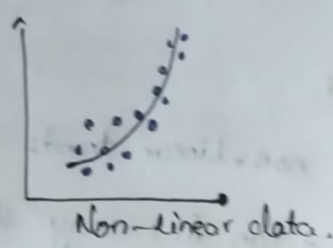
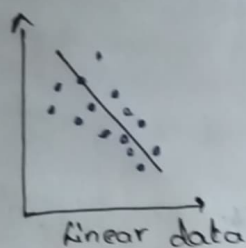
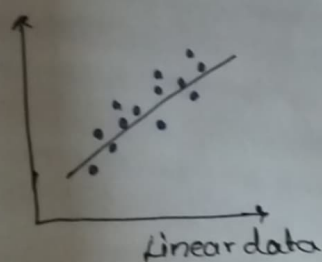


November 20:

Data $\begin{cases} \text{Linear data} \\ \text{Non-linear data.} \end{cases}$



* In case of linear data we can perform linear regression, but in case of non-linear data straight line will not be suitable as the distance b/w dots will be more hence, we need to produce curved line as best-fit line.

* Linear data — Linear Regression
Non-linear data — Polynomial Regression.

Polynomial Regression:

It is an extension of linear regression, where the relationship b/w the x & y is modelled as an n th degree polynomial.

$$\hat{y} = \alpha x + \beta$$

$$\hat{y} = \alpha_0 + \alpha_1 x + \alpha_2 x^2 + \alpha_3 x^3 + \dots + \alpha_n x^n + \beta$$

This allows the model to capture non-linear relationship b/w x & y .

Why polynomial regression?

* In Real-world data often doesn't follow a straight line,
* Polynomial Regression helps fit curved pattern such as parabolas, waves or exponential like structure/shapes.

Steps to perform polynomial regression:

1. Choose degree of polynomial (n)

2. Transform features : create x, x^2, x^3, \dots, x^n .

Ex: $x_1 \quad x_2 \quad \text{dof: } 3$

$$(x_1, x_1^2, x_1^3, x_2, x_2^2, x_2^3, x_1 x_2^2, x_1^0, x_1^1, x_1^2, x_2^0, x_2^1, x_2^2, x_1 x_2)$$

3. Fit Linear Regression on the transformed feature

4. Evaluate model (R^2 score, MSE, RMSE, ...)

Advantages:

- * Captures non-linear trends
- * Flexible - can fit many shapes.

Disadvantages:

- * High-degree polynomial may lead to overfitting.
- * Extrapolation beyond training data is unreliable.
- * More complex & harder to interpret.

Usually ML models falls under 2 problems:

1. Overfitting - train accuracy very high, test accuracy very low.
2. Underfitting - train & test accuracy are very low.