

The architecture of planetary systems - a machine learning approach

Yann ALIBERT



ISPM - 28/10/2022

European Research Council



1- Planet formation and the Bern model

2- Models *versus* observations

3- Planetary internal structure and Deep Learning

4- Correlation in planetary systems with random forest: finding a second Earth

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From giant molecular clouds to planetary systems

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Solar System

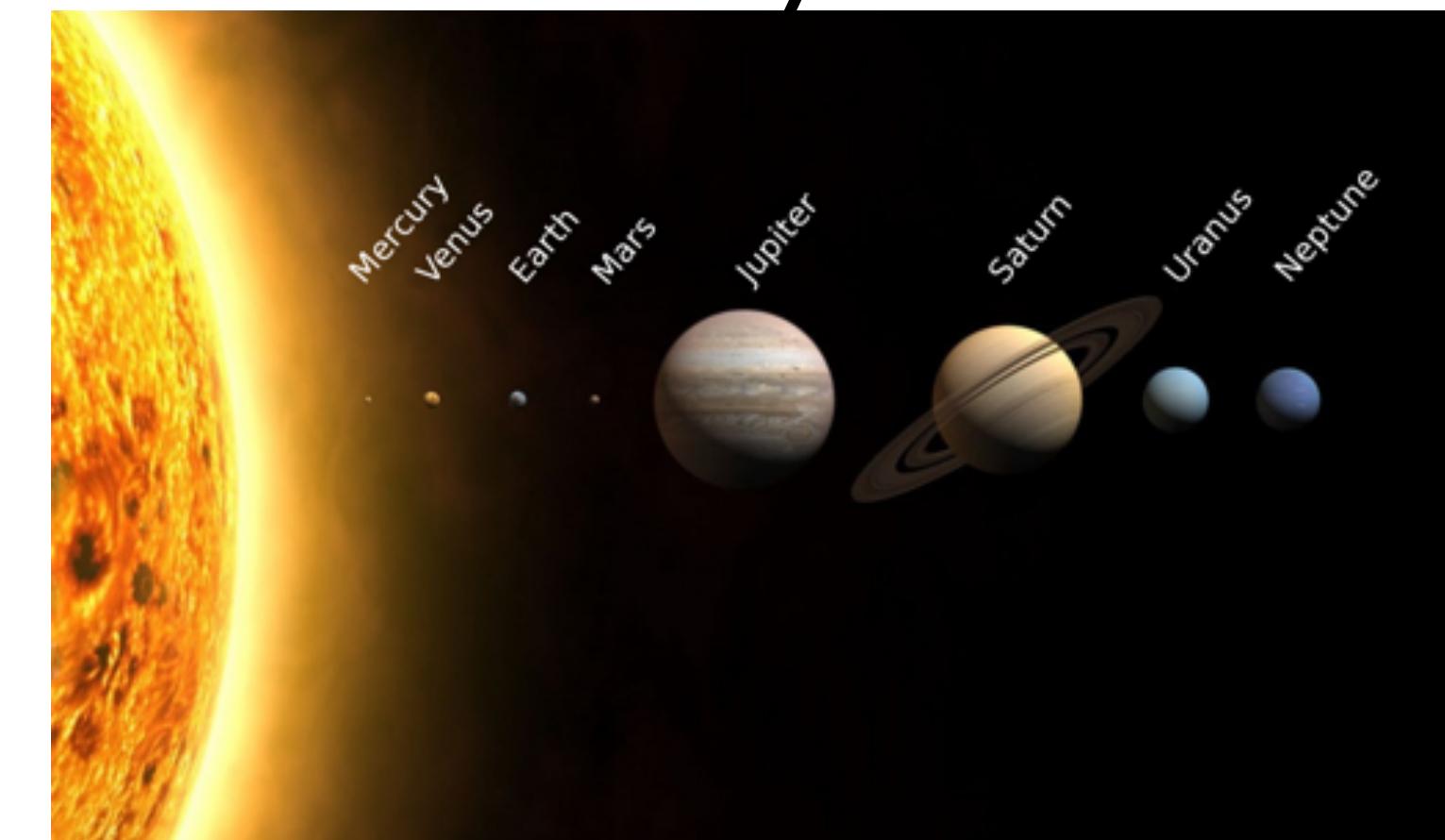
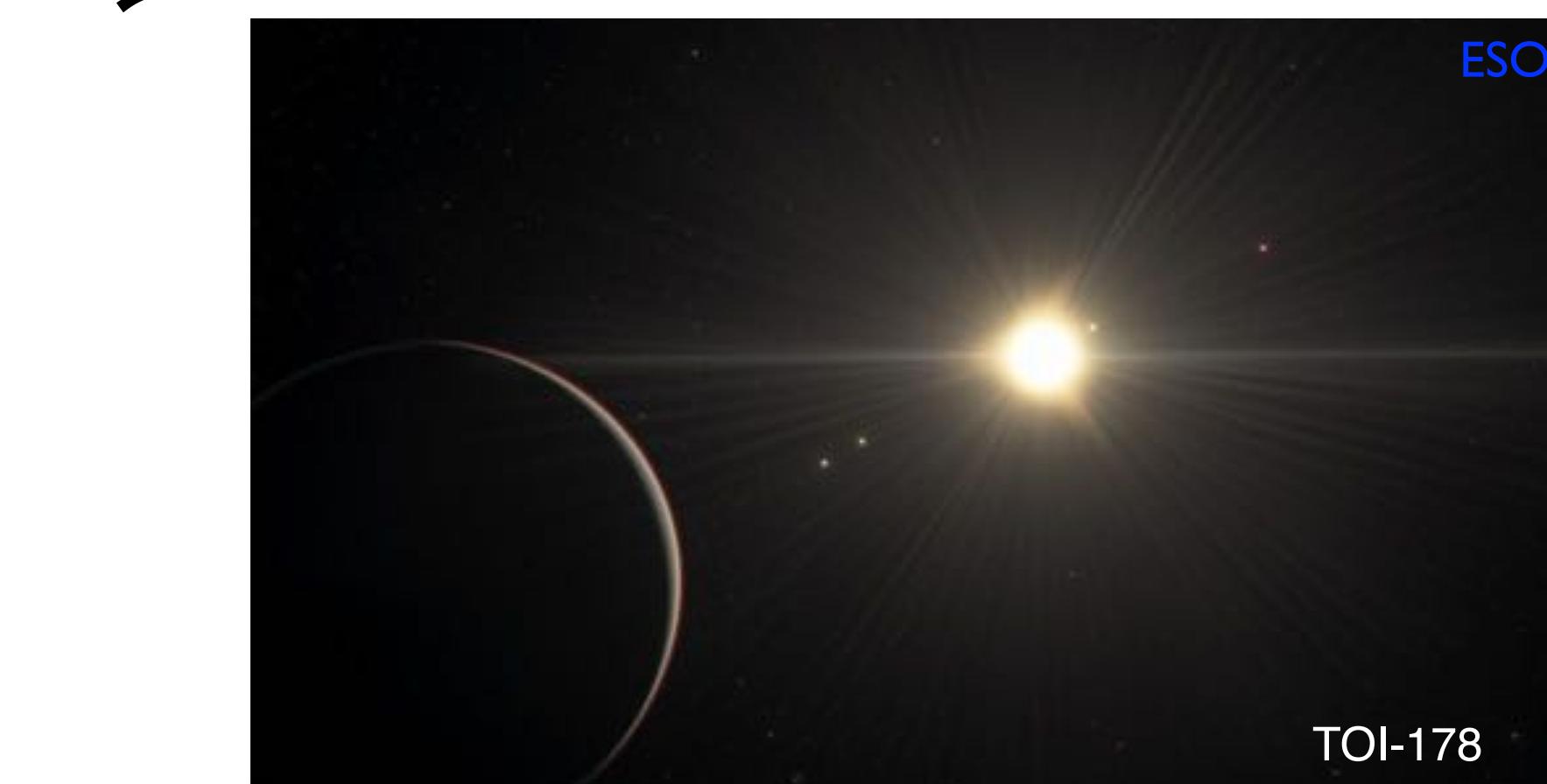


Image by WP - Planets2008.jpg, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=45708230>

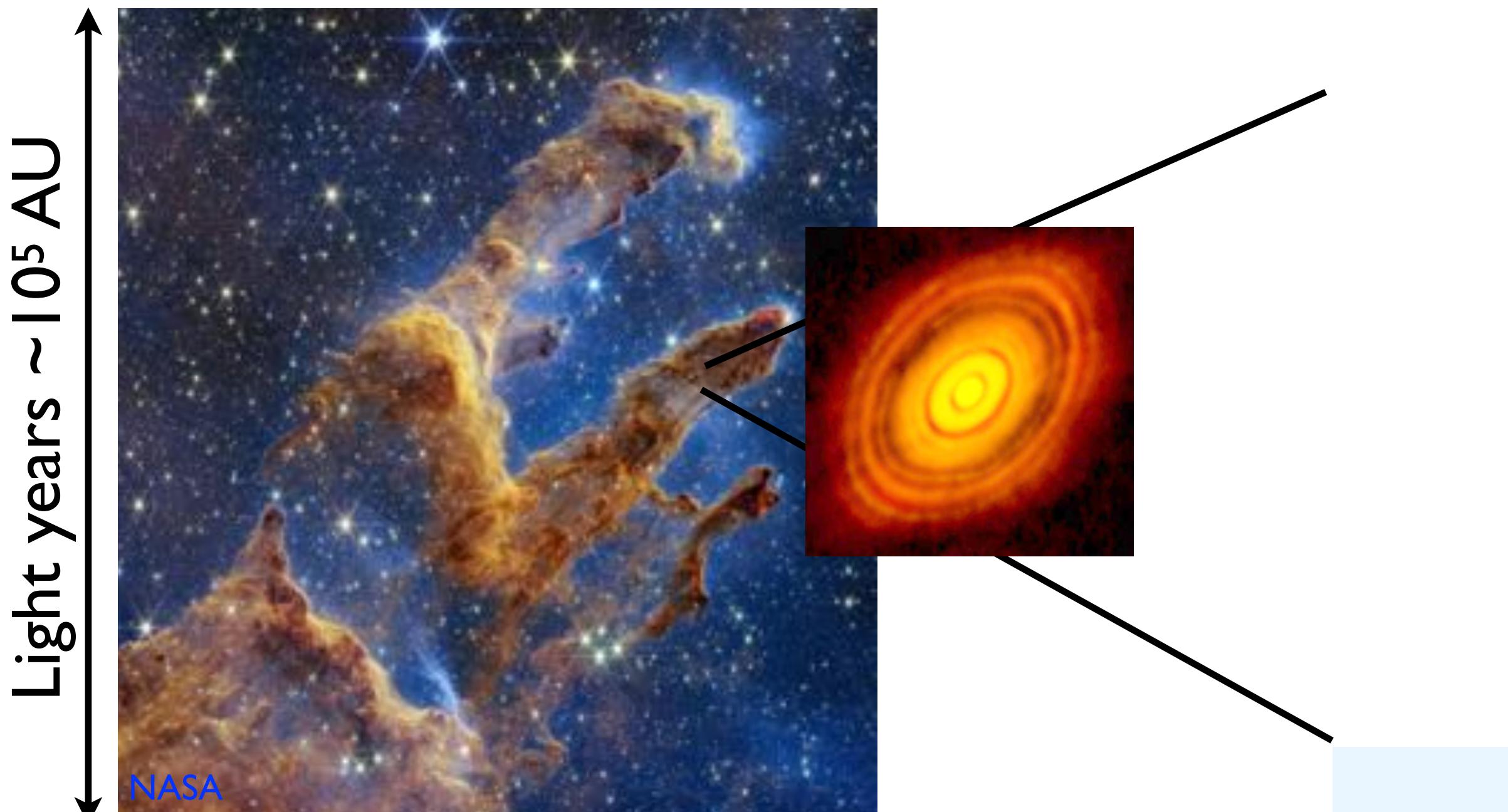


ALMA

~100s AU

99% gas 1% solids

$T_{\text{disk}} < 10^7 \text{ yr}$



The core accretion model (1)

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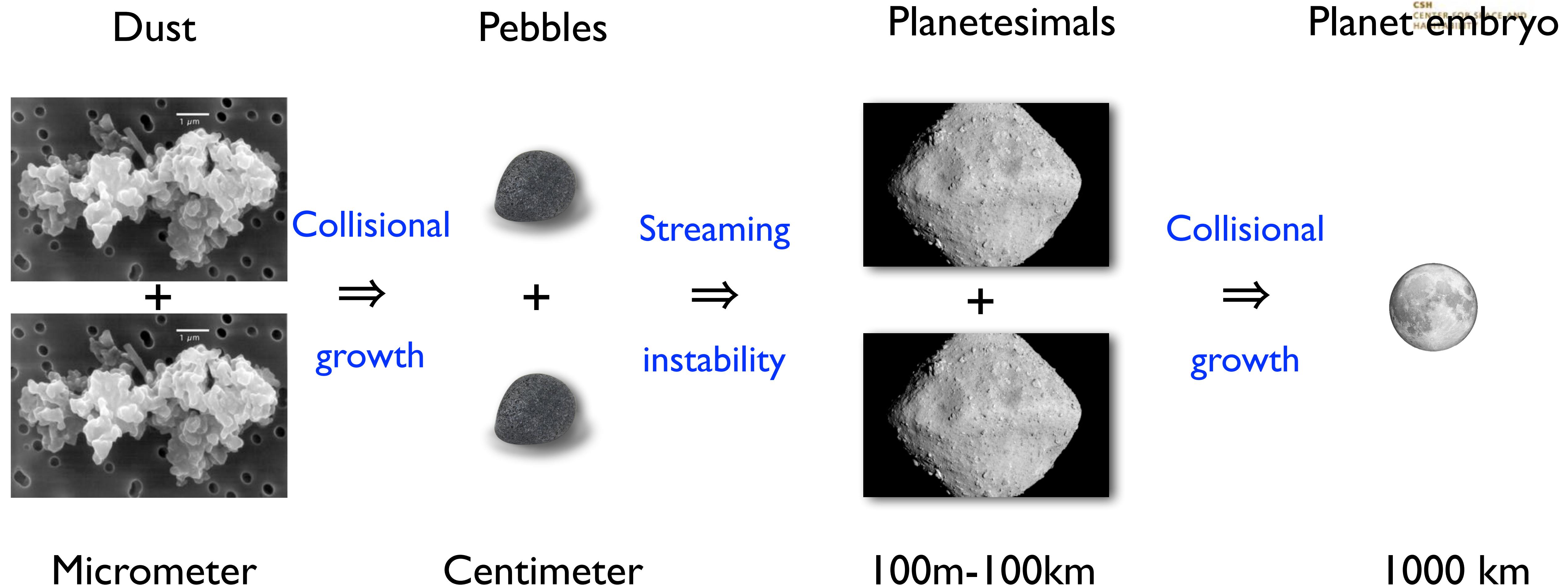


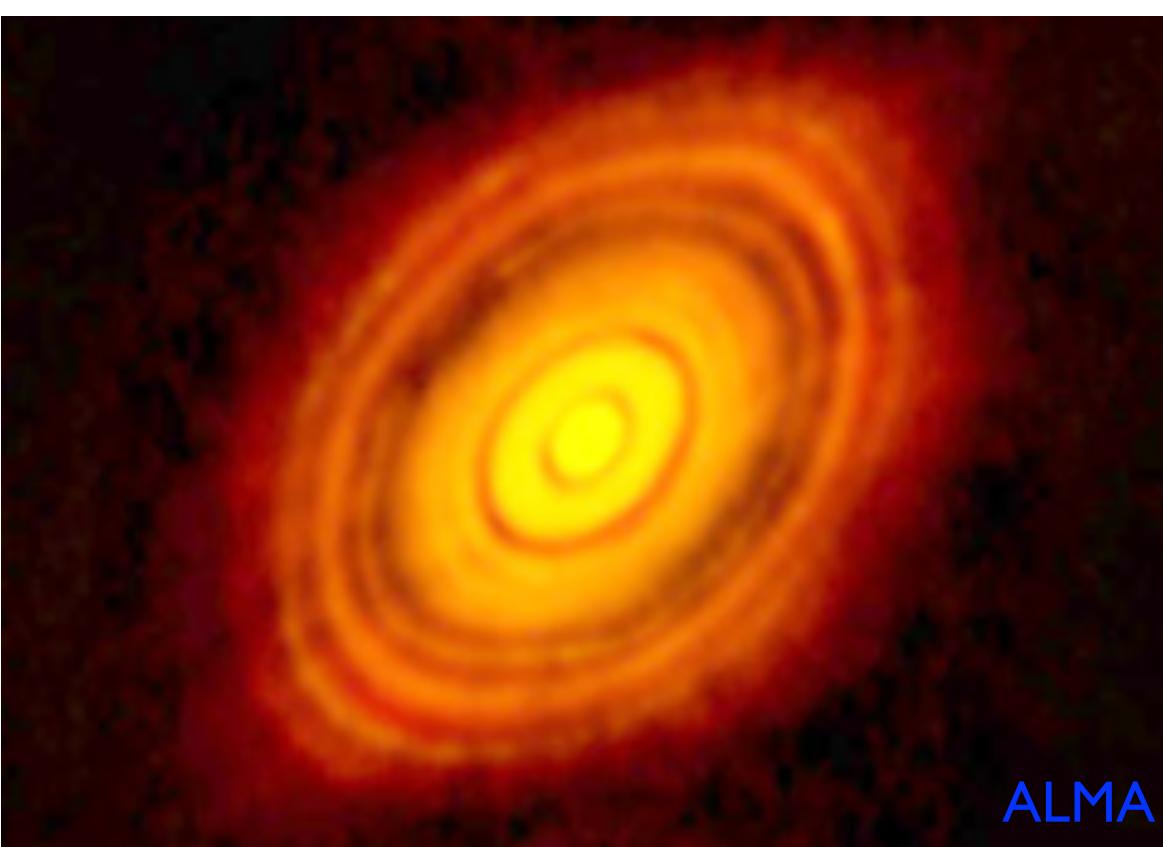
Image credit:
Dust: By The original uploader was Amara at English Wikipedia. - Transferred from en.wikipedia to Commons by Common Good using CommonsHelper., CC BY 1.0, <https://commons.wikimedia.org/w/index.php?curid=6267225>
Pebble: Eco outdoor
Ryugu: JAXA

The core accretion model

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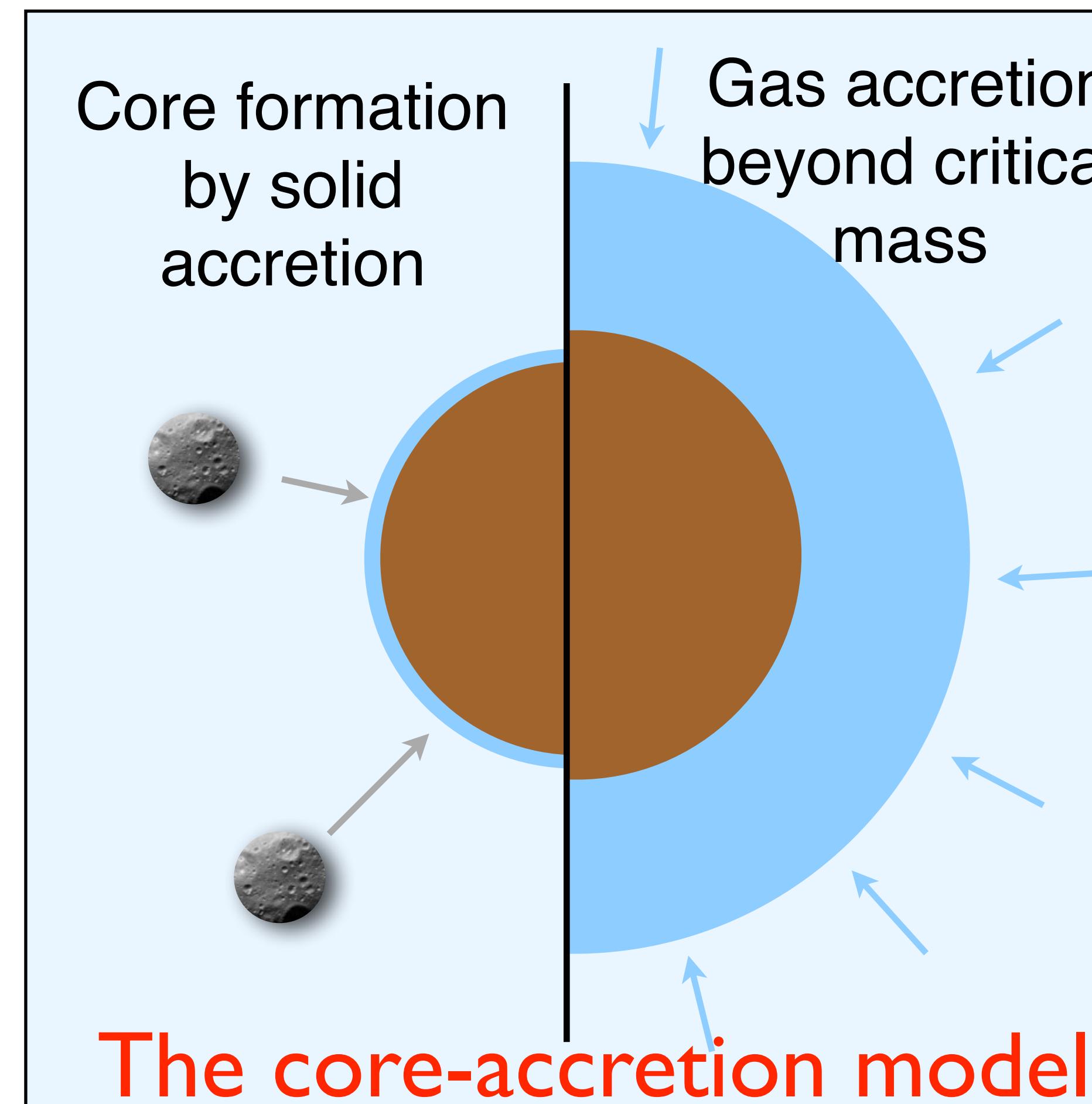
SPACE AND
CITY



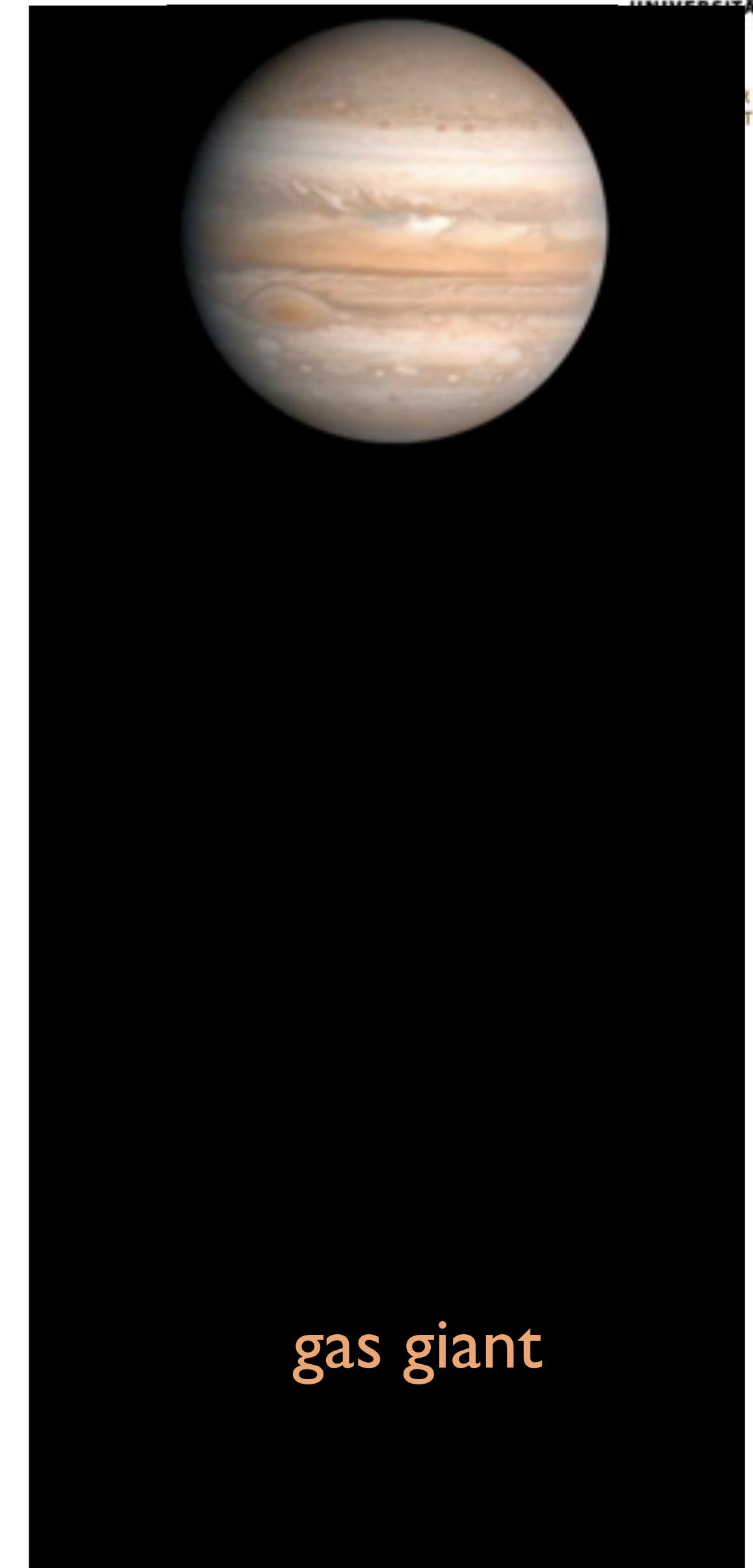
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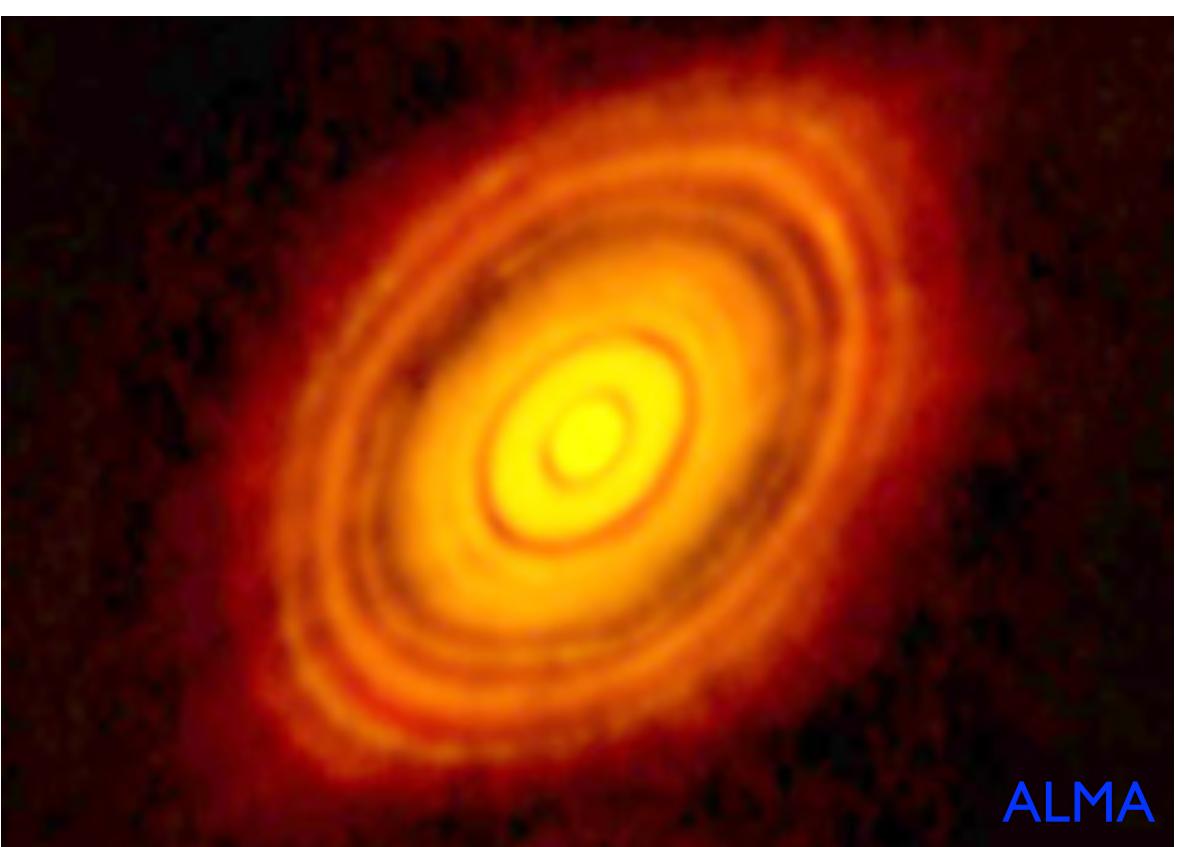


gas giant



The core accretion model

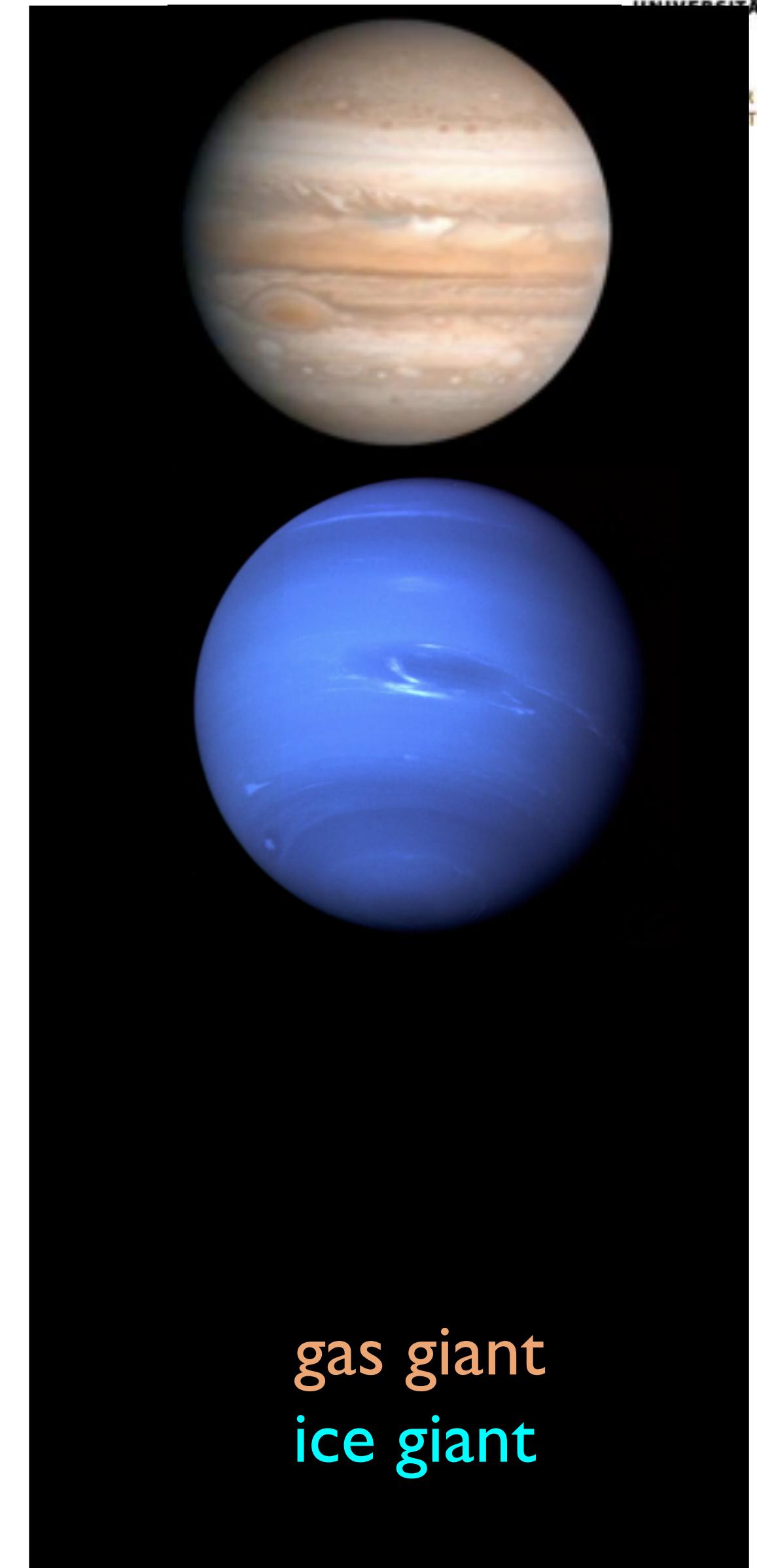
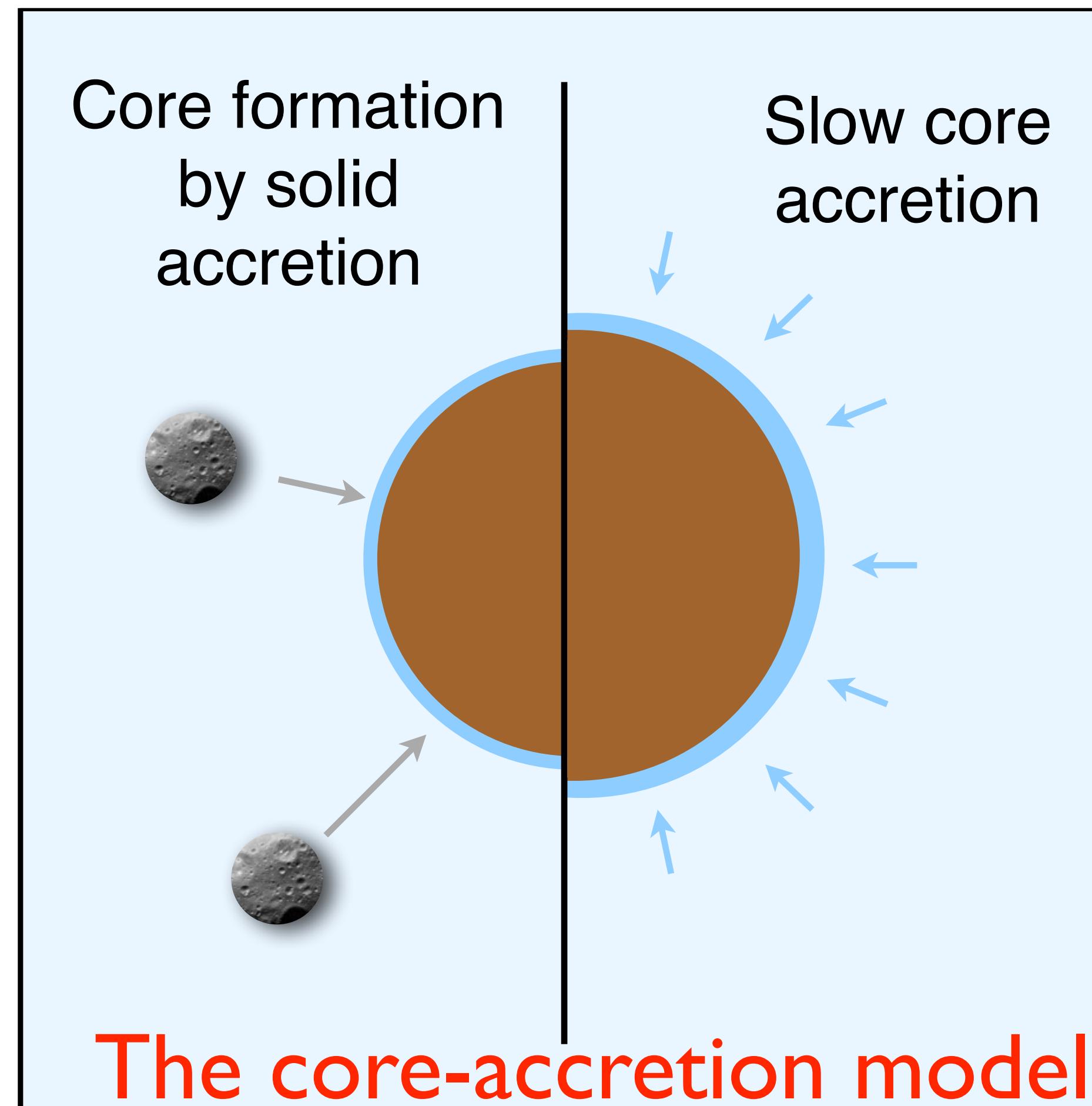
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$\sim 100s$ AU

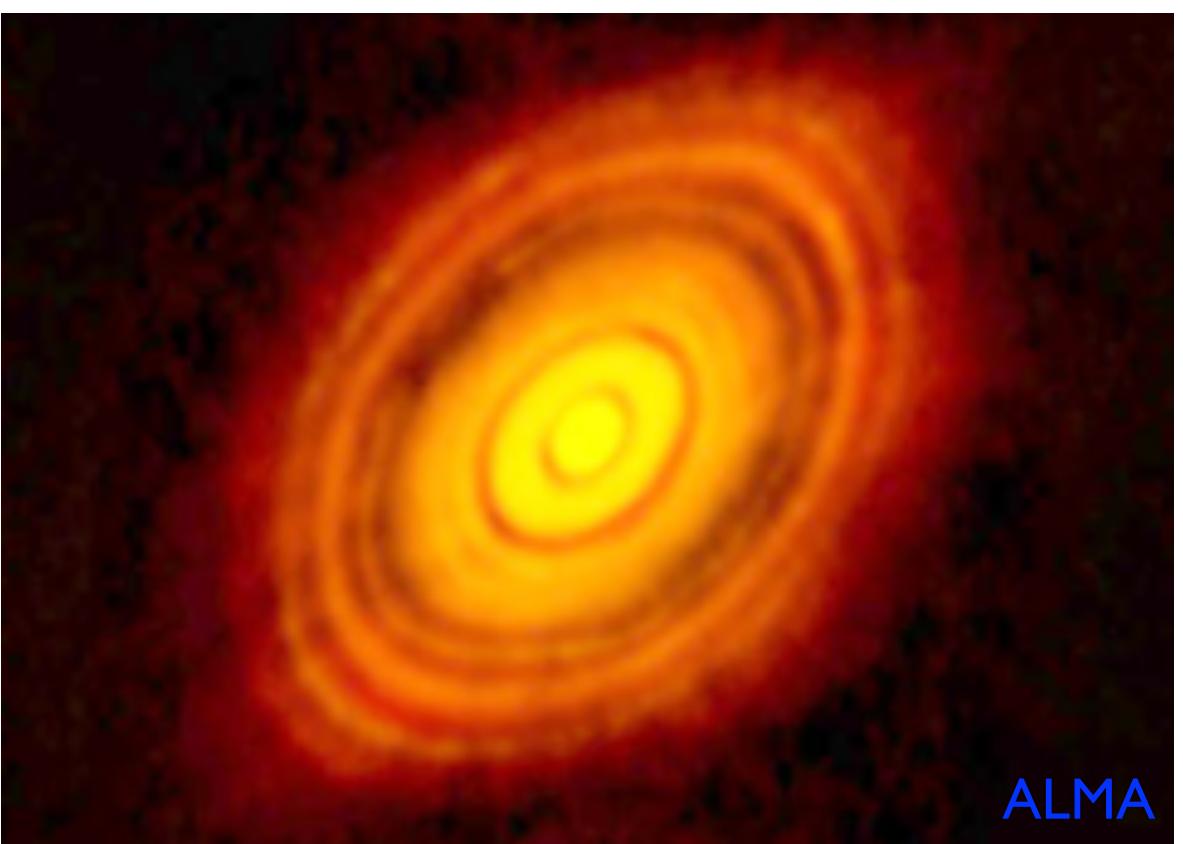
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The core accretion model

