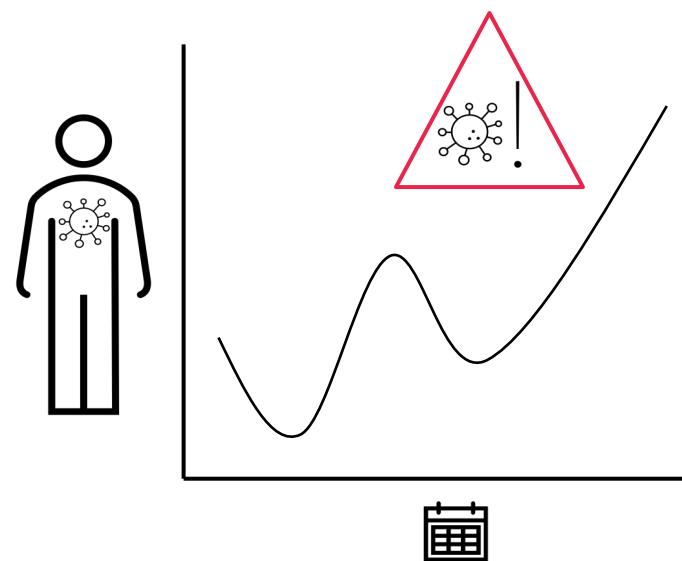


Early Warning Signals in Epidemiological data

INPUT Research meeting

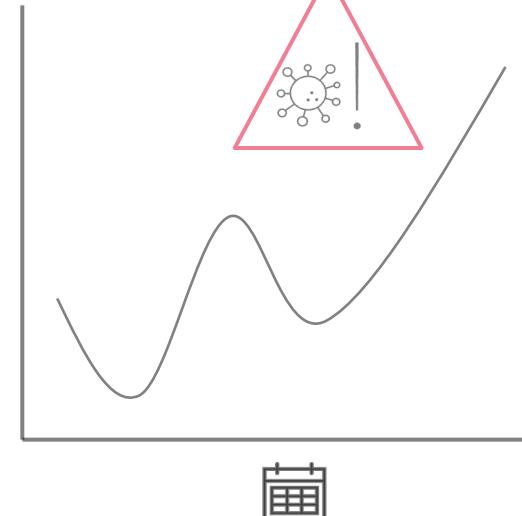
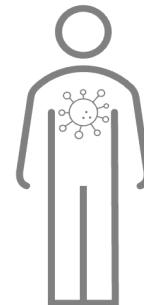
Bern, 16 September 2022



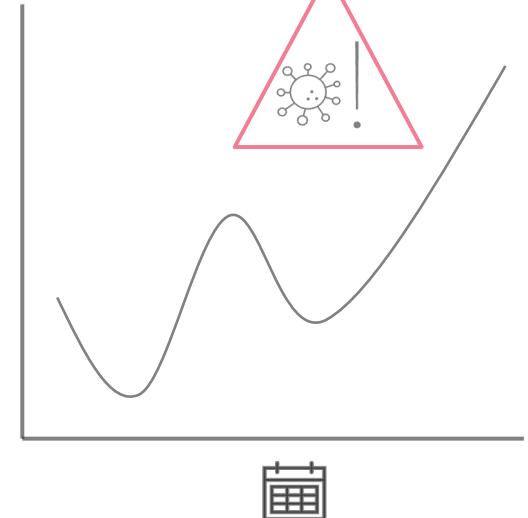
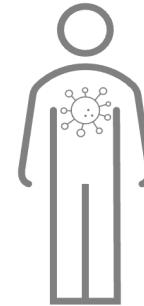
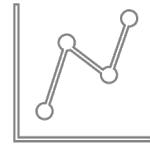
Several types of data



Predict epidemic waves

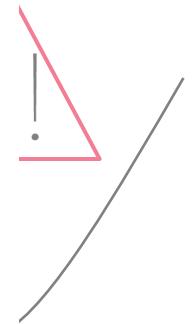


Several types of Early Warning Signals predict epidemic waves



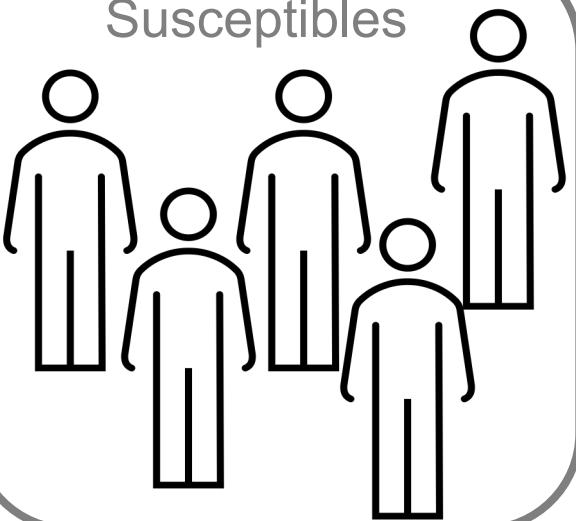
Several types of **Early Warning Signals** predict epidemic waves

- I. Introduction to dynamical systems and bifurcations
- II. The theory behind Early Warning Signals (EWS)
- III. Examples of EWS
- IV. Applications of EWS to COVID-19
- V. Challenges of EWS for COVID-19
- VI. EWS in the MCID project
- VII. Discussion

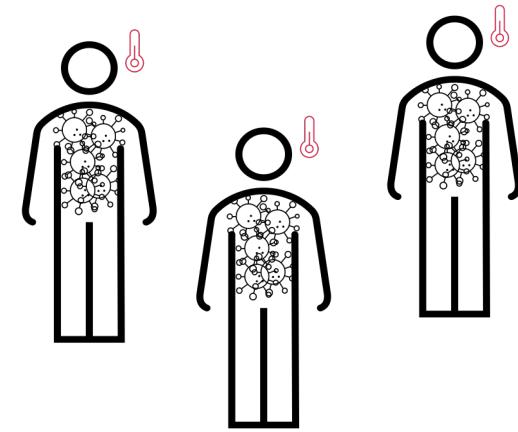


SIR Model

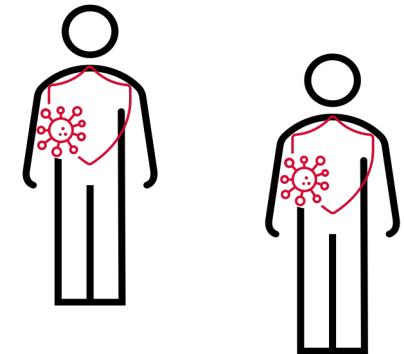
Susceptibles



Infected ind.



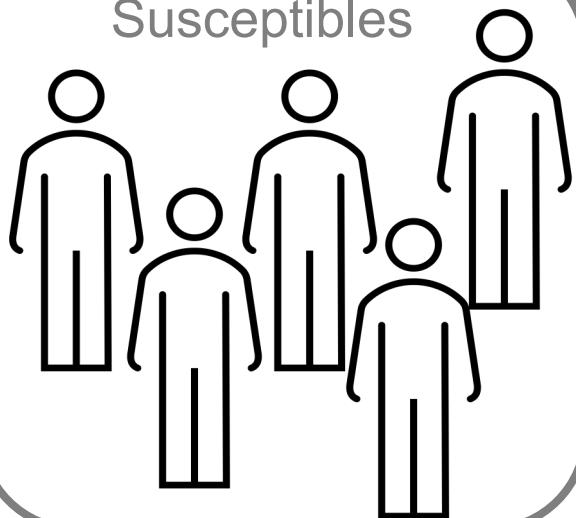
Recovered ind.



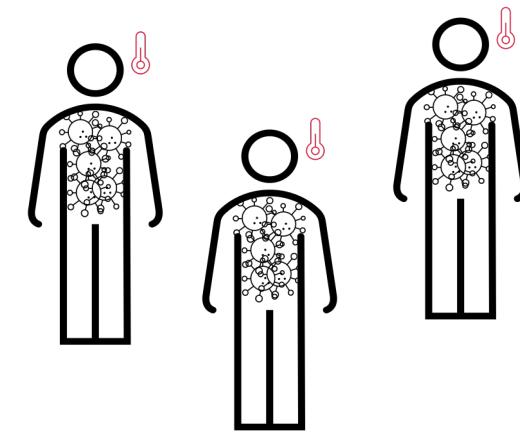
SIR Model

Transmission β

Susceptibles

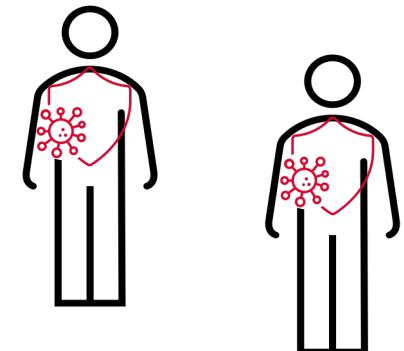


Infected ind.



Recovery γ

Recovered ind.



