

## **Step by Step Guide: Reflection and Congruence in Real-Life**

### **Pre-Class Preparation Checklist**

- Prepare large sheets of graph paper (A3 size if possible) for each group.
- Ensure rulers, protractors, coloured pencils (at least 4 colours per group), and set squares are available.
- Print the garden scenario handout with instructions and a blank Cartesian grid.
- Prepare a sample completed garden design to show as an exemplar (optional — show after student work).
- Collect 3–4 photographs of symmetric gardens, buildings, or natural objects (e.g., Taj Mahal, butterfly, symmetric building facade).
- Prepare the properties table and real-life applications table on chart paper or slides.
- Have tracing paper available for students who need to verify congruence physically.
- Prepare exit ticket handouts with 4 questions.

### **Phase 1: Problem-Solving and Discovery (15 minutes)**

#### **Opening Hook (3 minutes)**

[SAY] "Today, we're going to be garden designers! But not just any garden — a mathematically perfect garden."

[DO] Show a photograph of a symmetric garden (e.g., the Taj Mahal gardens or a formal French garden).

[ASK] "What do you notice about this garden? What makes it look so beautiful and balanced?"

[WAIT] Expected: "It's symmetric." "Both sides look the same." "It's like a mirror image."

[SAY] "Exactly! The garden uses REFLECTION and CONGRUENCE to create balance and beauty. Today, you're going to design your own symmetric garden using these mathematical concepts."

[ASK] "Can you think of other places where you see reflection and congruence in real life?"

[WAIT] Expected: "Butterfly wings." "Building facades." "Tiled floors." "Our faces."

[SAY] "Great examples! Let's see how mathematics makes all of this possible."

#### **Anchor Activity Launch (2 minutes)**

[DO] Distribute graph paper, rulers, coloured pencils, and the scenario handout.

[SAY] "Here's your design brief. You are designing a new garden for our school."

[SAY] "Read the scenario carefully." [Pause for 30 seconds.]

[SAY] "Your central pathway runs along the y-axis — that's the line  $x = 0$ . Draw it first."

[SAY] "On the LEFT side, design one flower bed as a polygon with at least 4 vertices. Label the coordinates."

[SAY] "Then REFLECT your flower bed across the pathway to create the second bed on the RIGHT side."

[SAY] "After that, add at least TWO more symmetric elements — benches, trees, a fountain, stepping stones — whatever you like."

[SAY] "Finally, answer the guiding question on your handout."

[SAY] "Work in your groups. You have 8 minutes. Be creative!"

### **Student Work Time (8 minutes)**

[DO] Circulate among groups.

[ASK] To a group drawing the flower bed: "What are the coordinates of your vertices?"

[WAIT] Expected: e.g., "A(-5, 2), B(-2, 2), C(-2, 6), D(-5, 6)."

[ASK] "Now, how do you reflect these across the y-axis?"

[WAIT] Expected: "Change the sign of the x-coordinate."

[SAY] "Correct! So A(-5, 2) becomes A'(5, 2). Plot all four reflected vertices."

[ASK] To another group: "How do you know the two flower beds are congruent?"

[WAIT] Expected: "They have the same side lengths." "We measured them."

[SAY] "Can you prove it using the distance formula? Calculate the length of each side."

[DO] For struggling groups: "Let's start simple. Make your flower bed a rectangle. What are the four corners?"

[ASK] To early finishers: "What if you put a circular fountain at the origin? What happens when you reflect a circle centred at (0, 0)?"

[WAIT] Expected: "It stays the same! The circle is symmetric about the y-axis."

[SAY] "Exactly! A circle centred on the mirror line is its own reflection. That's why fountains are often placed at the centre of symmetric gardens."

### **Class Sharing (2 minutes)**

[SAY] "Let's see some of your designs! Which group would like to share?"

[DO] Invite 2–3 groups to hold up their garden designs.

[ASK] "What is the mirror line in your design?"

[WAIT] Expected: "The y-axis." " $x = 0$ ."

[ASK] "How did you verify that the flower beds are congruent?"

[WAIT] Expected: "We measured the sides." "We used the distance formula."