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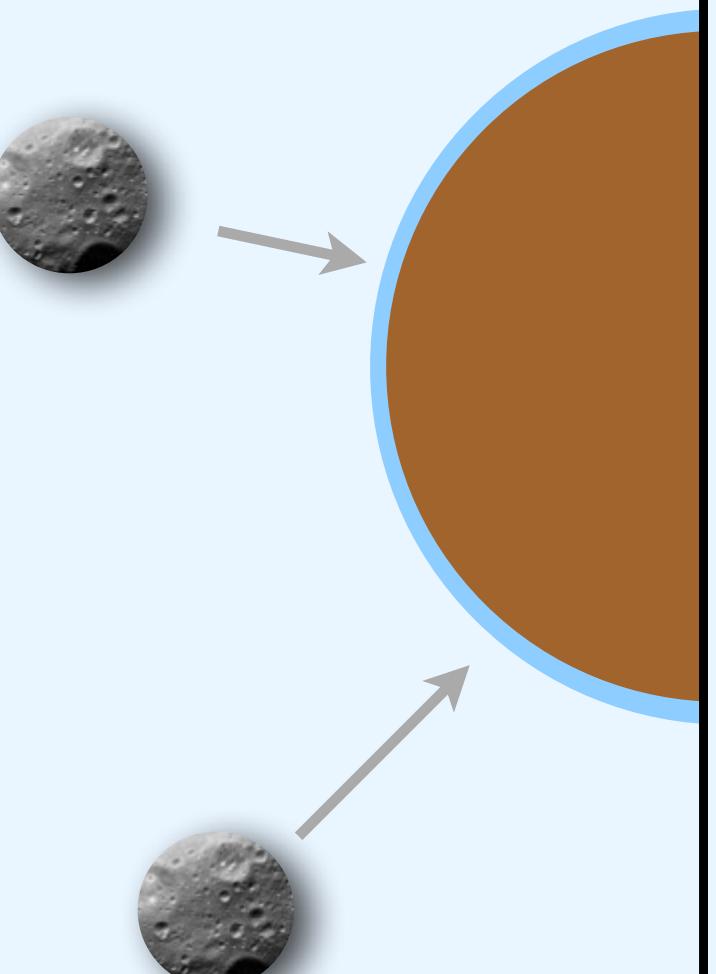


~ 100 s AU

99% gas 1% solids

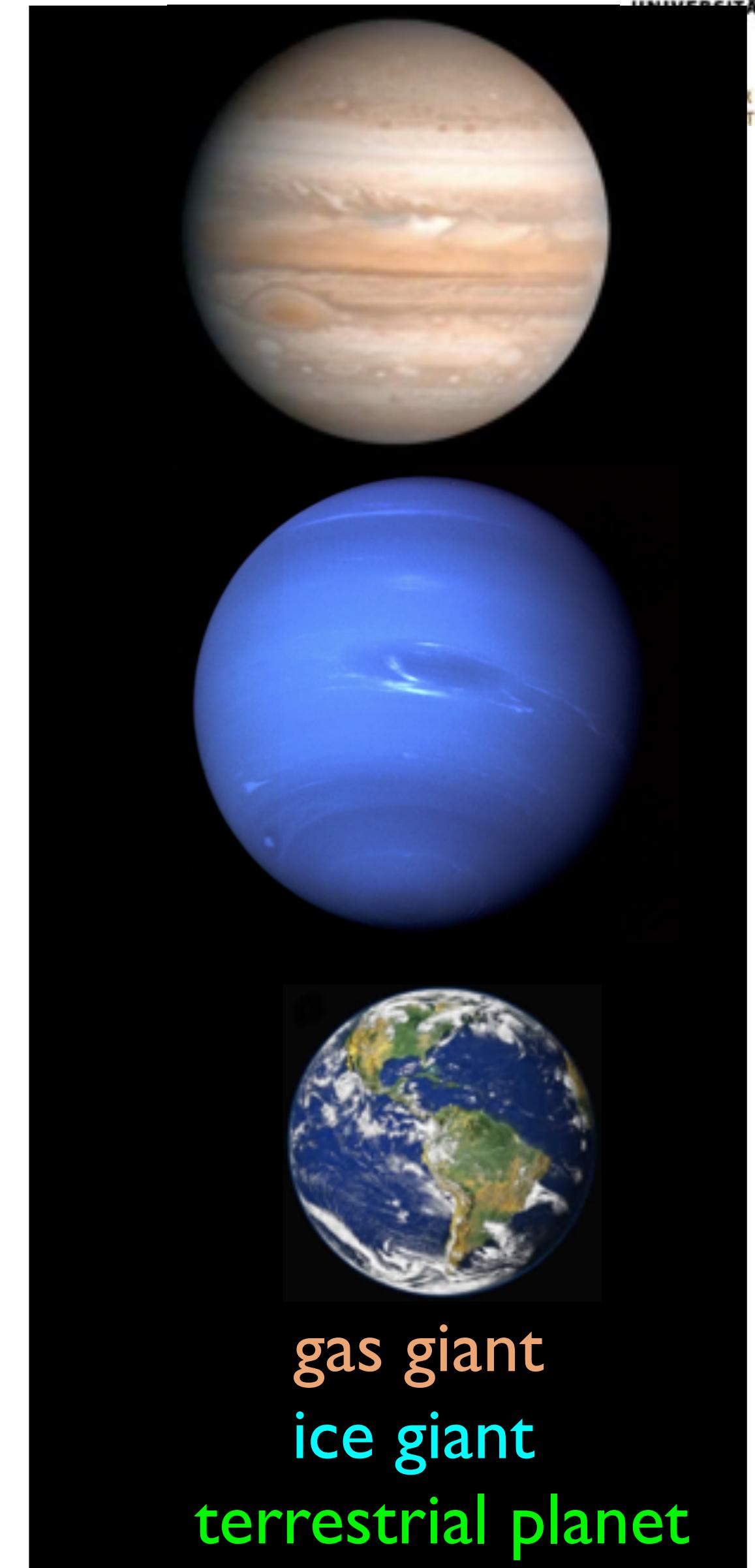
$T_{\text{disk}} < 10^7 \text{ yr}$

Core formation
by solid
accretion



The core-accretion model

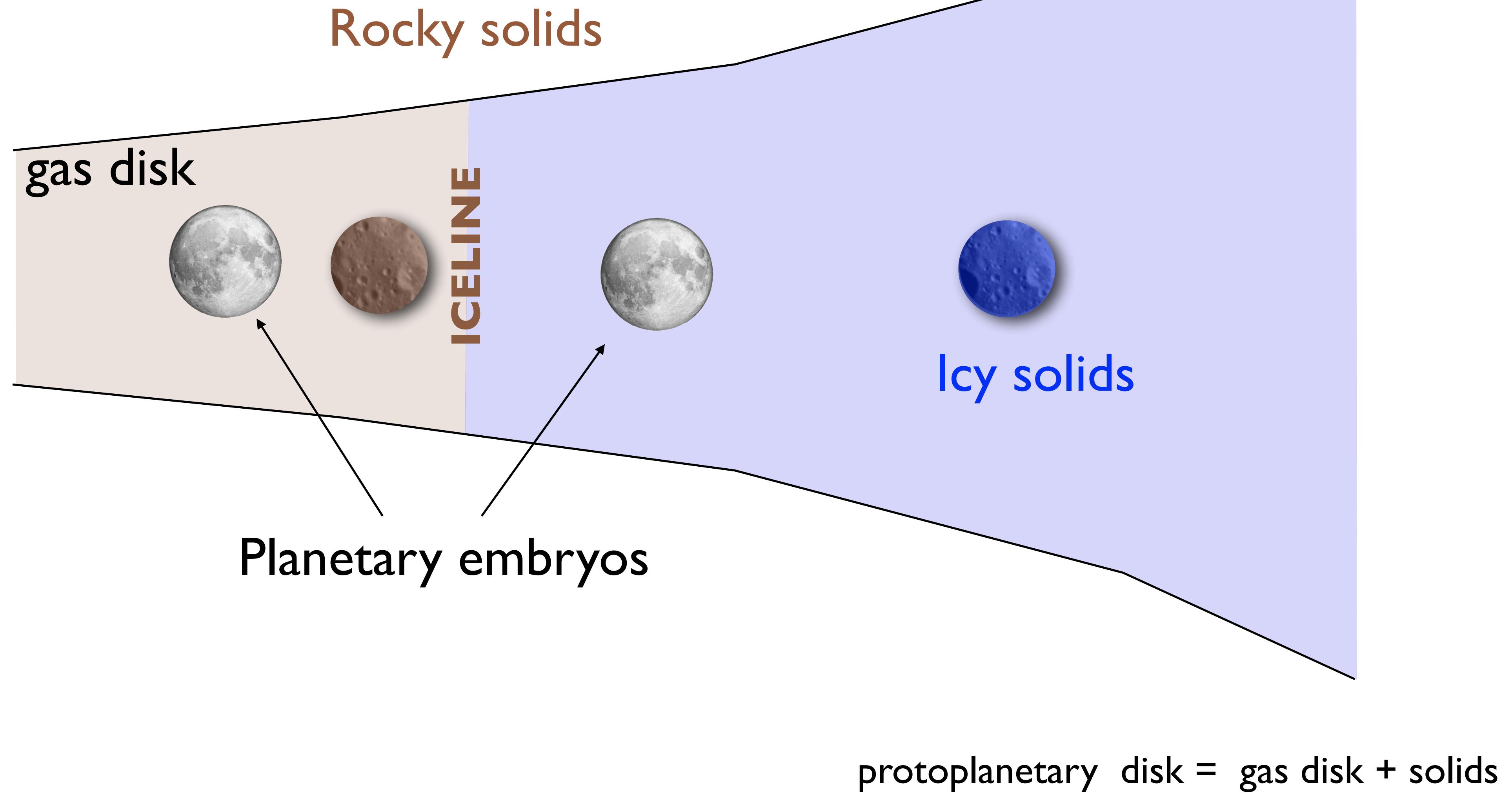
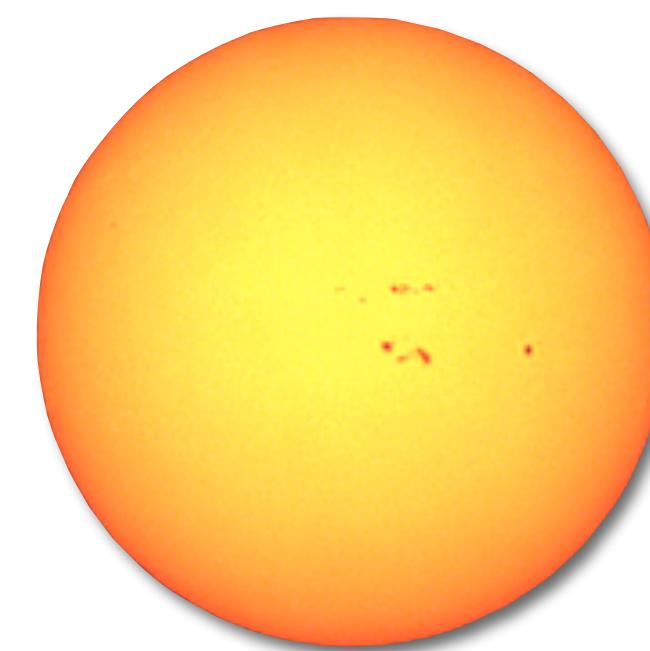
Jupiter: NASA/JPL/USGS
Neptune: NASA/JPL
Earth: NASA



The Bern model

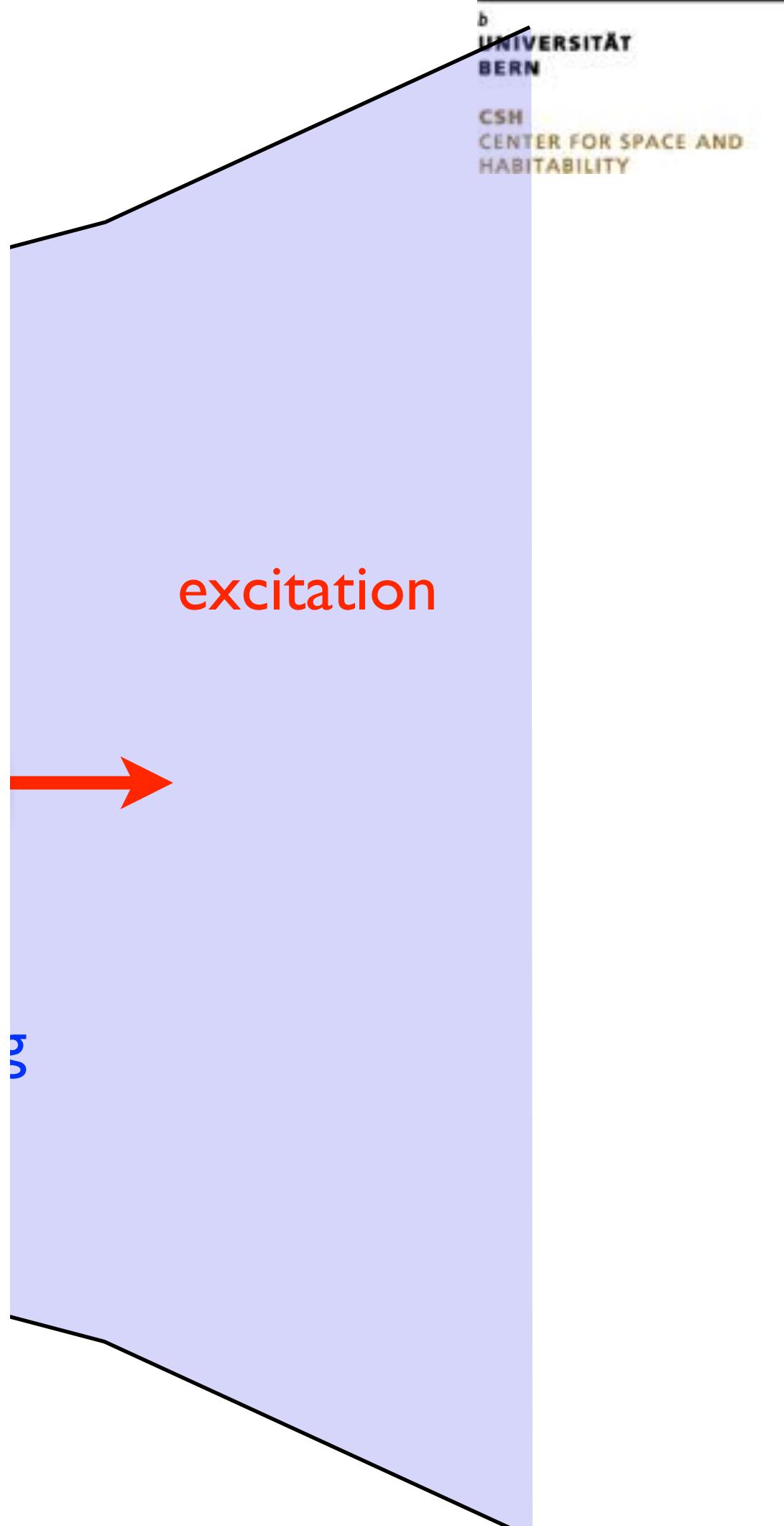
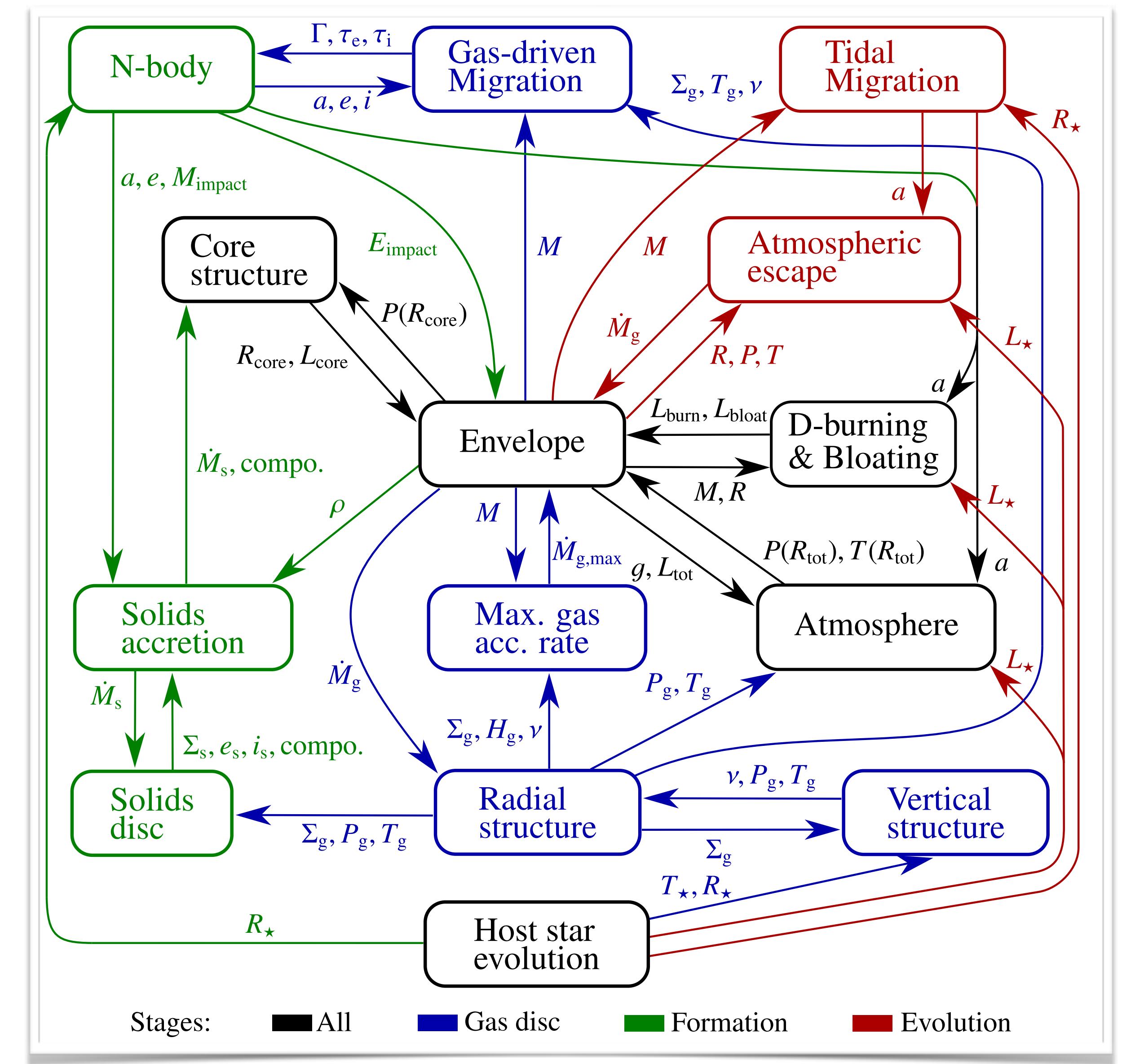
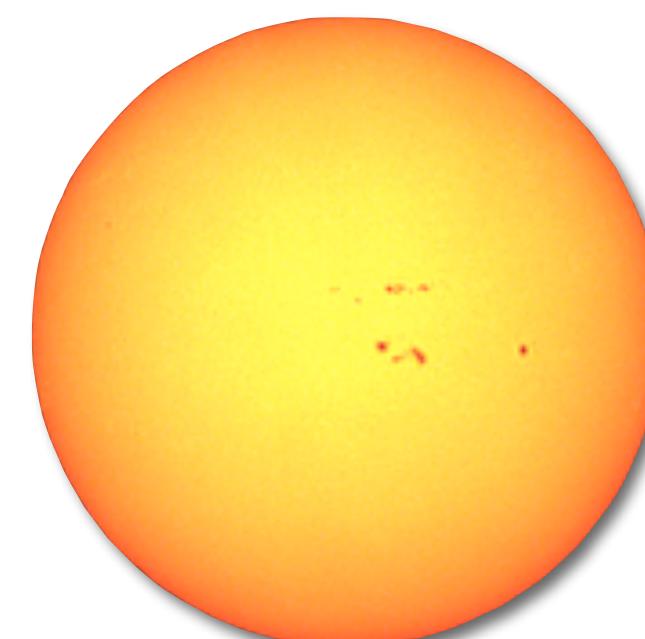
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Seen from the edge



The Bern model

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The Bern model - planetary population

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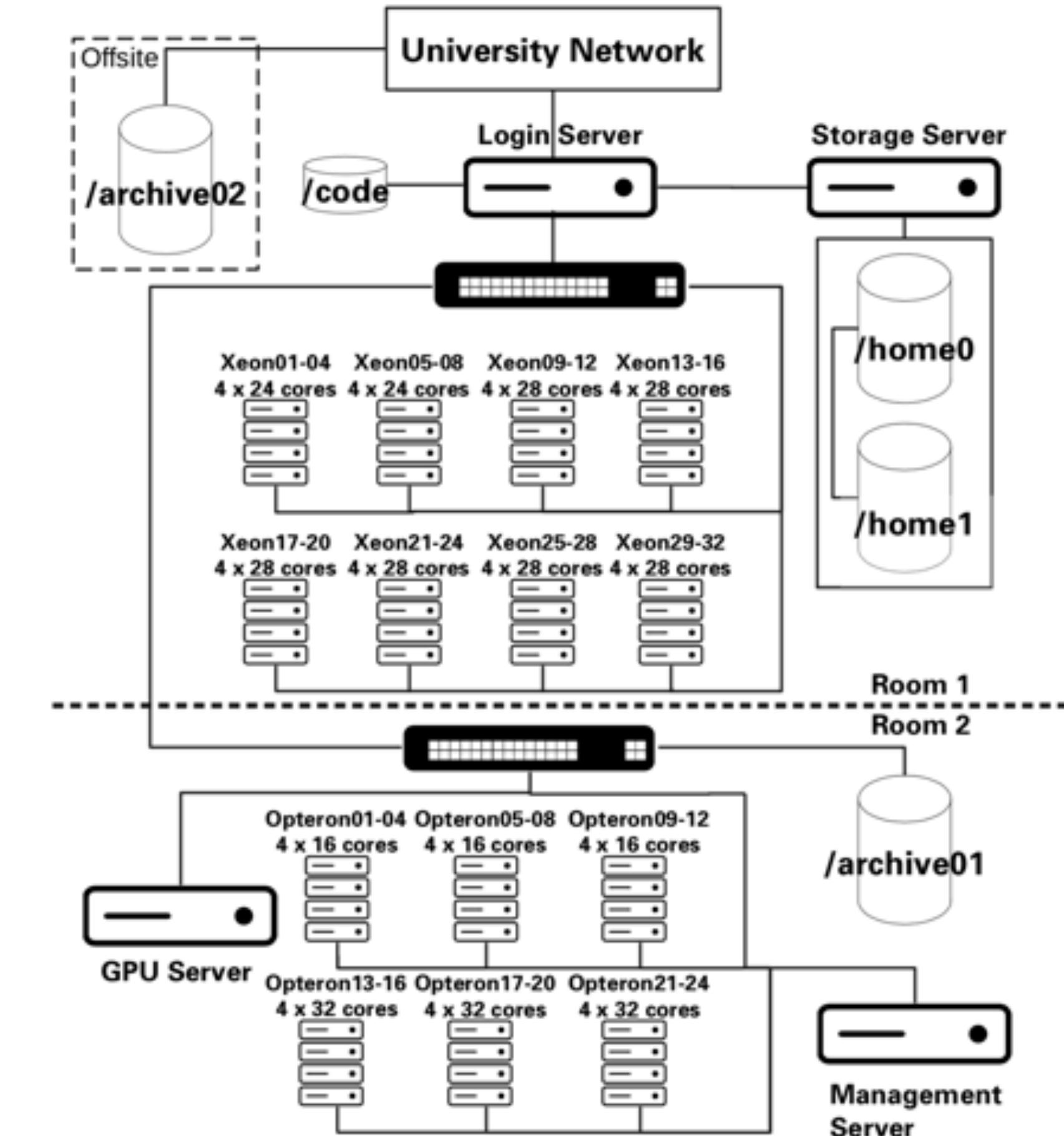
1000 systems

Starting with 100 planetary embryos

All stars are solar

Disk properties follow observations

~1 Million CPU hours



J. Haldemann, PhD Thesis

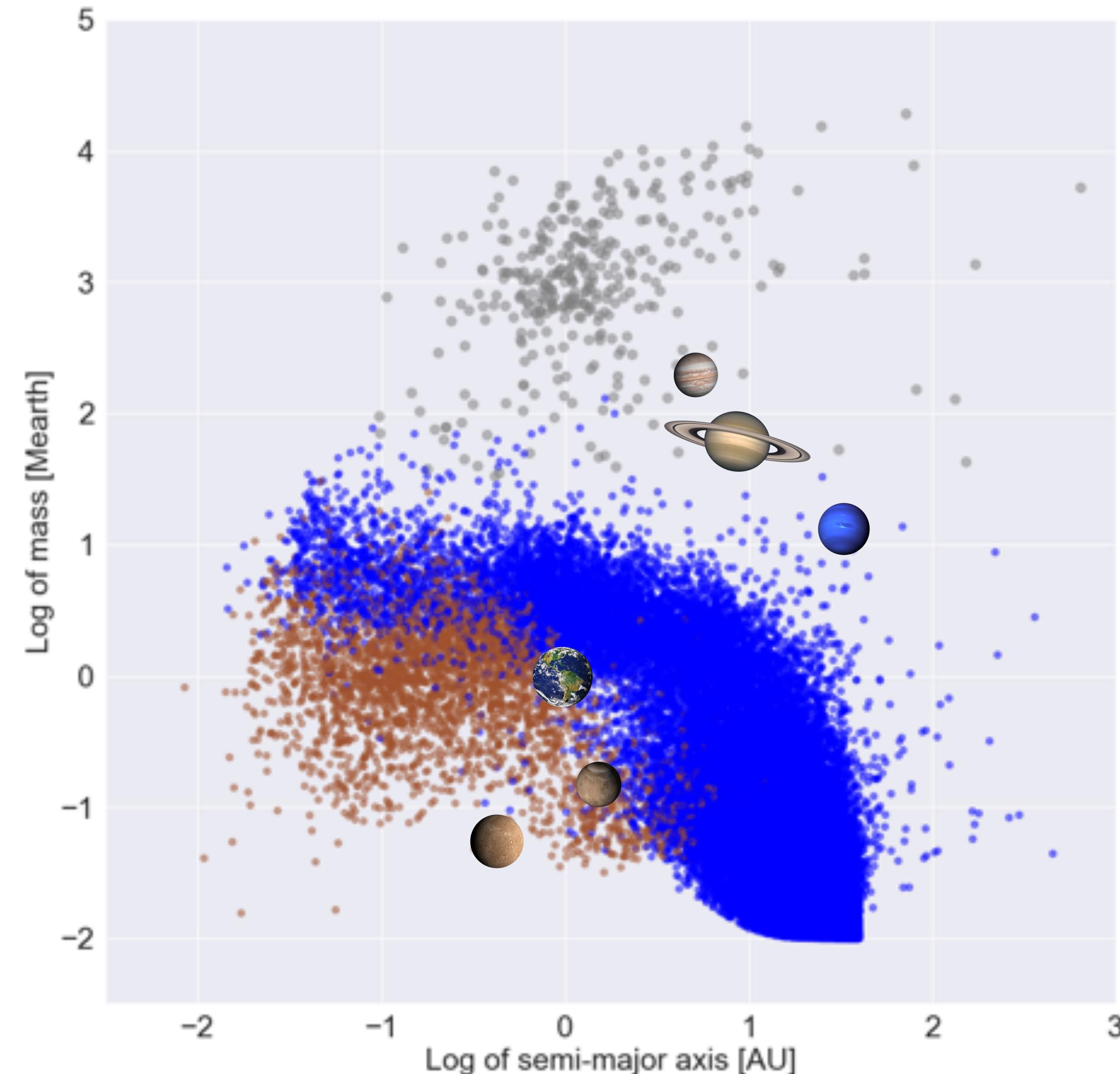
Adapted from Emsenhuber et al., 2021

The Bern model - planetary population

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- Gas giant
More than 50 wt% in gas
- Rocky planet
Less than 50 wt% in gas
- Less than 1 wt% in volatiles
- Icy planet
Less than 50 wt% in gas
- More than 1 wt% in volatiles

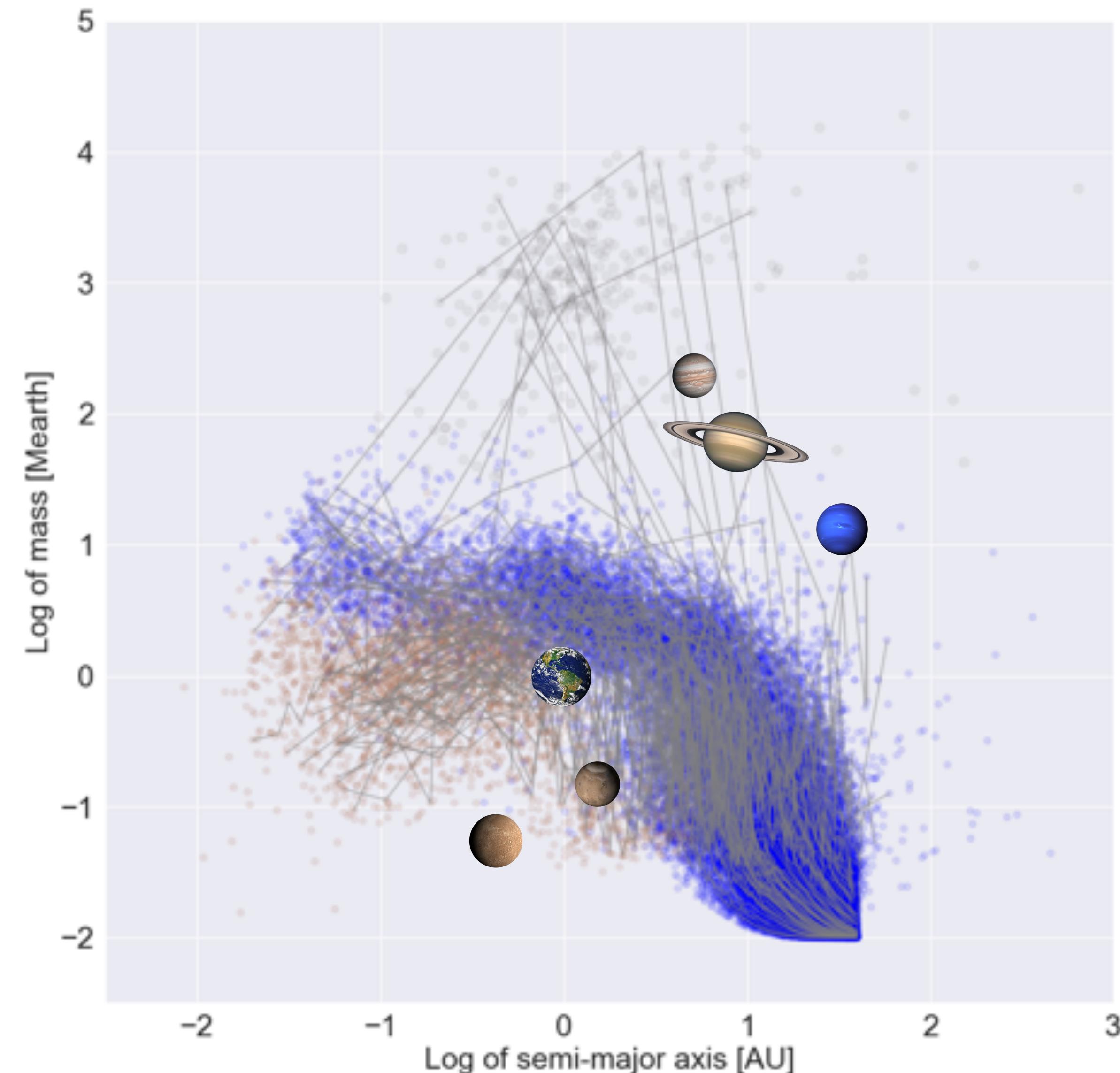
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The Bern model - planetary systems

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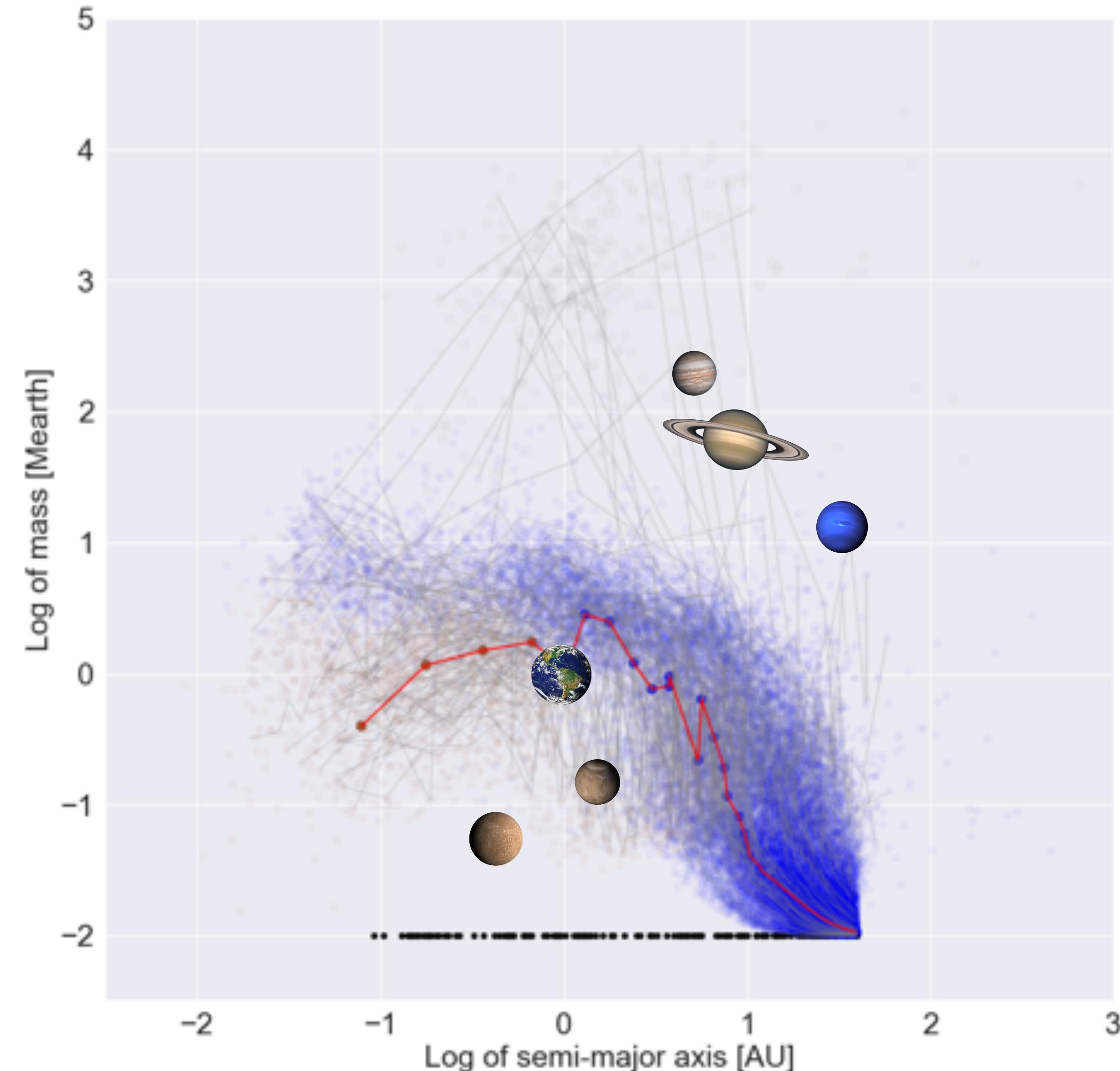
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The Bern model - planetary systems