ω

Loss of immunity

SIR Model

$$\frac{d}{dt} \begin{array}{c} \text{S} \\ \text{I} \end{array} = \omega * \begin{array}{c} \text{S} \\ \text{I} \end{array} - \beta * \begin{array}{c} \text{S} \\ \text{I} \end{array} * \begin{array}{c} \text{S} \\ \text{I} \end{array}$$

$$\frac{d}{dt} \begin{array}{c} \text{I} \\ \text{R} \end{array} = \beta * \begin{array}{c} \text{S} \\ \text{I} \end{array} * \begin{array}{c} \text{S} \\ \text{I} \end{array} - \gamma * \begin{array}{c} \text{I} \\ \text{R} \end{array}$$

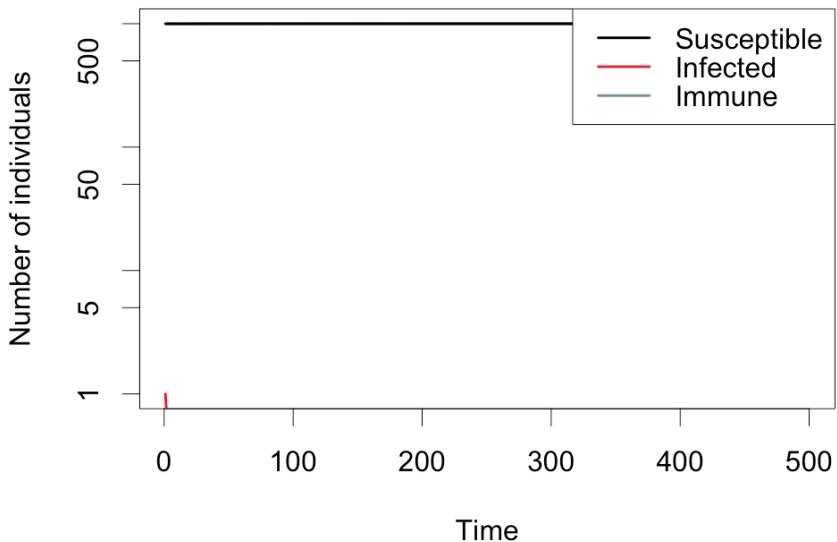
$$\frac{d}{dt} \begin{array}{c} \text{S} \\ \text{R} \end{array} = \gamma * \begin{array}{c} \text{I} \\ \text{R} \end{array} - \omega * \begin{array}{c} \text{S} \\ \text{R} \end{array}$$

SIR dynamics

$$\beta = 0.0002$$

$$\gamma = 0.45$$

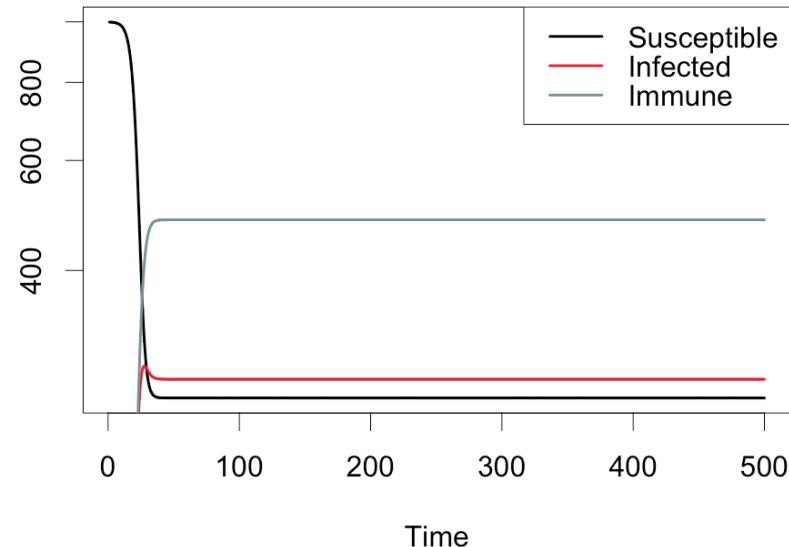
$$N = 1000$$



$$\beta = 0.001$$

$$\gamma = 0.45$$

$$N = 1000$$

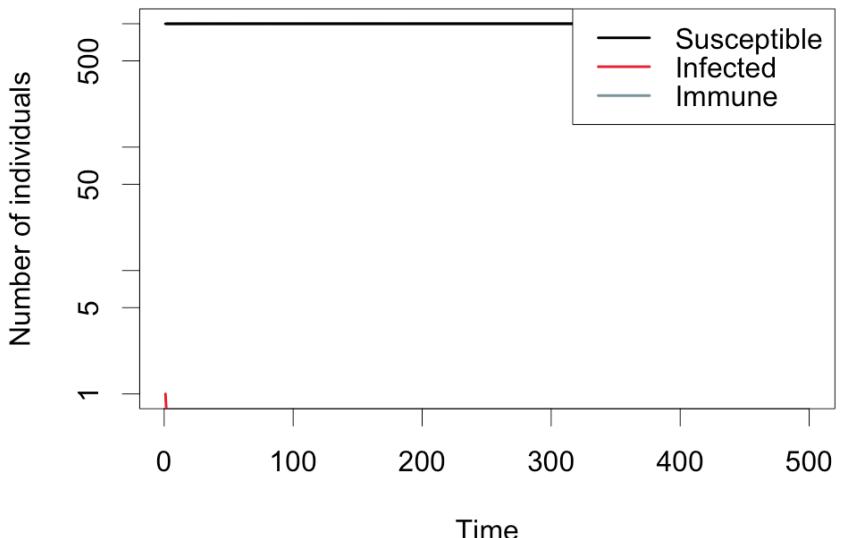


SIR dynamics

$$\beta = 0.0002$$

$$\gamma = 0.45$$

$$N = 1000$$

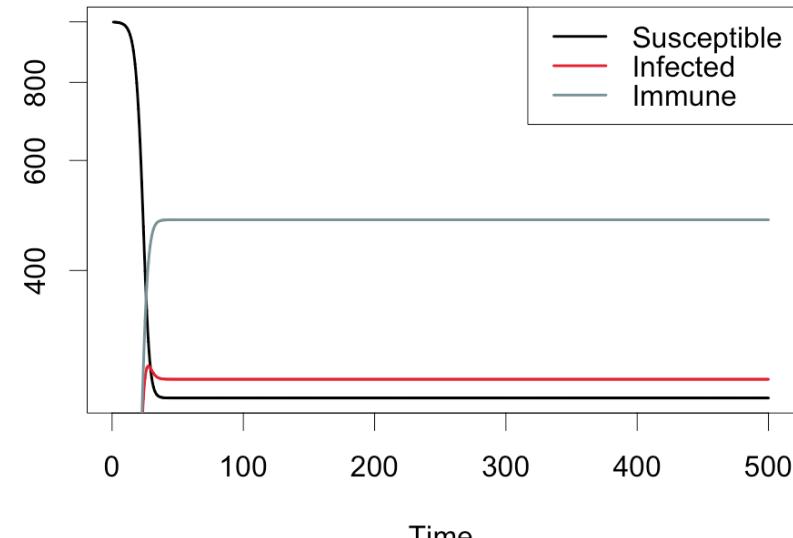


Disease free equilibrium

$$\beta = 0.001$$

$$\gamma = 0.45$$

$$N = 1000$$



Endemic equilibrium

Equilibria – where are they?

$$\frac{d}{d \text{calendar}} \left(\text{infected person} \right) = \beta * \text{uninfected person} * \text{infected person} - \gamma * \text{infected person} = 0$$

Equilibria – where are they?

$$\frac{d}{dt} \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} = \beta * \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} * \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} - \gamma * \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} = 0$$

$$\beta * \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} * \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} = \gamma * \begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array}$$

$$\begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} = 0$$

or

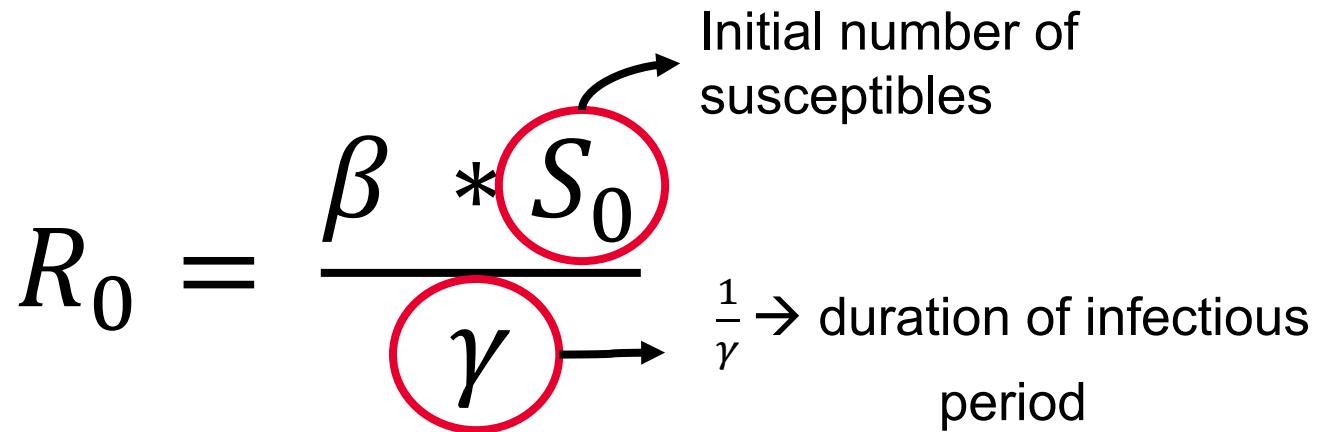
$$\begin{array}{|c|}\hline \text{S} \\ \text{I} \\ \text{R} \\ \hline \end{array} = \frac{\gamma}{\beta}$$