[ASK] "What extra elements did you add? Are they symmetric too?"

[SAY] "Beautiful designs! You've applied reflection and congruence like real landscape architects."

## **Phase 2: Structured Instruction (10 minutes)**

### **Properties Preserved Under Reflection (3 minutes)**

[SAY] "Your garden designs show something important: when you reflect a shape, the reflected image is **CONGRUENT** to the original. But what exactly is preserved?"

[WRITE] Build the table on the board:

[WRITE] "Side lengths — preserved. A 4-unit side stays 4 units."

[WRITE] "Angles — preserved. A  $90^\circ$  corner stays  $90^\circ$ ."

[WRITE] "Area — preserved. Both flower beds have the same planting area."

[WRITE] "Shape — preserved. A rectangle reflects to a rectangle."

[WRITE] "Orientation — REVERSED. The image is a mirror image (opposite congruence)."

[SAY] "This is why reflection creates congruent figures — everything is preserved except orientation."

### **Real-Life Applications Table (4 minutes)**

[SAY] "Reflection and congruence are everywhere in real life. Let me show you."

[WRITE] Build the applications table on the board:

[WRITE] "Garden design — symmetric flower beds across a pathway."

[SAY] "This is exactly what you just did!"

[WRITE] "Architecture — symmetric building facades, windows, doors."

[DO] Show a photograph of a symmetric building if available.

[WRITE] "Art & Design — mandala patterns, logos, kaleidoscopes."

[ASK] "Can you think of a company logo that uses reflective symmetry?"

[WAIT] Expected: Various answers (e.g., McDonald's arches, Mercedes-Benz star).

[WRITE] "Nature — butterfly wings, leaves, human face."

[SAY] "A butterfly's body is the mirror line. Each wing is a reflection of the other."

[WRITE] "Engineering — bridge design, aircraft wings."

[SAY] "Both wings of an aircraft must be congruent for balanced flight."

[WRITE] "Everyday life — tiled floors, wallpaper, fabric patterns."

### **Connecting to the Guiding Question (3 minutes)**

[SAY] "Now let's address the guiding question: How would you use reflection and congruence to improve the garden's design further?"

[ASK] "What elements could you add to enhance symmetry or balance?"

[WAIT] Expected: "A fountain in the centre." "Symmetric benches." "Matching trees." "A gate with two identical panels."

[SAY] "All excellent ideas! Notice that elements ON the mirror line — like a fountain at the origin — are their own reflections. Elements OFF the mirror line need a reflected partner."

[SAY] "This is exactly how professional landscape architects think. They start with a line of symmetry and build outward, ensuring every element has a congruent counterpart."

[ASK] "Why is symmetry important beyond just looking nice?"

[WAIT] Expected: "Balance." "Equal distribution." "Structural stability."

[SAY] "Yes! In engineering, symmetric designs distribute weight evenly. In gardens, symmetric layouts ensure equal sunlight and water access. Mathematics makes real-world design better."

### Phase 3: Practice and Application (10 minutes)

#### Worked Example: Reflecting a Triangular Flower Bed (3 minutes)

[SAY] "Let's work through an example together. A triangular flower bed has vertices A(-6, 1), B(-2, 1), and C(-4, 5). The pathway is the y-axis."

[WRITE] Plot the triangle on the board.

[SAY] "Step 1: Reflect each vertex. For the y-axis, change the sign of x."

[WRITE] "A(-6, 1) → A'(6, 1)"

[WRITE] "B(-2, 1) → B'(2, 1)"

[WRITE] "C(-4, 5) → C'(4, 5)"

[DO] Plot the reflected triangle on the board.

[SAY] "Step 2: Let's verify congruence. Calculate side lengths."

[WRITE] "AB = 4, A'B' = 4 ✓"

[WRITE] "AC =  $2\sqrt{5}$ , A'C' =  $2\sqrt{5}$  ✓"

[WRITE] "BC =  $2\sqrt{5}$ , B'C' =  $2\sqrt{5}$  ✓"

[SAY] "All three pairs of sides are equal. Therefore, the two flower beds are congruent by SSS."