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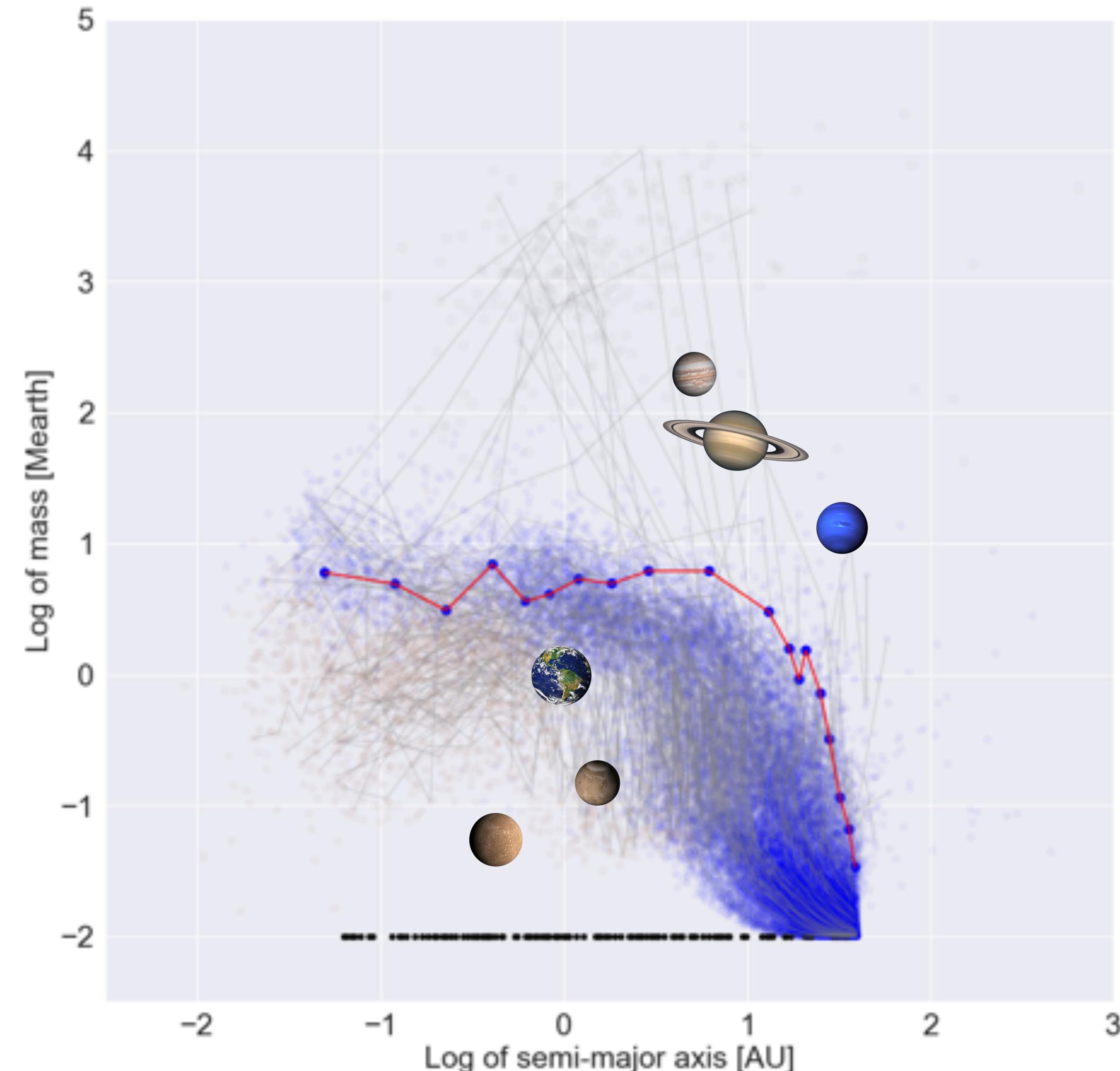
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The Bern model - planetary systems

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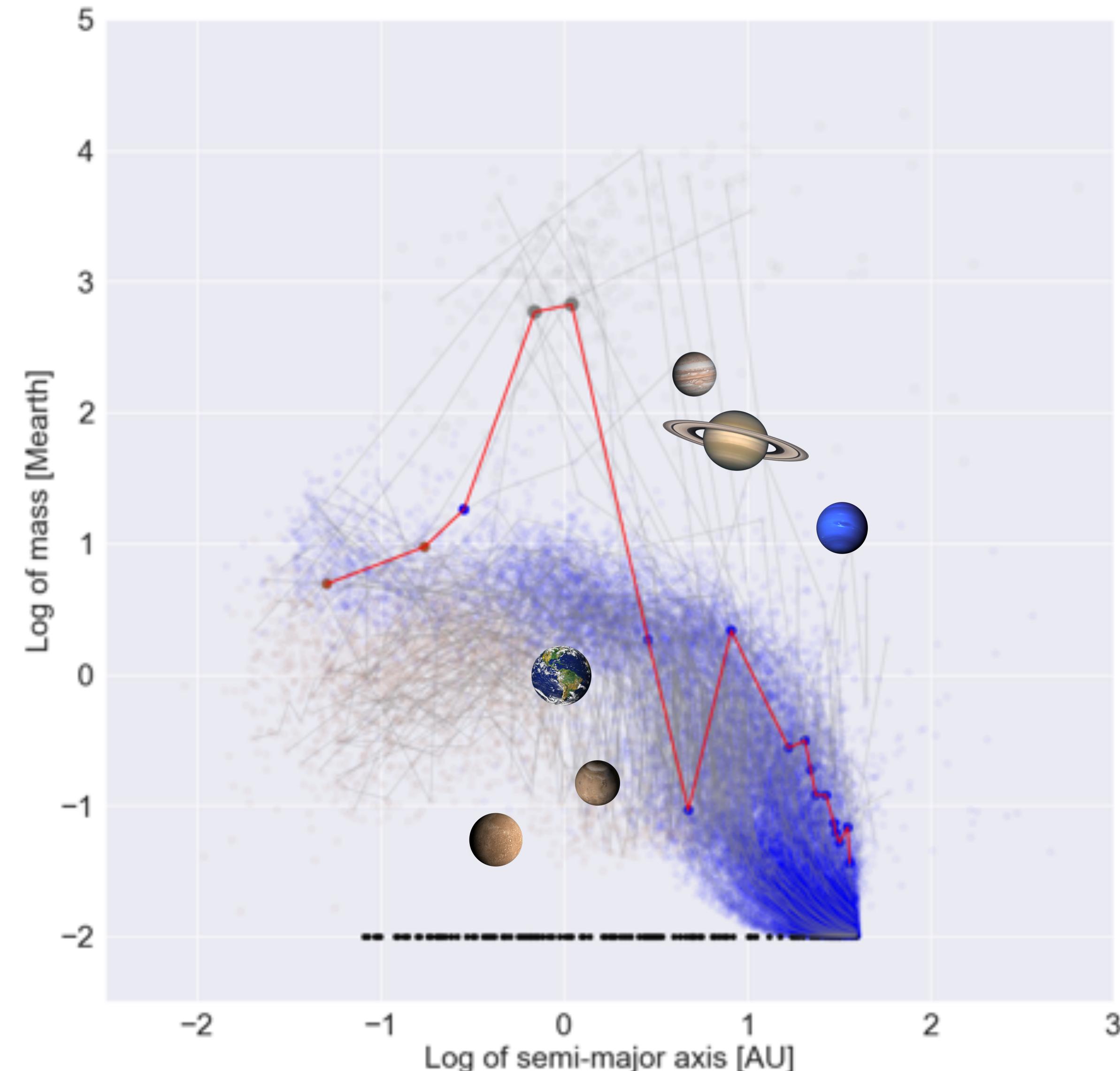
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The Bern model - planetary systems

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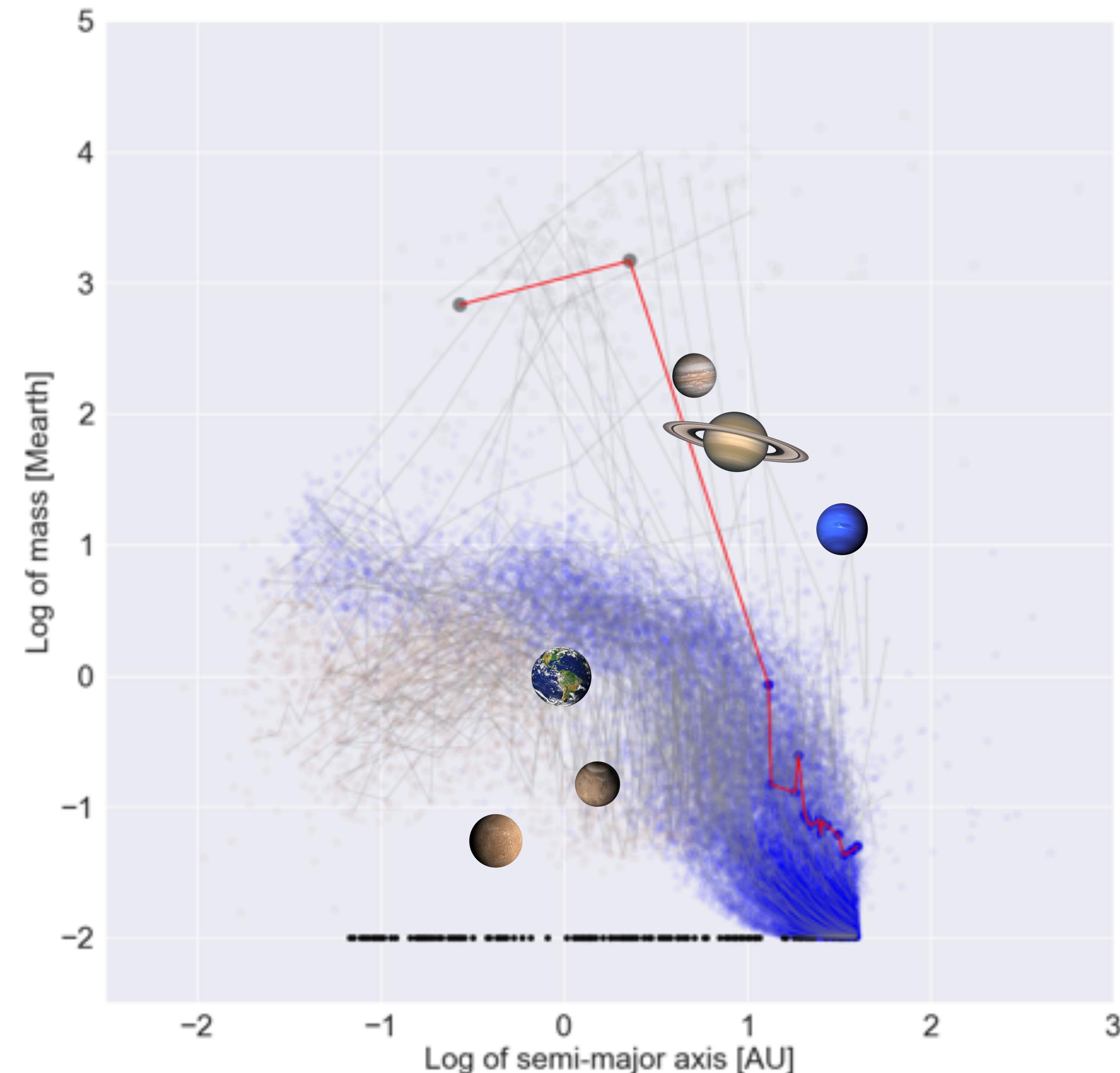


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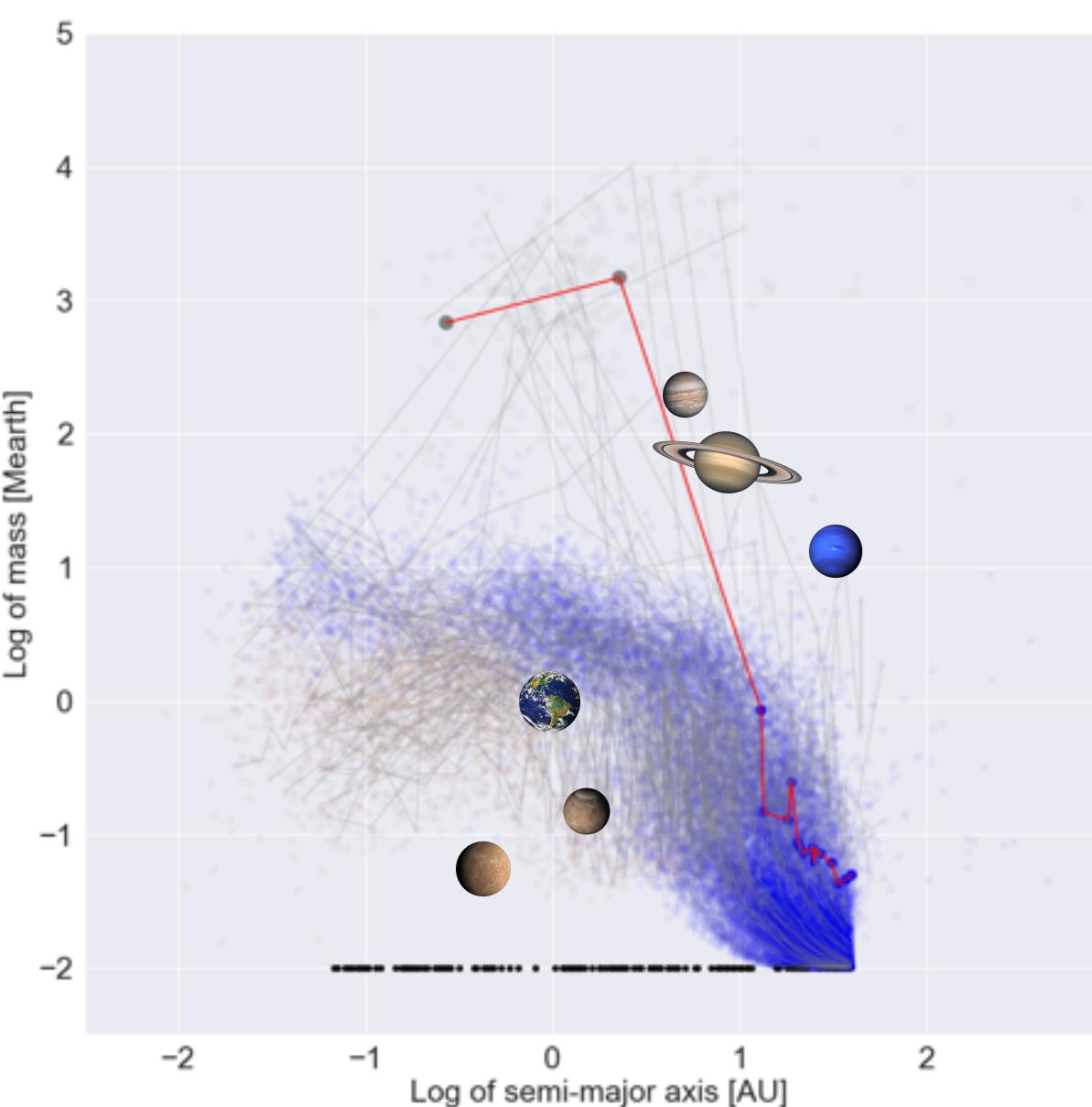
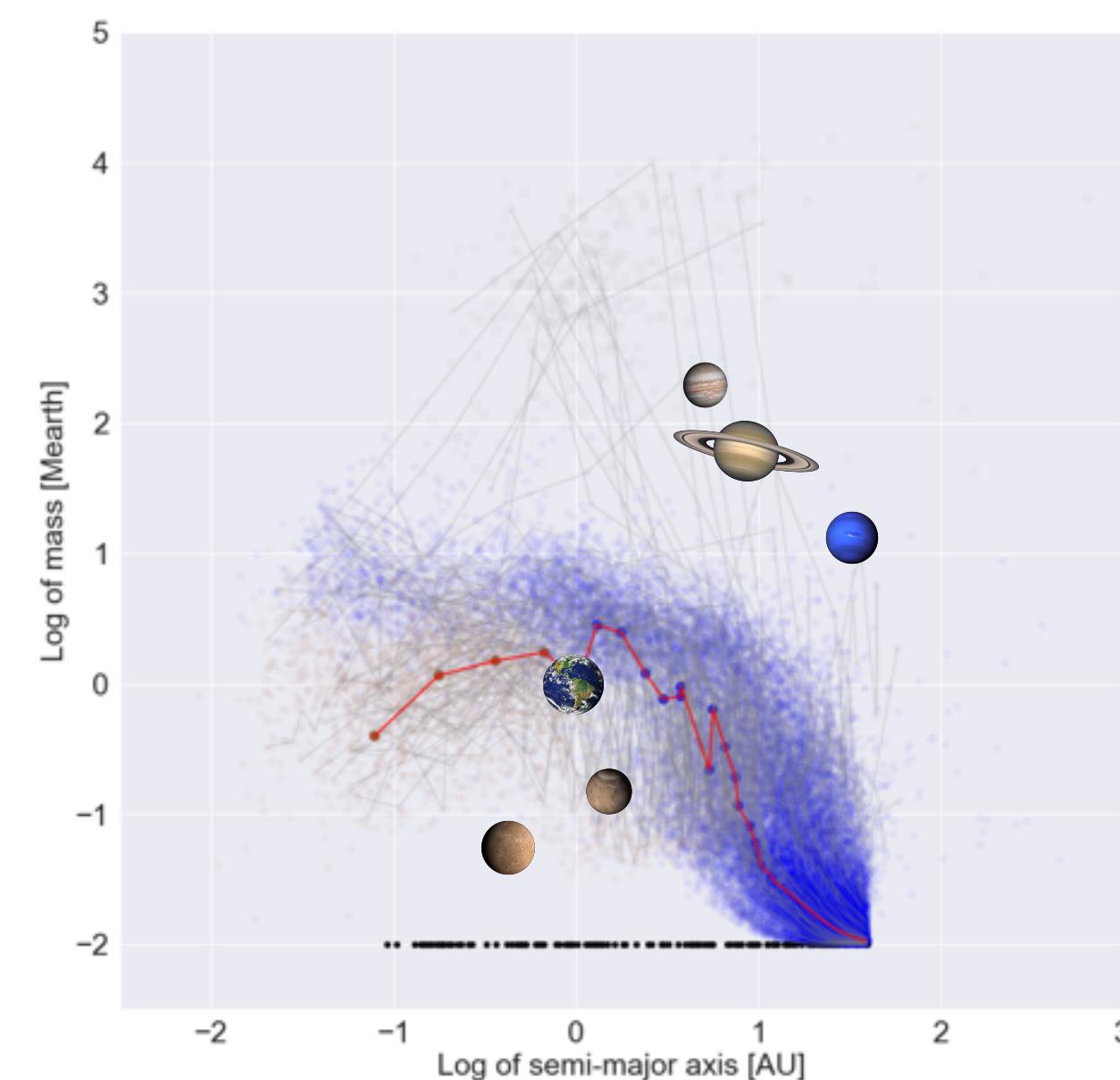
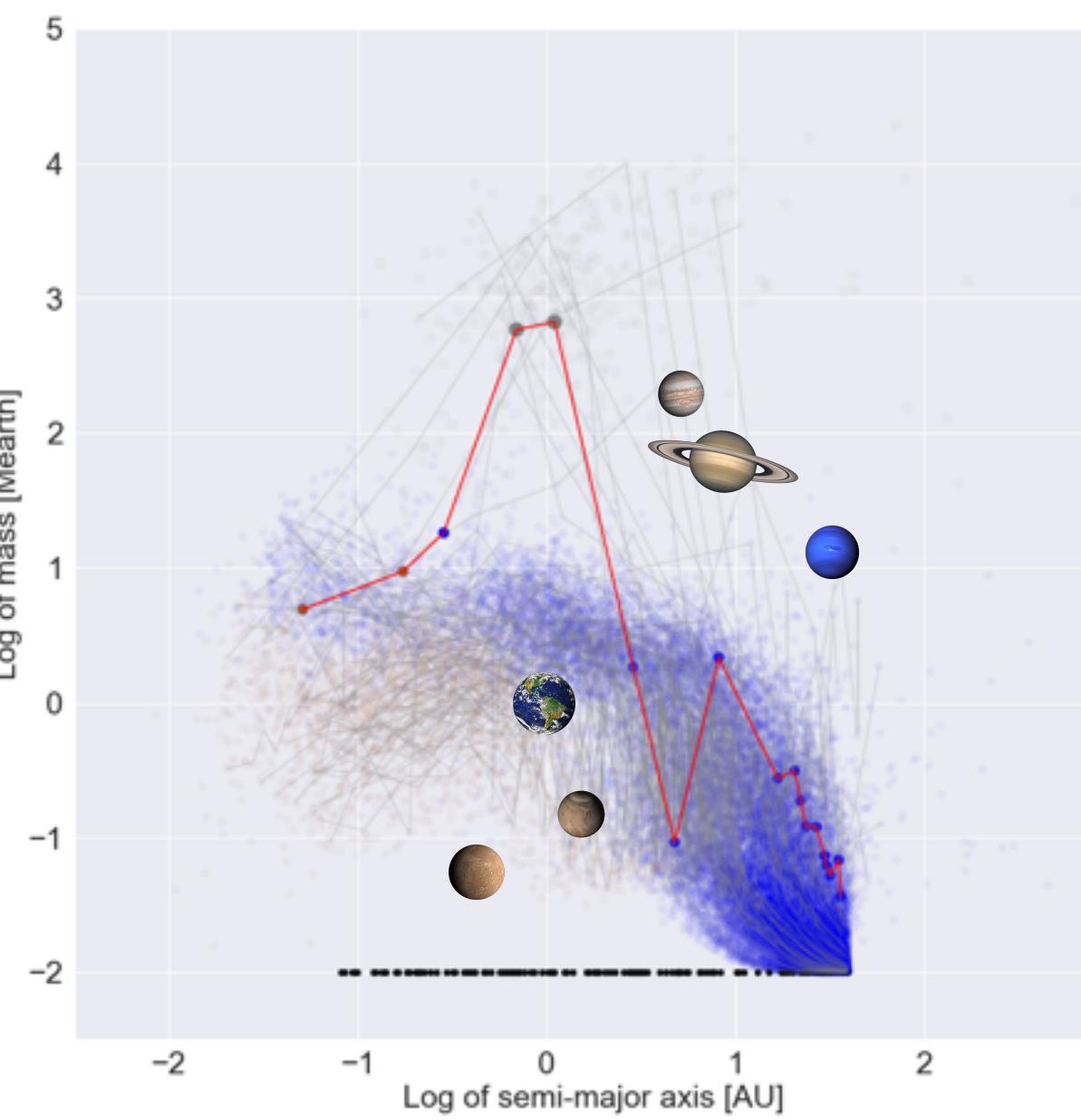
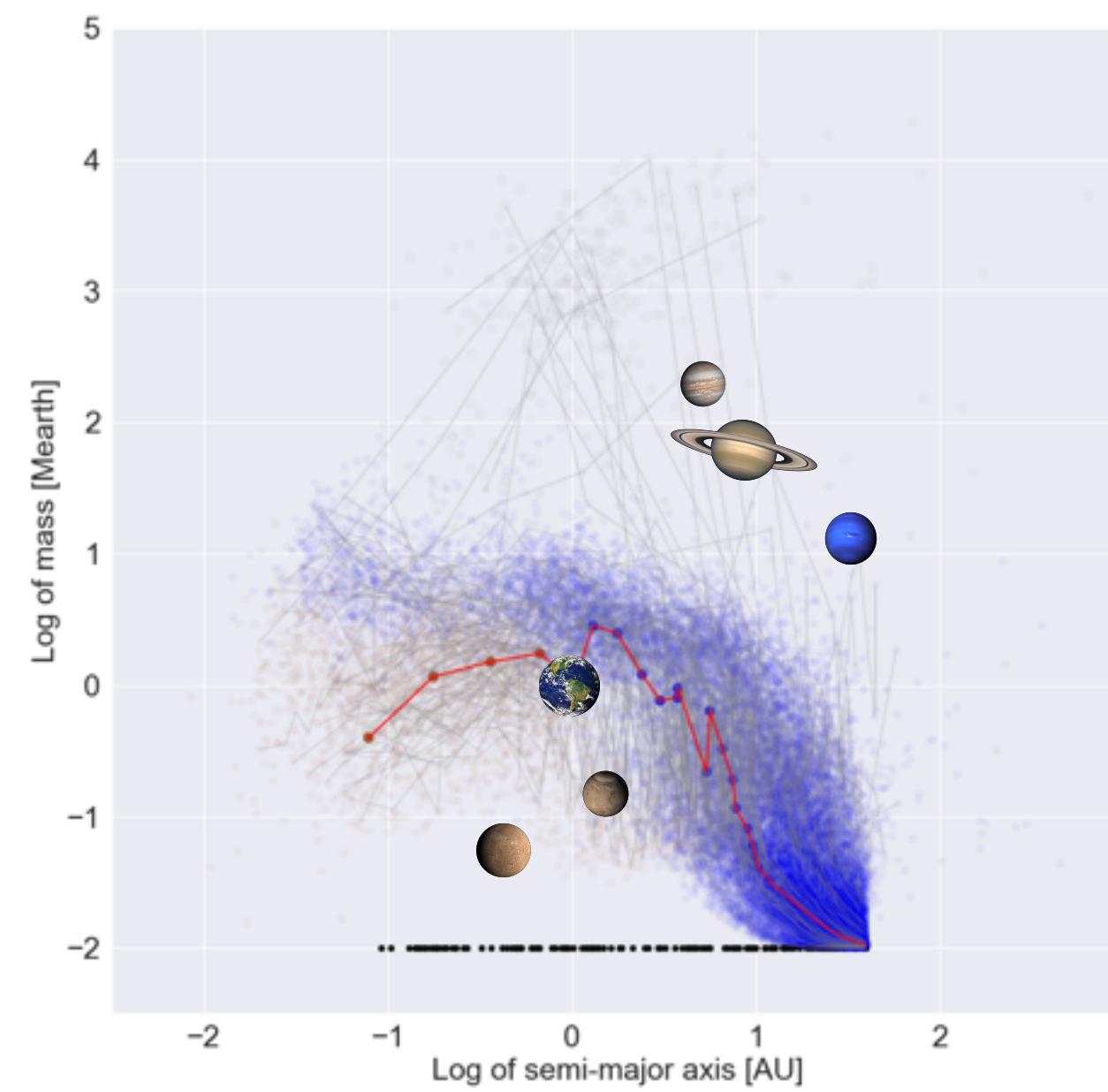
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The Bern model - planetary systems

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Which of the four systems looks more similar to the solar system?

1- Planet formation and the Bern model

2- Models *versus* observations

3- Planetary internal structure and Deep Learning

4- Correlation in planetary systems with random forest: finding a second Earth

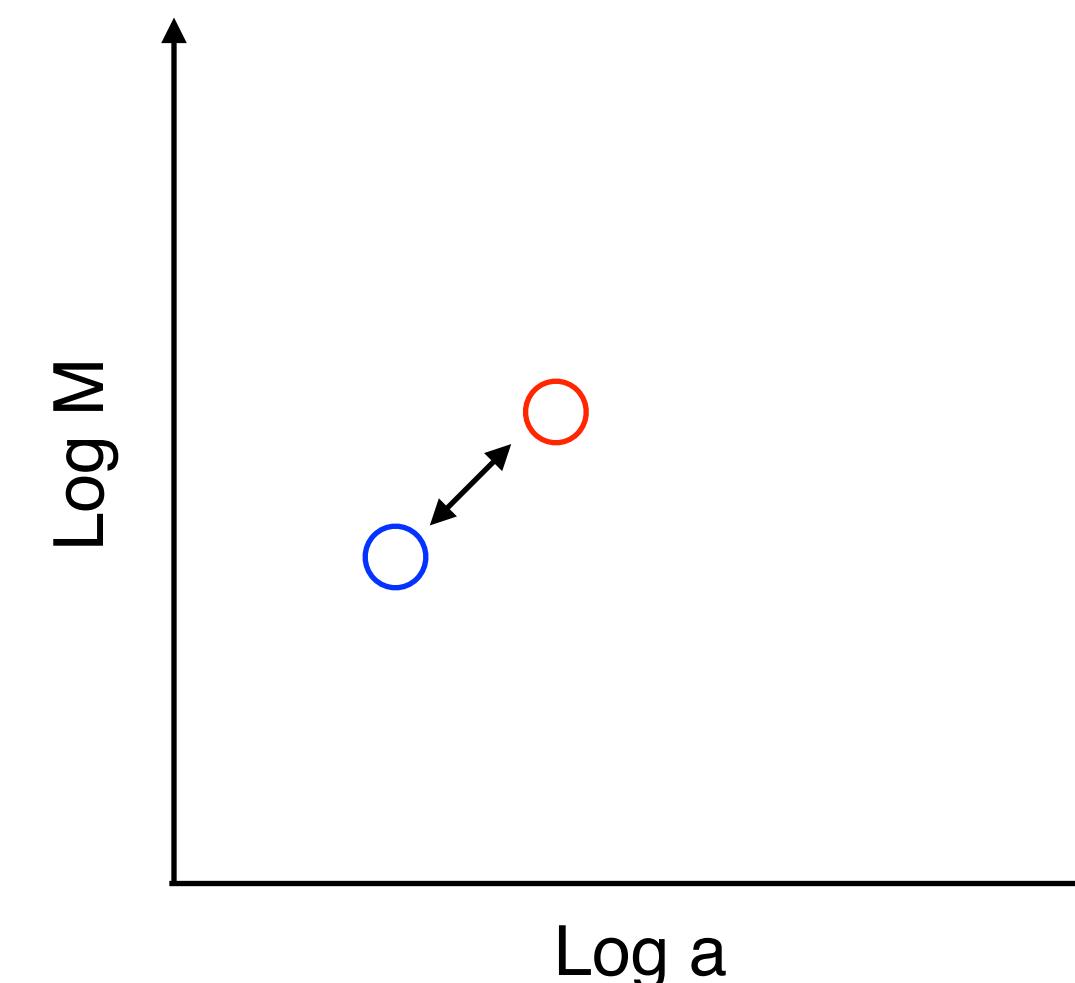
Distance between 2 systems - 1-planet case

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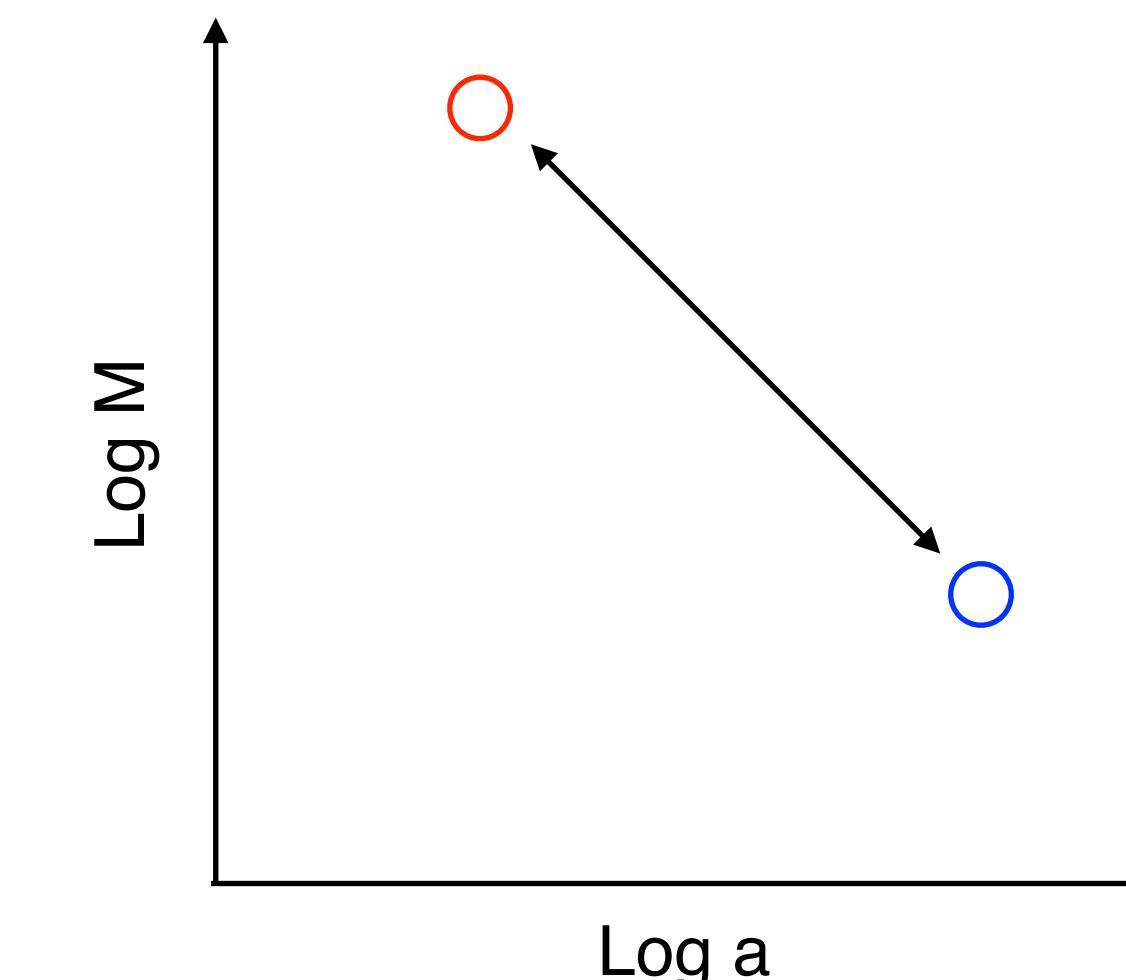
In the case $N=1$, the easiest concept of distance is the Euclidian distance in the $m-a$ space (we will concentrate on the case where only m and a are relevant to define a planet - an over simplistic view - but generalisation is easy).

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Very similar



Very dissimilar

As this distance is an Euclidian distance, it **is** a distance mathematically speaking!

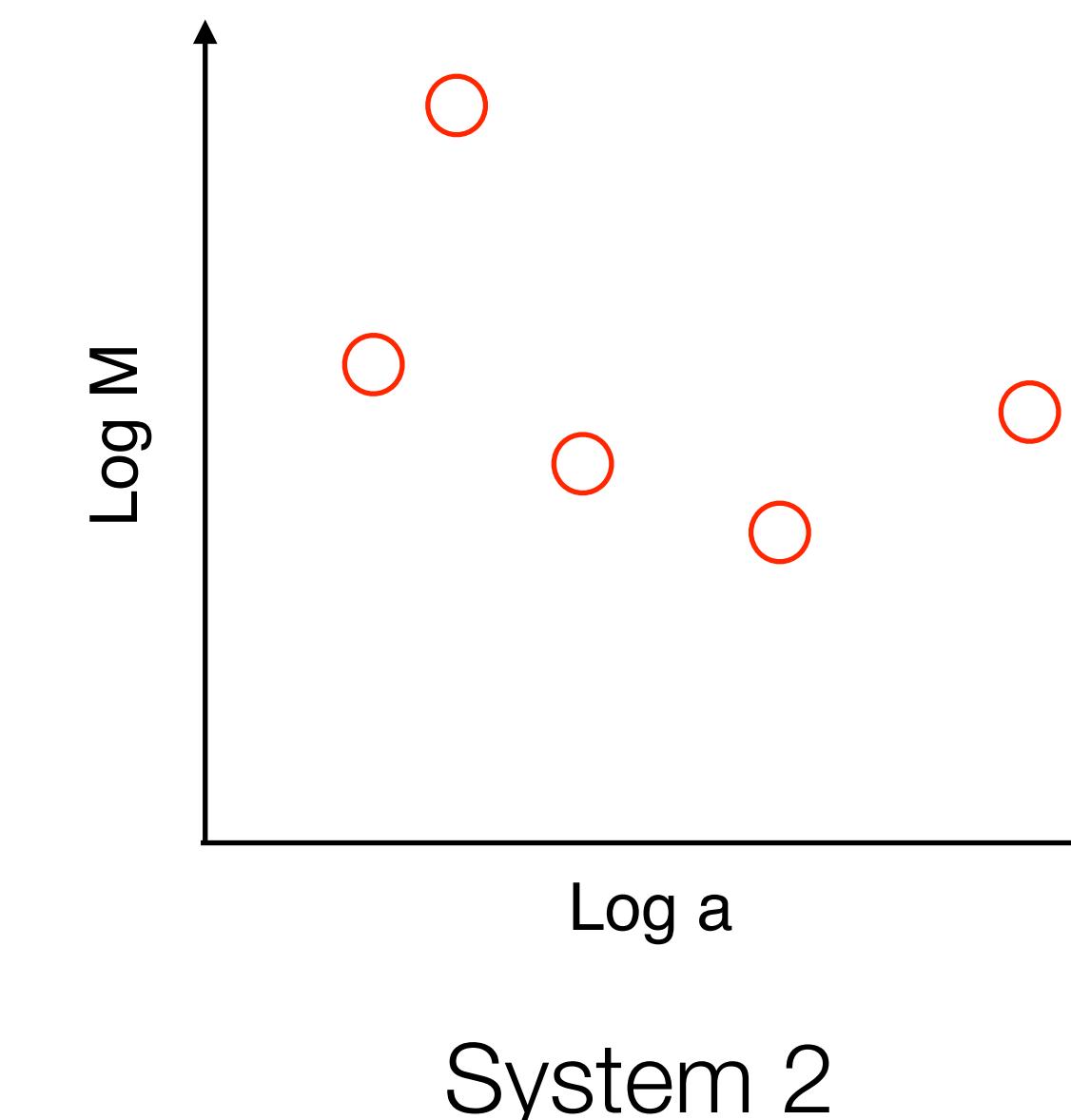
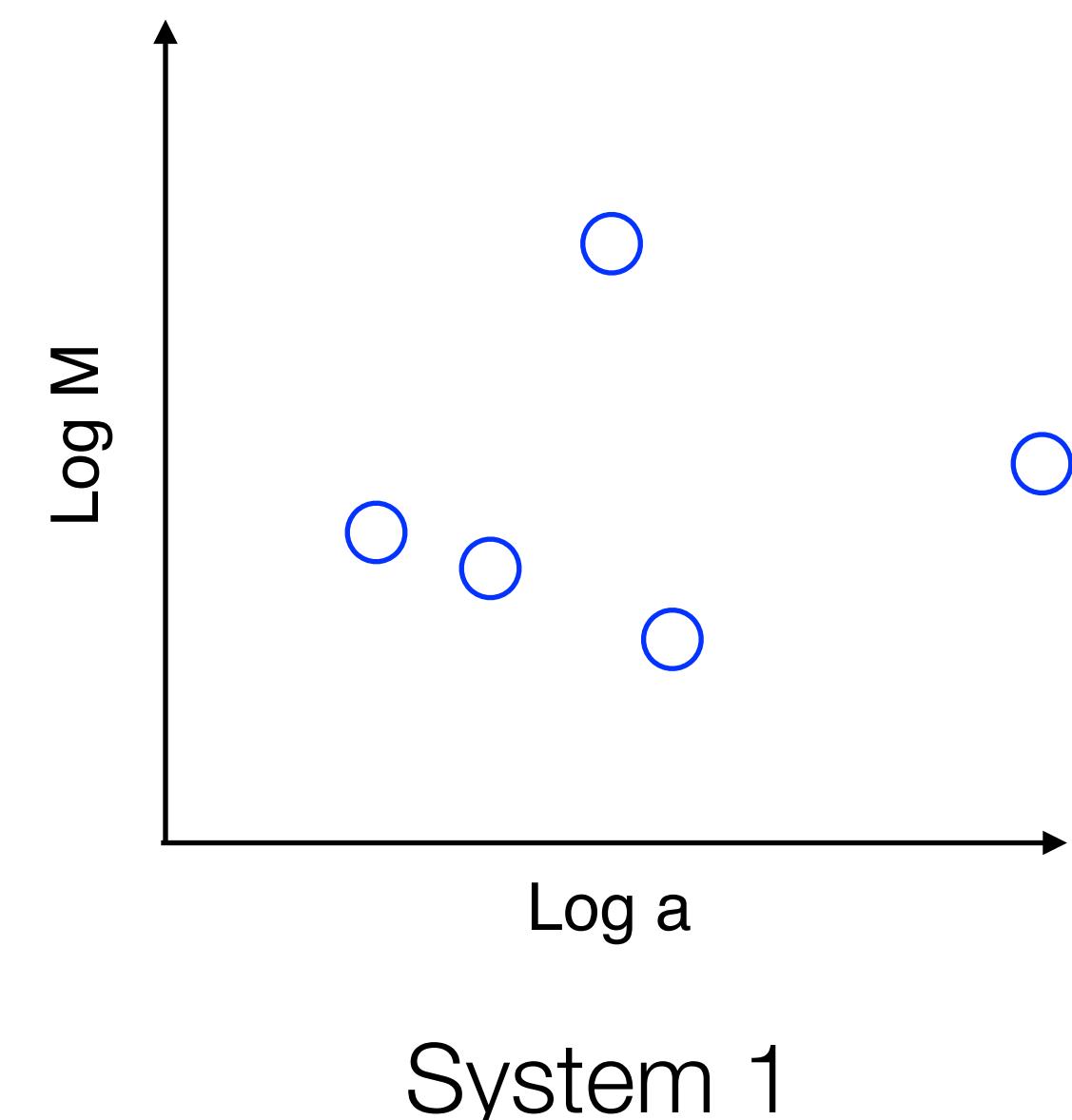
Distance between 2 systems - N-planet case

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In the case of two N-planet systems, with the same N for both, we would like to define the distance as ‘the sum of distances between one planet of one side and another planet of the other side’.