Basic reproduction number

$$R_0 = \frac{\beta * S_0}{\gamma}$$

Initial number of susceptibles

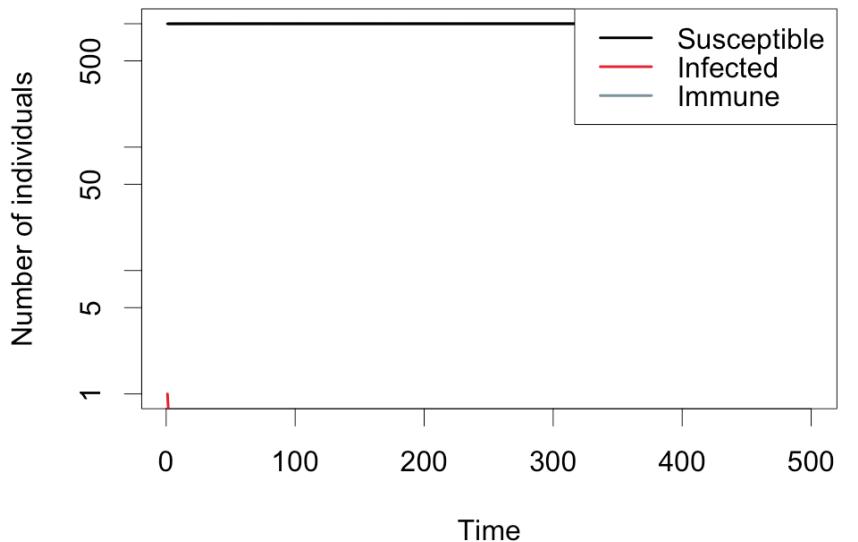
$\frac{1}{\gamma} \rightarrow$ duration of infectious period



