- Explore outward from the start node until reaching the goal node
- Can use iterative deepening to guarantee minimal cost path
 - Try paths of length 1, then 2, etc.





Solution 1

- Note that more than one path can lead to a node
 - Some of these paths are non-optimal
- Note that cycles are possible
- Observation: we need to eliminate duplicate states!

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Solution 2

- Trivial observation that searching to depth 1 is a waste of time since we are obviously more than 1 away from the goal
- Add to the search an evaluation function that estimates the distance to the goal
- What is a simple estimator of distance?

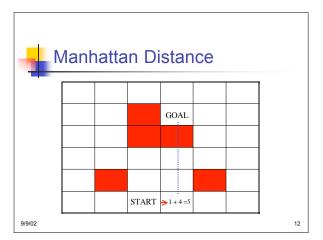
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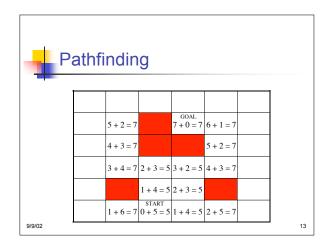
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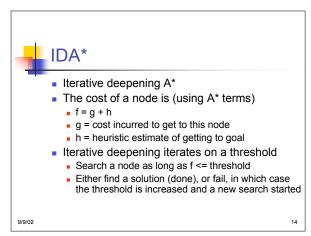


Solution 2

- For pathfinding, a good estimate of distance to go is the Manhattan distance
 - Number of horizontal and vertical moves to the goal node
- Cost of reaching a node is now two parts:
- Distance already traveled
- Estimate of distance to go
- If the cost of a node exceeds the iterative deepening threshold, then stop searching that path







```
threshold = Eval( s );
done = false;
while( not done ) {
   done = IDA*( s, 0, threshold );
   if( done == false ) threshold++;
}
```

```
IDA* (2)

IDA*( state s, int g, threshold t ) {

    h = Eval( s );

    if( h == 0 ) return( true );

    f = g + h;

    if( f > threshold ) return( false );

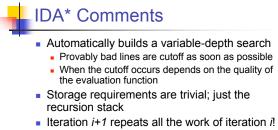
    for( i = 1; i <= numchildren; i++ ) {

        done = IDA*( s.child[ i ], g + cost( child[ i ] ), t );

        if( done == true ) return( true );

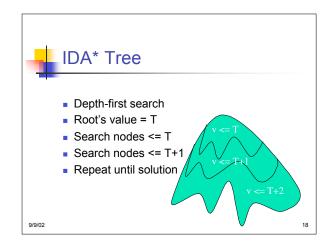
    }

    return( false );
}
```



- For some domains you can do better than iterate by 1

• Use the mimimum f-value seen at a leaf node during an iteration as the next threshold





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IDA* Comments

- Is IDA* guaranteed to produce an optimal answer?
- Yes!
- But only if...
- The evaluation function has to be admissible:
 - It must always be a lower bound on the true solution length

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Manhattan Distance

- Computes a direct path from a node to the goal
- Ignores all obstacles, which can only lengthen the path
- Therefore it is an admissible heuristic



Monotonicity

- Most admissible heuristics also have the monotonicity property
- The f values never decrease along a path if monotonicity holds
- If you have a non-monotonic heuristic, one can always modify the search to make the heuristic monotonic...
 - How?

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Examining h

- Simplified cost of a search
- Uniform branching factor b
- Search depth d
- Ignore all other enhancements
- No heuristic: bd
- Average heuristic value is h: b^{d-h}
- The quality of the heuristic has an enormous impact on the search efficiency

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Examining h

- What does it mean to iterate?
- If the first iteration finds an answer, then h had no error
- If a second iteration is required, then there is an error of 1 in h
- The number of iterations indicates the degree of error in h

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Eliminating Redundant Nodes

- Need to eliminate duplicate nodes
- Trivial optimization for many domains is to disallow move reversals
- For more sophisticated detection of redundant nodes, we can use a transposition table

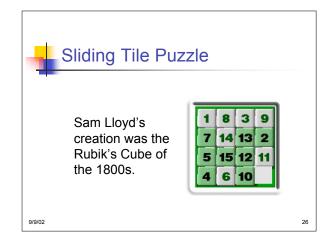
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Transposition Table

- Store the t and g values in the table, and only search a transpositon node with the smallest g, and only once for the current t
- Use table only to indicate which nodes not to search
- No need to store values, since the search stops when a solution is found
- All other TT issues (table size, hashing, table entry replacement) remain the same as for two-player games