-> many different possible pairs possible -> how can we choose?

Distance between 2 systems - N-planet case

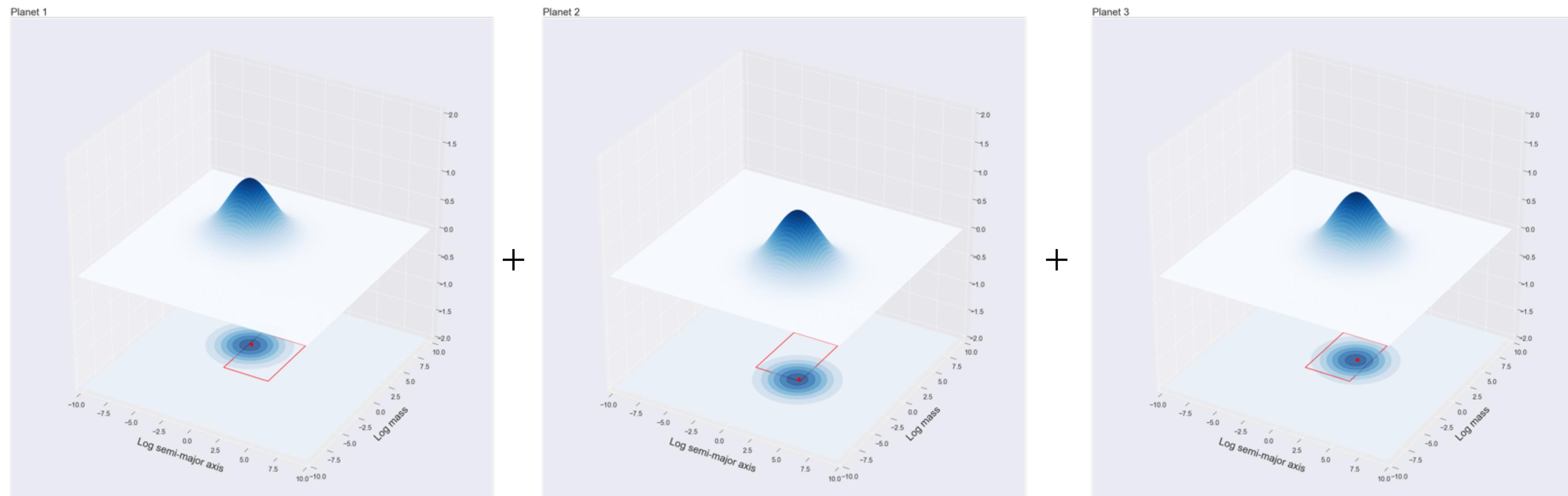
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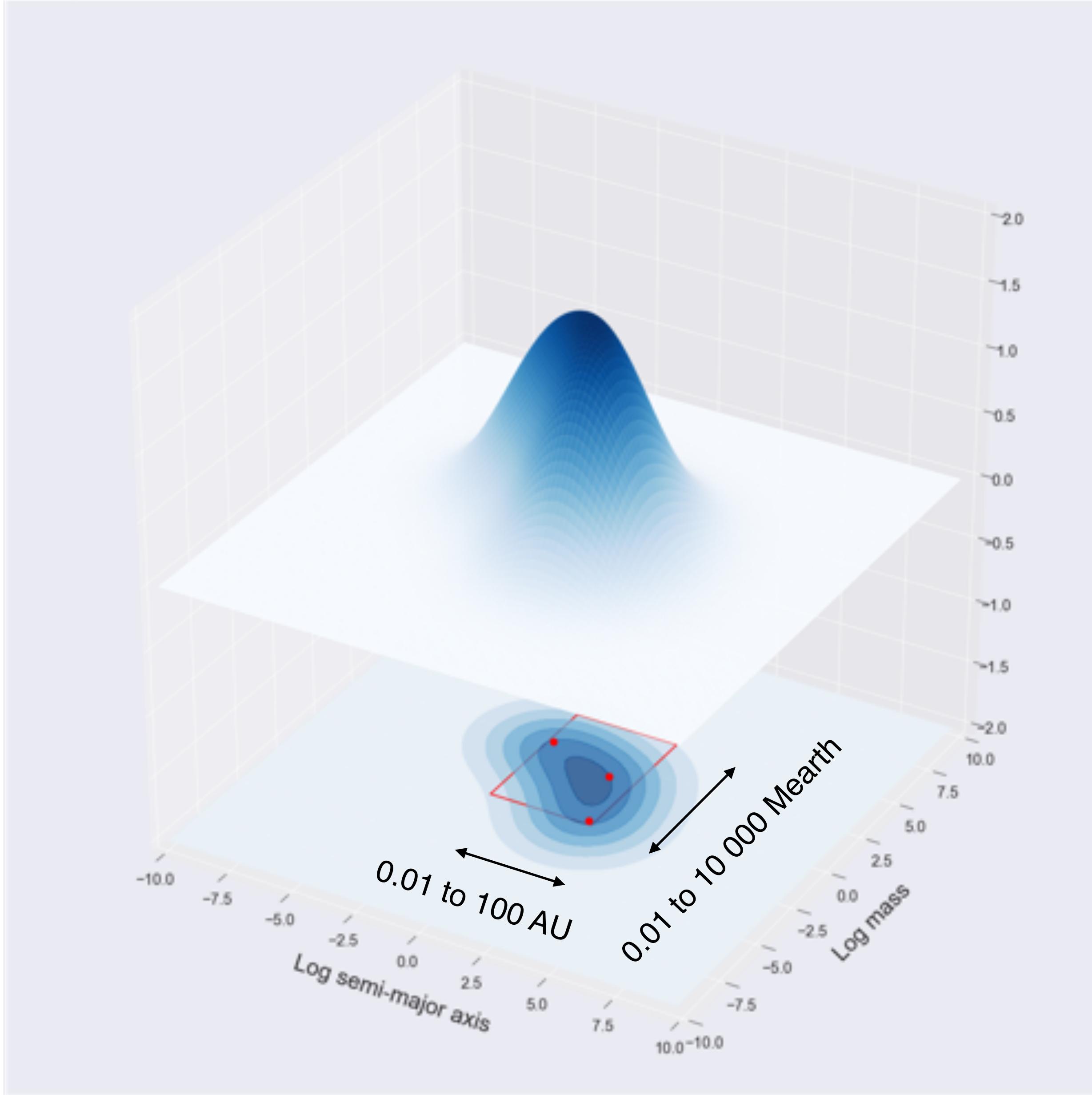
We first ‘spread’ planets in the Log(a) - Log(M) space.

$$f_p(M, a) = \exp\left(-\left(\frac{\log M - \log M_p}{2\sigma_m}\right)^2 - \left(\frac{\log a - \log a_p}{2\sigma_a}\right)^2\right)$$



Distance between 2 systems - N-planet case

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$$\psi_s(M, a) = \sum_{p \in s} f_p(M, a)$$

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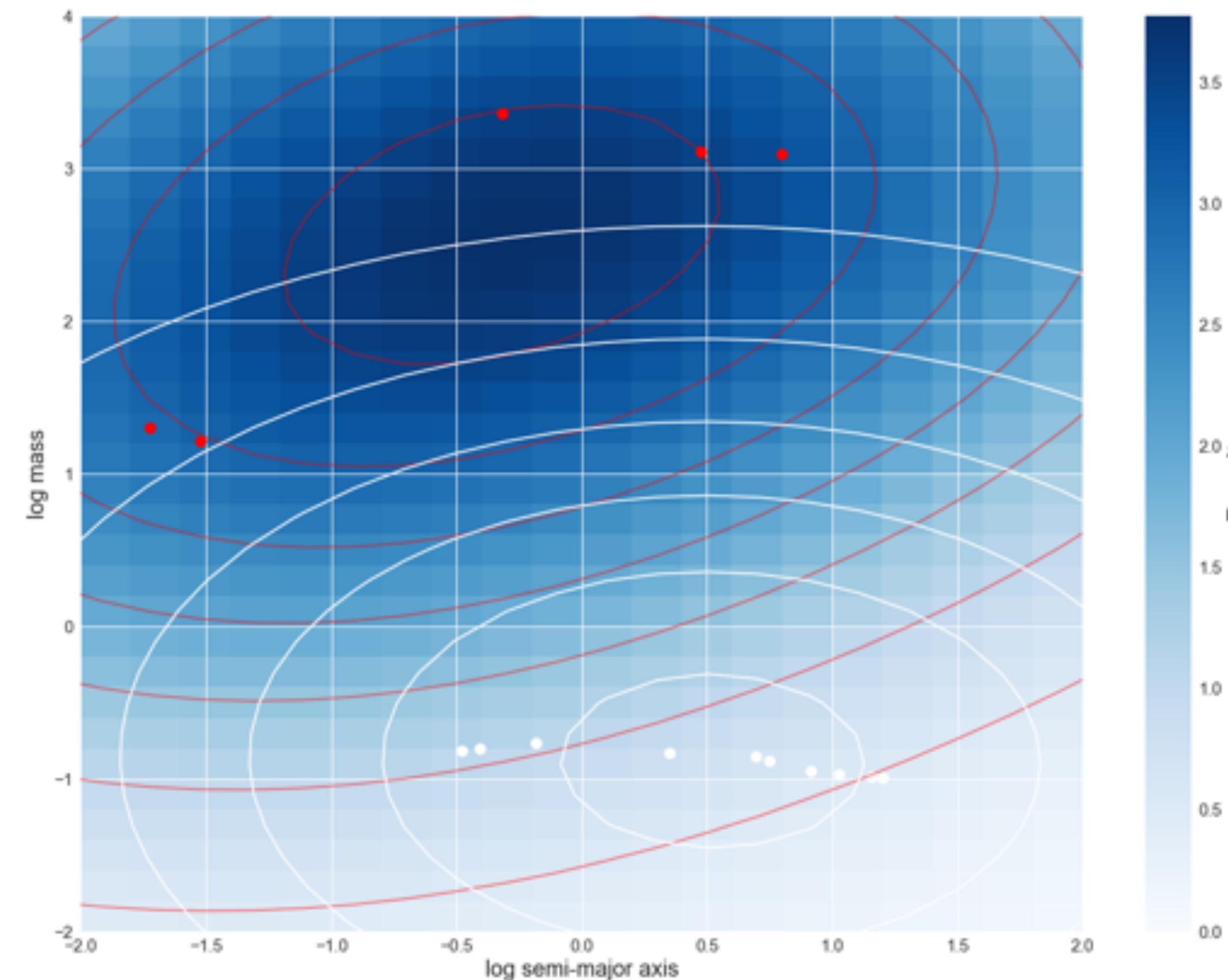
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Distance between 2 systems - N-planet case

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The square of the distance between two planetary systems is then

$$d(s_1, s_2) = \sqrt{\int (\psi_{s_1} - \psi_{s_2})^2 d \log M d \log a}$$



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from 20-D to 2-D using T-SNE

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We want to project our 200-D data points on 2D, while keeping the maximum of information. For this we minimise the KL divergence:

$$D(p||q) = \sum_{i,j \in S} p_{i,j} \log \left(\frac{p_{i,j}}{q_{i,j}} \right)$$

p: similarity in system space (200D)

q: similarity in projection space (2D)

-> measures the gain in information we get by using the p distribution (the real high-D one) instead of the q distribution (the low-D one).

If p is large, q needs to be large. If p is small, q can be whatever

-> the local structure is preserved (close-in points), not the global one

If q is small, p is small: systems far away in the 2D space are dis-similar in the 200-D space.

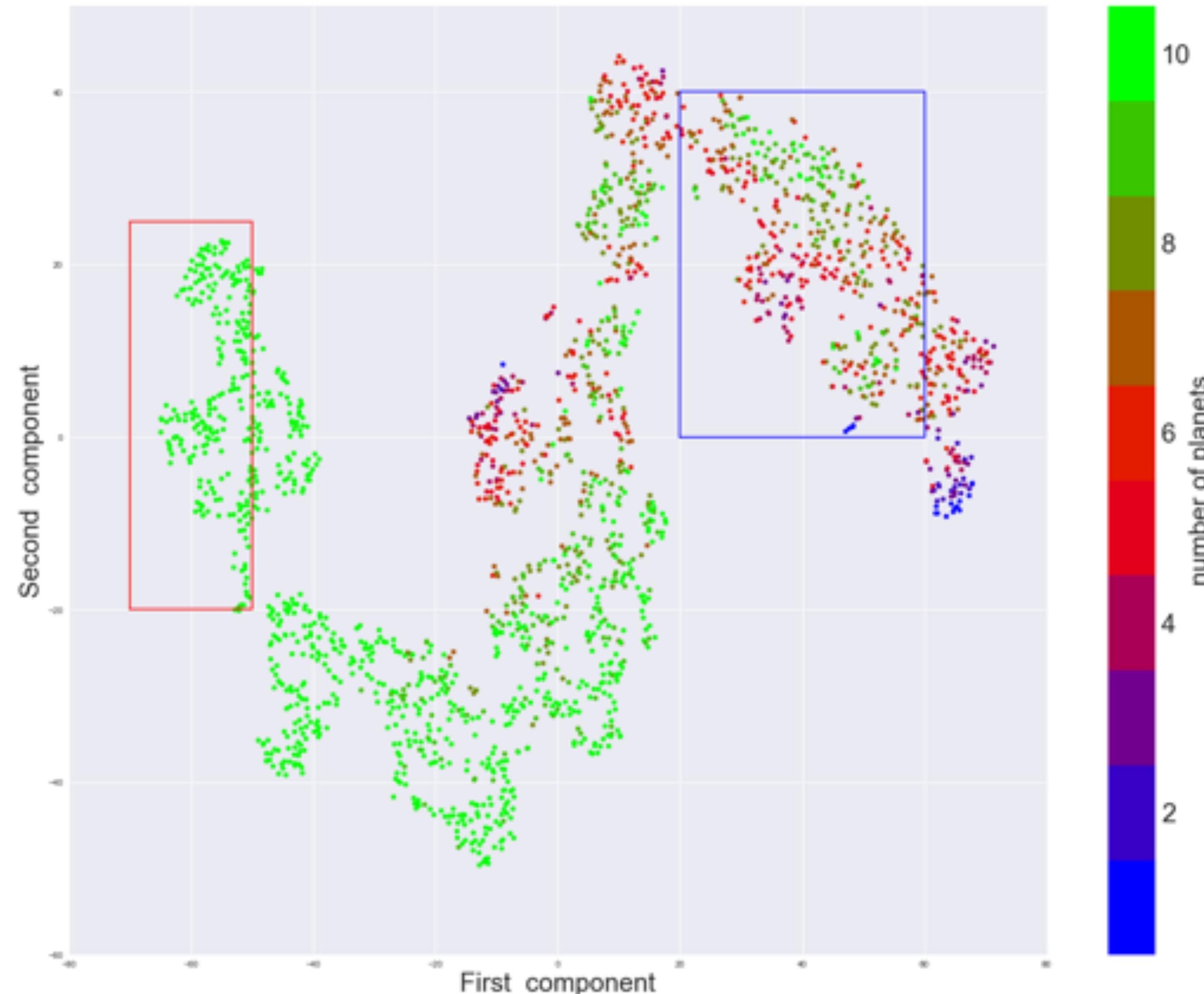
!! this requires the distance to be a distance !!

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T-SNE - reference population

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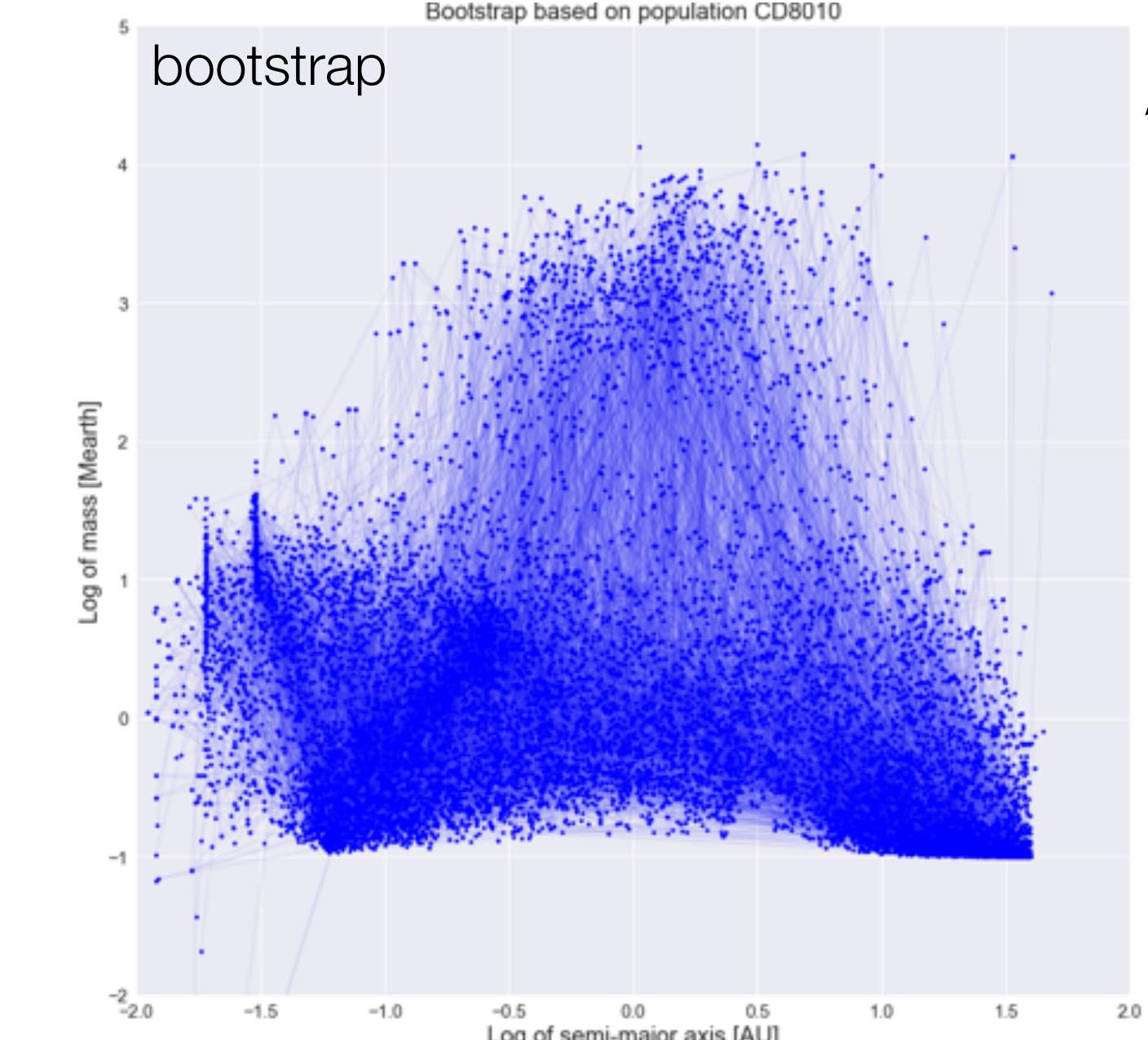
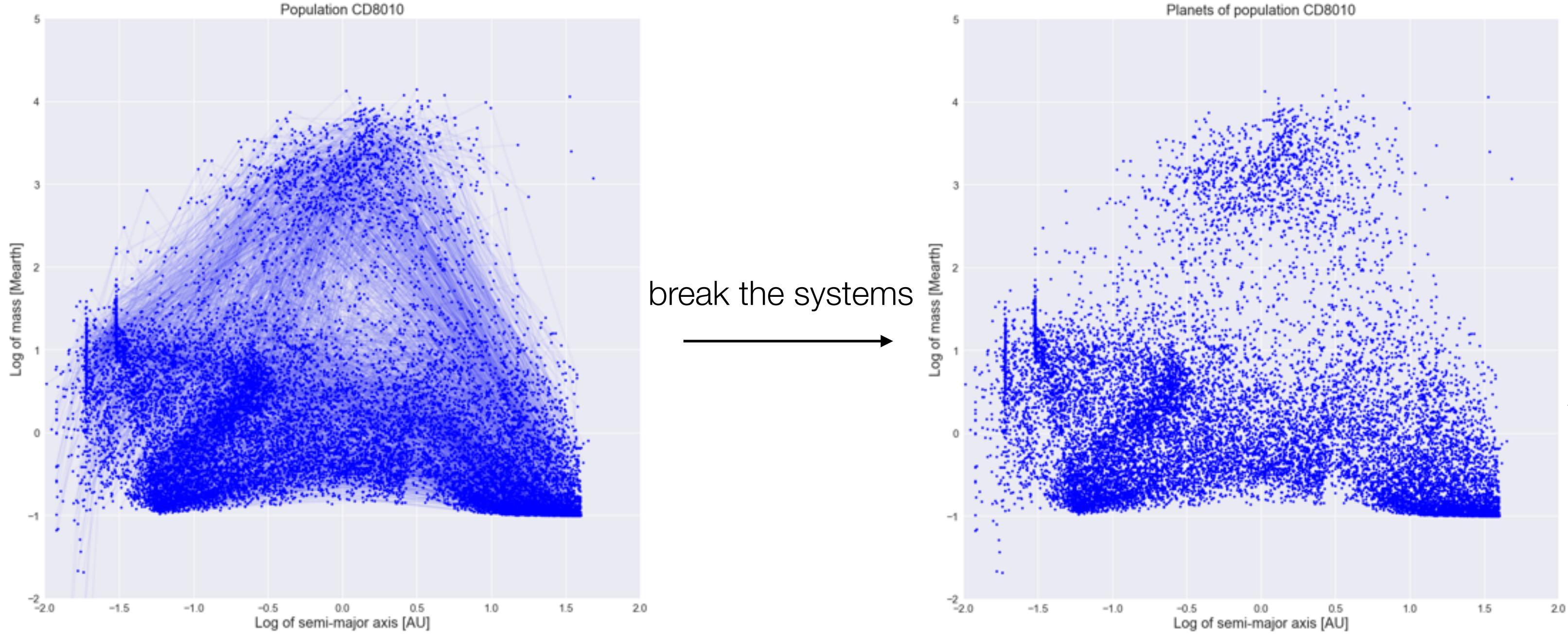


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comparing with a population that has same planets but different architecture



distribution of final number of planets in each system is kept unchanged

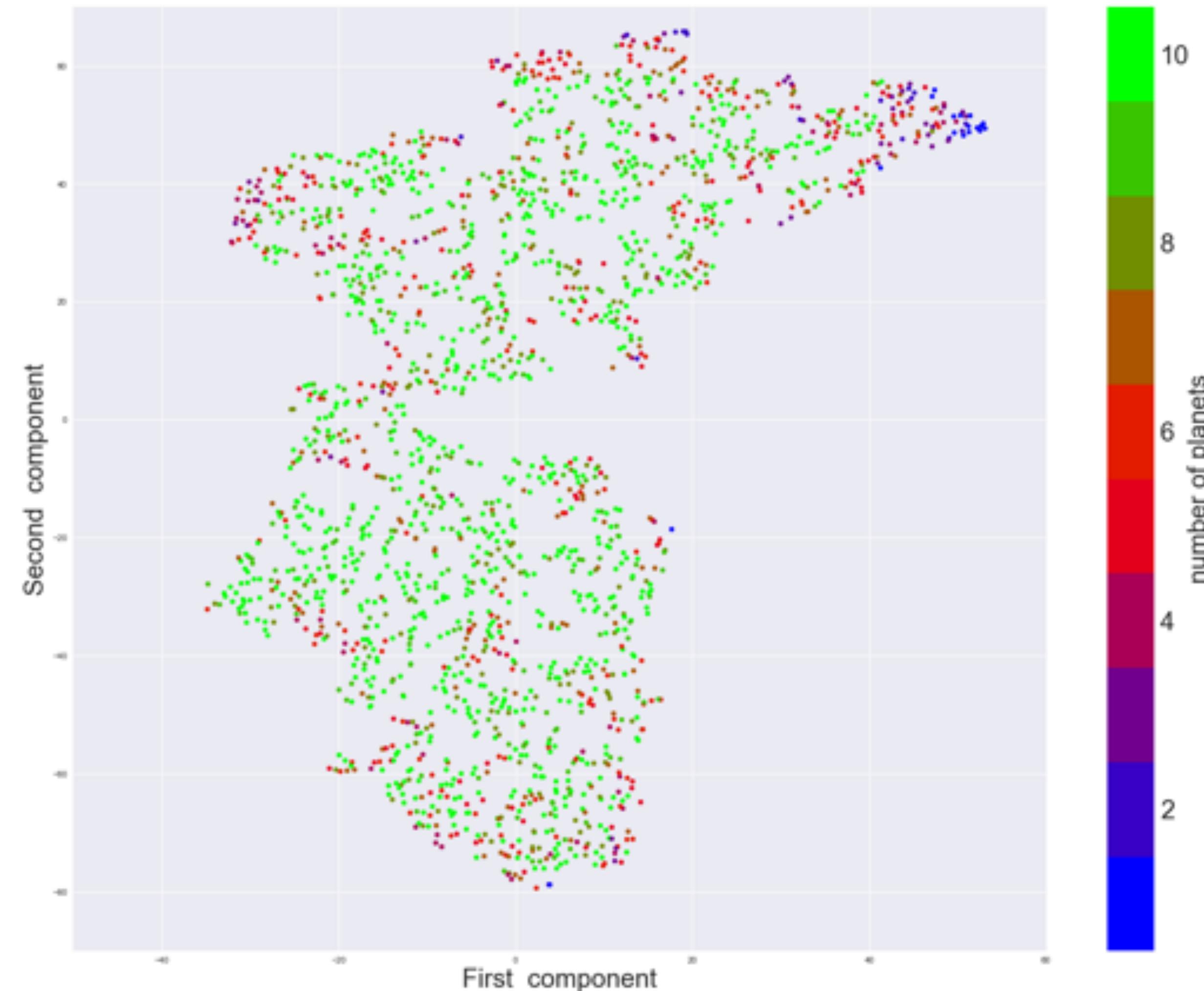
T-SNE - non physical population

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Physical systems are intrinsically difference from un-physical systems built with the same planets -> simulations lead to different *architectures*.

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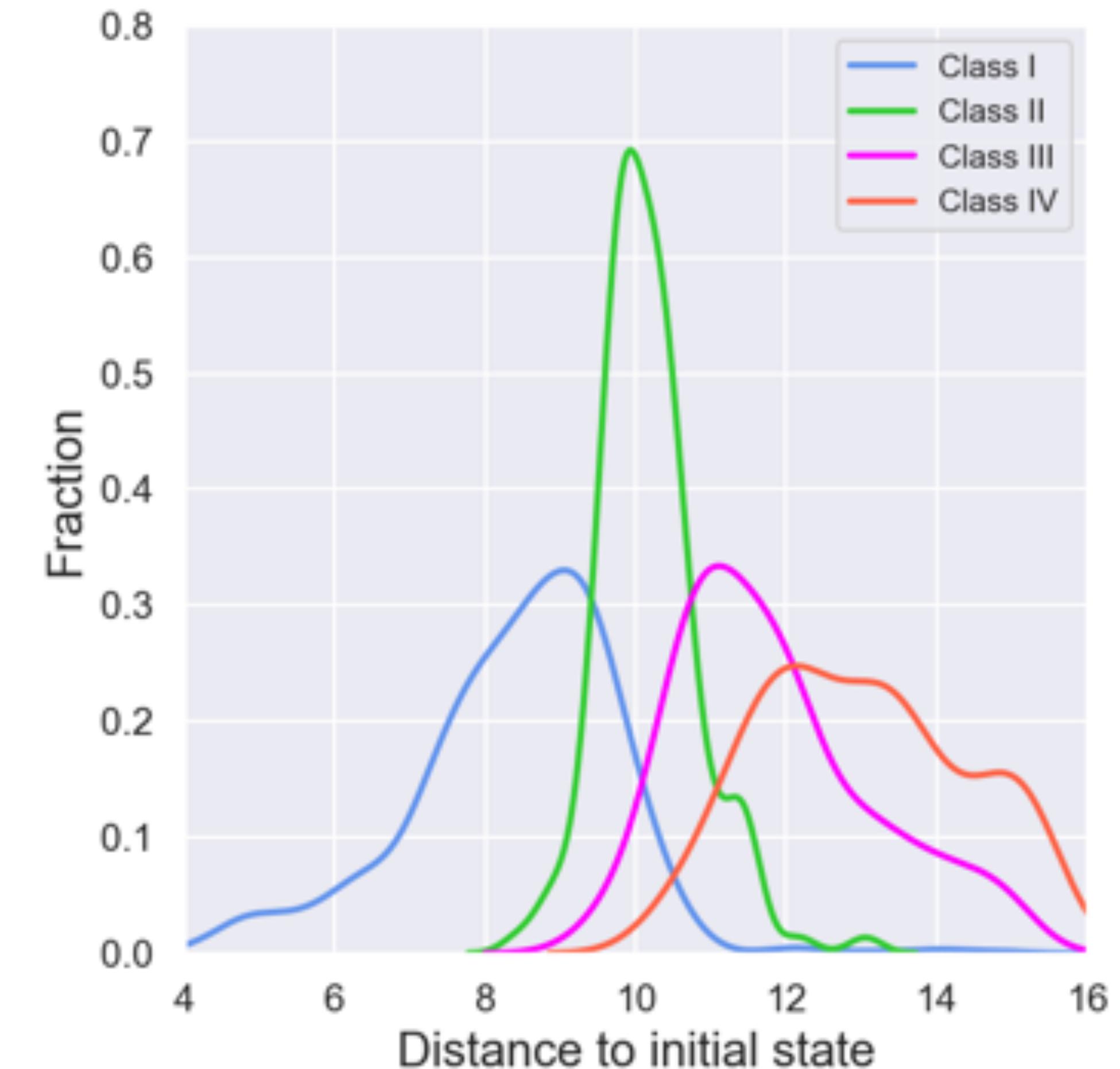
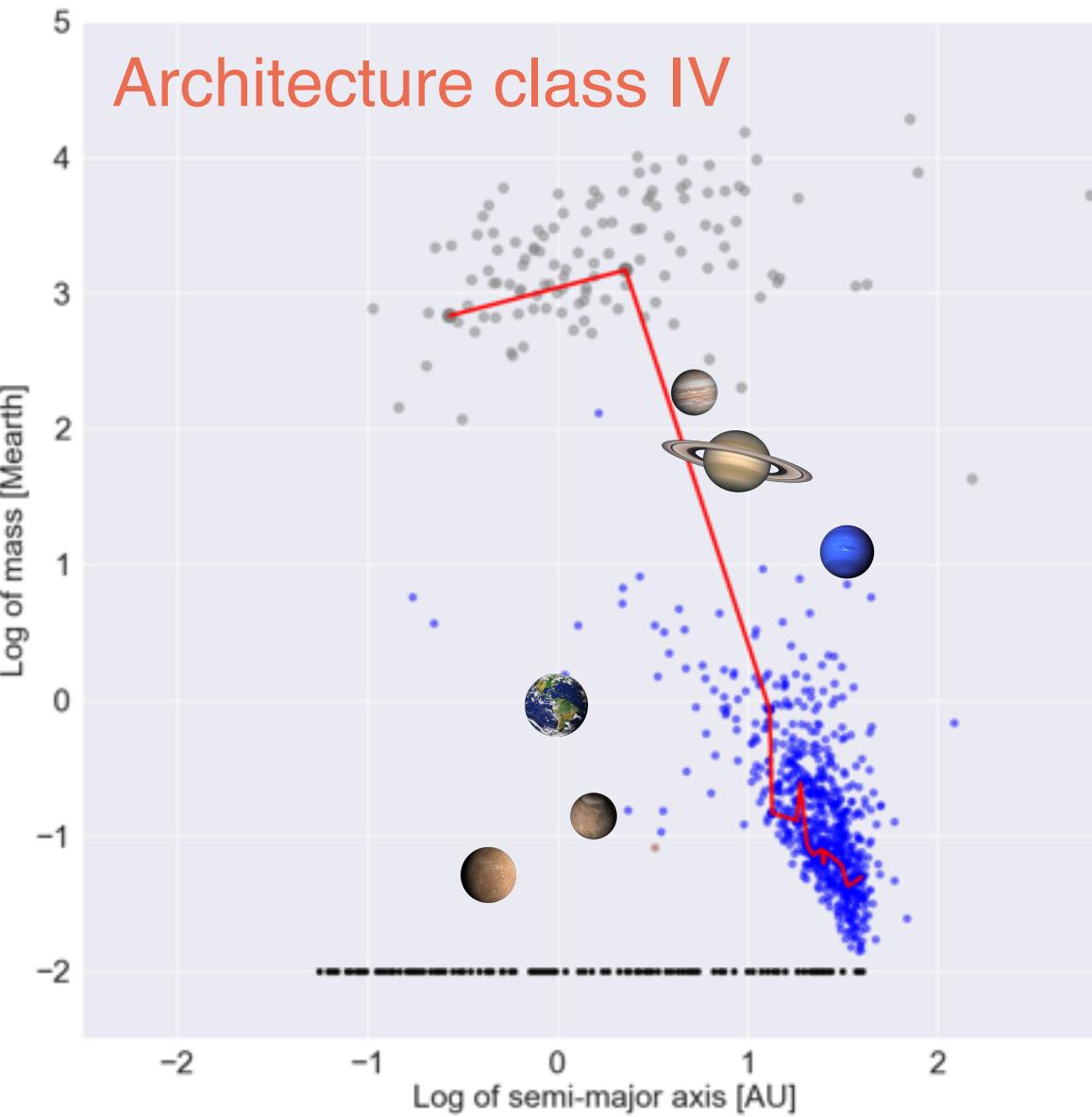
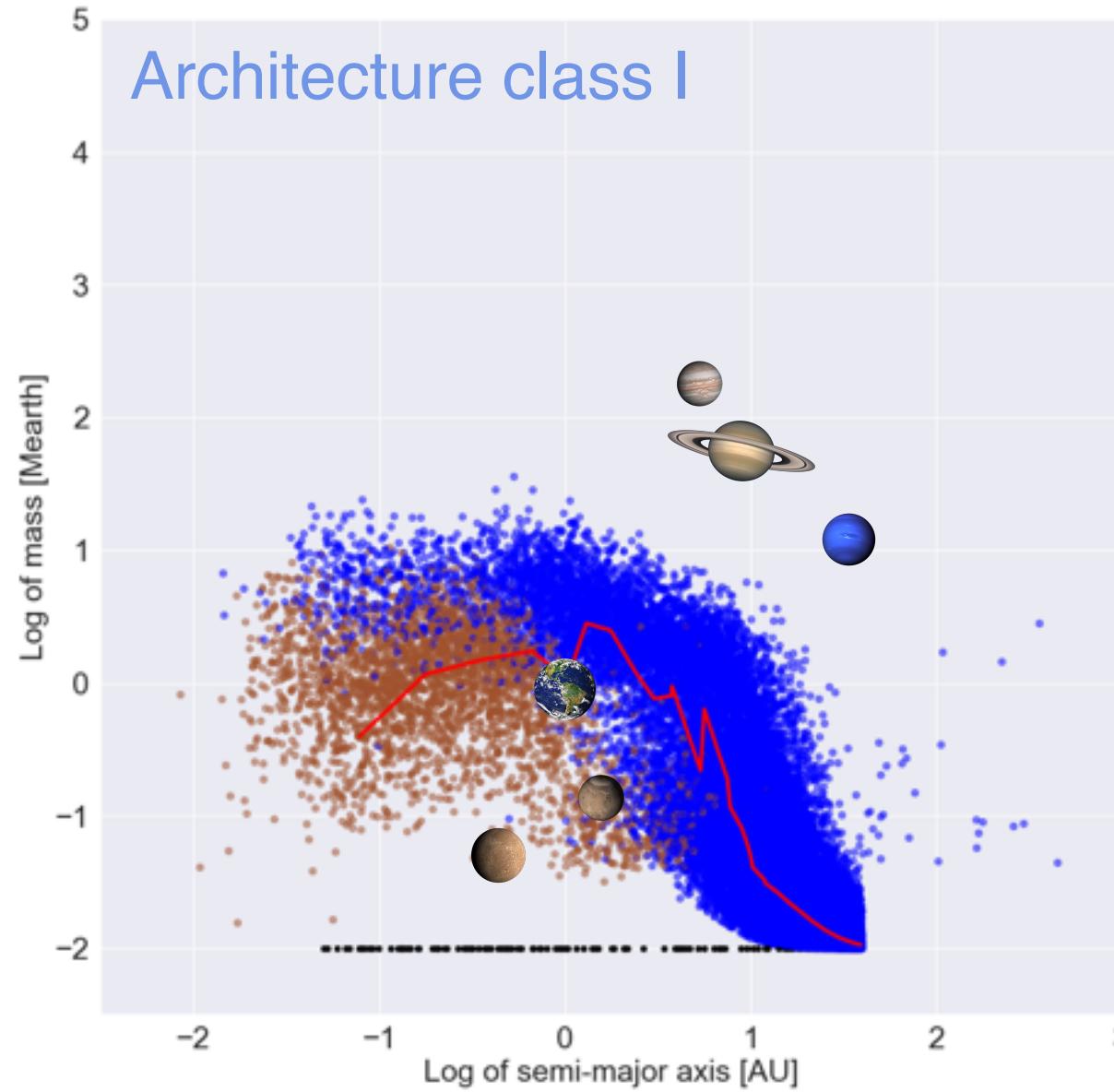
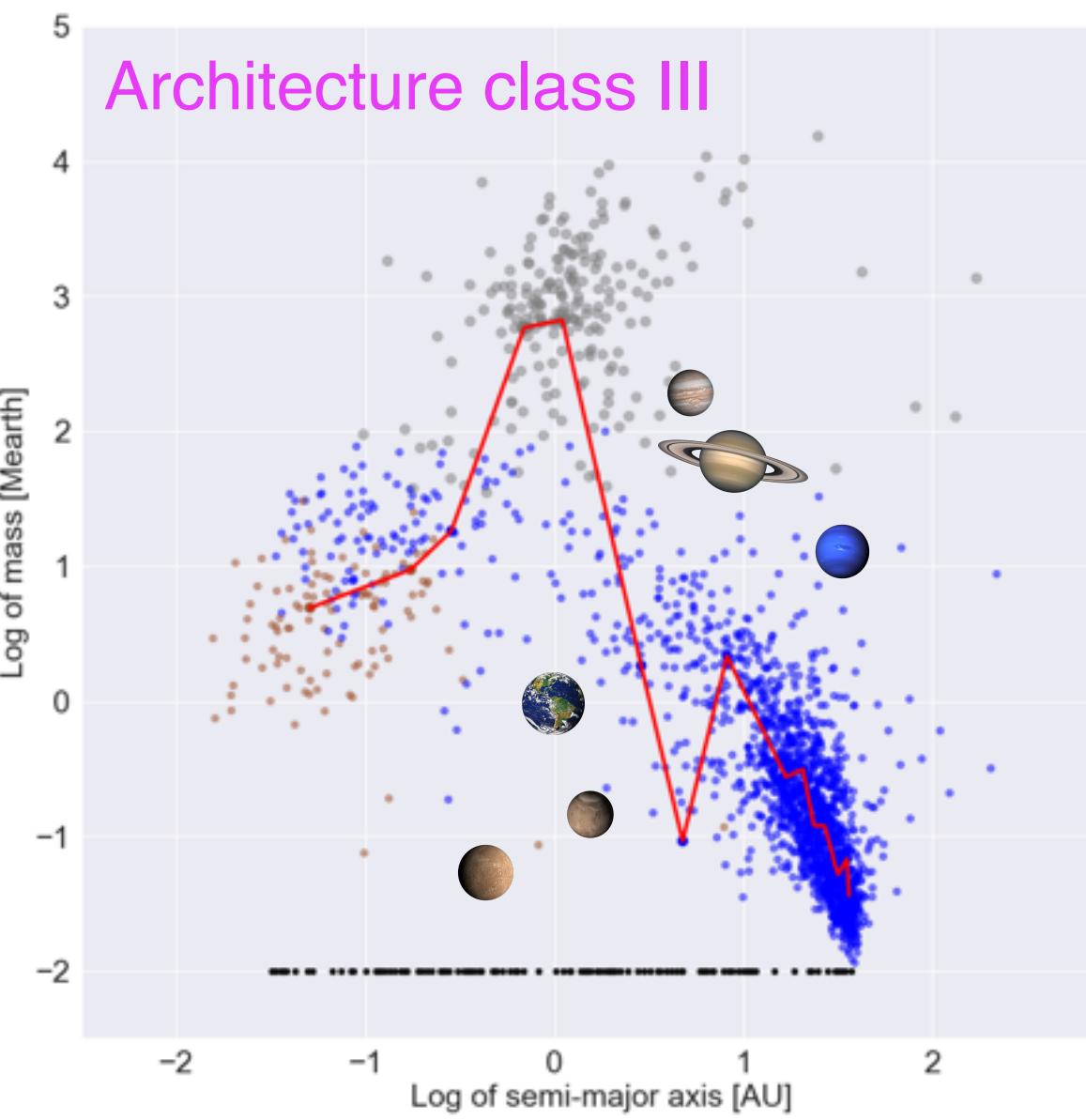
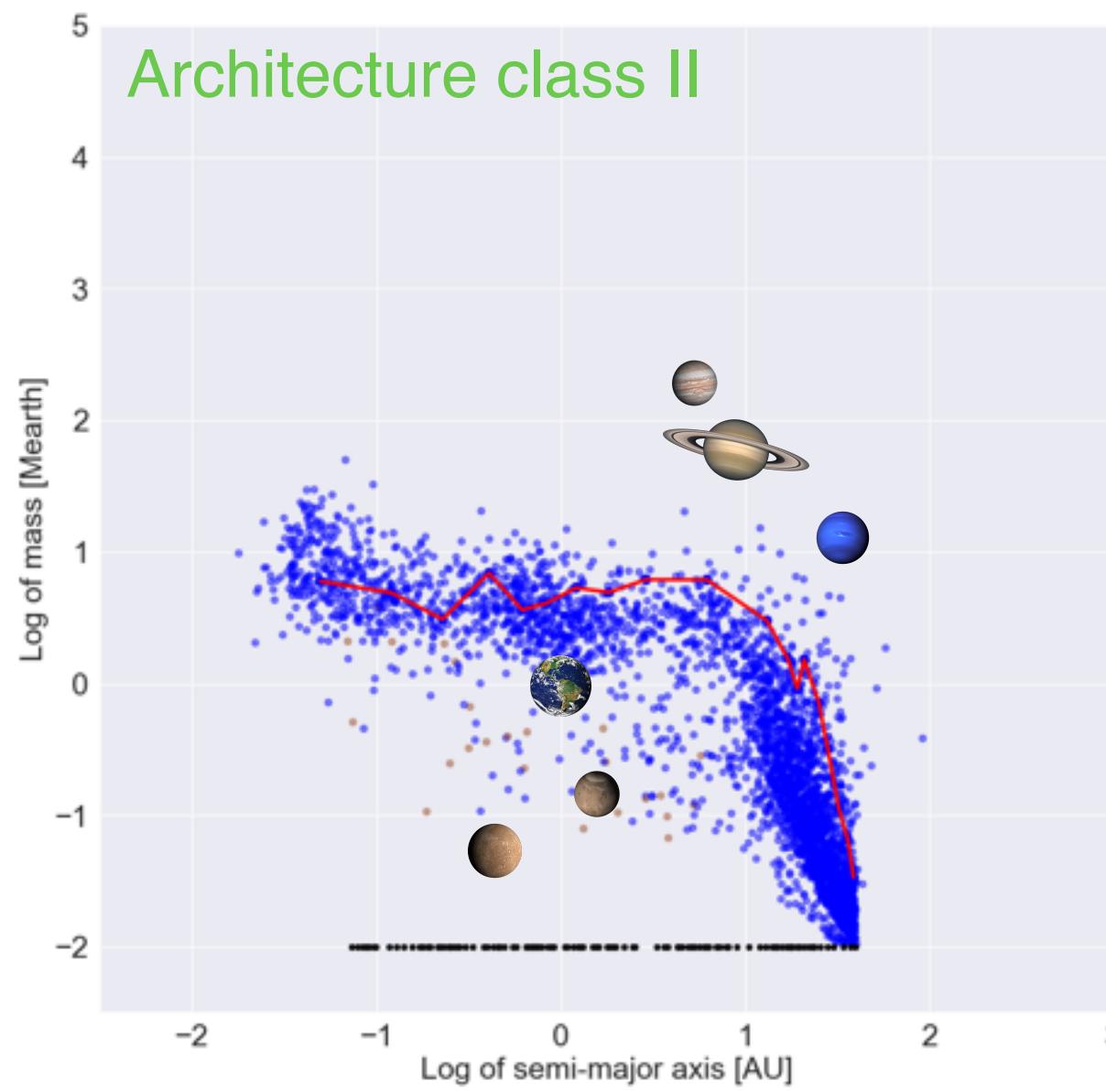