SIR dynamics

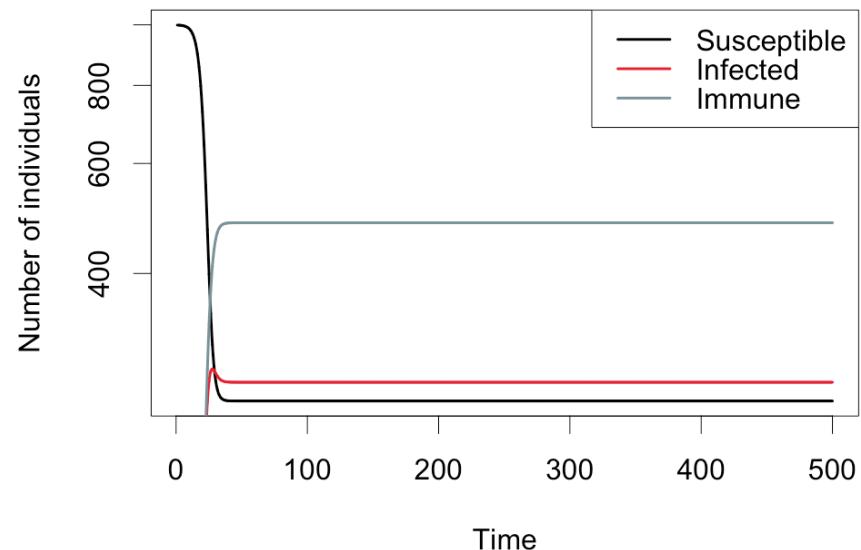
$$R_0 < 1$$

$$R_0 = 0.44$$



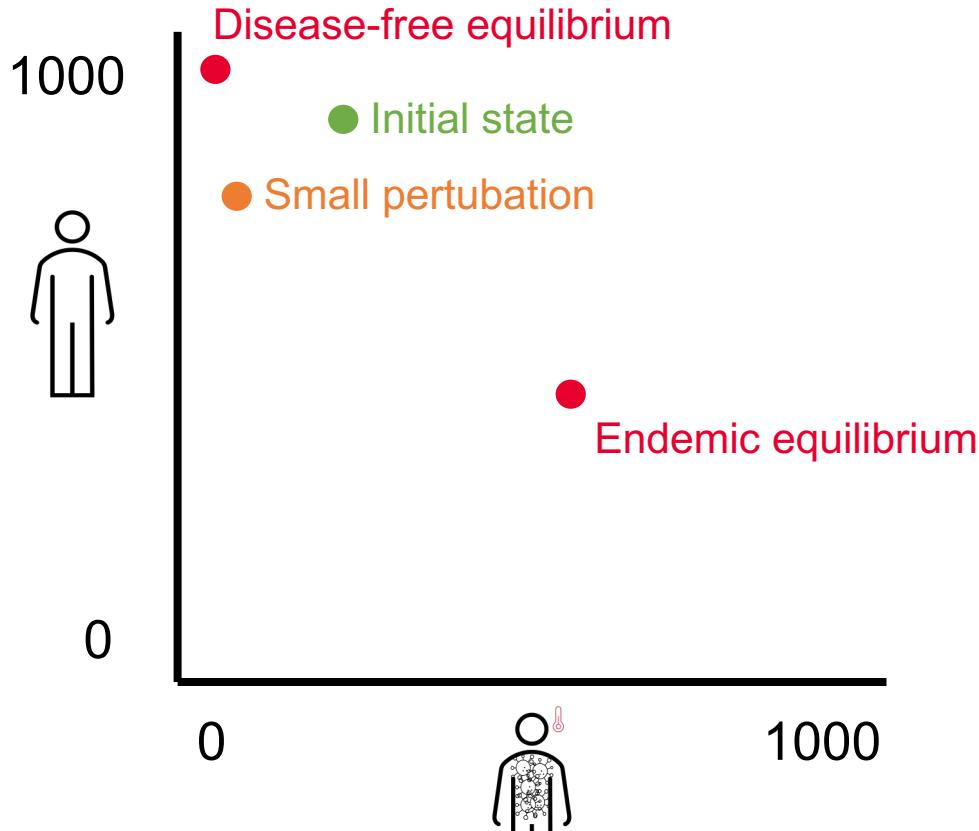
$$R_0 > 1$$

$$R_0 = 2.2$$



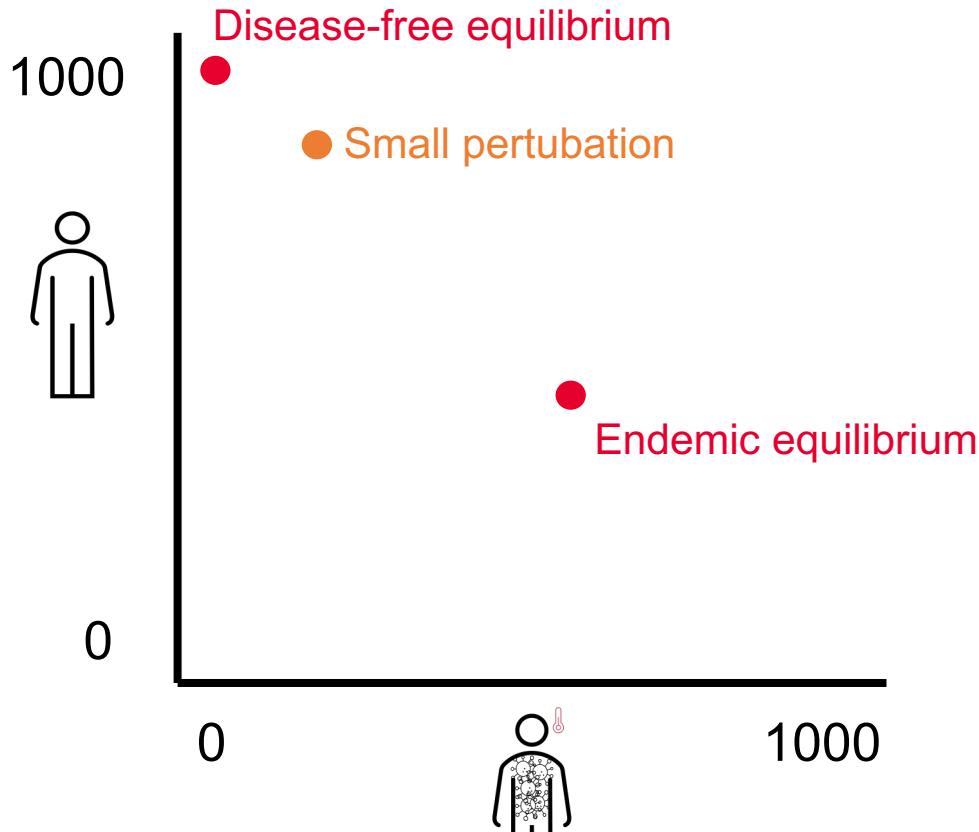
Stability of equilibria

$$R_0 = 0.44$$

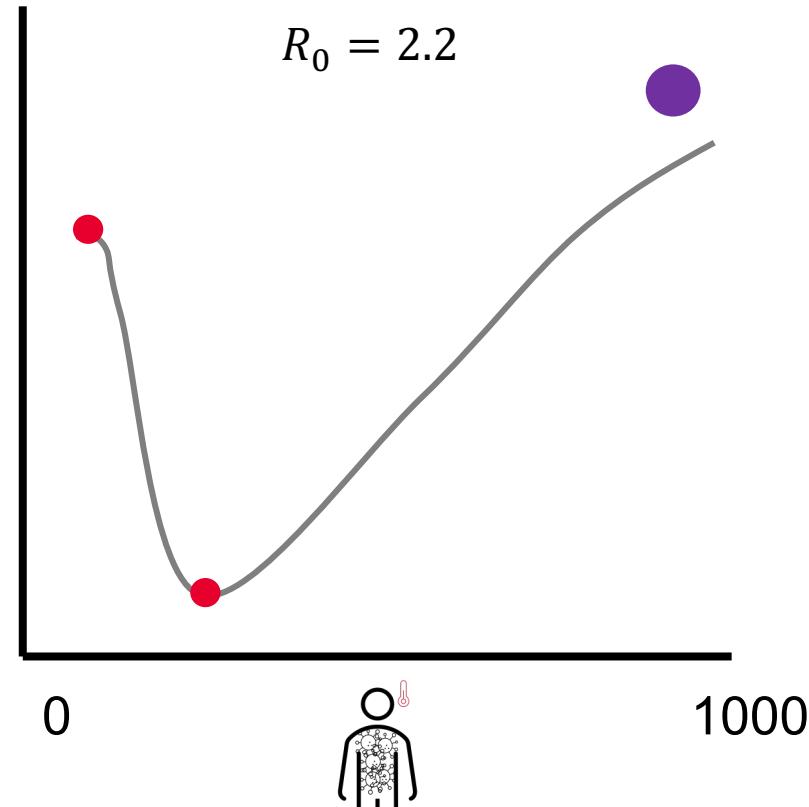
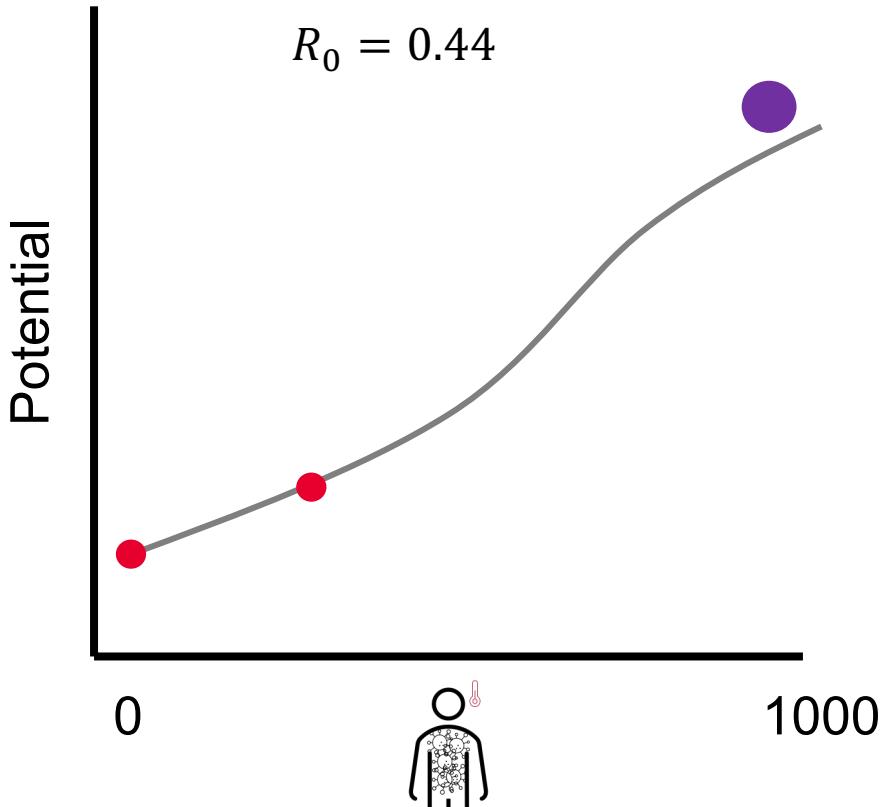


Stability of equilibria

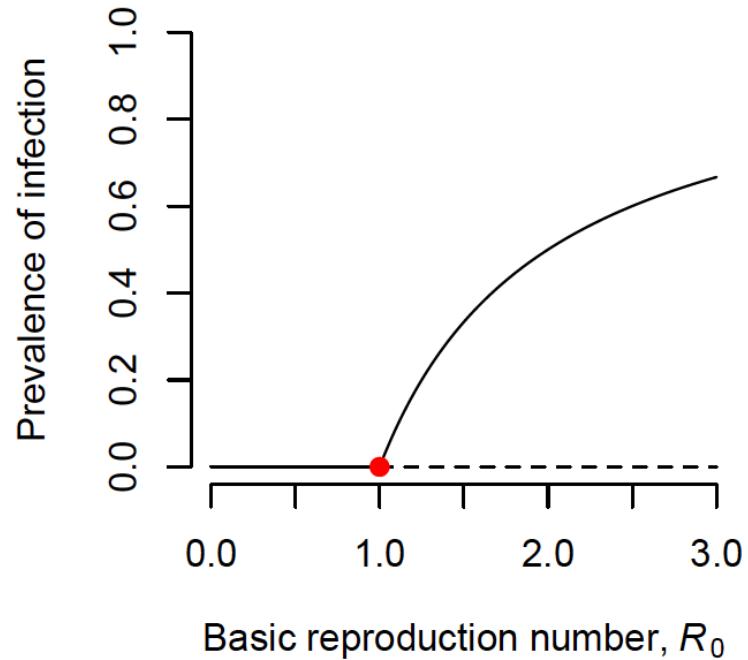
$$R_0 = 2.2$$



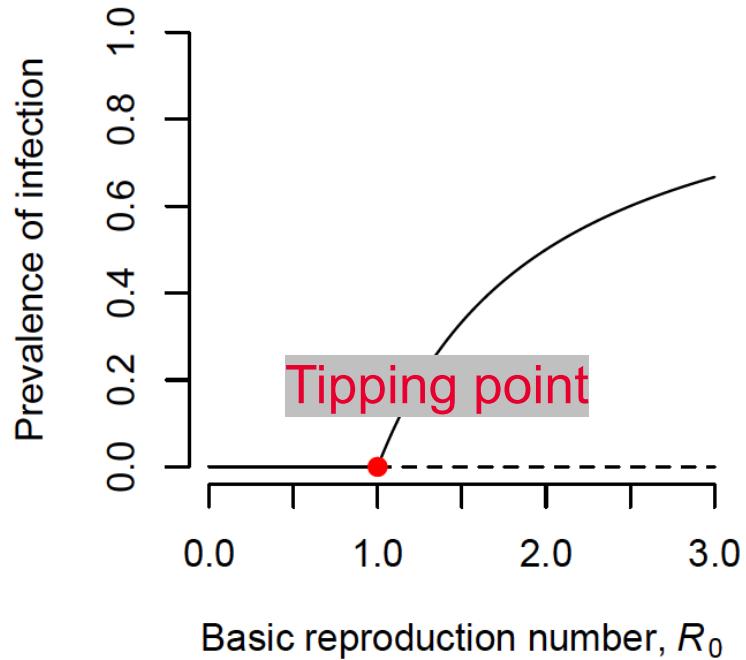
Stability of equilibria – Potential of the system