#### Student Practice: Real-World Identification (4 minutes)

[SAY] "Now it's your turn. I want you to identify THREE examples of reflection and congruence in our school environment."

[SAY] "For each example, describe: (a) the mirror line, (b) the congruent elements, and (c) which congruence criterion applies."

[SAY] "Work with your partner. 3 minutes."

[WAIT] 3 minutes.

[SAY] "Let's hear some examples."

[ASK] "What did you find?"

[WAIT] Expected: "The windows on either side of the door." "The two halves of the football pitch." "The school gate panels."

[SAY] "Excellent! You're now seeing mathematics everywhere you look."

### **Quick Check: Reflection Rules (3 minutes)**

[ASK] "Quick check. If I reflect the point (3, 7) across the y-axis, what do I get?"

[WAIT] Expected: "(-3, 7)."

[ASK] "If I reflect (-2, 5) across the x-axis?"

[WAIT] Expected: "(-2, -5)."

[ASK] "If I reflect (4, 1) across the line  $y = x$ ?"

[WAIT] Expected: "(1, 4)."

[ASK] "Is the reflected figure always congruent to the original?"

[WAIT] Expected: "Yes!"

[SAY] "Always. Reflection ALWAYS produces a congruent image. That's why it's so useful in design."

### **Phase 4: Assessment — Exit Ticket (5 minutes)**

[SAY] "For our exit ticket, answer these four questions on a separate piece of paper. You have 5 minutes."

[SAY] "Question 1: A rectangular flower bed has vertices P(-5, 1), Q(-1, 1), R(-1, 4), S(-5, 4). The pathway is the y-axis. Find the reflected vertices and prove the beds are congruent."

[SAY] "Question 2: A building facade has a window at W(-4, 6) and a door at D(-2, 0). The axis of symmetry is  $x = 0$ . Where are the corresponding window and door on the right half?"

[SAY] "Question 3: Explain why a butterfly's wings demonstrate reflection and congruence. Identify the mirror line."

[SAY] "Question 4: One flower bed has vertices (1, 1), (3, 1), (2, 4). Find the vertices of three more beds to create a pattern with two lines of symmetry."

[DO] Collect exit tickets as students finish.

### Answer Key:

- 1.  $P'(5,1)$ ,  $Q'(1,1)$ ,  $R'(1,4)$ ,  $S'(5,4)$ .  $PQ = P'Q' = 4$ ,  $QR = Q'R' = 3$ , all sides equal  $\rightarrow SSS$ .
- 2.  $W'(4, 6)$  and  $D'(2, 0)$ .
- 3. Body is the mirror line. Wings are reflections. Congruent by SSS (all corresponding lengths equal).
- 4. Reflect across y-axis:  $(-1,1),(-3,1),(-2,4)$ . Reflect across x-axis:  $(1,-1),(3,-1),(2,-4)$ . Both axes:  $(-1,-1),(-3,-1),(-2,-4)$ .

## Differentiation Notes

### Struggling Learners:

Provide pre-drawn garden templates with the mirror line and one flower bed already plotted. Use simple reflection rule: change sign of x for y-axis reflection. Allow tracing paper for physical verification. Focus on rectangular shapes. Provide a step-by-step checklist.

### On-Level Learners:

Complete full garden design with multiple reflected elements. Use distance formula to prove congruence. Identify real-world examples in school. Attempt reflection across  $y = x$ .

### Advanced Learners:

Design garden with two lines of symmetry (four-quadrant layout). Reflect across non-standard lines. Investigate relationship between rotational and reflective symmetry. Explore tessellations. Calculate total areas and verify equality.

## Post-Lesson Reflection

1. Did the garden design scenario effectively engage students and make reflection/congruence tangible?
2. Were students able to correctly reflect coordinates across the y-axis?
3. Did students understand that reflection preserves side lengths, angles, and area?
4. Were students able to prove congruence using SSS and the distance formula?

5. Did students make meaningful connections to real-world applications?
6. Were students creative in their garden designs?
7. Did the guiding question generate thoughtful discussion?
8. What adjustments would improve the lesson for future delivery?