Four classes of architecture

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1- Planet formation and the Bern model

2- Models *versus* observations

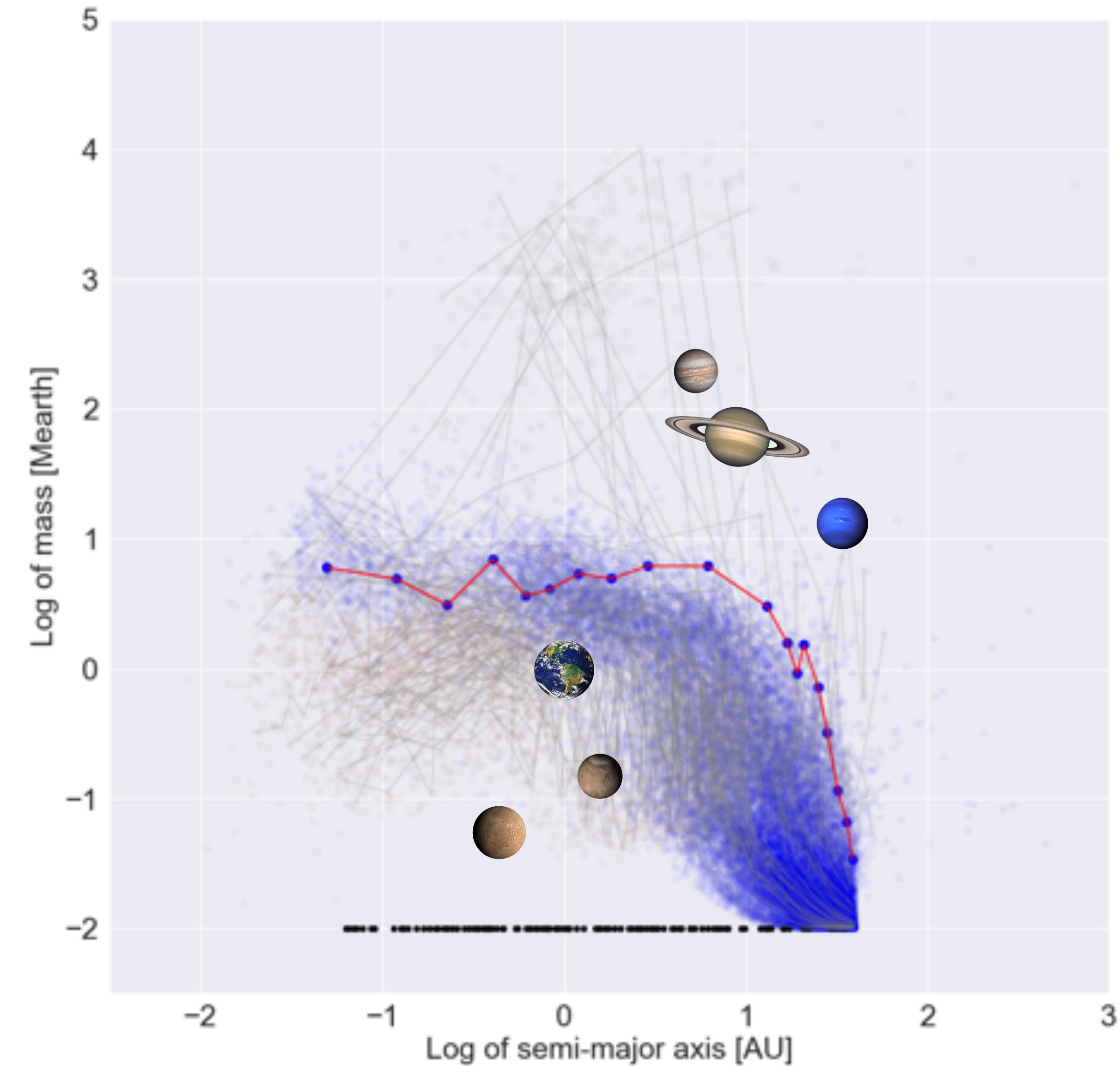
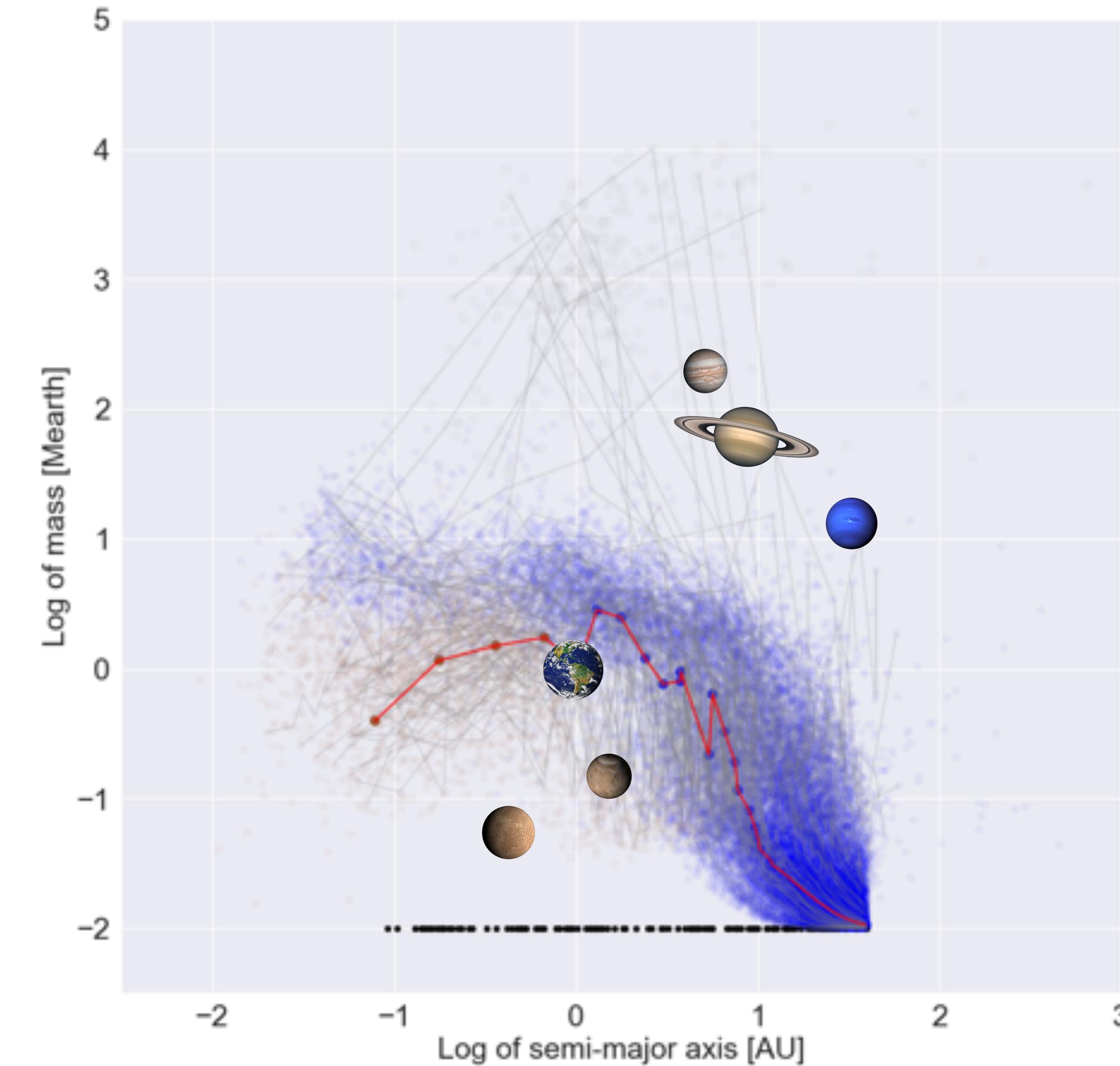
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Architecture versus composition

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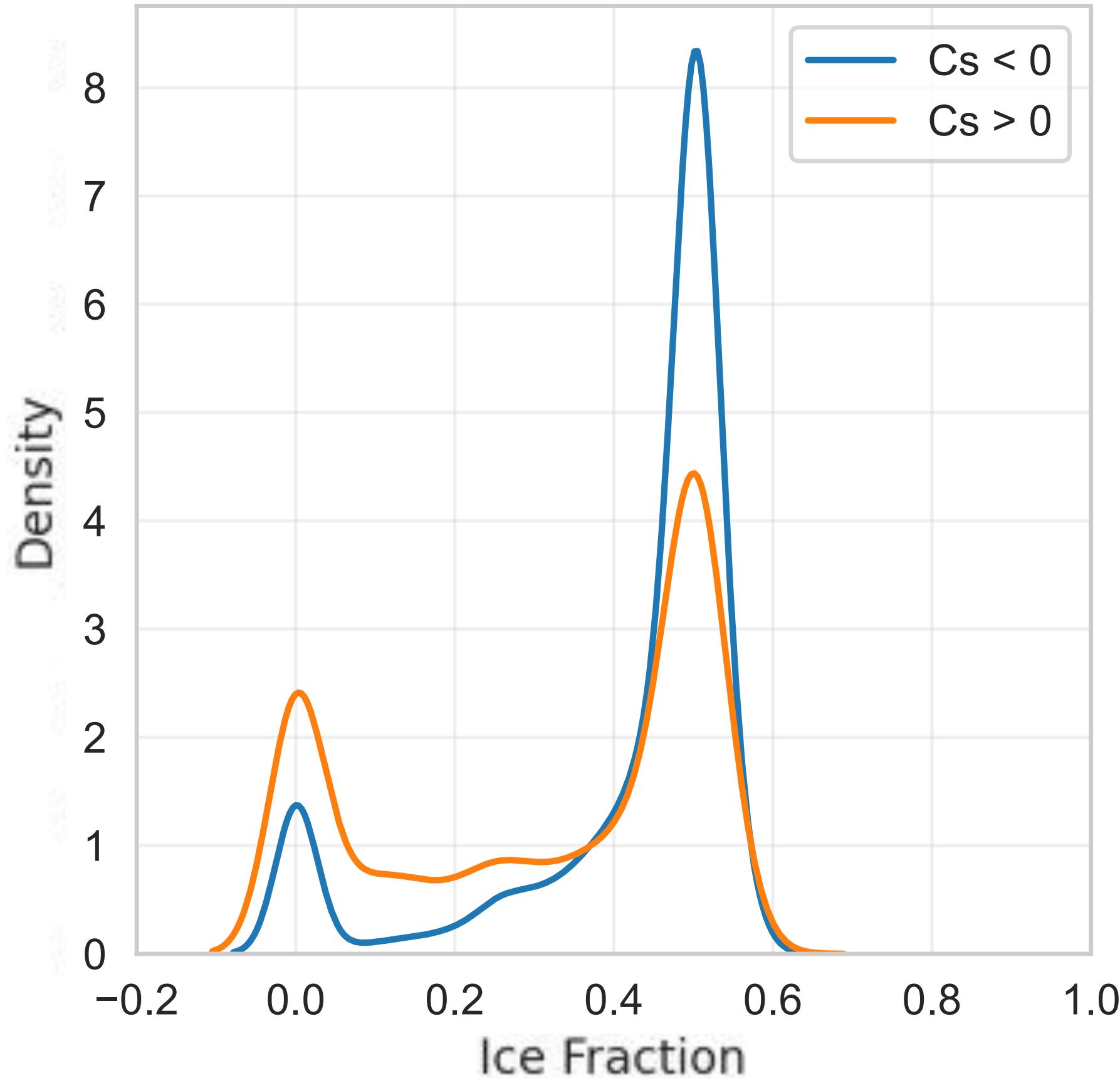


Architecture versus composition

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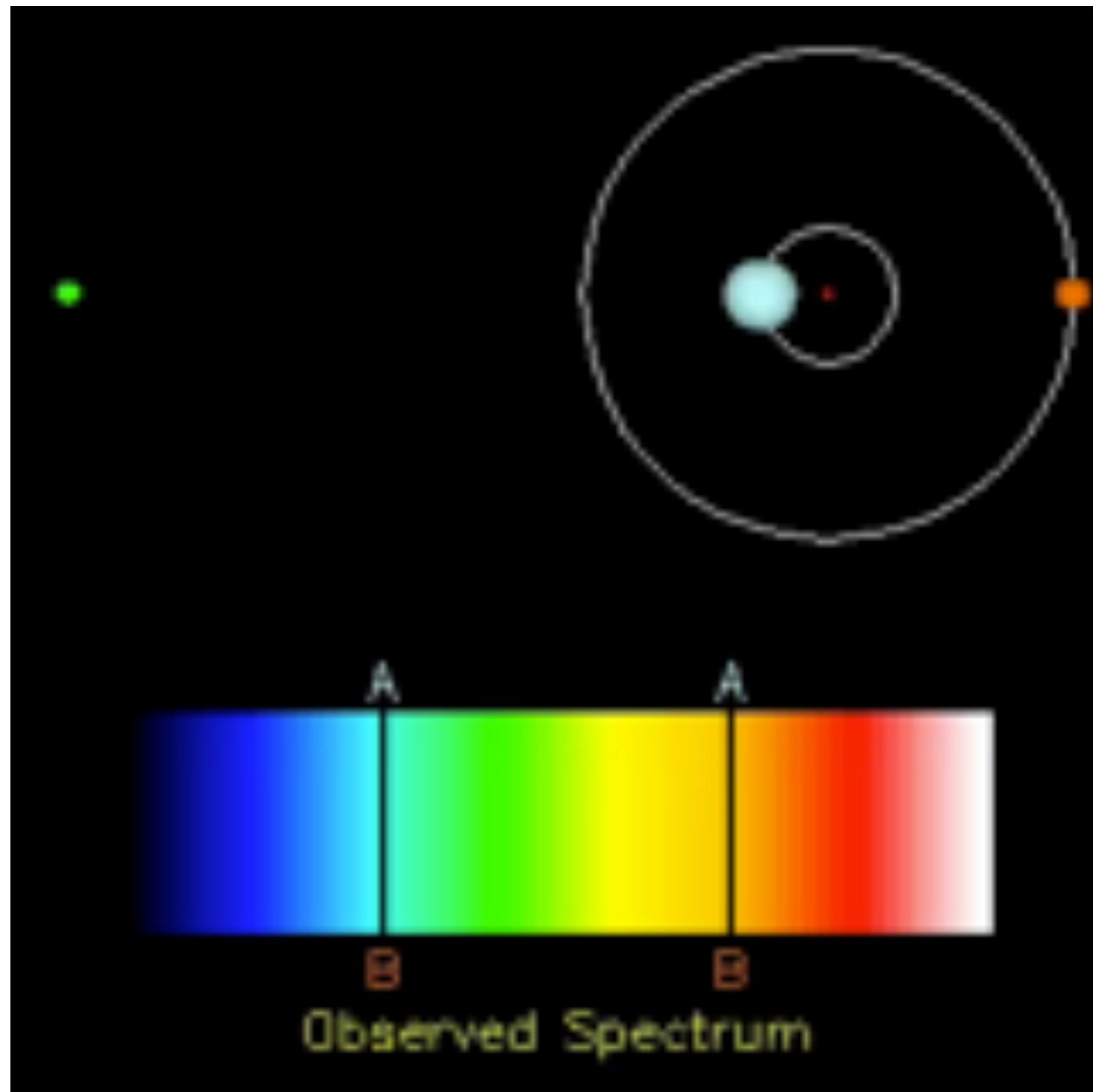
how can we observationally determine
the ice fraction?

Observing planets

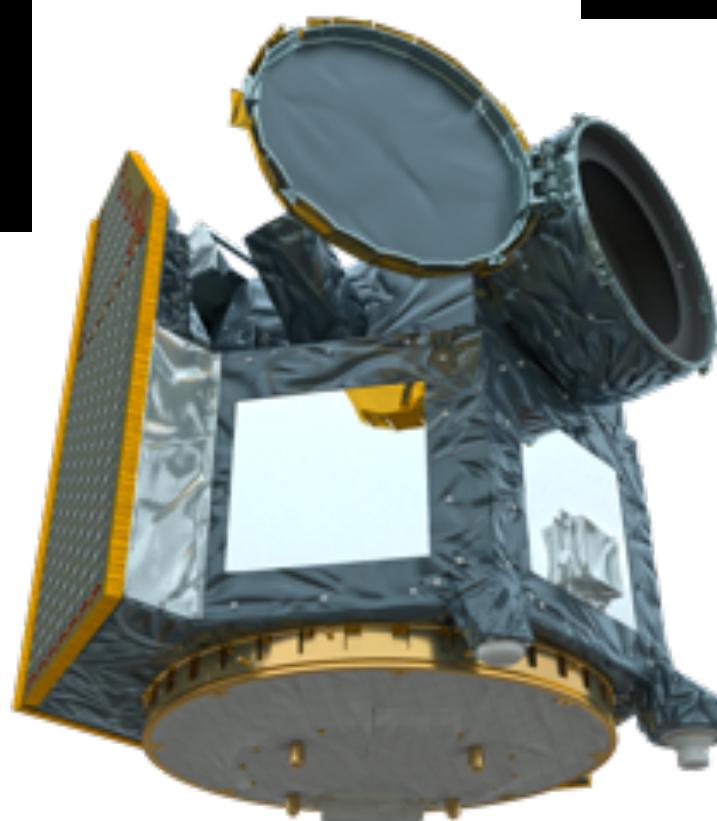
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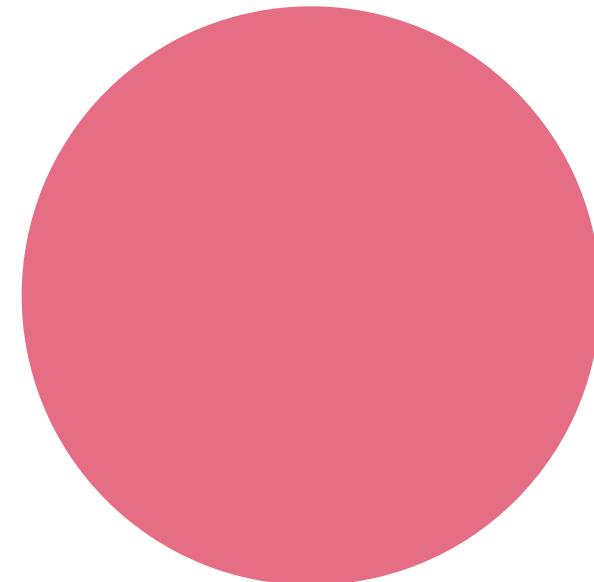
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$$M_p/M_{\text{star}}$$



$$(R_p/R_{\text{star}})^2$$

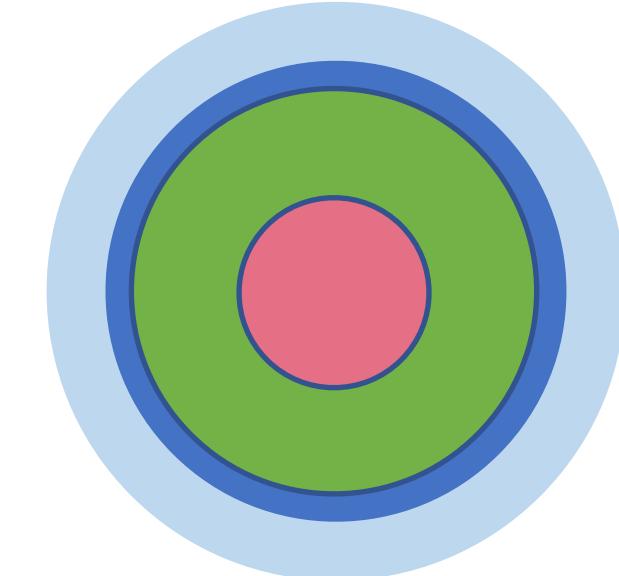


Observations

- Mass
- Radius



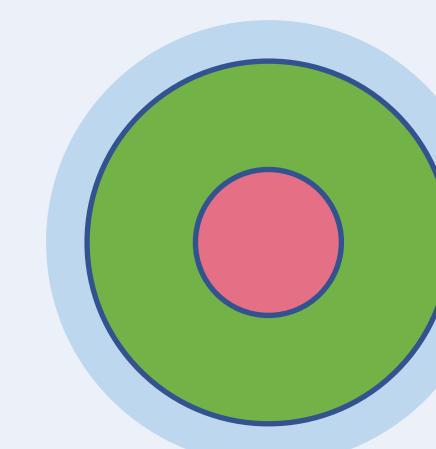
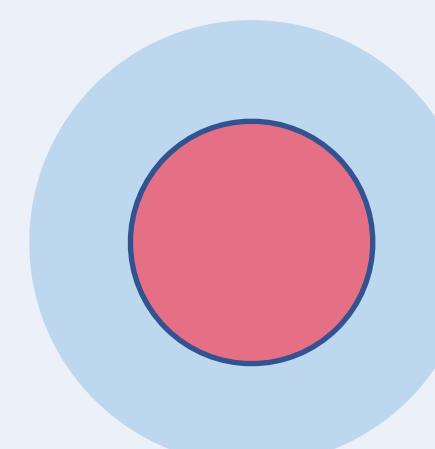
Internal
Structure



Problem:

Inherent degeneracy - multiple structures can lead to the same mean density

Example:



Calculate conditional probability of model parameters (x) given the observations (y)

Bayes' Theorem:

$$p(x|y) = \frac{p(y|x) p(x)}{p(y)}$$

$p(x y)$	posterior
$p(y x)$	likelihood
$p(x)$	prior
$p(y)$	marginal likelihood (Bayes integral)

Bayesian notion of probability:

$p(x)$ - degree of belief that x will occur

Internal structure and composition

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Spherically symmetric 1D model
with fully differentiated layers:

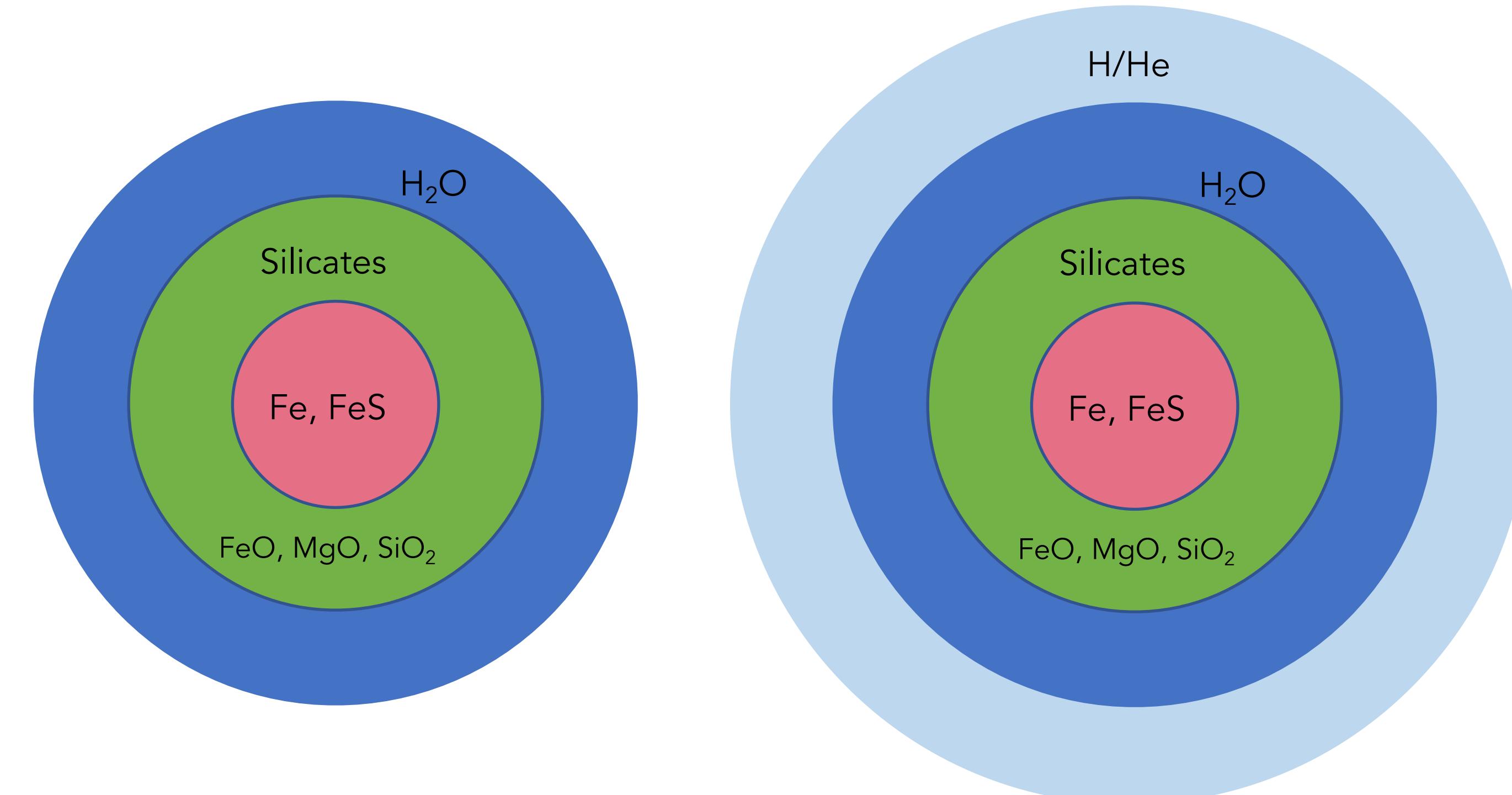
Input parameters:

- mass
- luminosity
- equilibrium temperature
- layer mass fractions
- core composition
- mantle composition

Model solves the
planetary structure equations
(Kippenhahn et al. 2012)

Output parameters:

- transit radius
- layer thicknesses



Spherically symmetric 1D model
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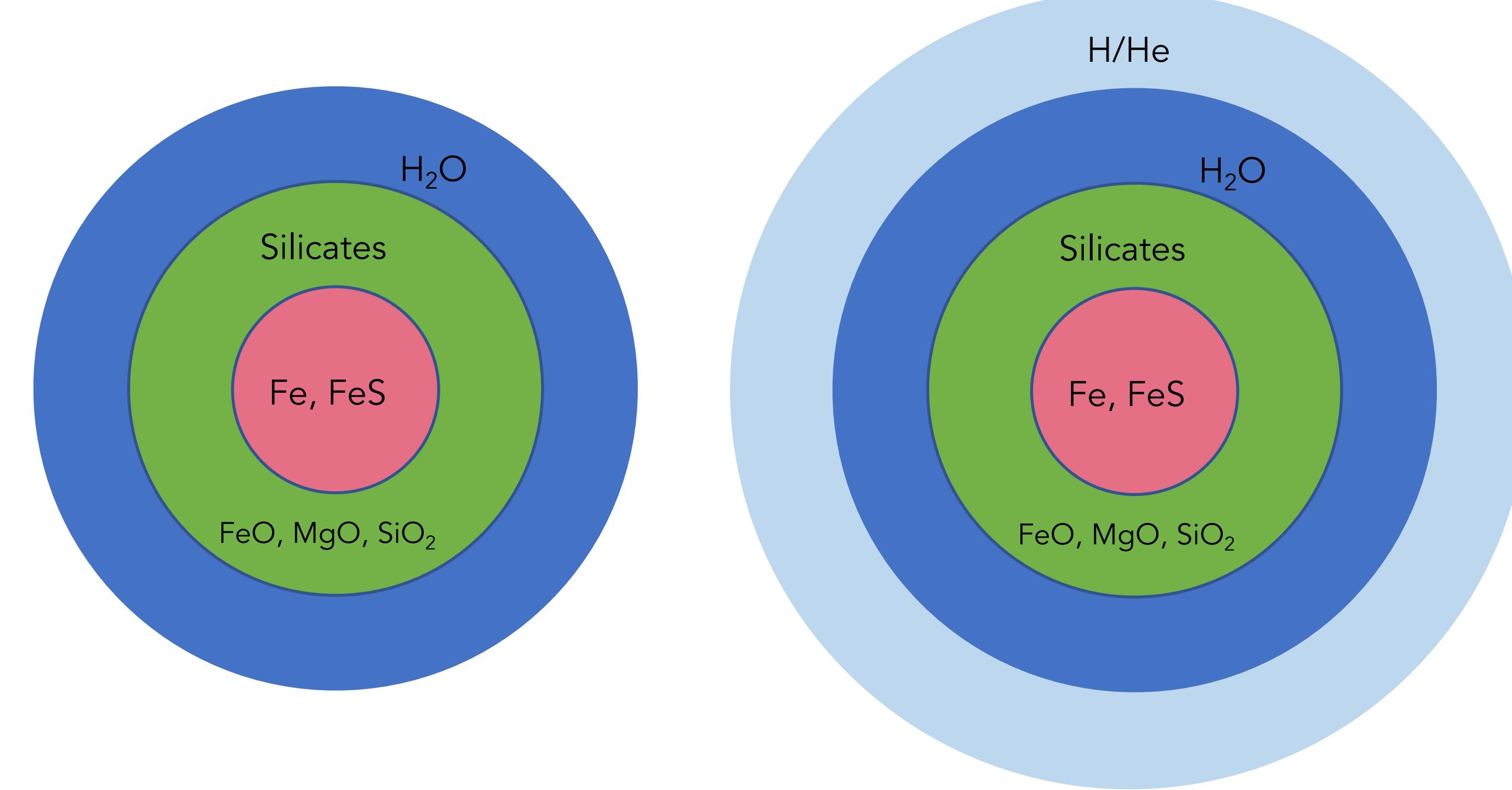
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Problem:

Solving planetary structure equations takes computation time
(around 2 hours for 1000 structures)

1- MCMC approach

Method: random walk inside parameter space,
biased to explore ideal part of it for the given problem

Problems:

- difficult to know when MCMC method has actually converged to final distribution
- in case of multimodal posterior distribution, potentially only one mode is found

2- Brut force approach

Method: explore the whole parameter space

Problems:

- even more models to compute

Problem with both MCMC and brut force approach:

Measurements of observable quantities taken with respect to stellar quantities
high correlation between planets in multiplanetary systems

Modelling n planets in a system simultaneously means

- dimension of parameter space is multiplied by n
- necessary number of sampling points (and therefore computation time) increases drastically

Spherically symmetric 1D model
with fully differentiated layers:

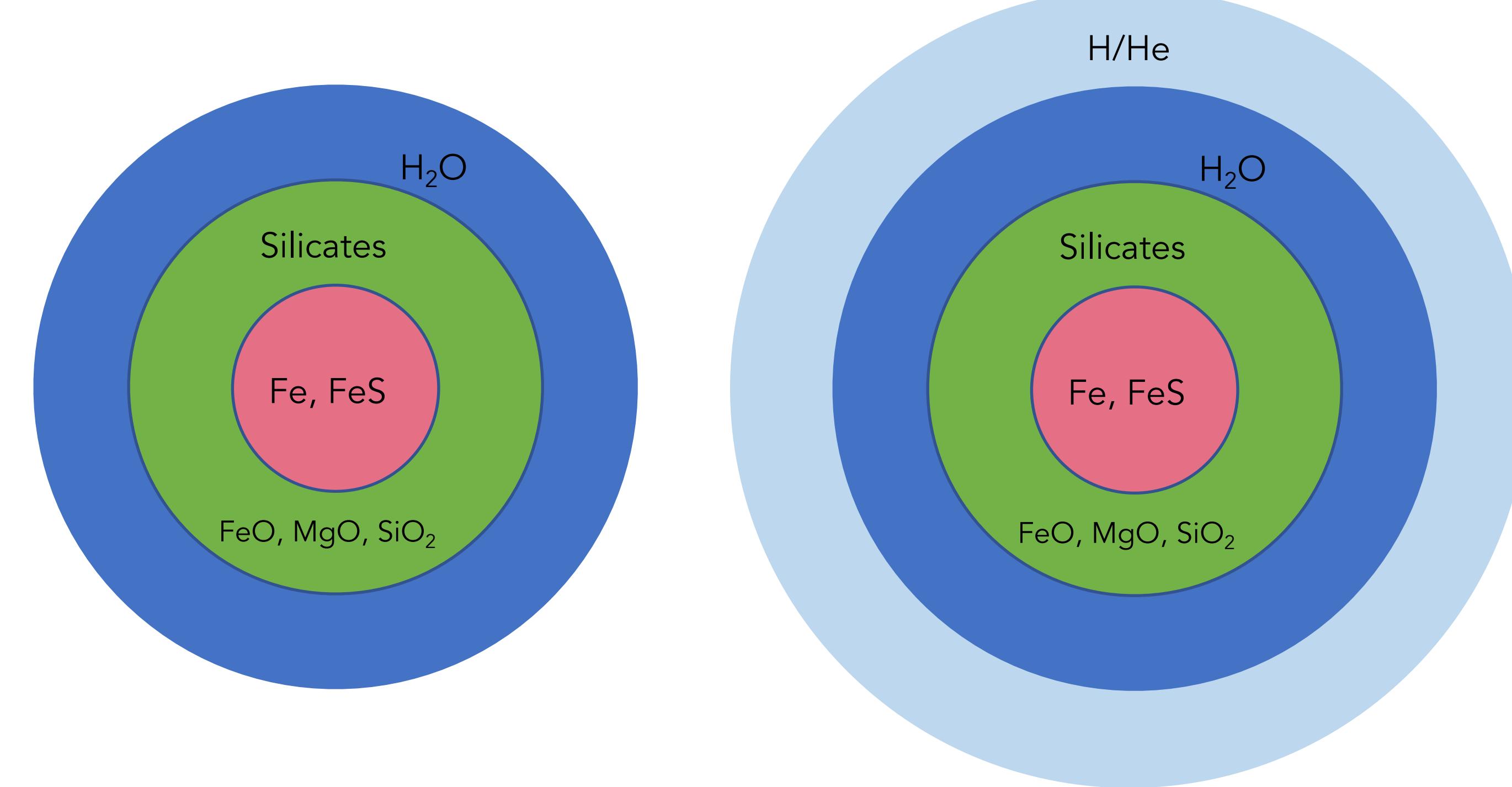
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(Kippenhahn et al. 2012)

Output parameters:

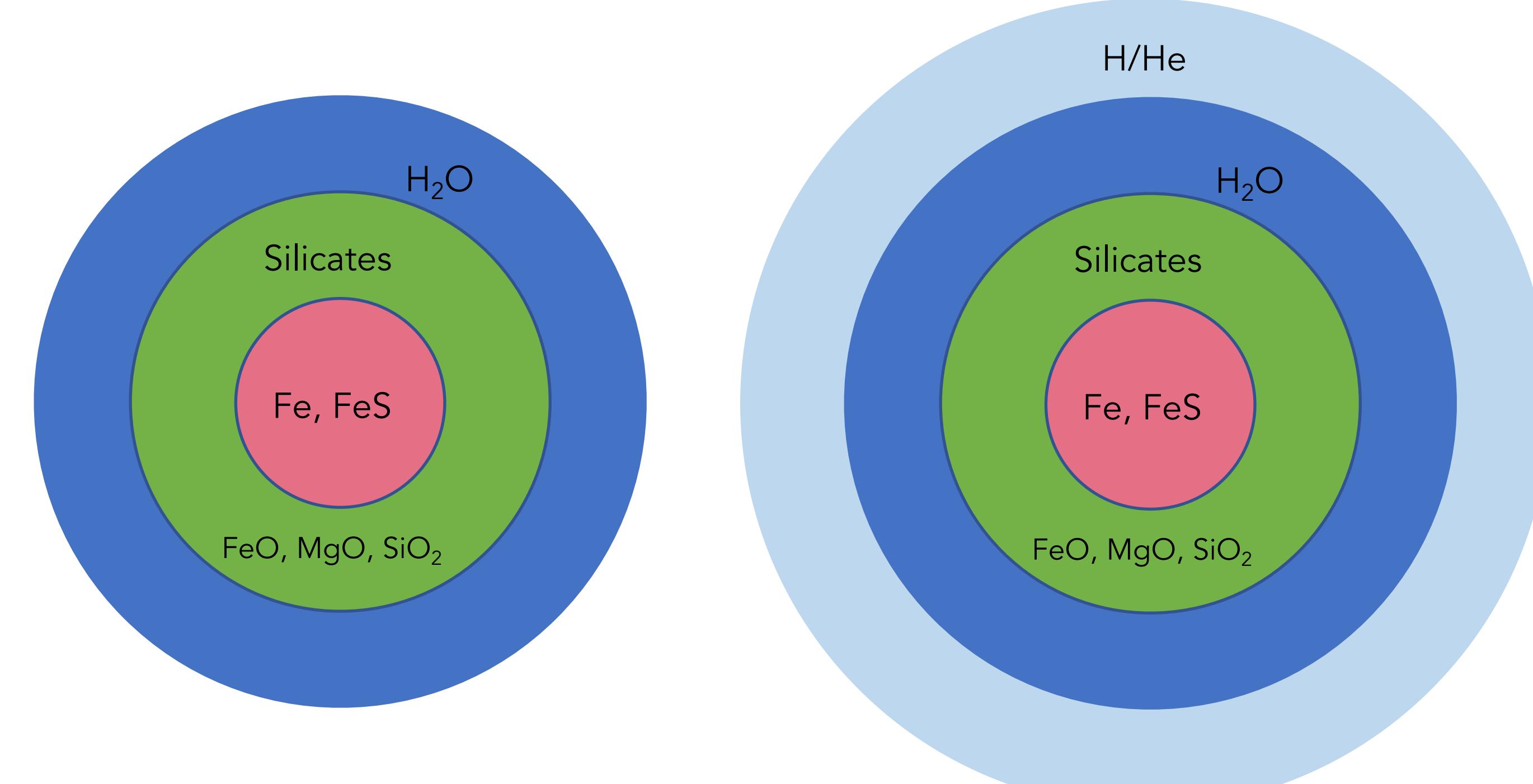
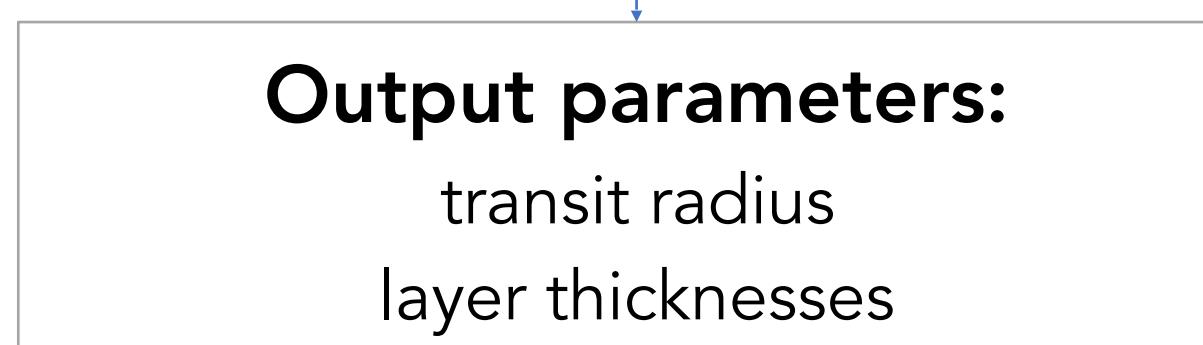
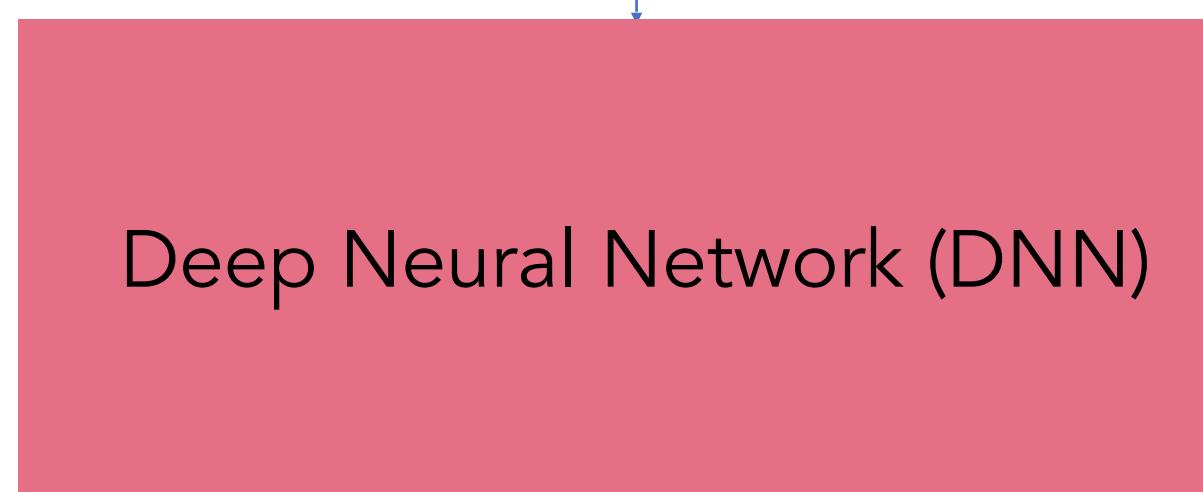
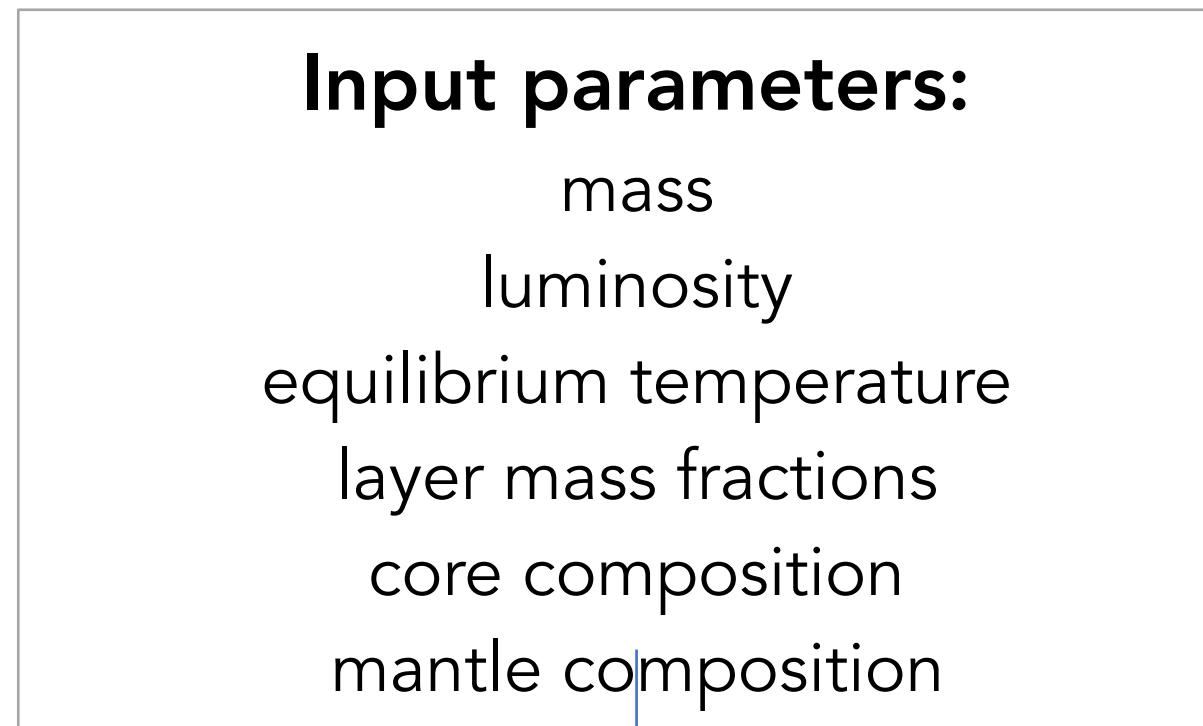
- transit radius
- layer thicknesses



Problem:

Solving planetary structure equations takes computation time
(around 2 hours for 1000 structures)

Spherically symmetric 1D model
with fully differentiated layers:



Train DNN based on internal structure model

Training the DNN

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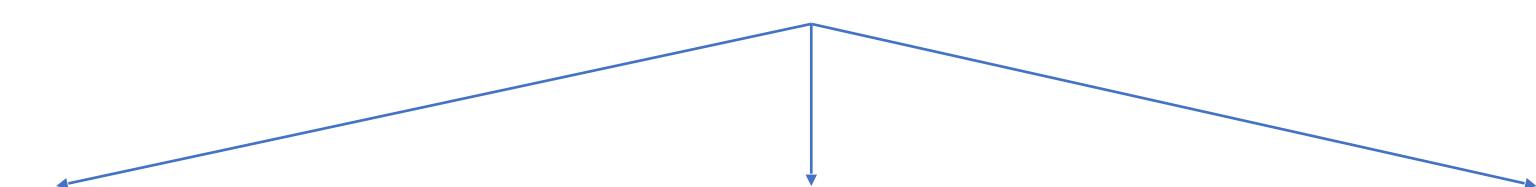
Generate database of 37 million data points

$M_{\text{tot}} [M_{\text{earth}}]$	T_{eq} [K]	L_{int} [erg/s]	w_{core}	w_{water}	w_{atmo}	$x_{S,c}$	$x_{\text{FeO,m}}$	$x_{\text{SiO}_2,\text{m}}$	R_{transit} [R_{earth}]	R_{core} [R_{earth}]	R_{mantle} [R_{earth}]	R_{water} [R_{earth}]	R_{atmo} [R_{earth}]
-------------------------------------	------------------------	--------------------------	-------------------	--------------------	-------------------	-----------	--------------------	-----------------------------	--	--	---	---	--

1.645	1548.2	1.35E20	0.135	0.324	0.021	0.031	0.249	0.158	1.272	0.149	0.452	0.501	0.204
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...
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split into:



Training Data
20 million data points

Validation Data
2 million data points

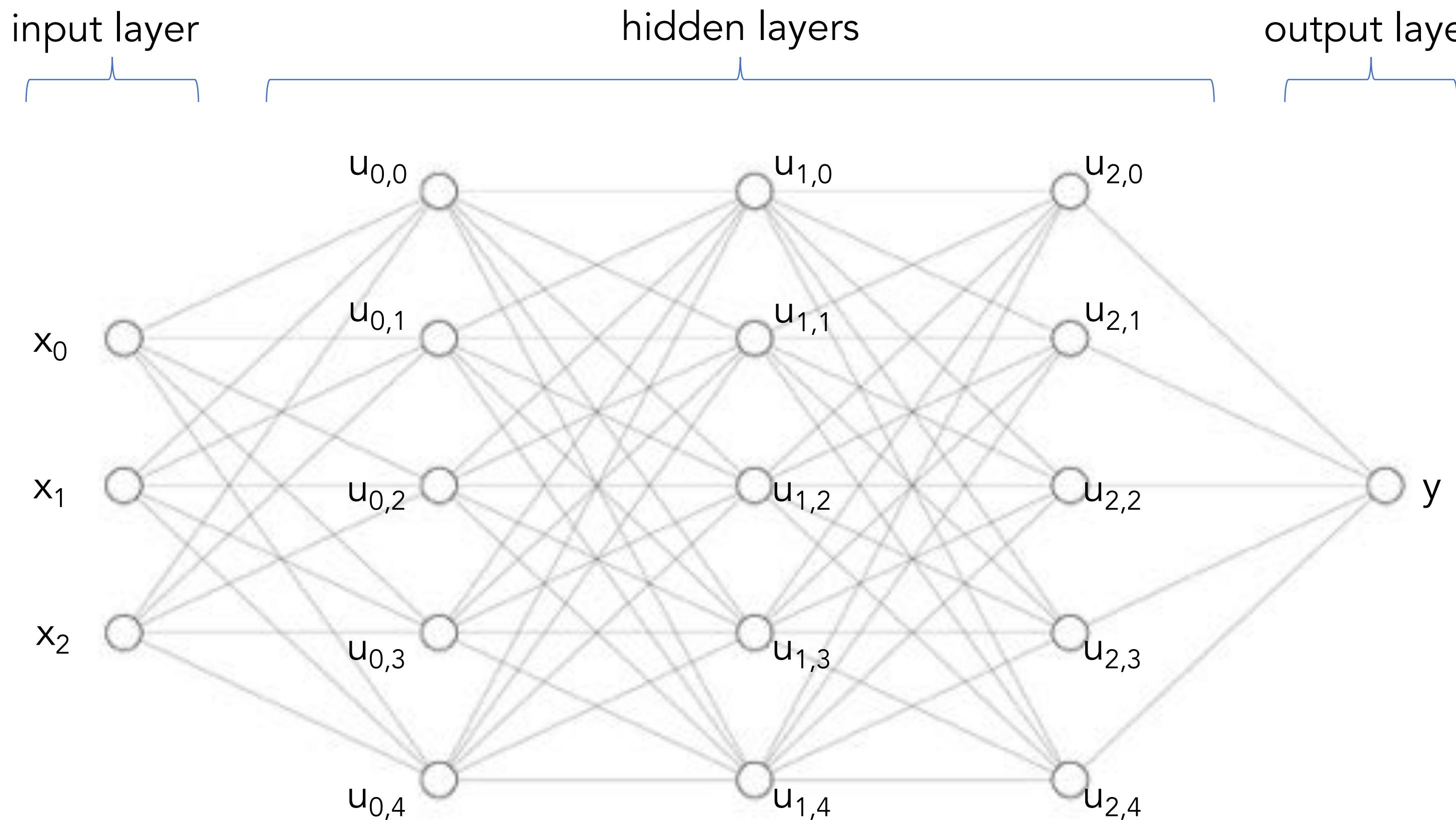
Test Data
15 million data points

Training the DNN

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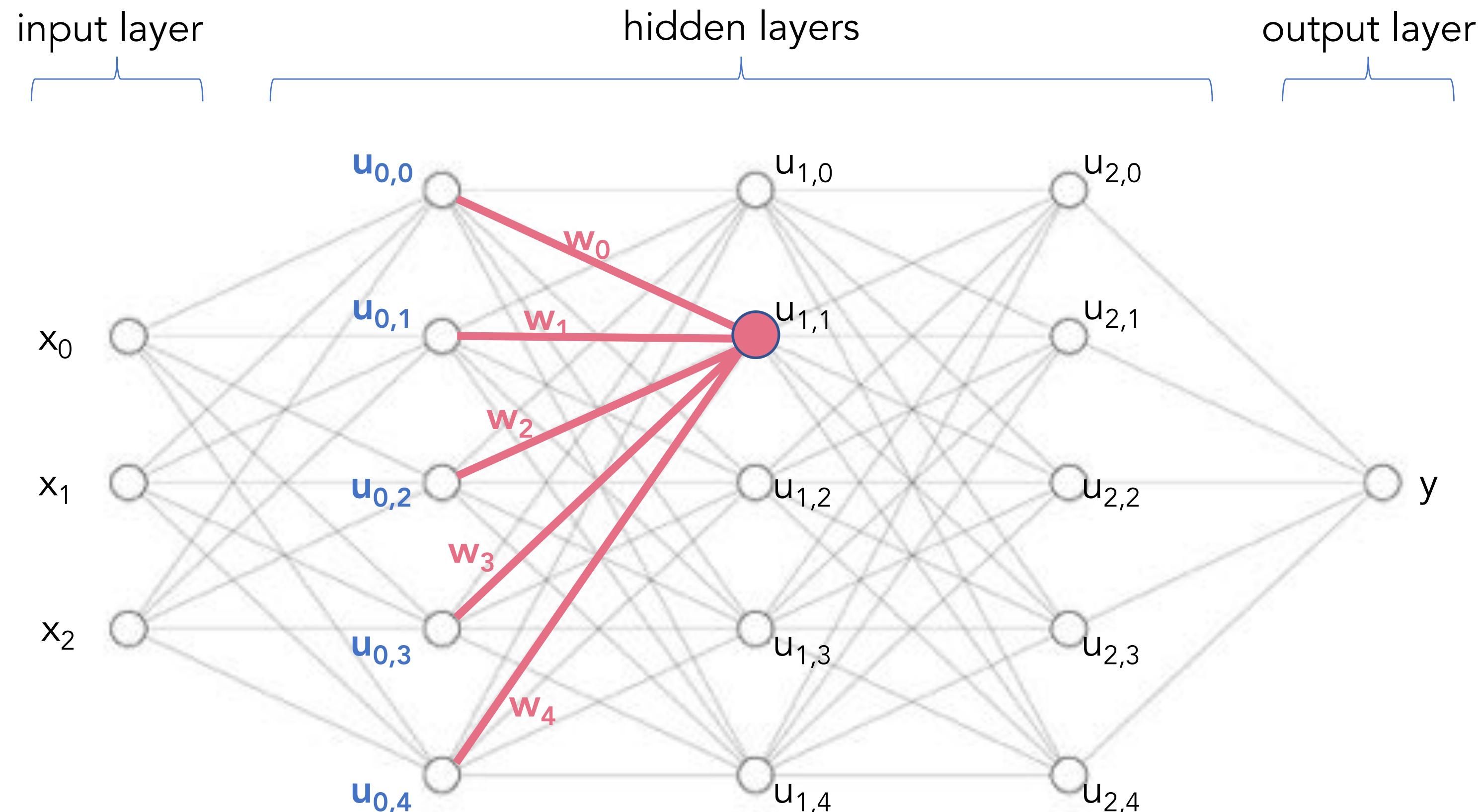


Training the DNN

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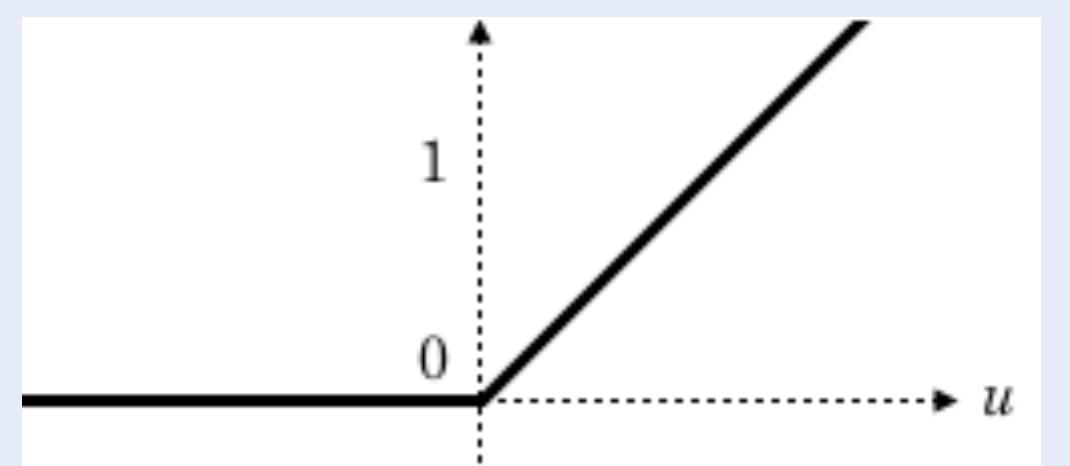
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Calculate output:

Activation function is used to allow for nonlinearity, e.g.
ReLU:

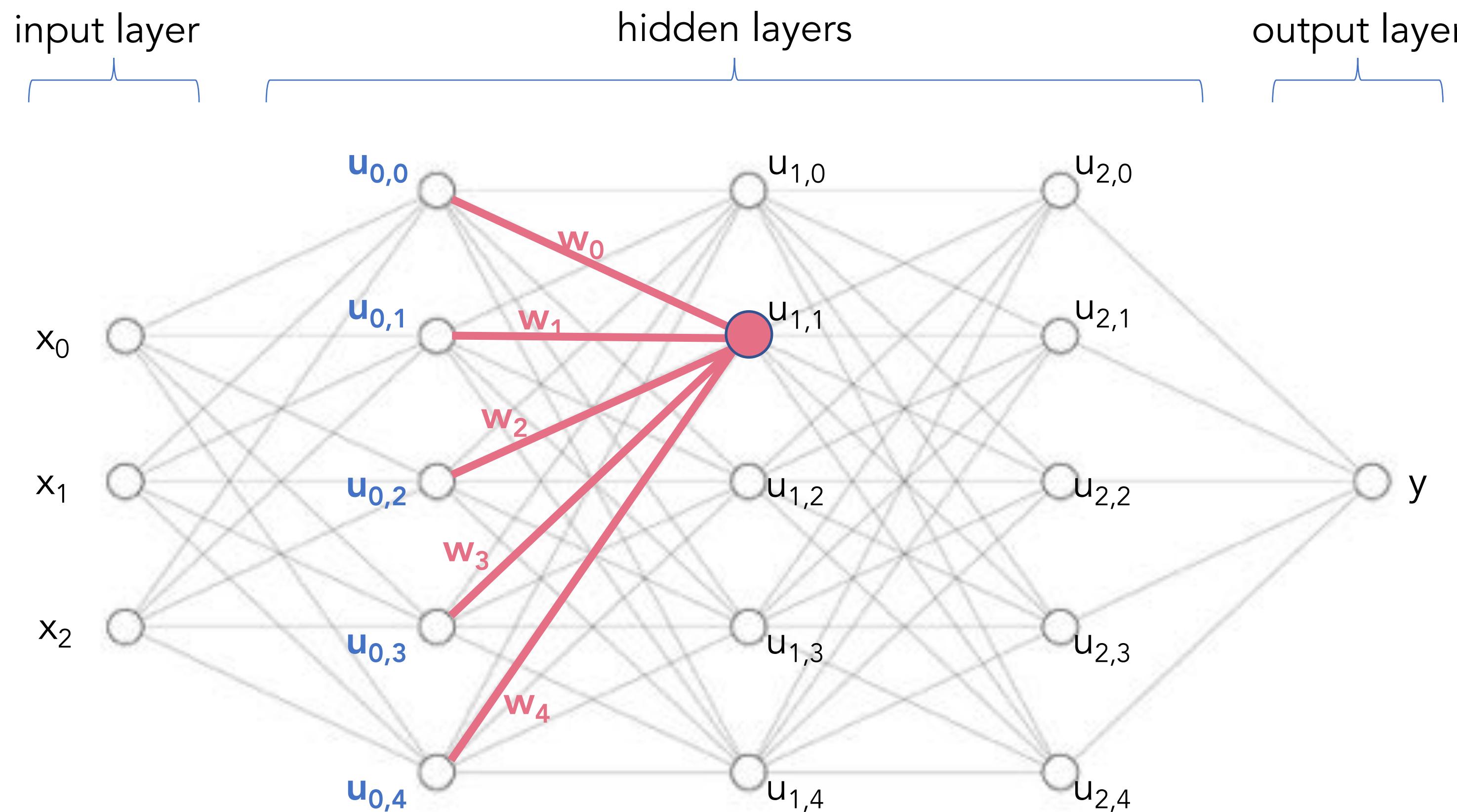


Training the DNN

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Training DNN:

Define loss function, e.g.
MSE:

Find good set of weights
by searching for a local
minimum of

Training the DNN

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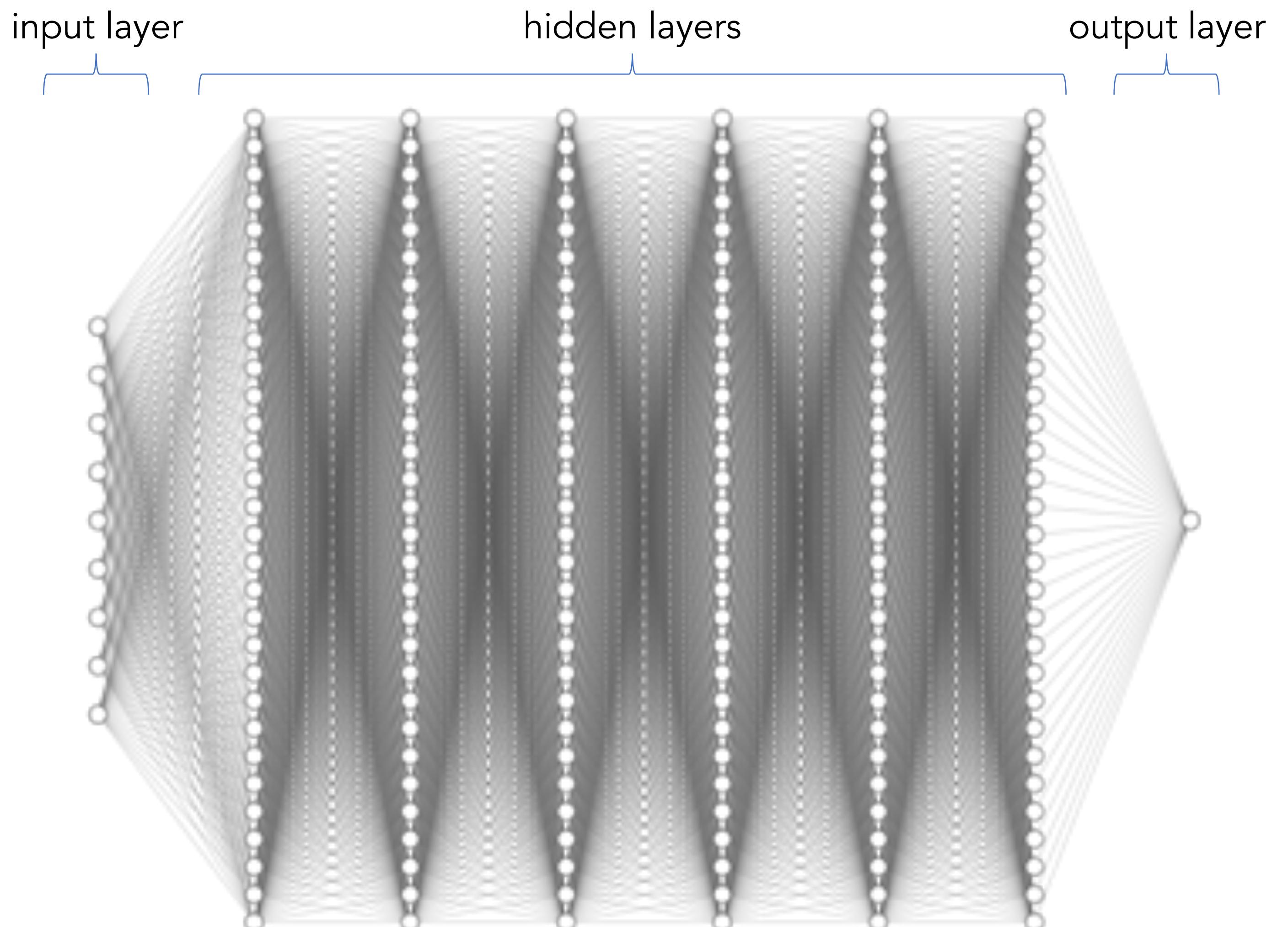
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6 hidden layers
2048 units per hidden layer

Input parameters:
mass
luminosity
equilibrium temperature
layer mass fractions
core composition
mantle composition

Output parameters:
transit radius
future project: layer thicknesses

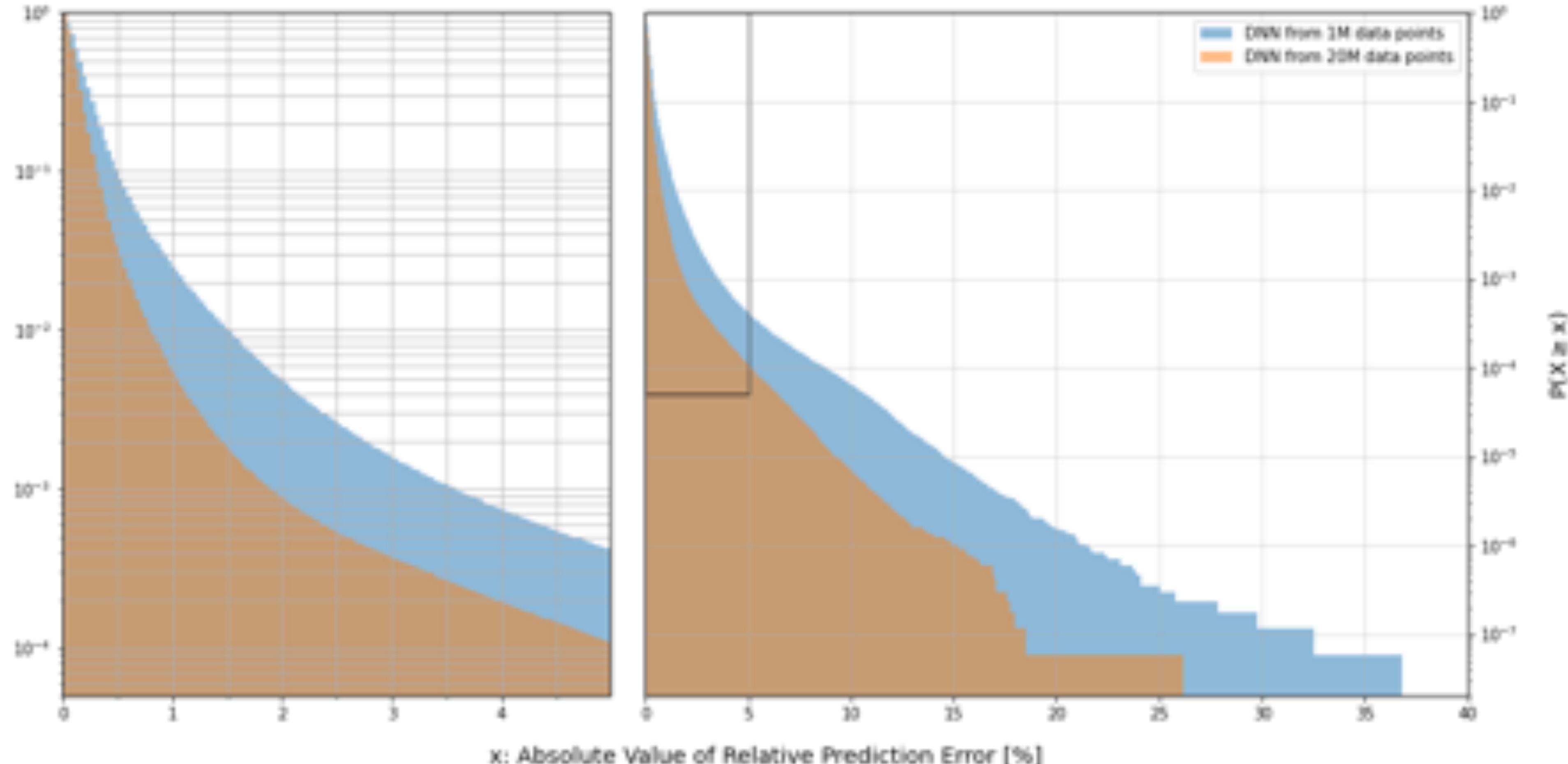


DNN performances

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Data generation = 1 week

1. Choose priors of internal structure parameters

2. Sample from entire parameter space according to priors

3. For each sampled structure, use internal structure model to calculate radius

4. Keep the structure based on likelihood (probability of observation given parameters)



posterior distribution of internal structure parameters

Advantages:

- relatively low computation time (~1-3 hours)
- no problem of local maxima
- no problem of convergence

Problem with both MCMC and brut force approach:

Measurements of observable quantities taken with respect to stellar quantities
high correlation between planets in multiplanetary systems

Modelling n planets in a system simultaneously means

- dimension of parameter space is multiplied by n
- necessary number of sampling points (and therefore computation time) increases drastically

Sampling the posterior distribution

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1. Sample from stellar parameter space

2. Create planets for each generated star:
For each planet in the system, sample from priors of internal structure parameters