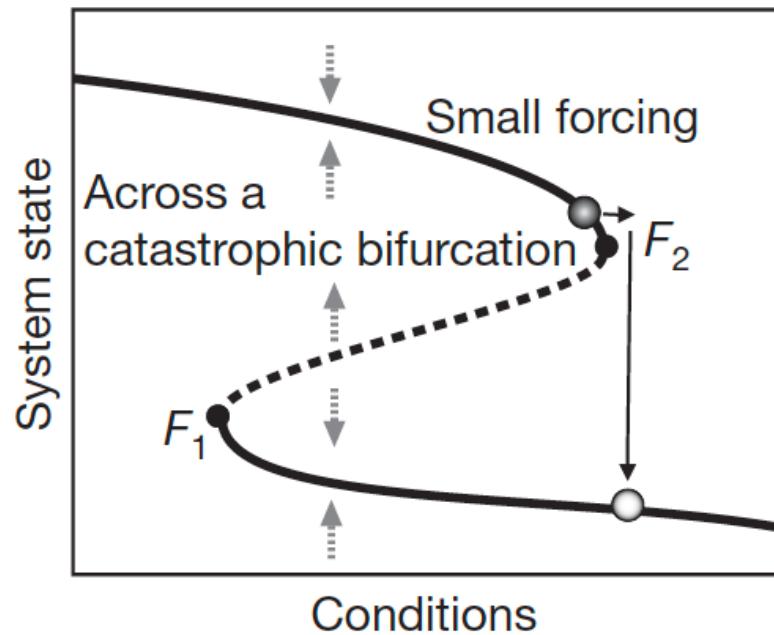
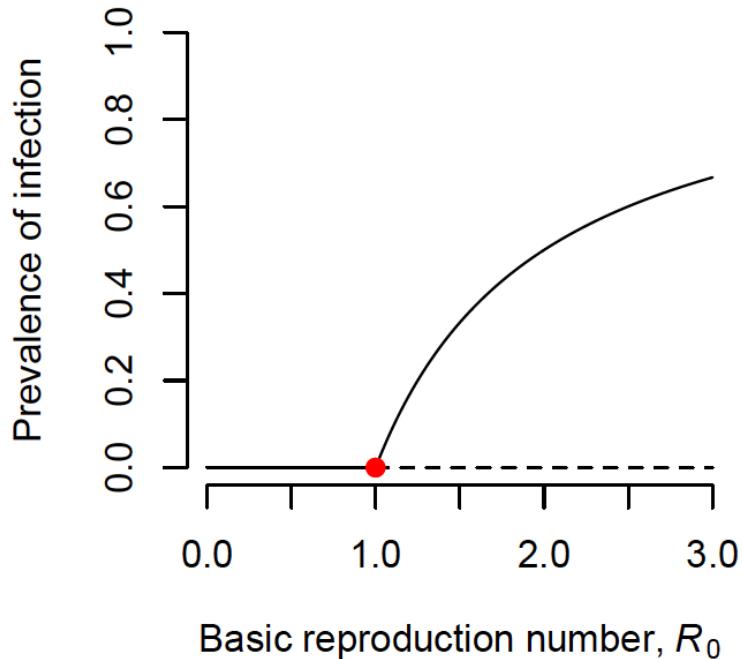
Bifurcation



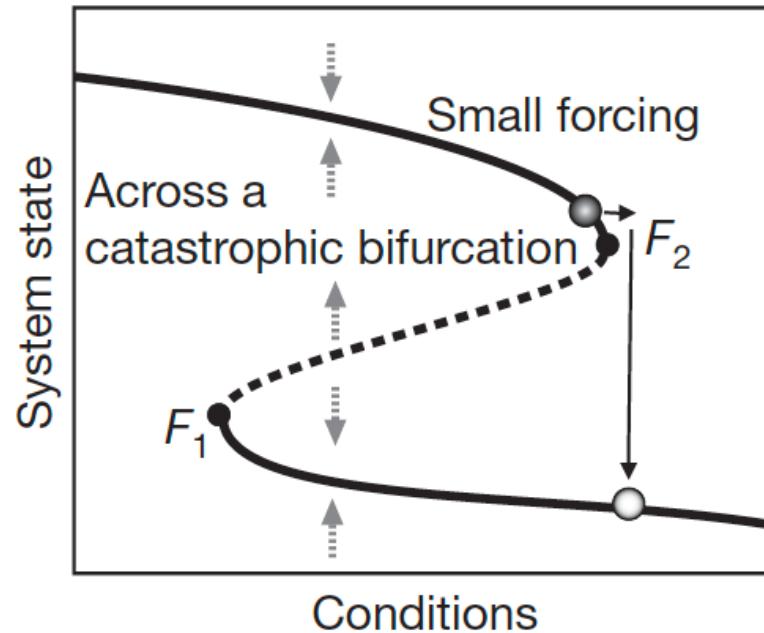
Bifurcation



Critical transitions

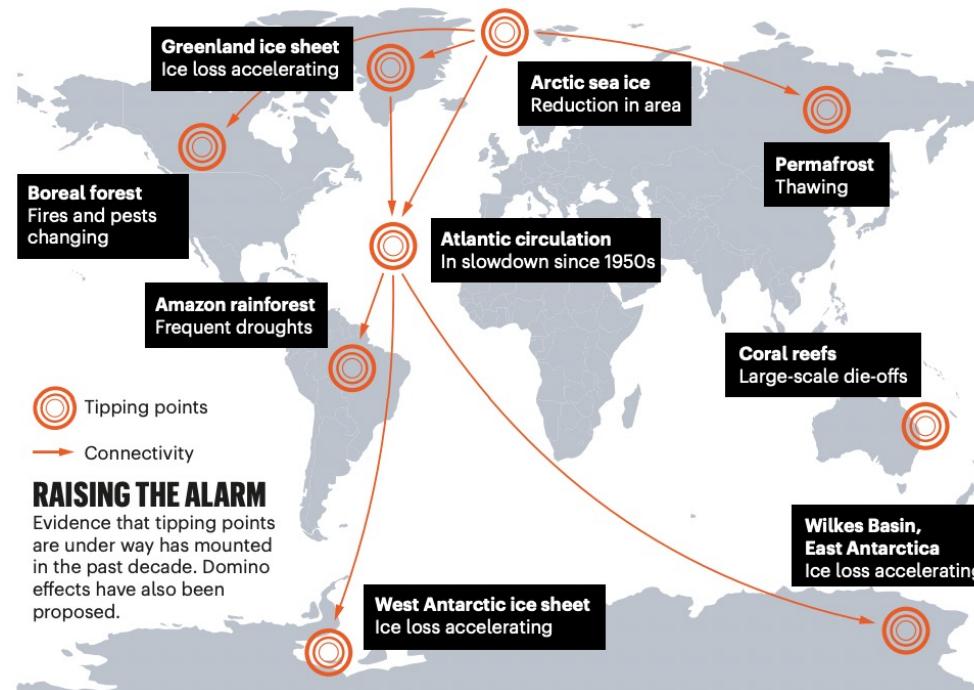


Critical transition for coral bleaching



Scheffer et al, Nature, 2009

Many examples from climate science



Predicting critical transitions

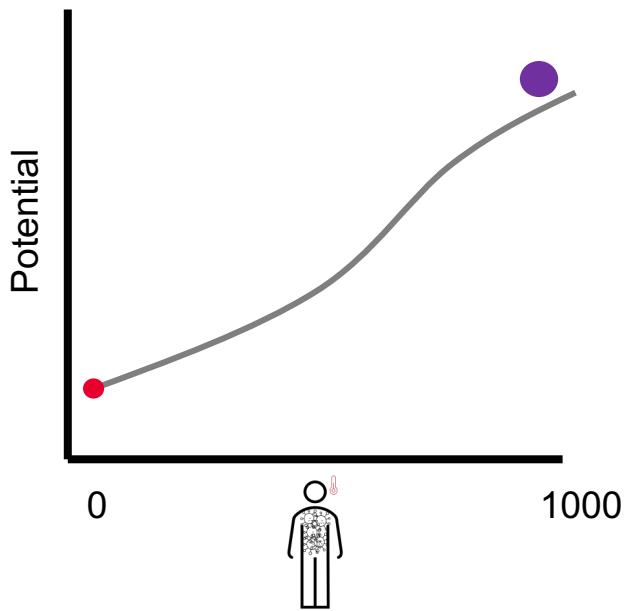
Early Warning Signs predict **critical transitions** in a wide range of dynamical models

Generic properties near critical point:

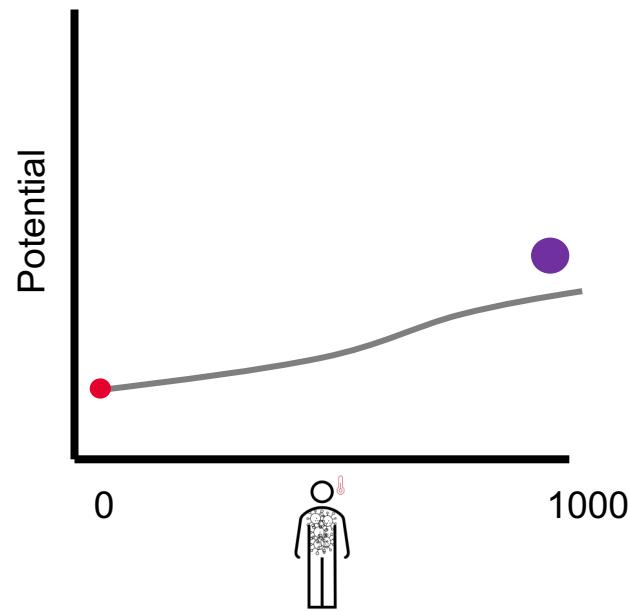
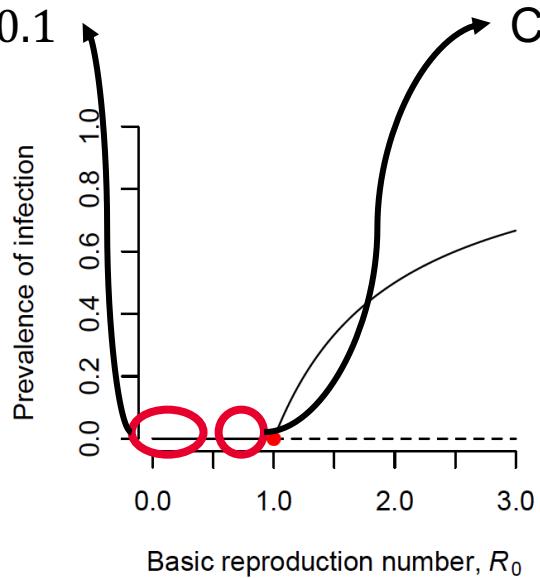
- More time to recover from a small perturbation close to a transition:
critical slowing down
- **Asymmetry of fluctuations** increases
- Flickering between two steady states