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Experiments

- Korf problem set of 100 positions
- Search 36700
- Search move reversals 100
- Search + TT (256K) 37

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_A

- Single-agent search began in the 1960s with the A* algorithm [2]
- This algorithm dominated AI search for two decades, but has competition now from IDA*
- Why teach IDA* first? Easy to explain once you've seen Alpha-Beta

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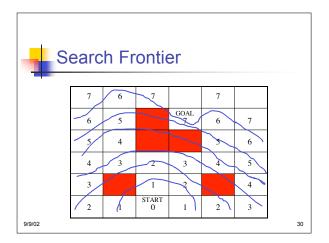
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- Each iteration of IDA* re-searches the tree over again beginning at the root
- All that overhead can be eliminated...
- ... by keeping track of the search frontier, and only expanding nodes on the frontier
- A* is a *best-first* search algorithm

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A* Data Structure

- OpenList
 - List of nodes in the tree that are not yet fully considered
 - Ordered from best to worst f value
- ClosedList
 - Nodes that have been fully expanded
 - No longer on any optimal path

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A* Algorithm (1)

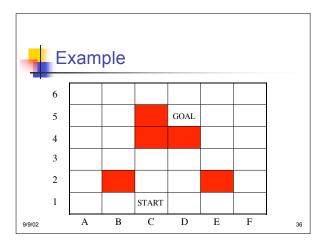
- Take best (first) node from OpenList
 - Check for solution
 - Expand all the children
 - Move node to the ClosedList
 - As far as we know, done with this node

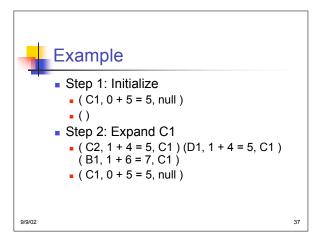
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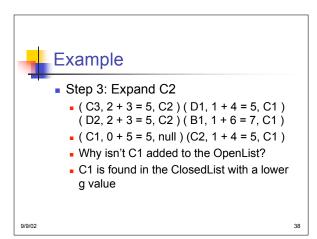


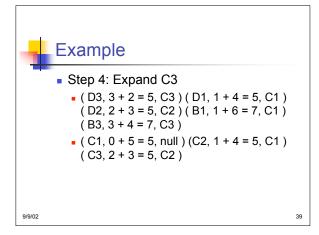
- Expanding a child
 - Check if seen before Open/ClosedList
 - If the node has been seen before with the same or better g value, then reject
 - Add to OpenList for consideration
- In effect the lists act as a cache of previously seen results
- NOTE: the algorithm requires all nodes to be in these lists, unlike a TT

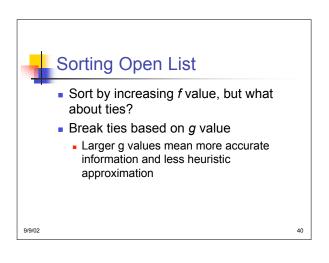
```
Consider( state from, state to ) {
    newg = from.g + Cost( from, to );
    if( ( to is in OpenList or ClosedList ) and
        ( to.g <= newg ) ) return;
    to.g = newg; to.h = Eval( to );
    to.f = to.g + to.h; to.parent = from;
    if( to is in ClosedList ) remove to from ClosedList
    if( to is not in OpenList ) insert to in OpenList sorted
        by f-value
}
```













A*

- Does not have the iterative overhead of IDA*
- Only expands nodes that are shown to be relevant
- Needs to maintain a history of all nodes previously searched
- In practice, faster than IDA*, but A* runs out of memory very quickly!

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IDA* versus A*

- For many types of problems, IDA* flounders in the cost of the re-searches, causing many to prefer A* over IDA*
 - Why?
- But... IDA* is handicapped with no storage!
 - A* uses a closed list -- in effect a perfect cache of previously seen states
 - IDA* uses almost no storage
 - IDA* with a transposition table can be competitive with A*



Which to Choose?

- IDA* is guaranteed to work, albeit possibly more slowly
- A* is more efficient, but can run out of memory
 - Can also run slower because of cache effects
- The right choice depends on properties of your application

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References

- [1] R. Korf. "Best-first Iterative-Deepening: An Optimal Admissible Tree Search", *Artificial Intelligence*, vol. 27, no.1, pp. 97-109, 1985.
- [2] P. Hart, N. Nilsson and B. Raphael. "A Formal Basis for the Heuristic Determination of Minimum Cost Paths", *IEEE Trans. Syst. Sci. Cyber.*, vol. 4, no. 2, pp. 100-107, 1968.

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