3. Use DNN to calculate radii of planets

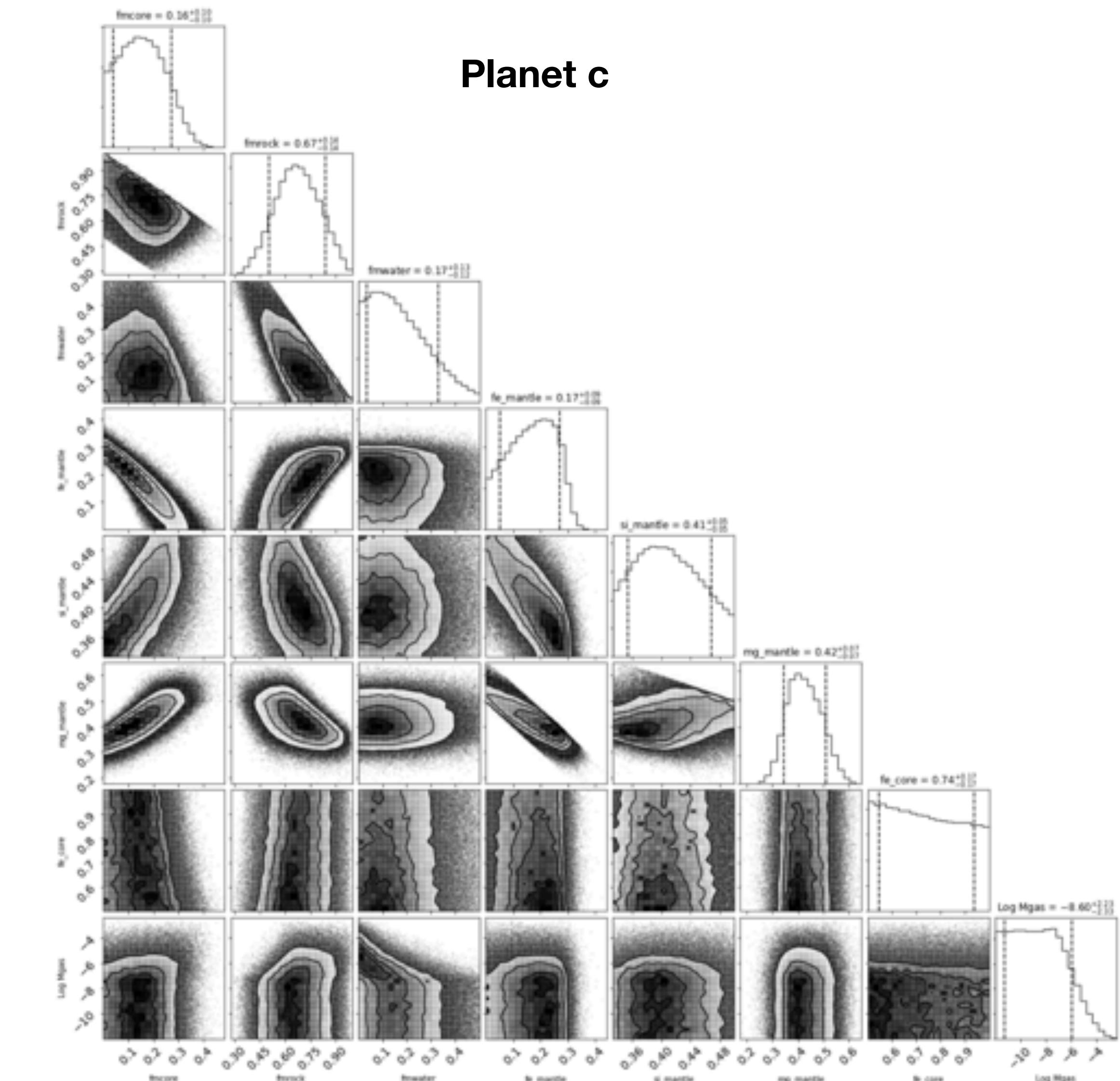
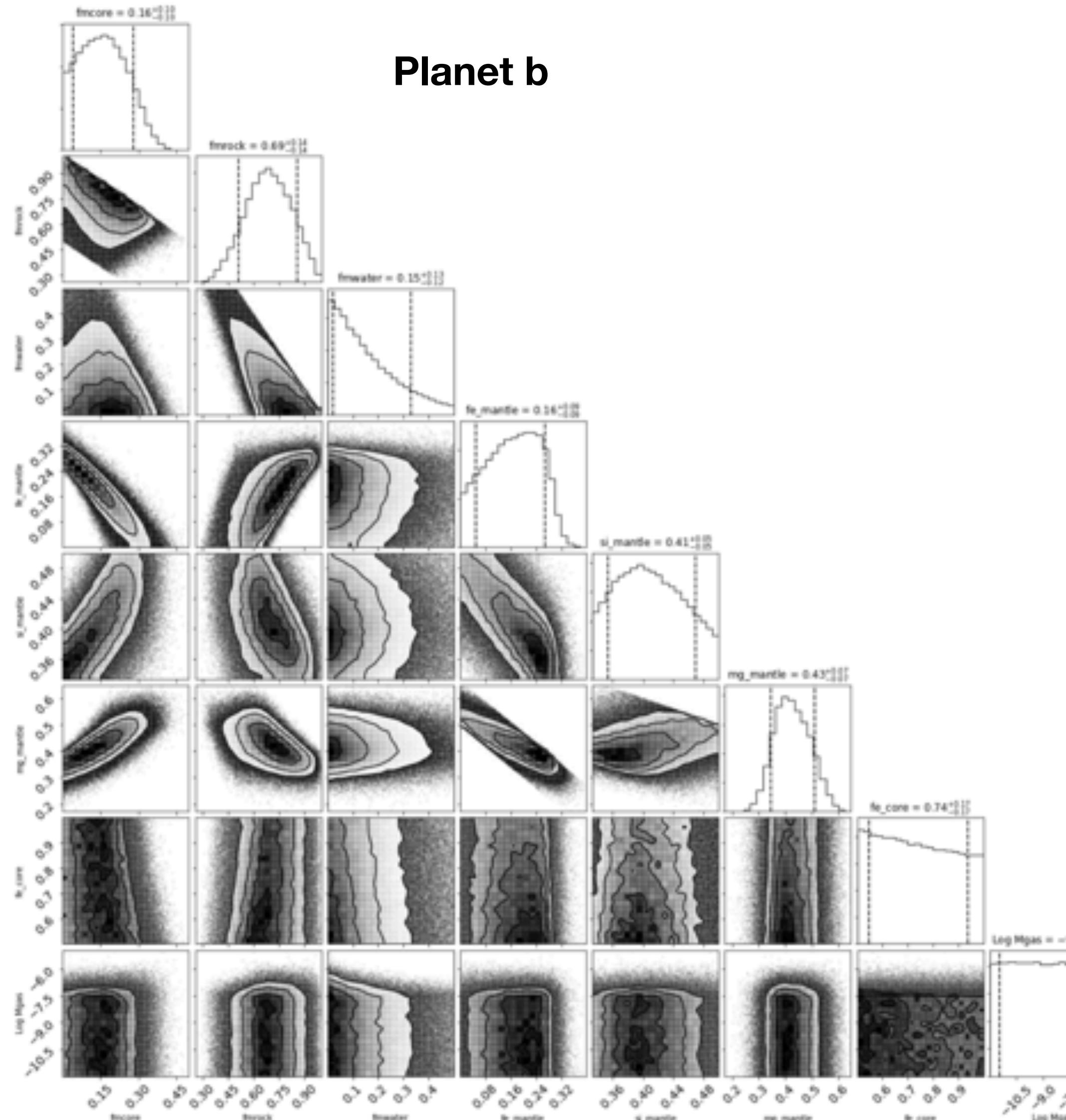
4. Calculate transit depth and keep the system based on likelihood of planets:

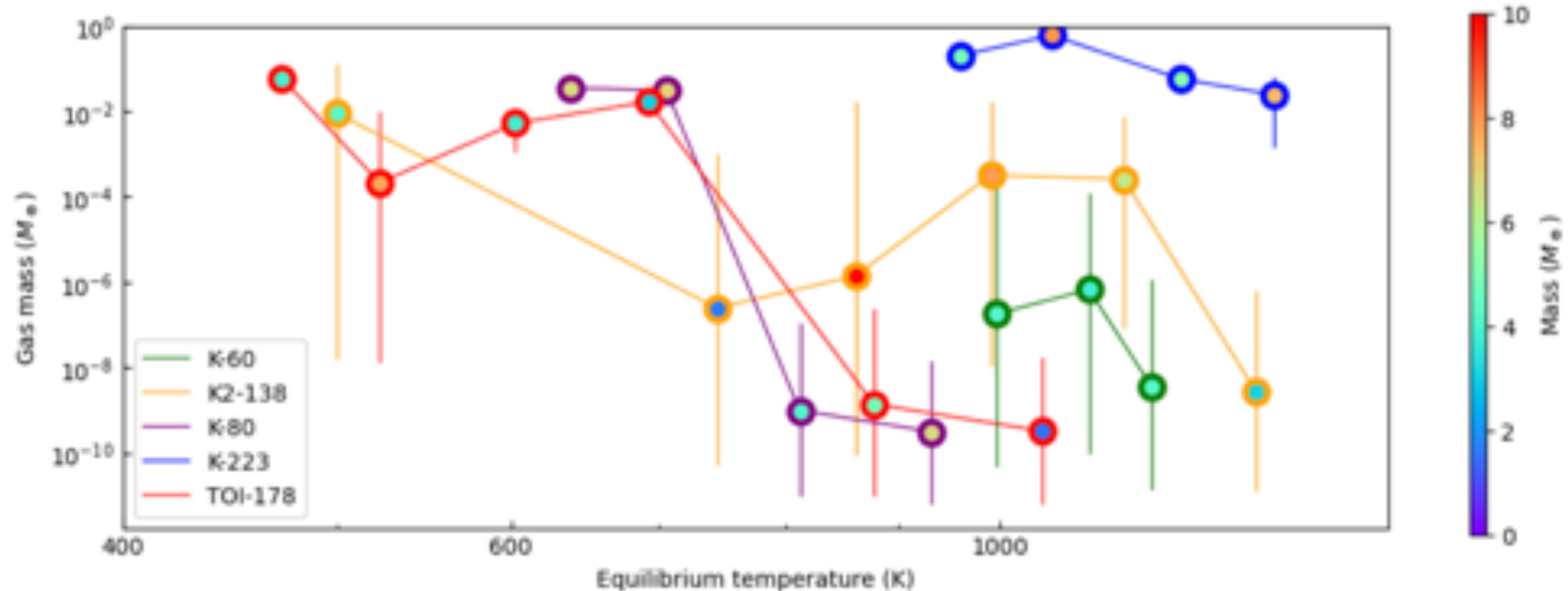
Exemple of TOI178

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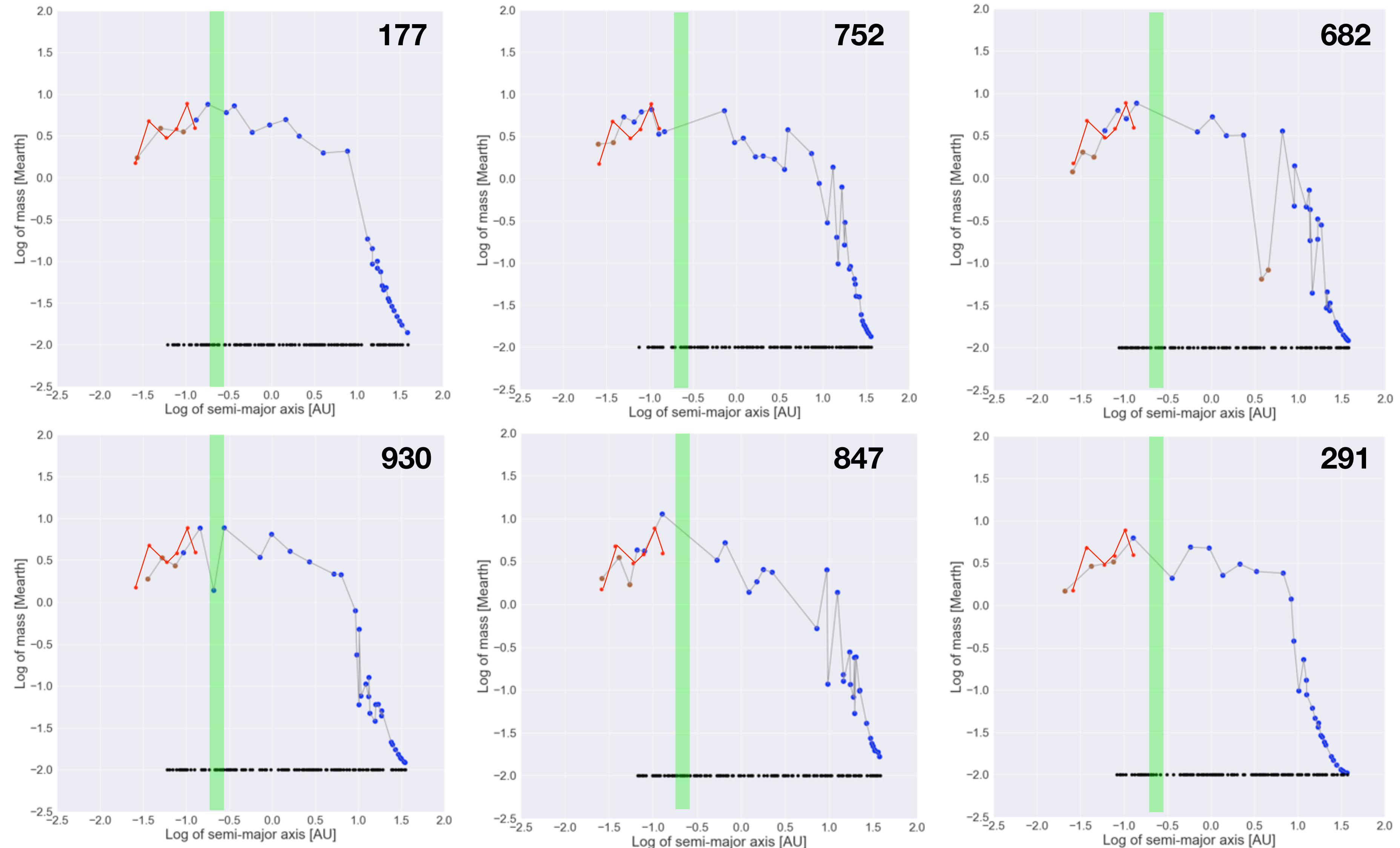


Exemple of TOI178

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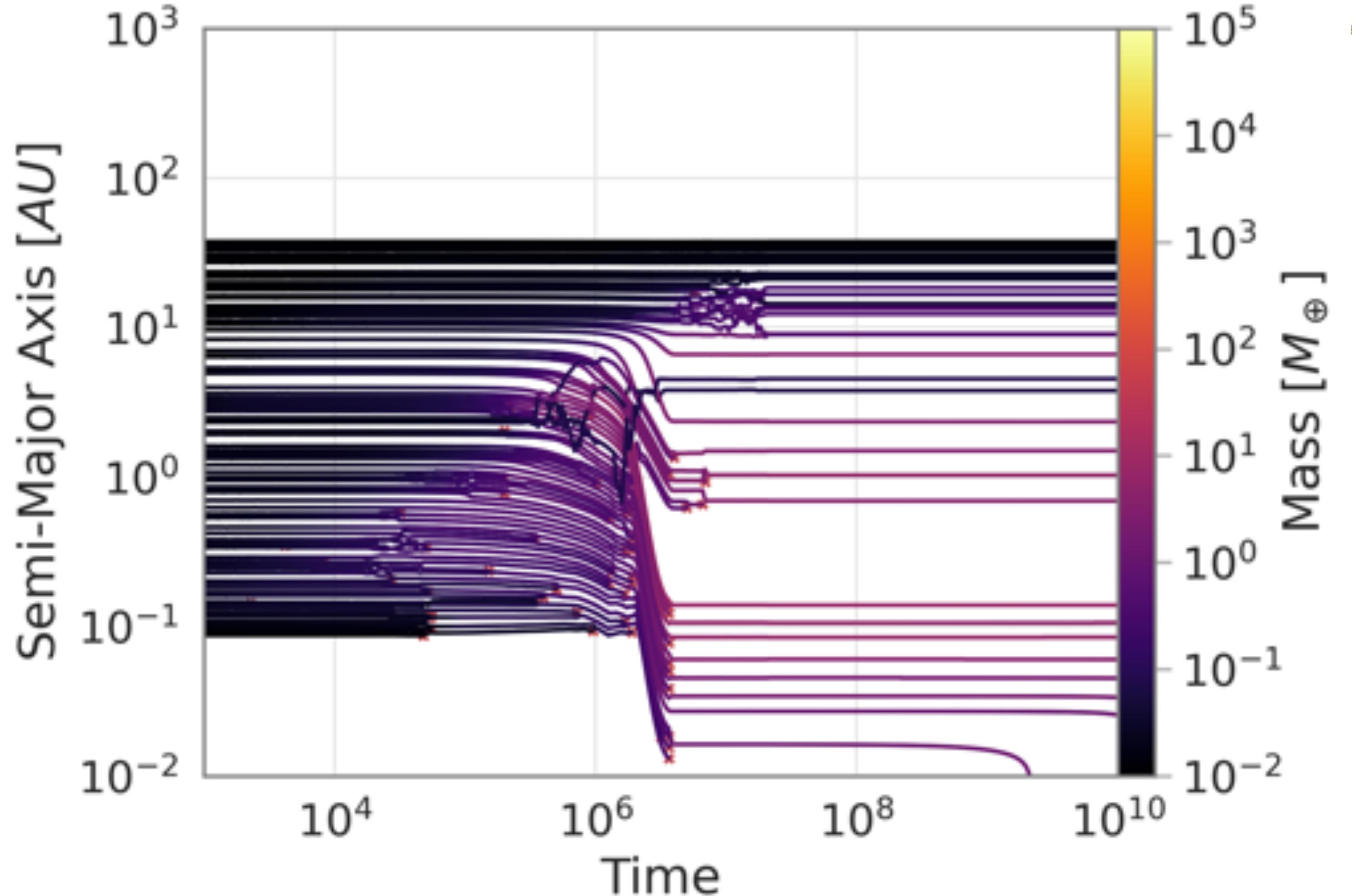
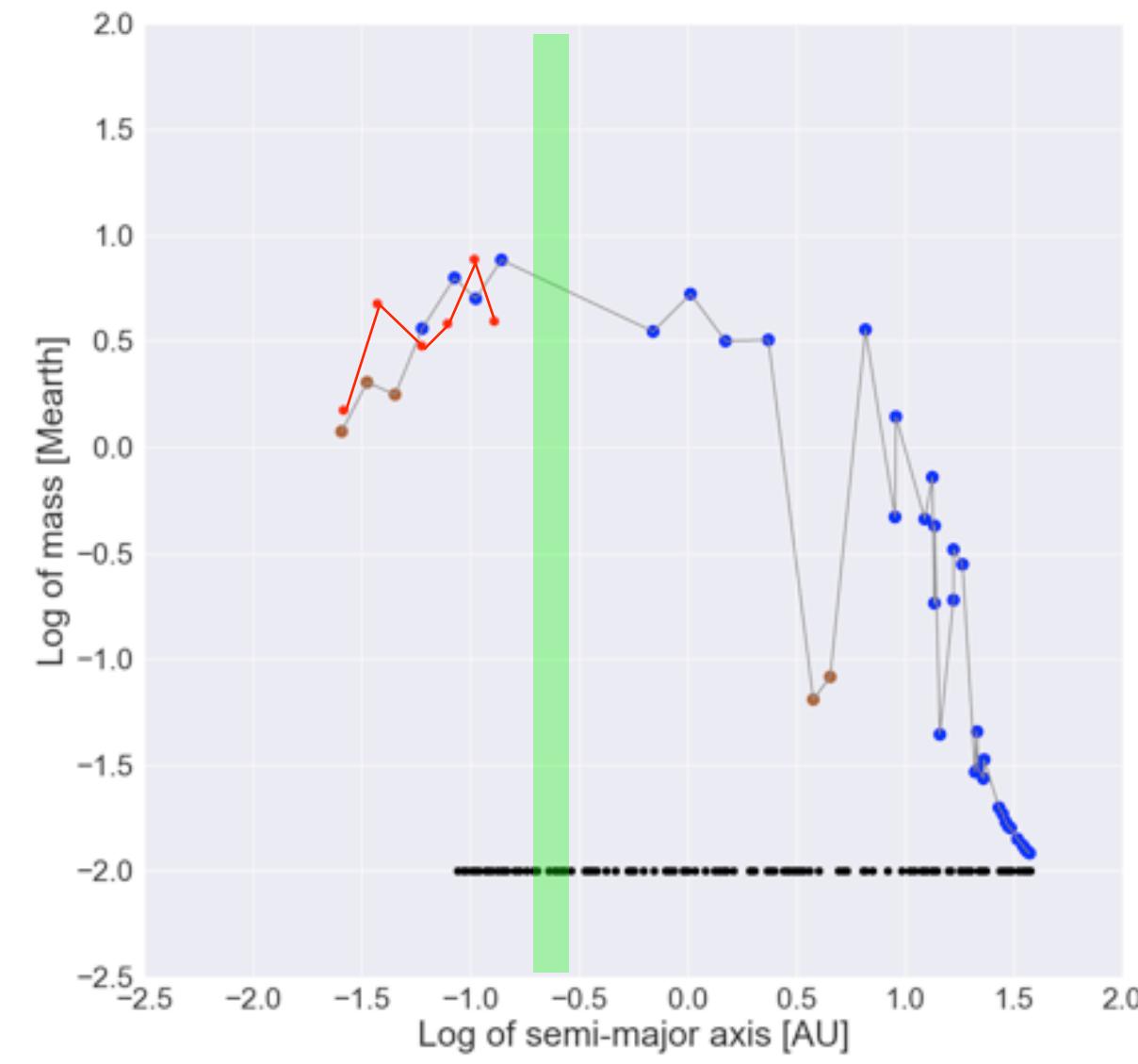


Exemple of TOI178

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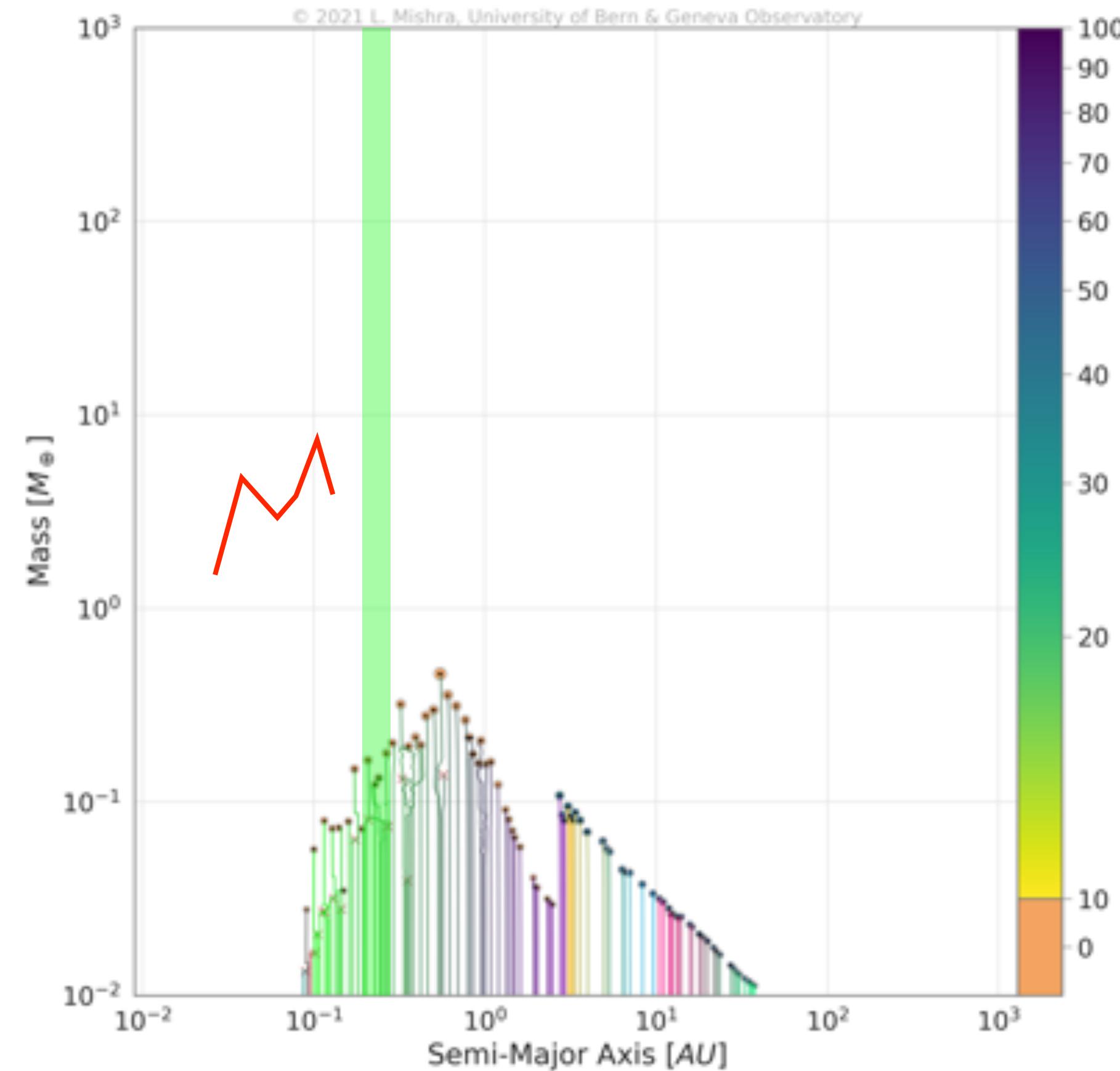


System 682

Bern Model: Mass vs SMA Diagram at Time = 1.00e+05 yr

Population: NG76 Gas Disc Mass Coefficient of Similarity
System ID: 682 Initial = $0.025 M_{\odot}$ C_{sim} (mass) = -0.00
#embryos: 100 Acc. = $0.001 M_{\odot}$ (2.7 %) C_{sim} (radius) = 0.00
Multiplicity: 87 Evap. = $0.002 M_{\odot}$ (8.3 %) C_{sim} (density) = -0.00

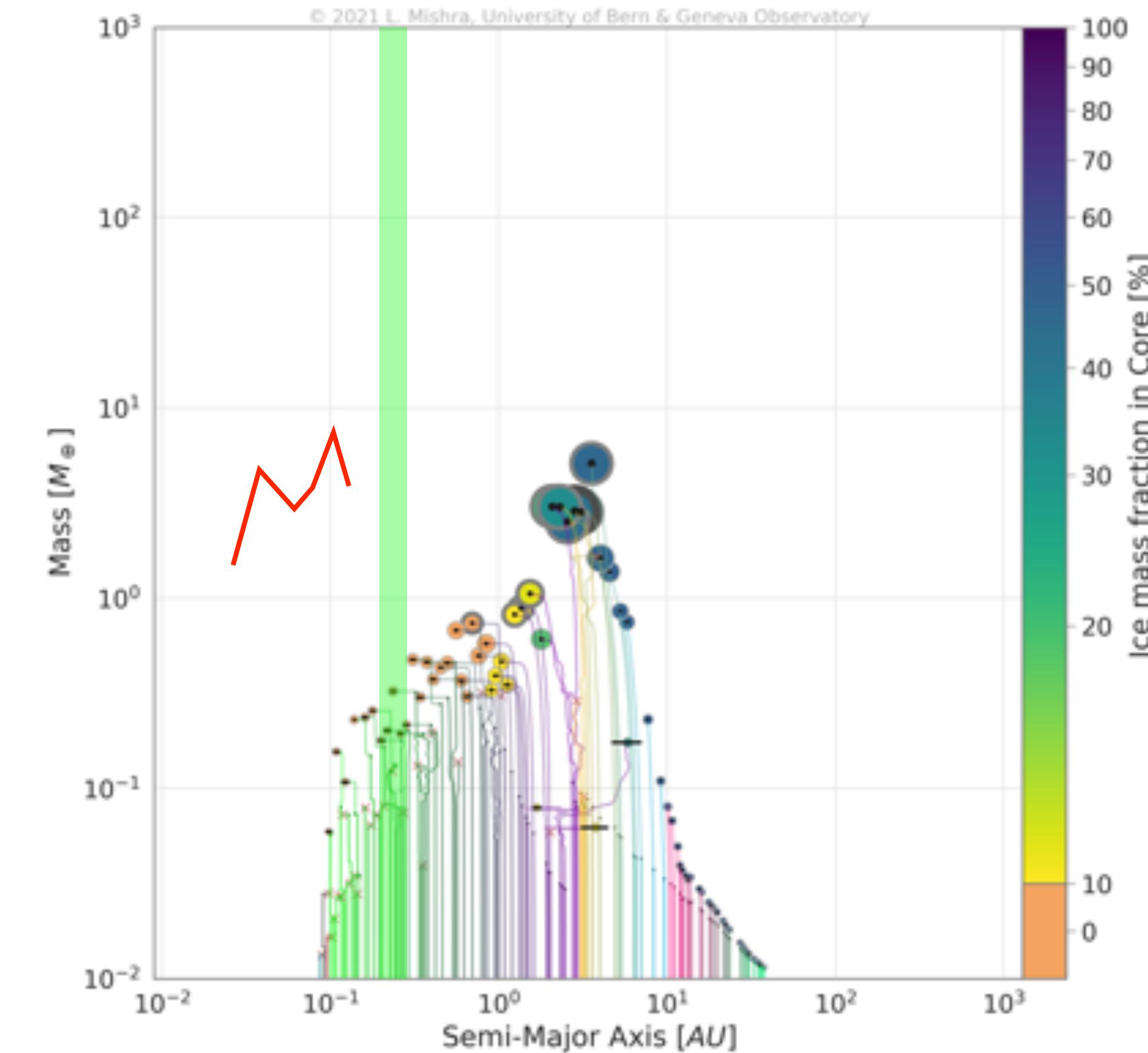
Star Solid Disc Mass System Property
Mass = $1.0 M_{\odot}$ Initial = $113.43 M_{\oplus}$ Compactness = 1.7×10^{-2}
Radius = $3.1 R_{\odot}$ Acc. = $6.81 M_{\oplus}$ (6.0 %) Composition = $65.7 R_{\oplus}^2$
[Fe/H] = 0.07 dex Eject = $0.00 M_{\oplus}$ (0.0 %) Dynamics = 2.1×10^{-7} AU



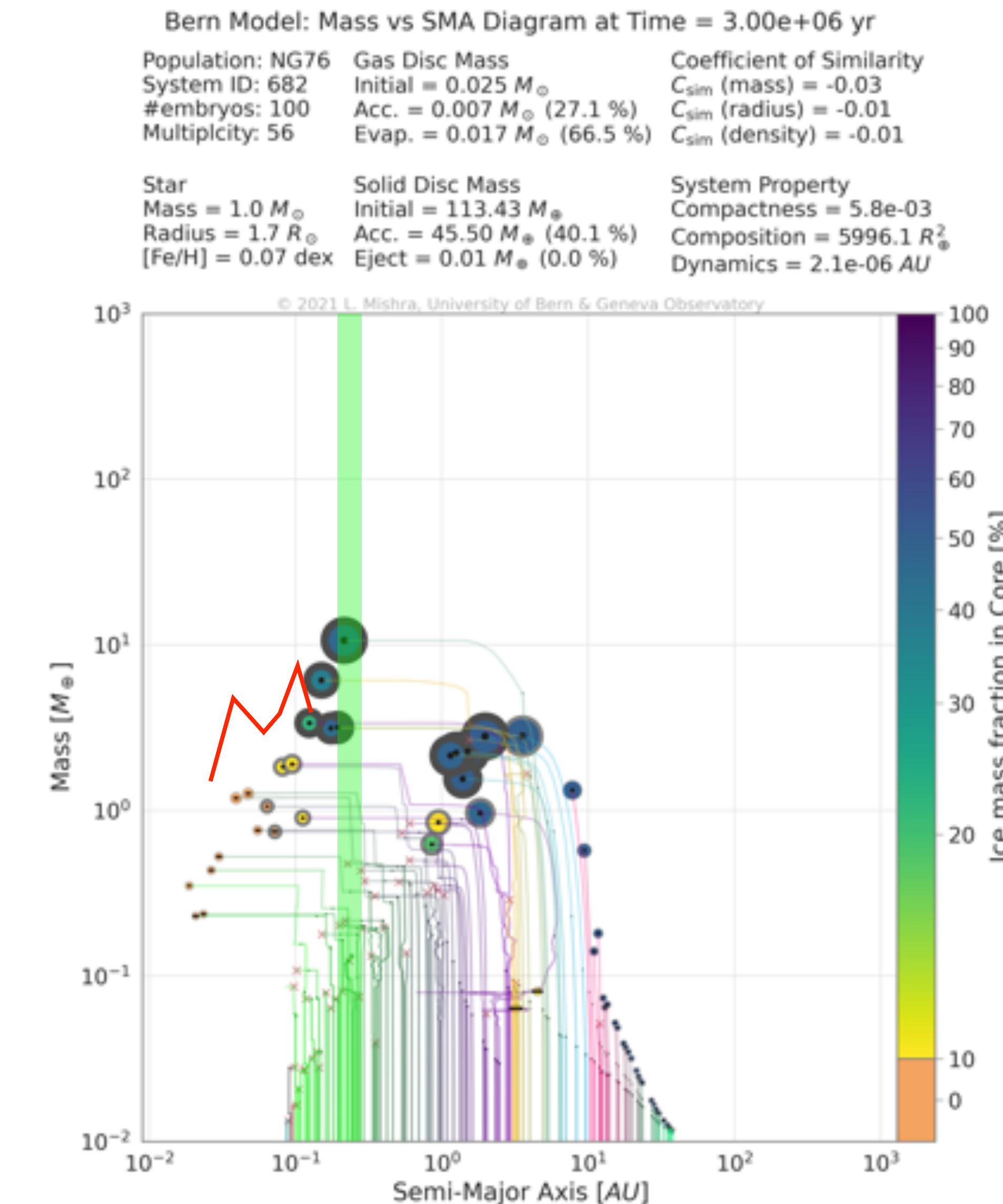
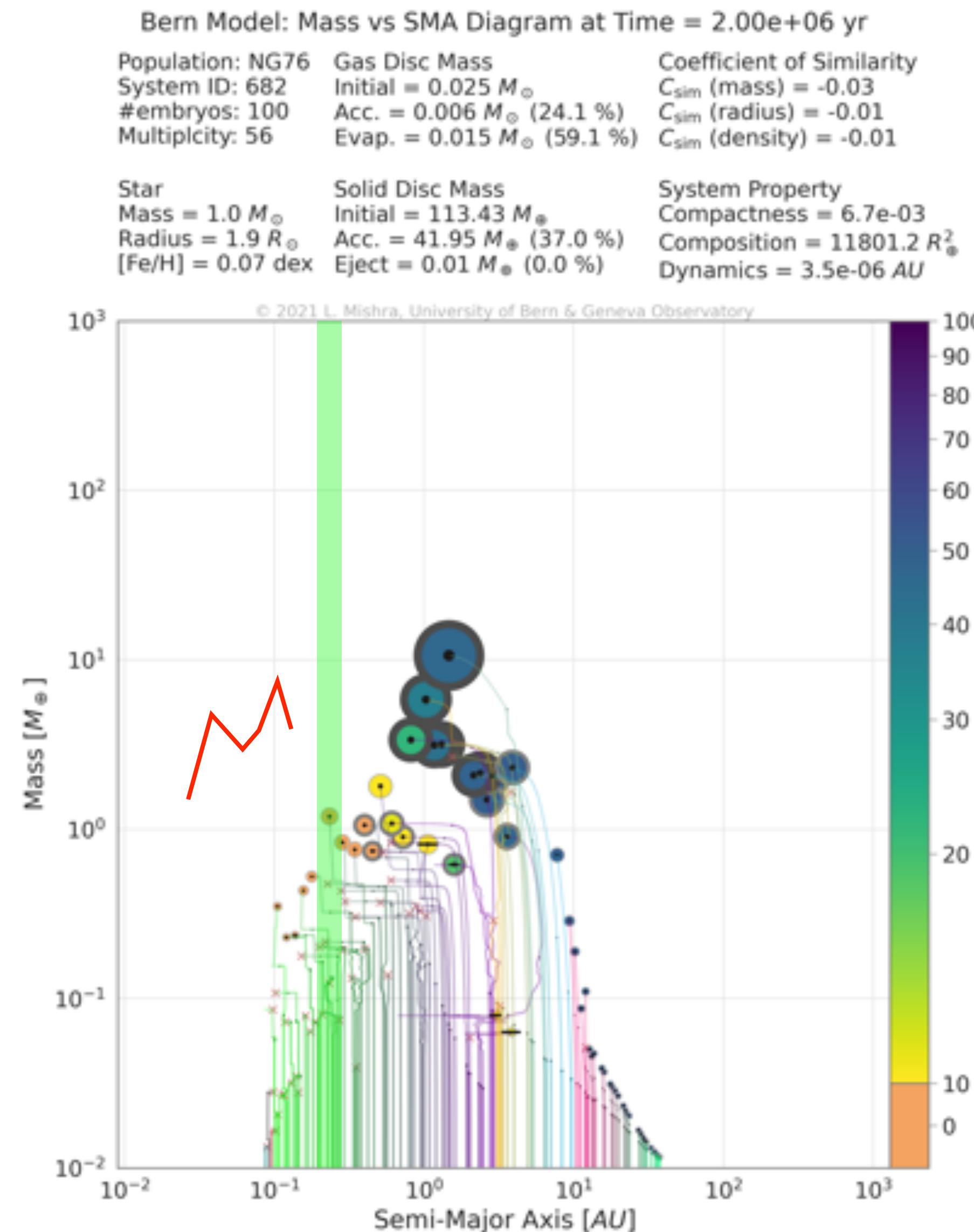
Bern Model: Mass vs SMA Diagram at Time = 1.00e+06 yr

Population: NG76 Gas Disc Mass Coefficient of Similarity
System ID: 682 Initial = $0.025 M_{\odot}$ C_{sim} (mass) = -0.01
#embryos: 100 Acc. = $0.004 M_{\odot}$ (16.8 %) C_{sim} (radius) = -0.00
Multiplicity: 74 Evap. = $0.010 M_{\odot}$ (42.0 %) C_{sim} (density) = -0.01

Star Solid Disc Mass System Property
Mass = $1.0 M_{\odot}$ Initial = $113.43 M_{\oplus}$ Compactness = 1.1×10^{-2}
Radius = $2.4 R_{\odot}$ Acc. = $35.65 M_{\oplus}$ (31.4 %) Composition = $4679.1 R_{\oplus}^2$
[Fe/H] = 0.07 dex Eject = $0.01 M_{\oplus}$ (0.0 %) Dynamics = 3.6×10^{-6} AU



System 682

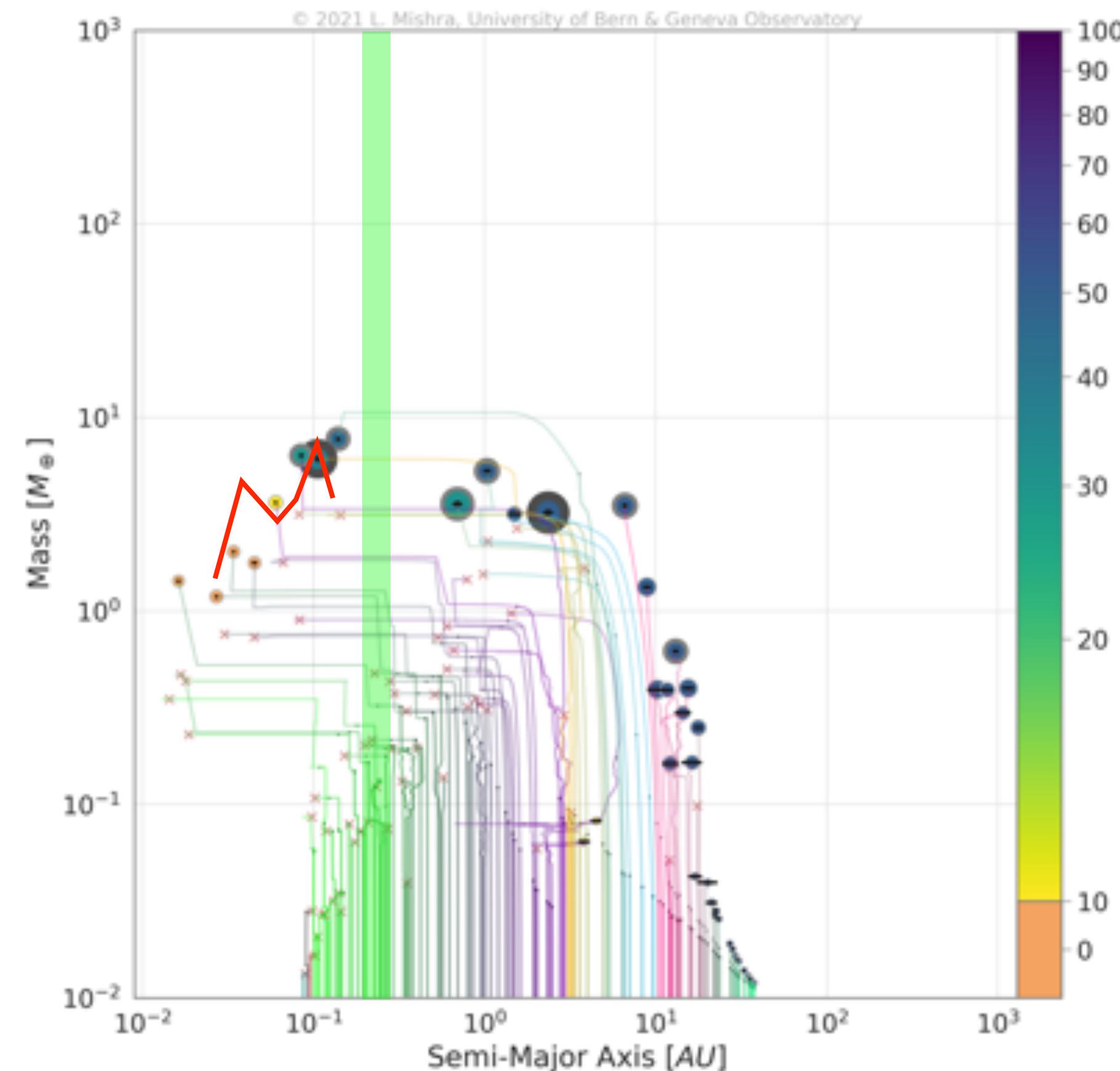


System 682

Bern Model: Mass vs SMA Diagram at Time = 1.00e+07 yr

Population: NG76 Gas Disc Mass Coefficient of Similarity
System ID: 682 Initial = $0.025 M_{\odot}$ C_{sim} (mass) = -0.05
#embryos: 100 Acc. = $0.007 M_{\odot}$ (27.6 %) C_{sim} (radius) = -0.01
Multiplicity: 40 Evap. = $0.017 M_{\odot}$ (69.0 %) C_{sim} (density) = -0.01