Critical slowing down

Far from bifurcation: $R_0 = 0.1$



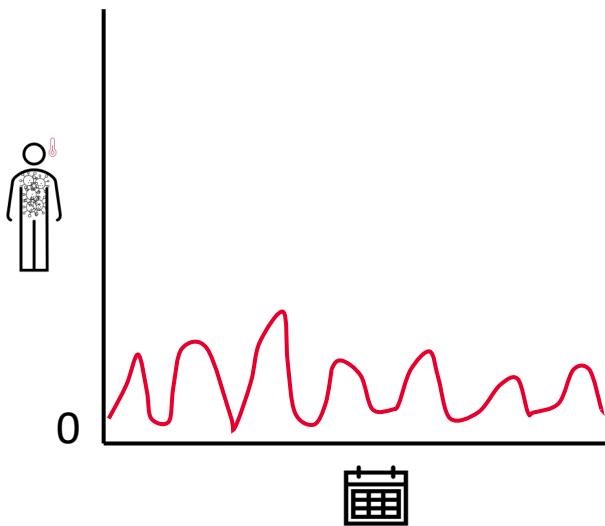
Close to bifurcation: $R_0 = 0.95$



Critical slowing down – recovery rate

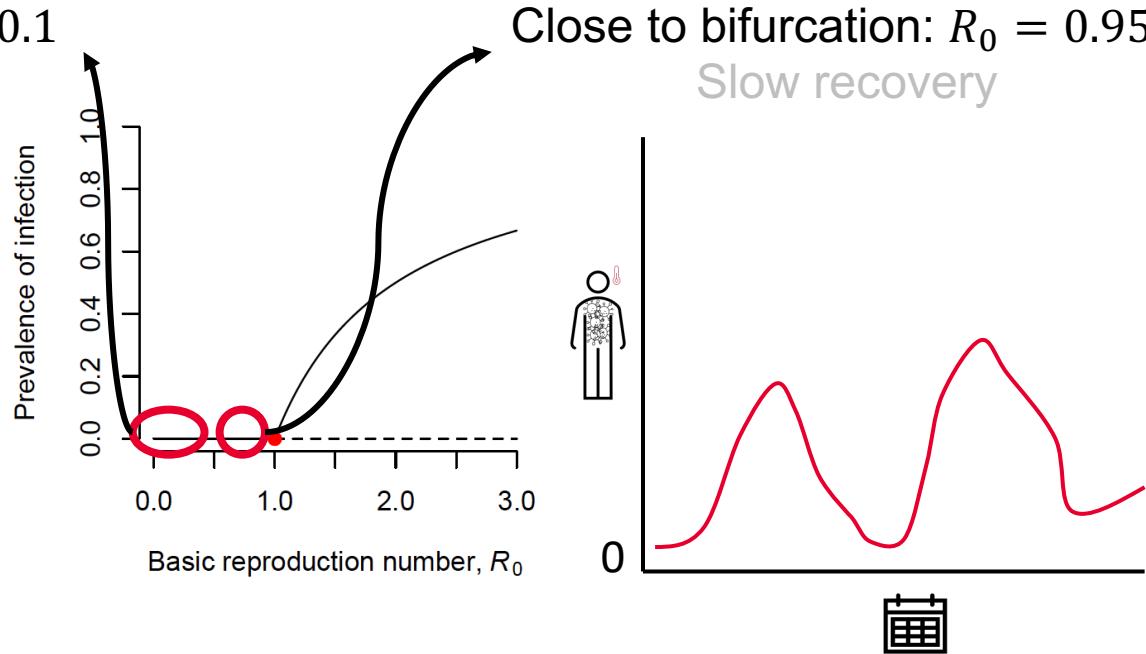
Far from bifurcation: $R_0 = 0.1$

Fast recovery



Close to bifurcation: $R_0 = 0.95$

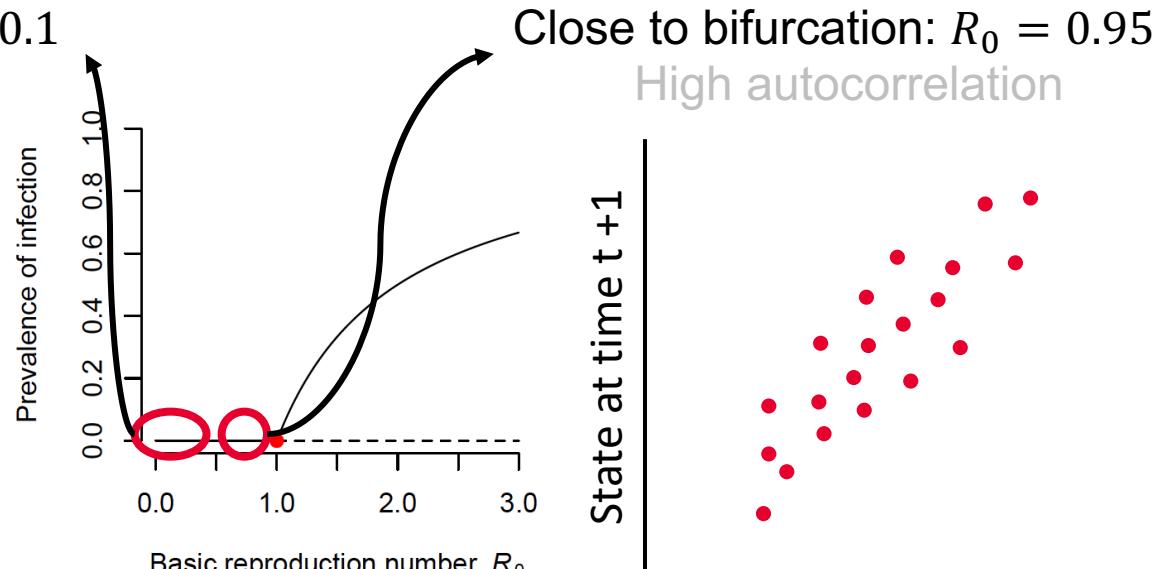
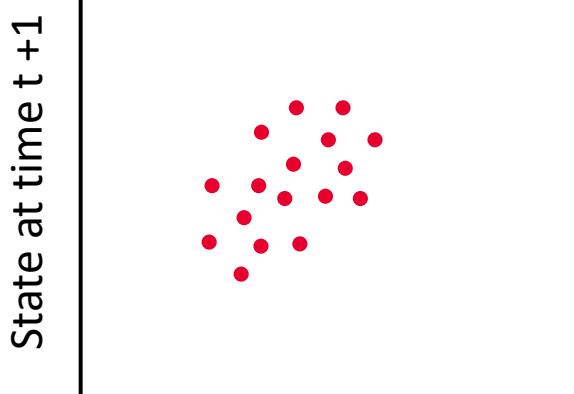
Slow recovery