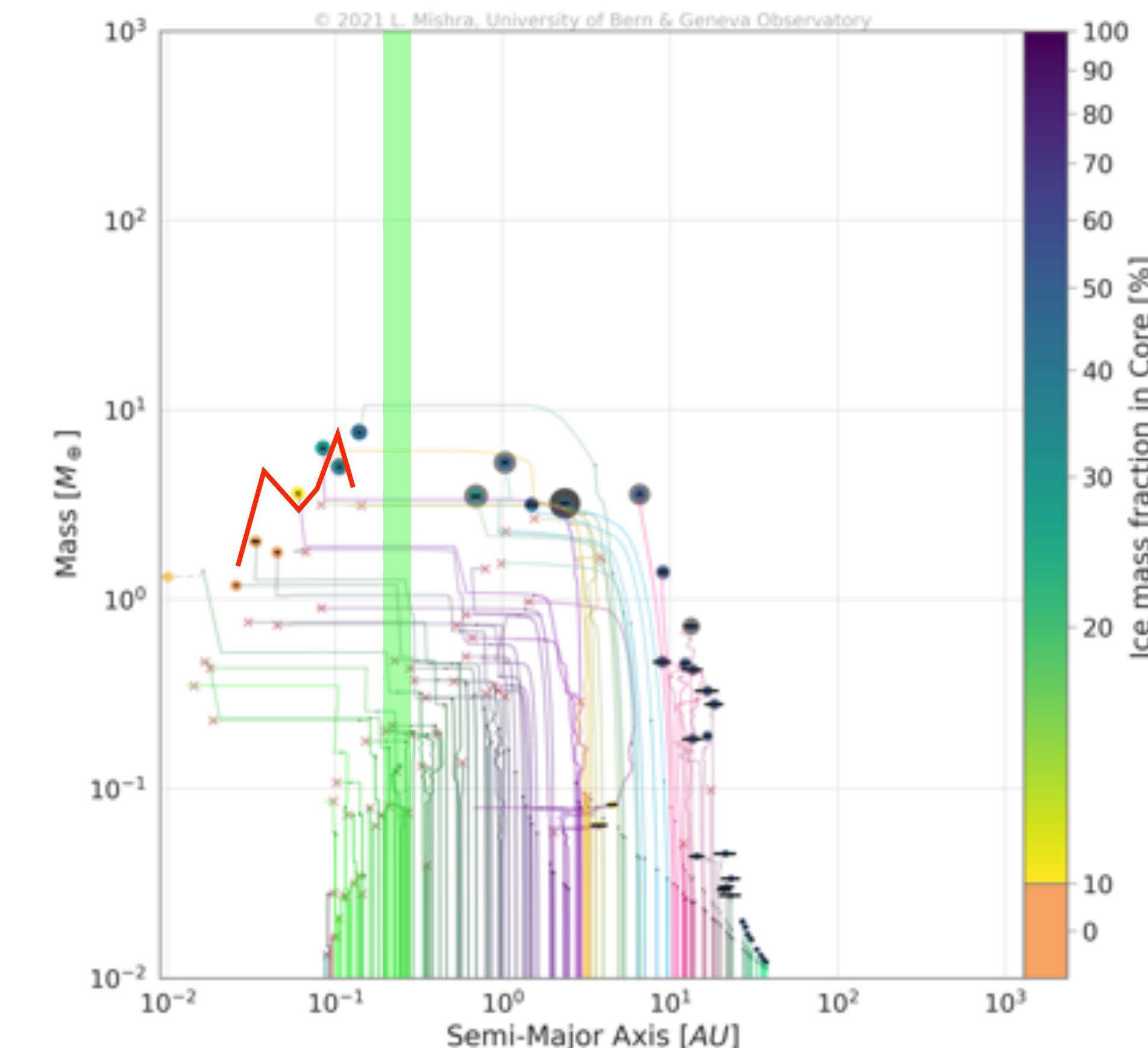
Star Solid Disc Mass System Property
Mass = $1.0 M_{\odot}$ Initial = $113.43 M_{\oplus}$ Compactness = 2.9×10^{-3}
Radius = $1.2 R_{\odot}$ Acc. = $50.34 M_{\oplus}$ (44.4 %) Composition = $930.5 R_{\oplus}^2$
[Fe/H] = 0.07 dex Eject = $0.02 M_{\oplus}$ (0.0 %) Dynamics = 3.4×10^{-6} AU



Bern Model: Mass vs SMA Diagram at Time = 1.00e+10 yr

Population: NG76 Gas Disc Mass Coefficient of Similarity
System ID: 682 Initial = $0.025 M_{\odot}$ C_{sim} (mass) = -0.05
#embryos: 100 Acc. = $0.007 M_{\odot}$ (27.6 %) C_{sim} (radius) = -0.01
Multiplicity: 39 Evap. = $0.017 M_{\odot}$ (69.0 %) C_{sim} (density) = -0.01

Star Solid Disc Mass System Property
Mass = $1.0 M_{\odot}$ Initial = $113.43 M_{\oplus}$ Compactness = 2.9×10^{-3}
Radius = $1.2 R_{\odot}$ Acc. = $50.89 M_{\oplus}$ (44.9 %) Composition = $235.2 R_{\oplus}^2$
[Fe/H] = 0.07 dex Eject = $0.02 M_{\oplus}$ (0.0 %) Dynamics = 3.6×10^{-6} AU



1- Planet formation and the Bern model

2- Models *versus* observations

3- Planetary internal structure and Deep Learning

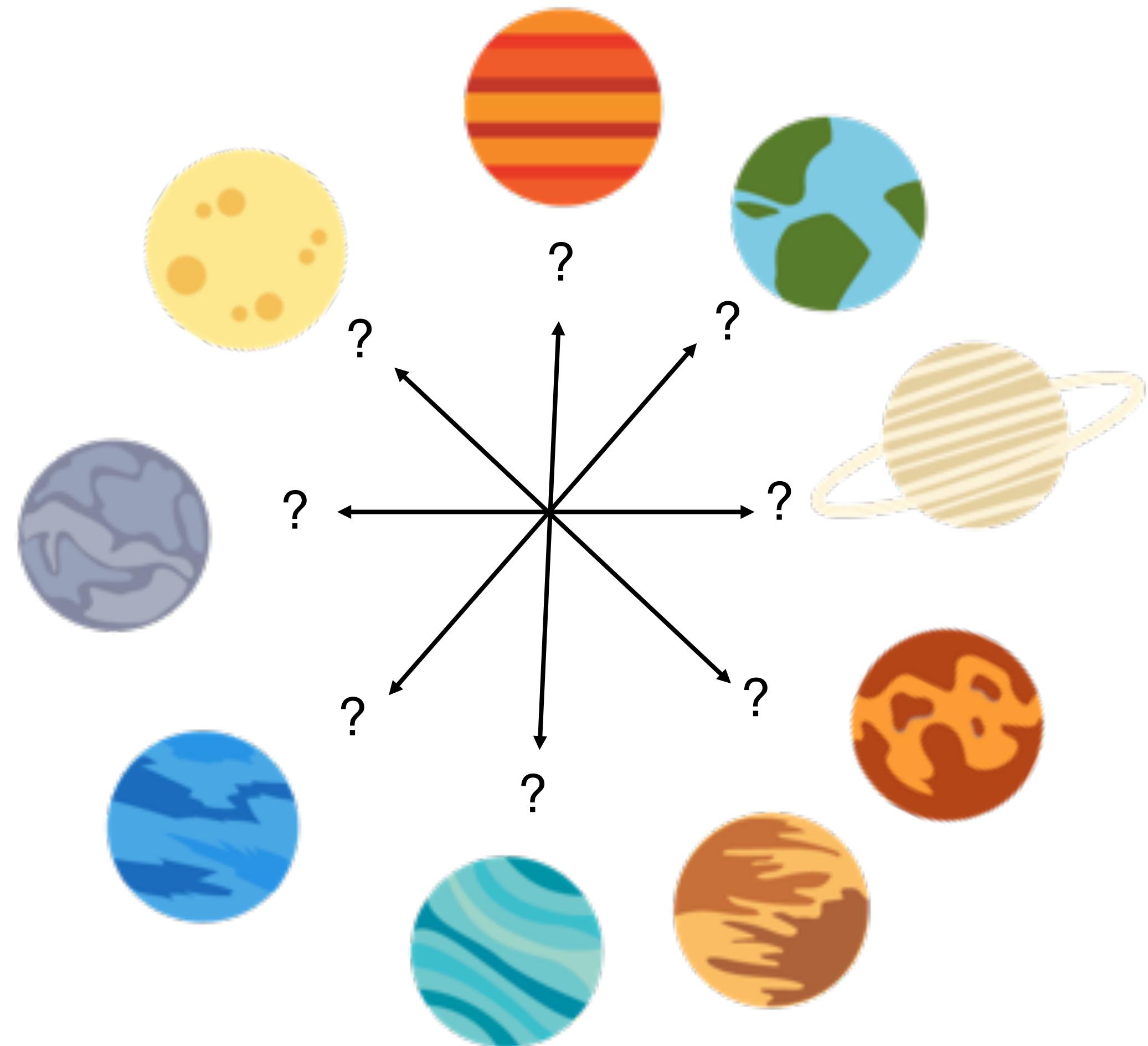
4- Correlation in planetary systems with random forest: finding a second Earth

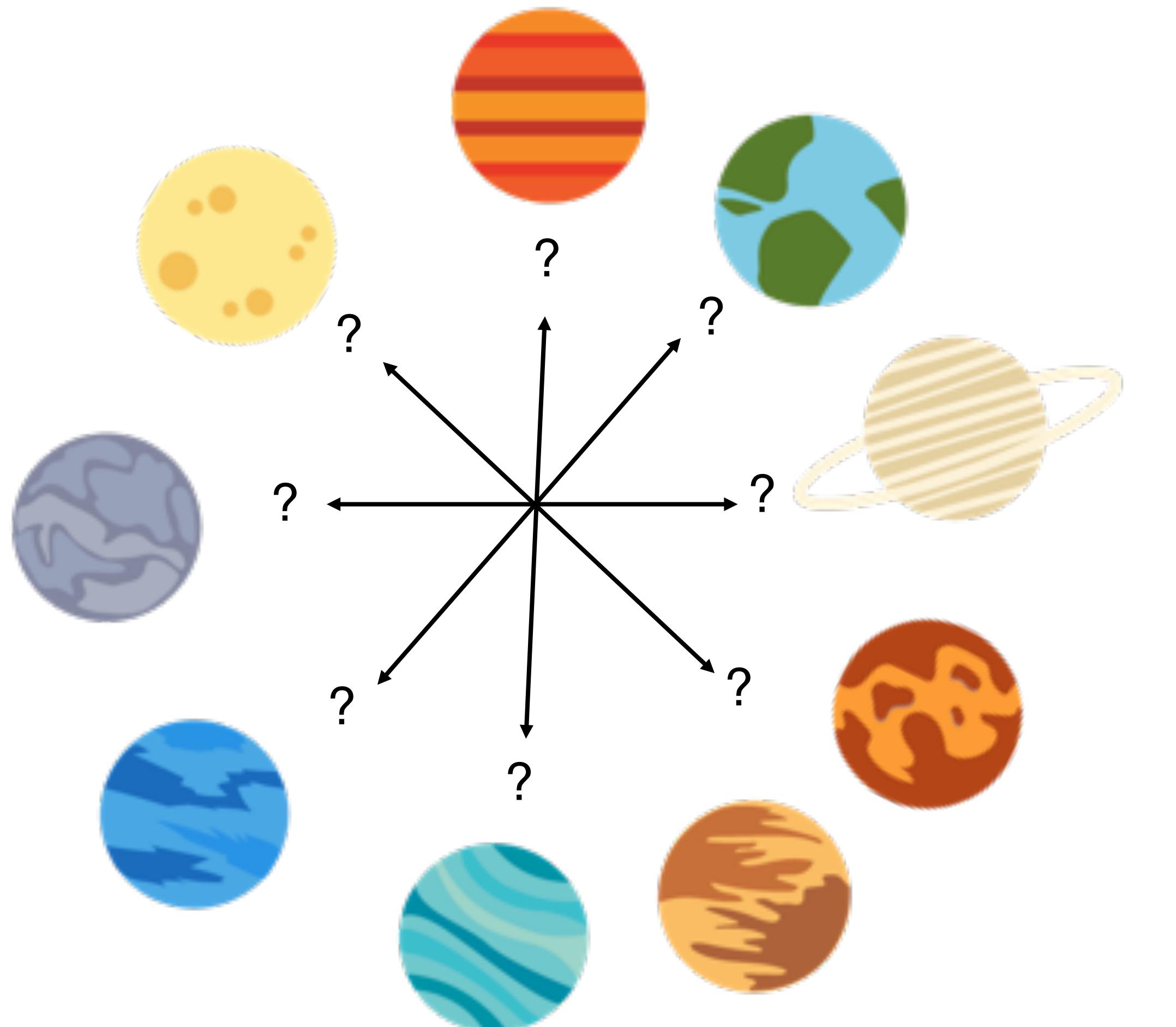
Correlations in planetary systems

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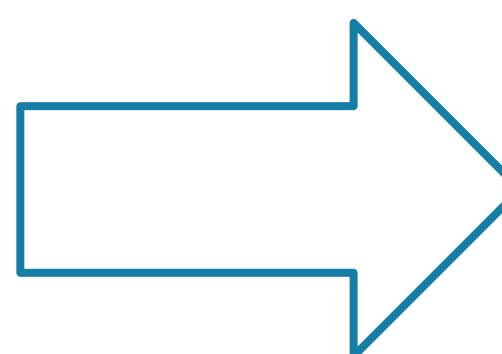
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Formation and evolution
of planetary systems ?

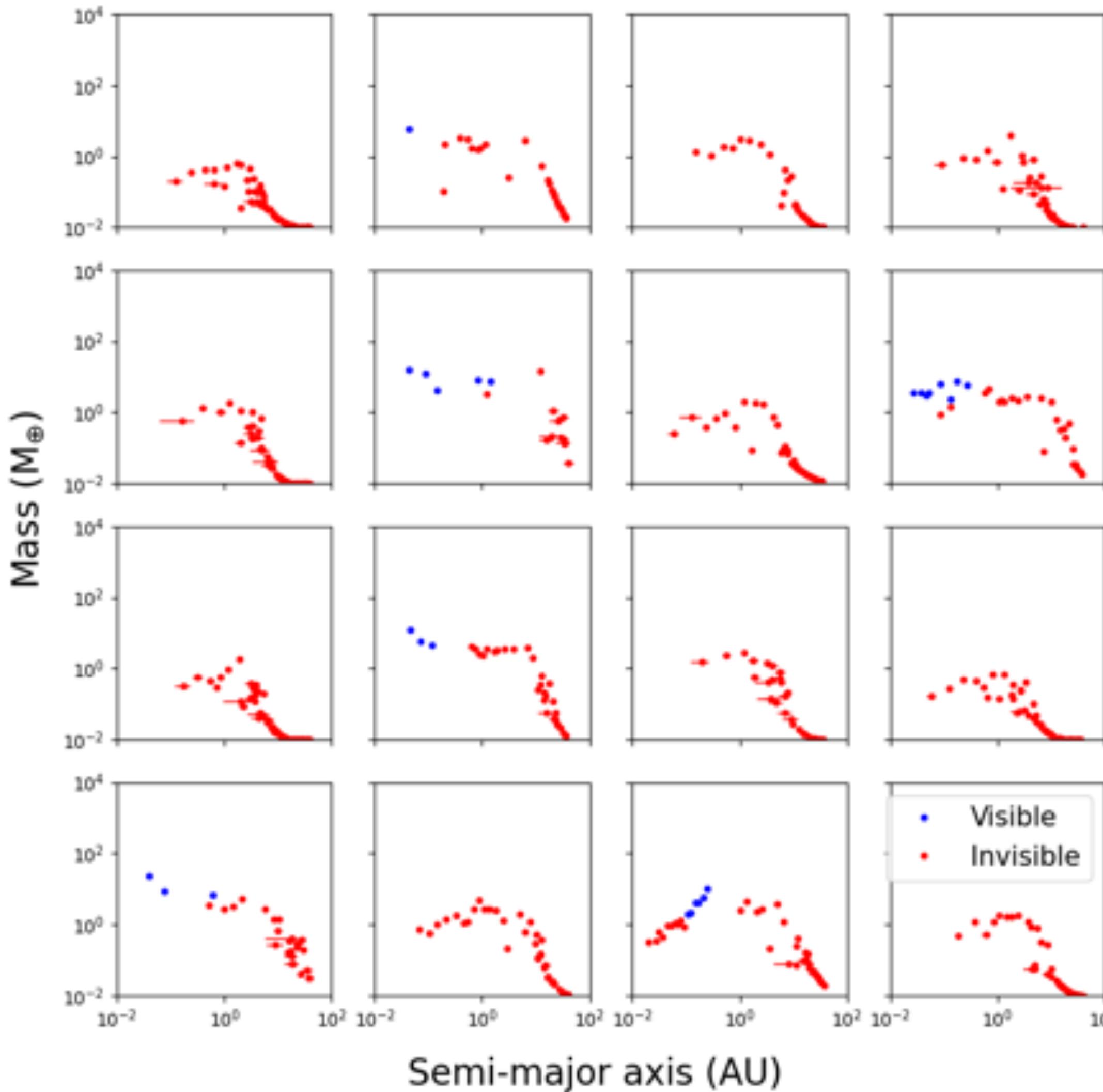


Properties
of
hidden planets ?

Systems with Earth-like planet

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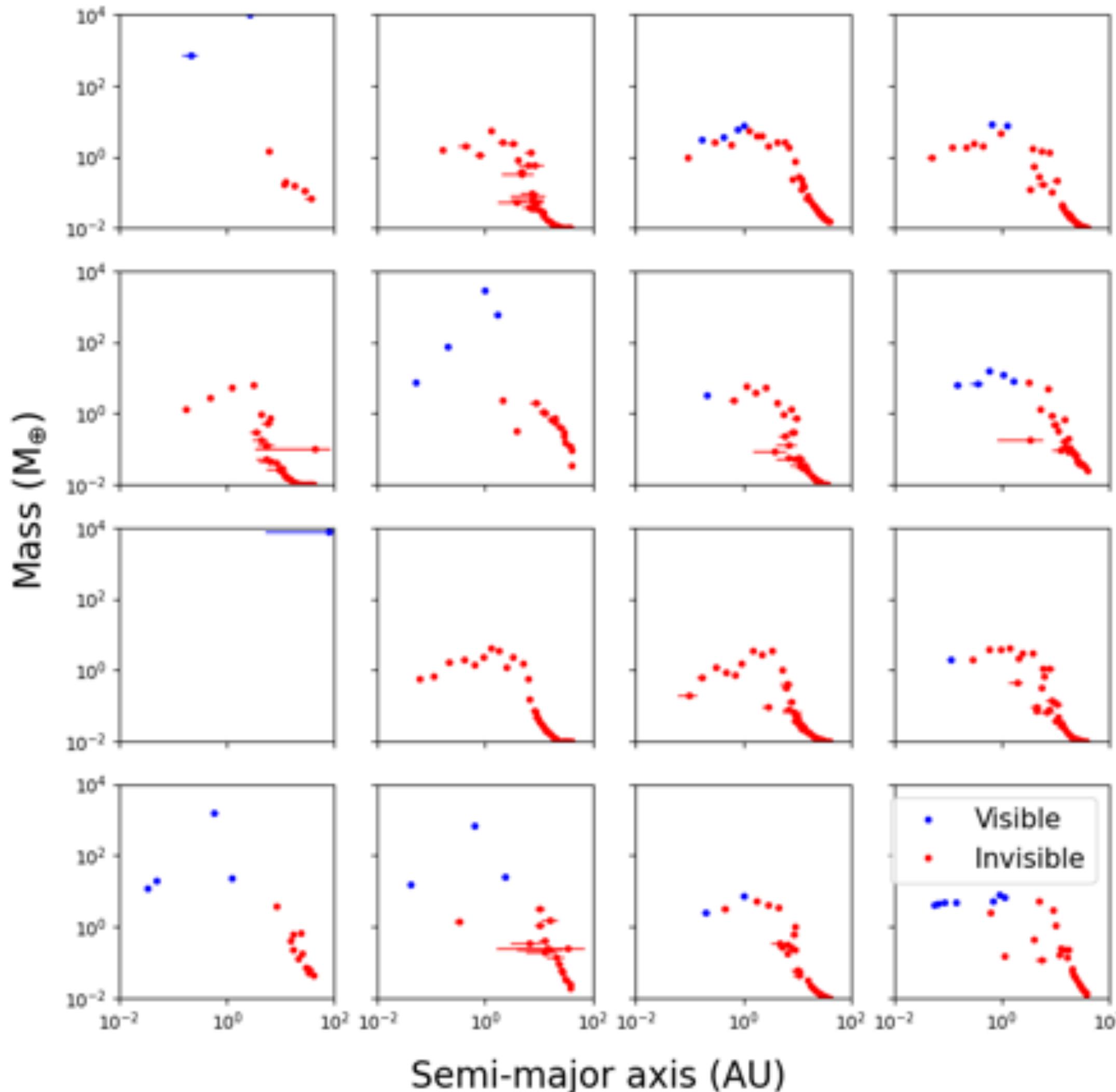
- Systems look regular
- Almost no Giant planet ($> 100 M_{\oplus}$)
- Some Neptunes ($\sim 10 M_{\oplus}$)
- Few visible planets
- The innermost planet is often smaller than 1 Mearth

Systems without Earth-like planet

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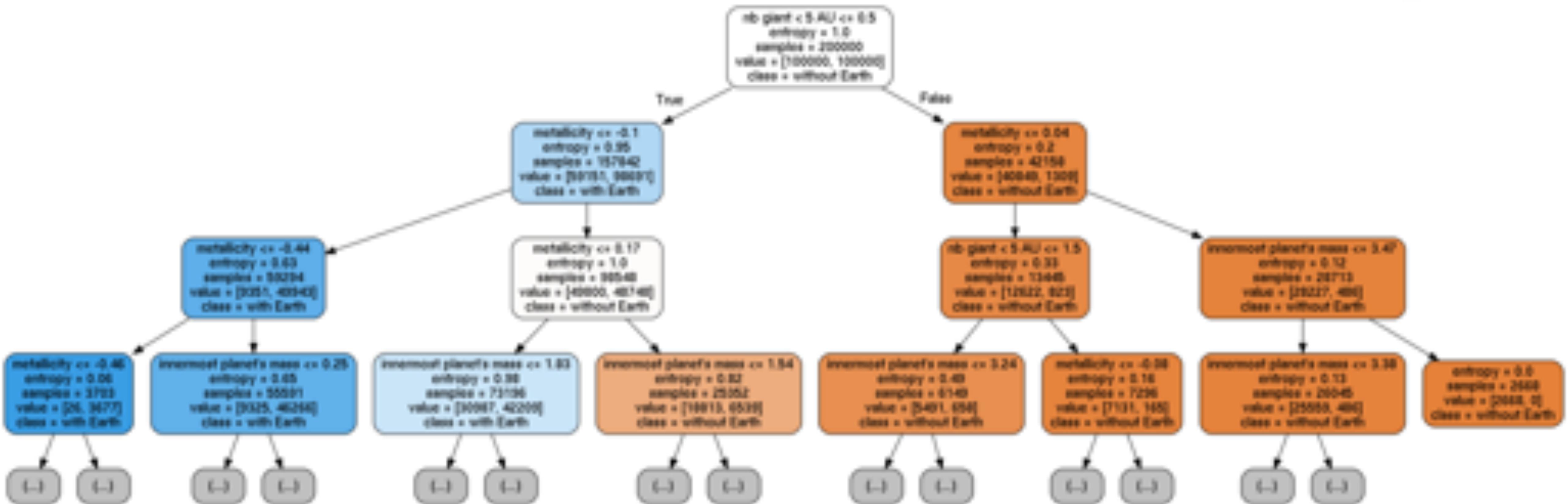
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- Systems look less regular
- More giant planets ($> 100 M_{\oplus}$)
- Presence of a Neptune is common ($> 10 M_{\oplus}$)
- More visible planets
- The mass of the innermost planet can be high

16 systems from population NG76 without any Earth-like planet

Random forest classifier



- The number of visible planets
- The number of giant planets inside 5 AU
- The innermost planet's mass

- Metallicity of the star
- Mass of the star

1- 1000 trees, all slightly different

2- Final decision depends on fraction of positive/negative trees (50%, 70%...)

3- Performances depend on this threshold

≥ 50%	Precision score	0.73
	Recall score	0.87
	Accuracy score	0.74
≥ 70%	Precision score	0.83
	Recall score	0.44
	Accuracy score	0.61
≥ 90%	Precision score	0.86
	Recall score	0.05
	Accuracy score	0.44

1- 1000 trees, all slightly different

2- Final decision depends on fraction of positive/negative trees (50%, 70%...)

3- Performances depend on this threshold

50%	Precision score	0.73
	Recall score	0.87
70%	Precision score	0.83
	Recall score	0.44

<- more false positive

<- more false negative

4- 3 systems identify > 80% threshold

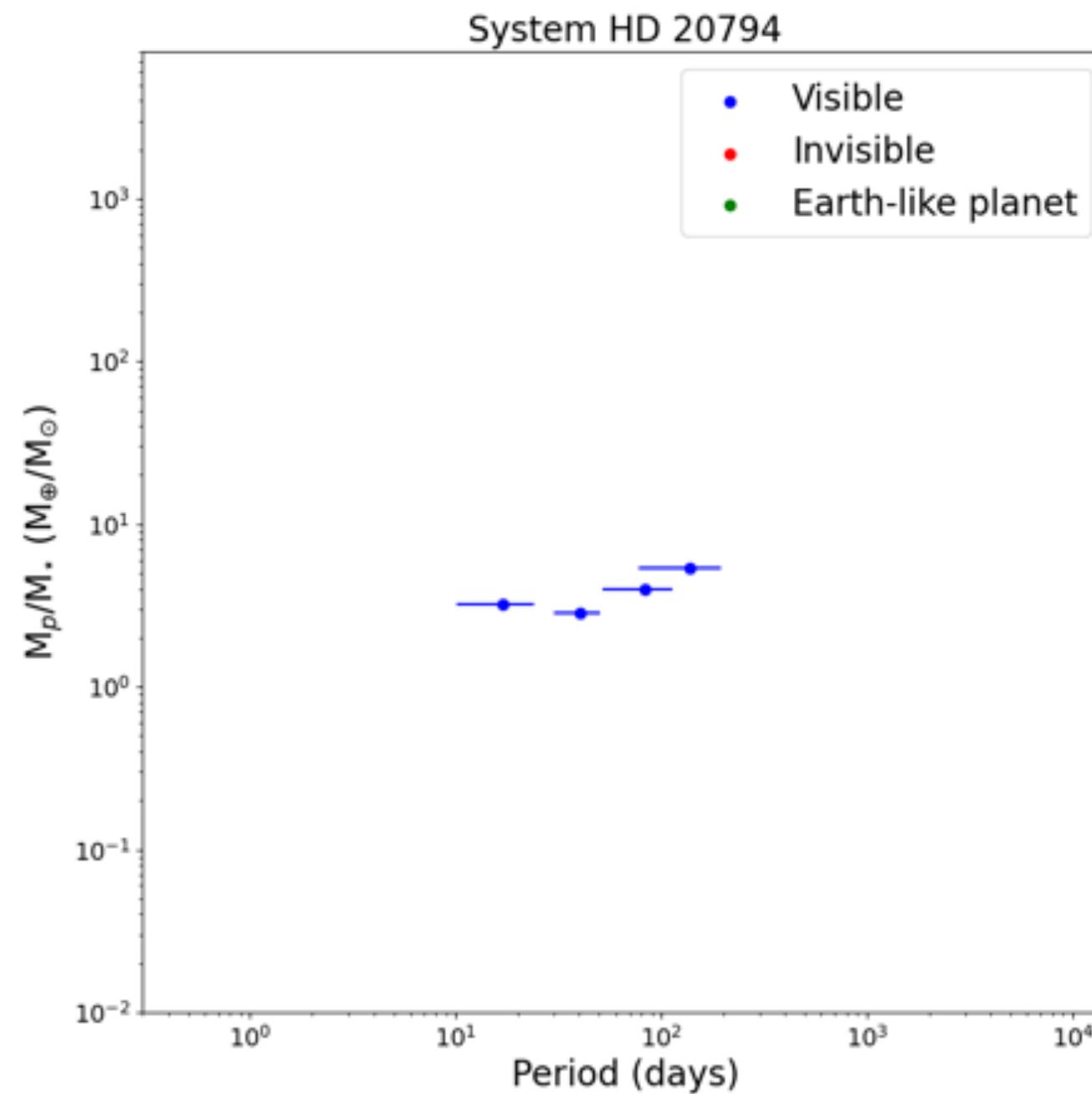
Random forest classifier

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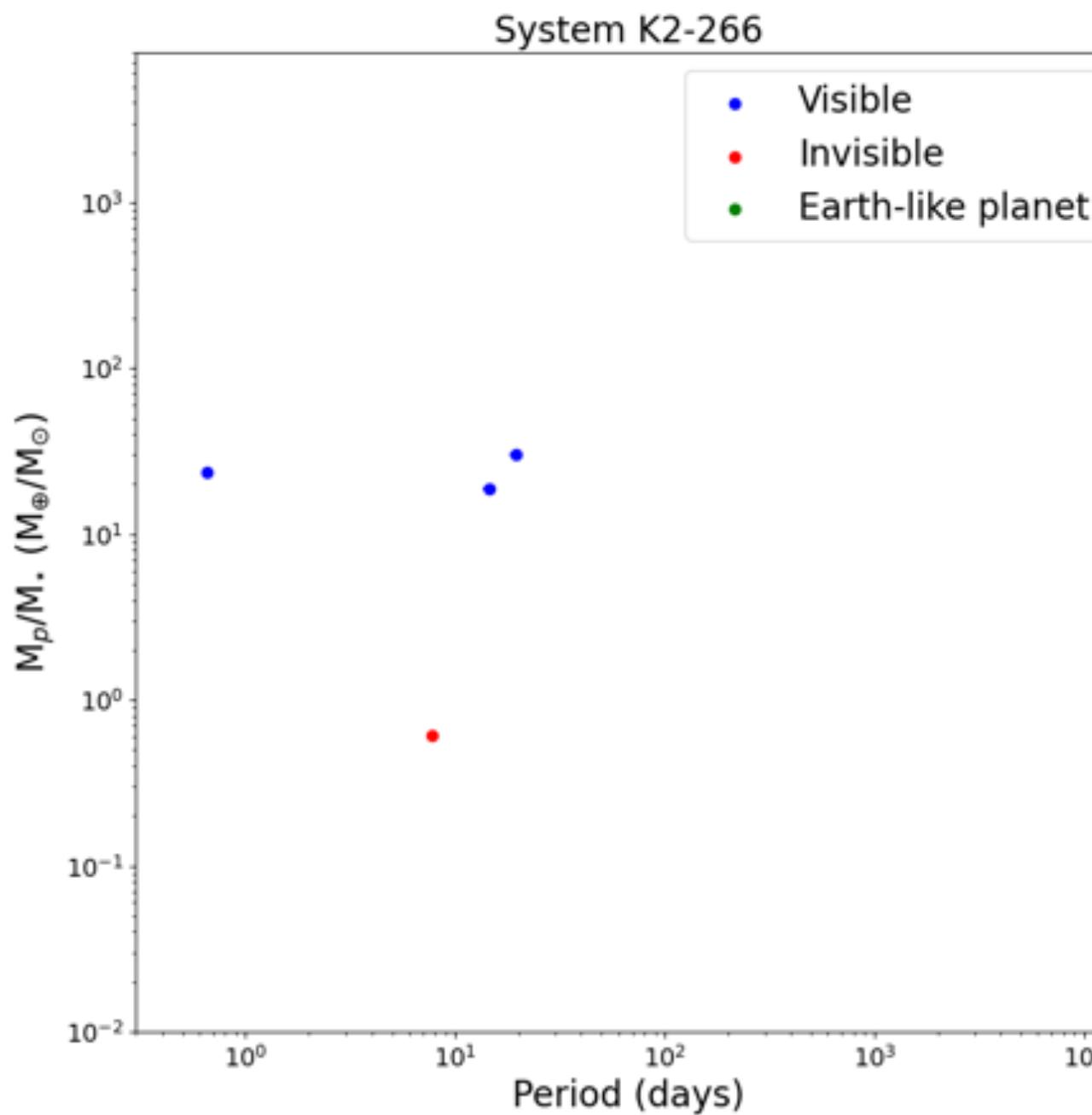
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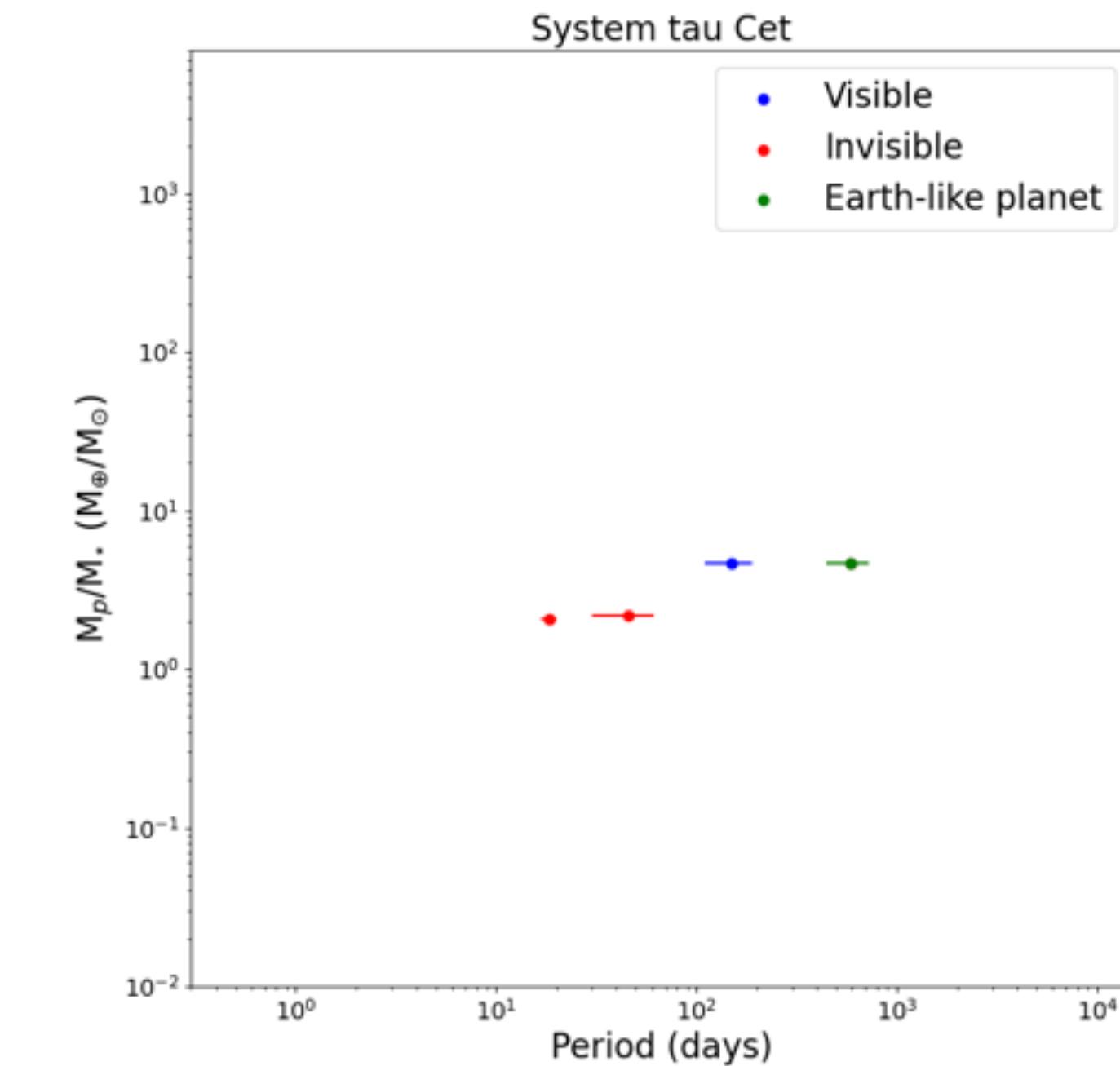
0.94 Msol



0.69 Msol



0.92 Msol



One system has an 'Earth-like' planet (hidden to the classifier), for the two others, observations are ongoing...

Conclusion

1- Planetary system formation is a complicated non-linear process

- > simulations rely on HPC computing
- > analysis of simulation results require specific tools

2- Turning observations into planetary composition is degenerate

- > DNN-based tool (trained on simulations) increases dramatically the search efficiency

3- Models can be used to know where to search Earth-twins

- > random forest classifiers will be used to optimize future observations

Question?