Critical slowing down – Autocorrelation

Far from bifurcation: $R_0 = 0.1$

Low autocorrelation



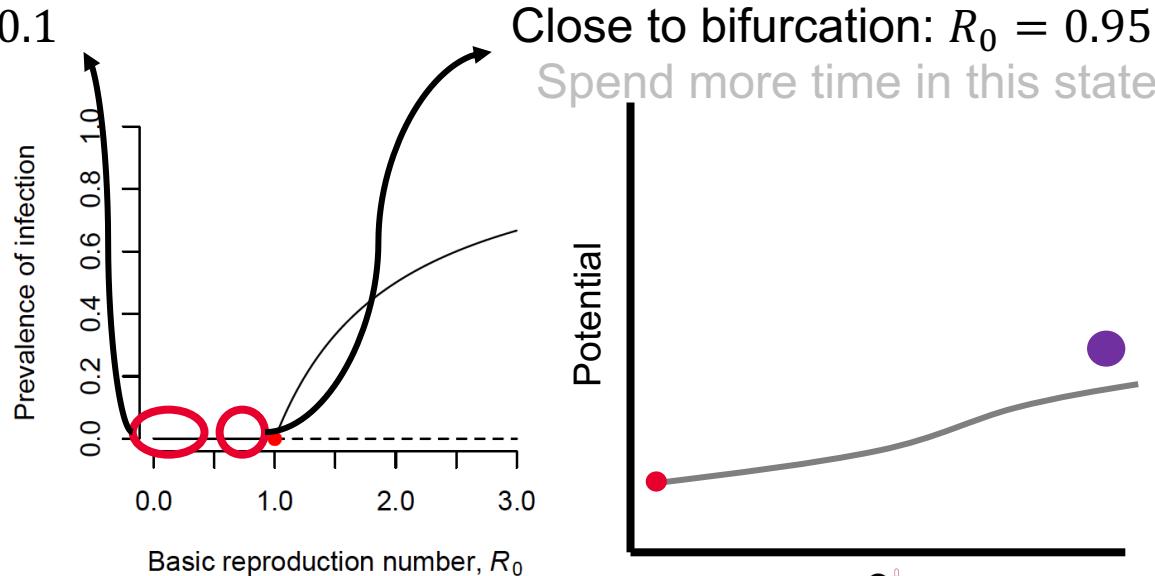
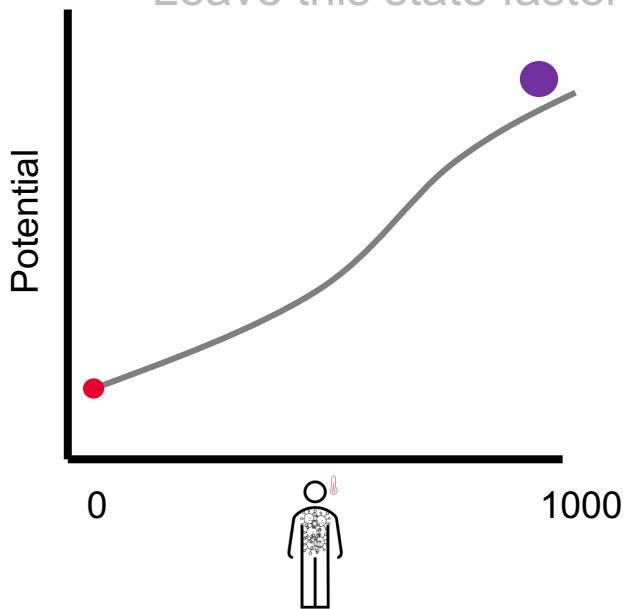
State at time t

State at time t

Asymmetry of fluctuations – Skewness & kurtosis

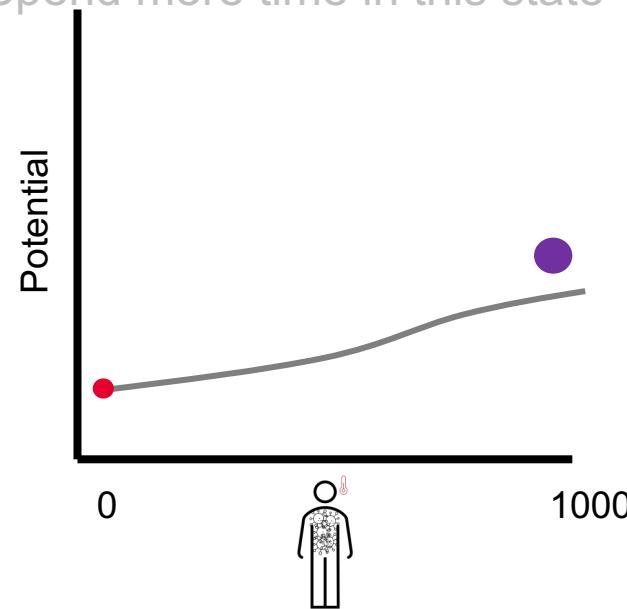
Far from bifurcation: $R_0 = 0.1$

Leave this state faster



Close to bifurcation: $R_0 = 0.95$

Spend more time in this state



Different types of EWS

Due to critical slowing down increase in:

- recovery time
- Variance
- Coefficient of variation
- Autocorrelation

Due to asymmetry of fluctuations increase in:

- Skewness
- Kurtosis

Due to flickering:

- bi-modality

Different types of EWS

Due to critical slowing down increase in:

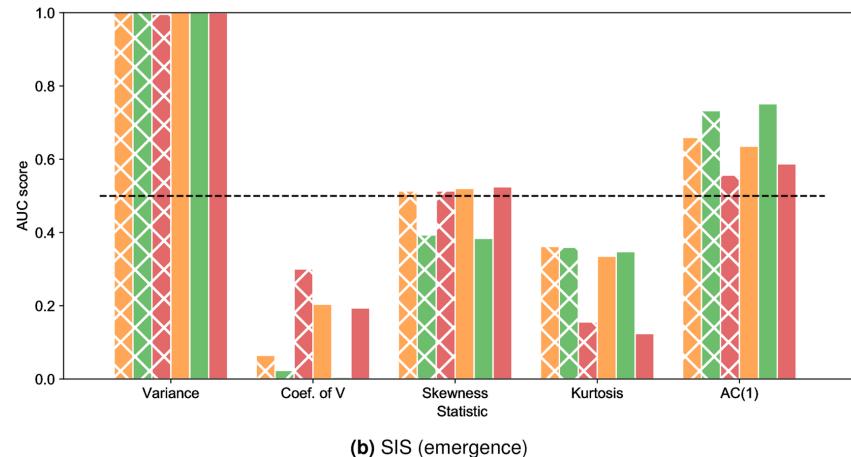
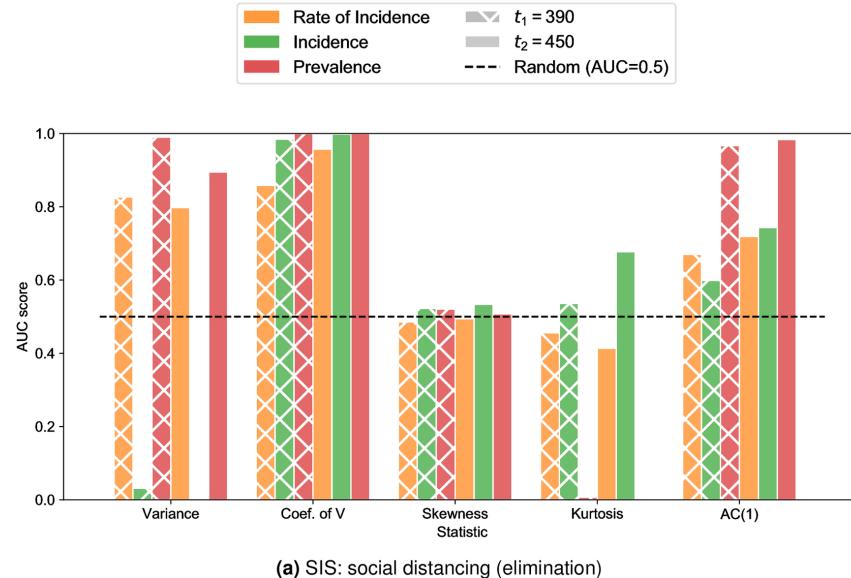
- recovery time
- Variance
- Coefficient of variation
- Autocorrelation

Due to asymmetry of fluctuations increase in:

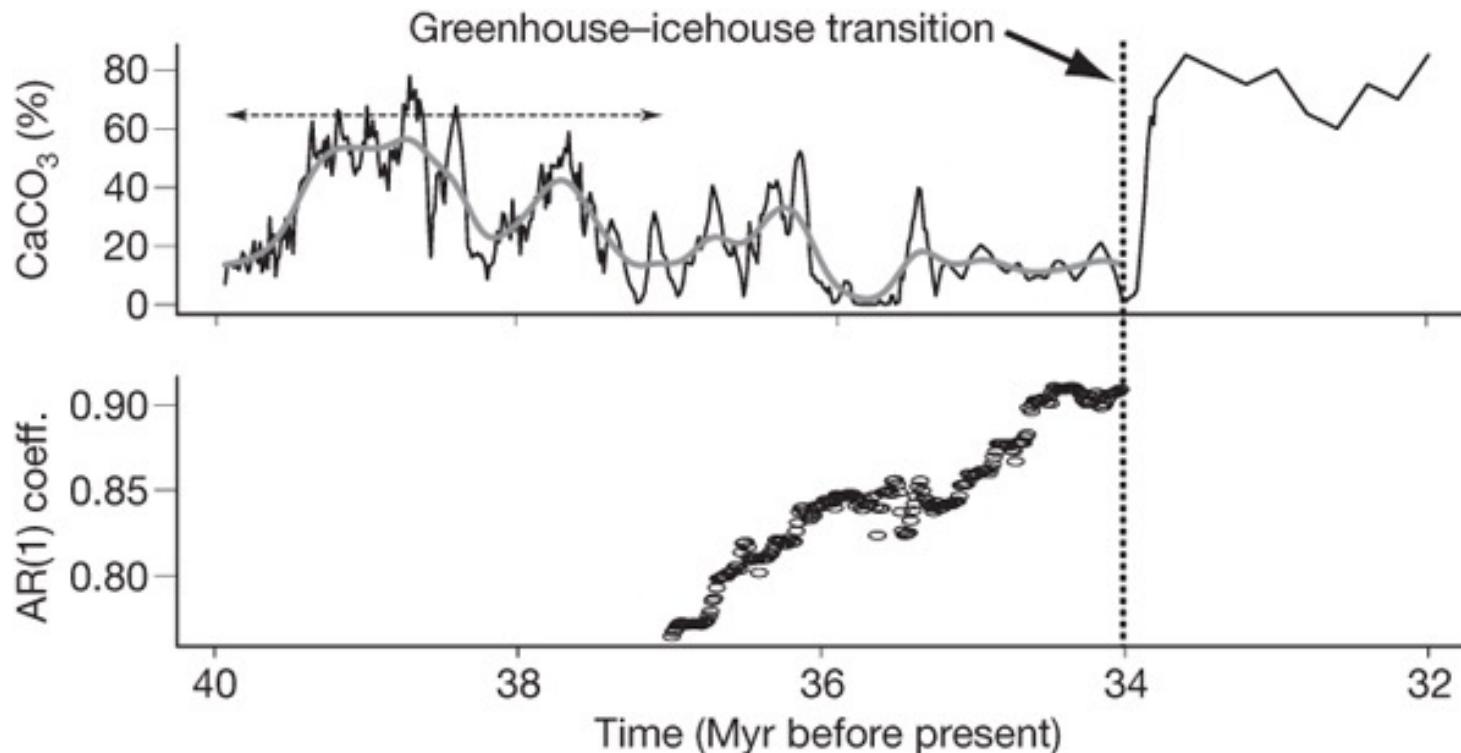
- Skewness
- Kurtosis

Due to flickering:

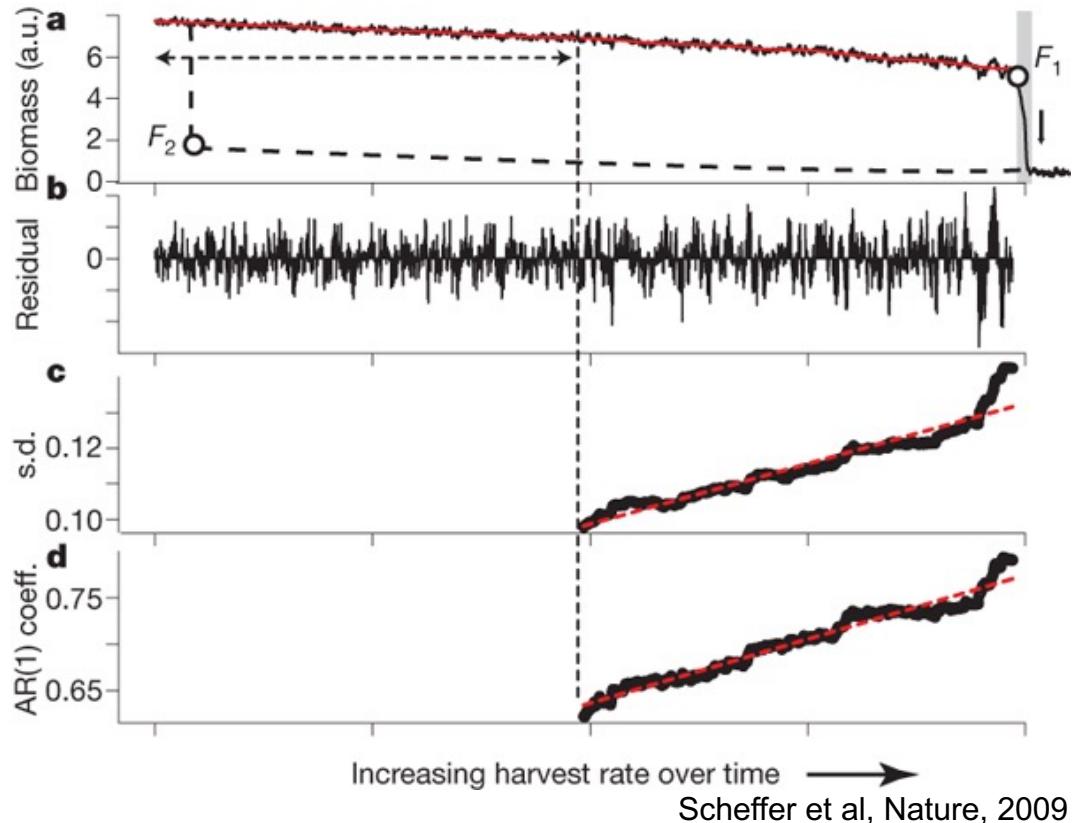
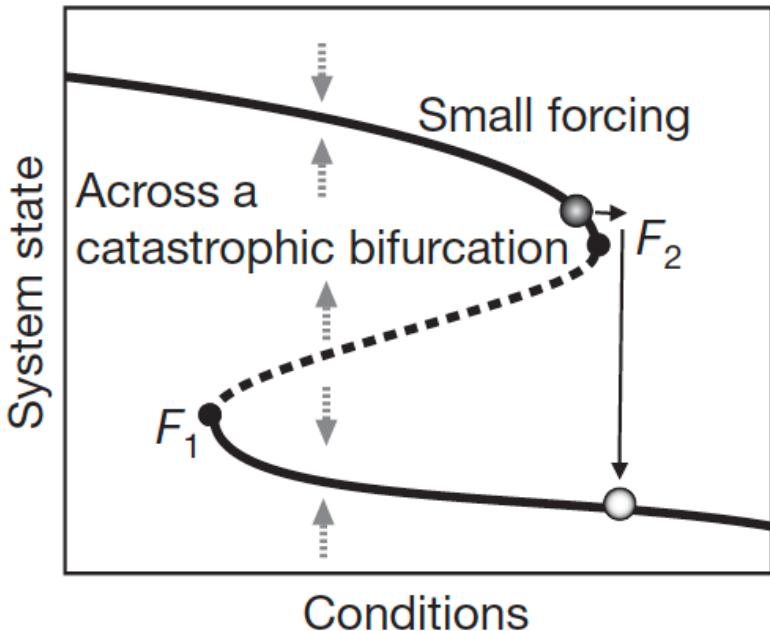
- bi-modality



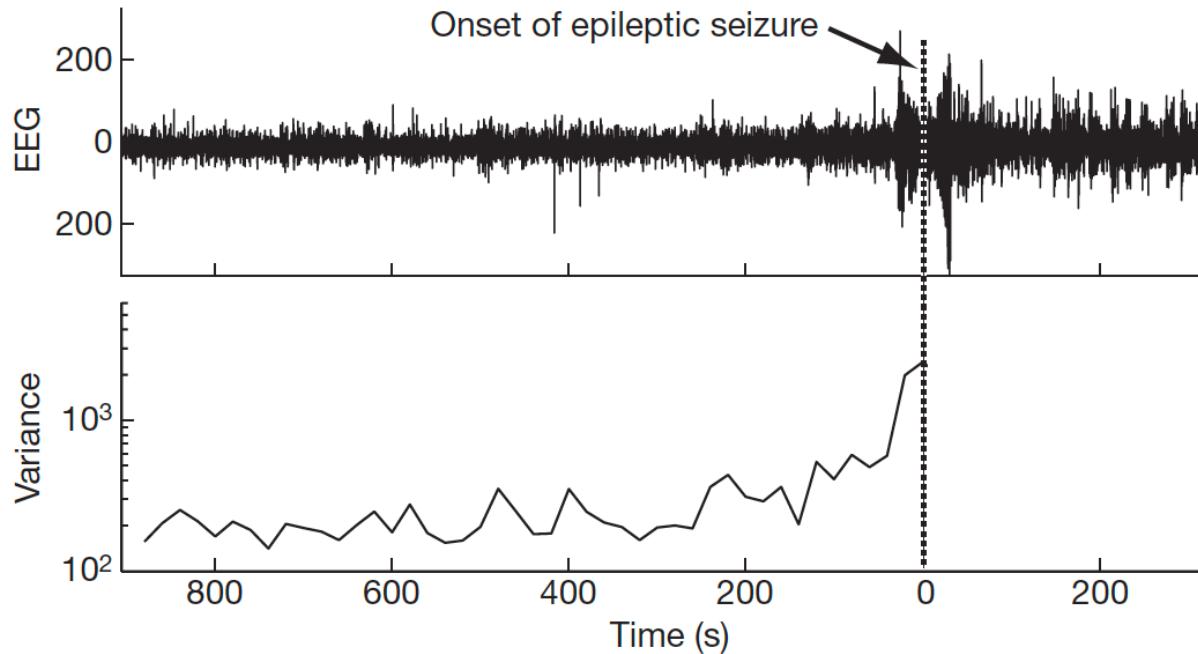
Greenhouse-icehous transition



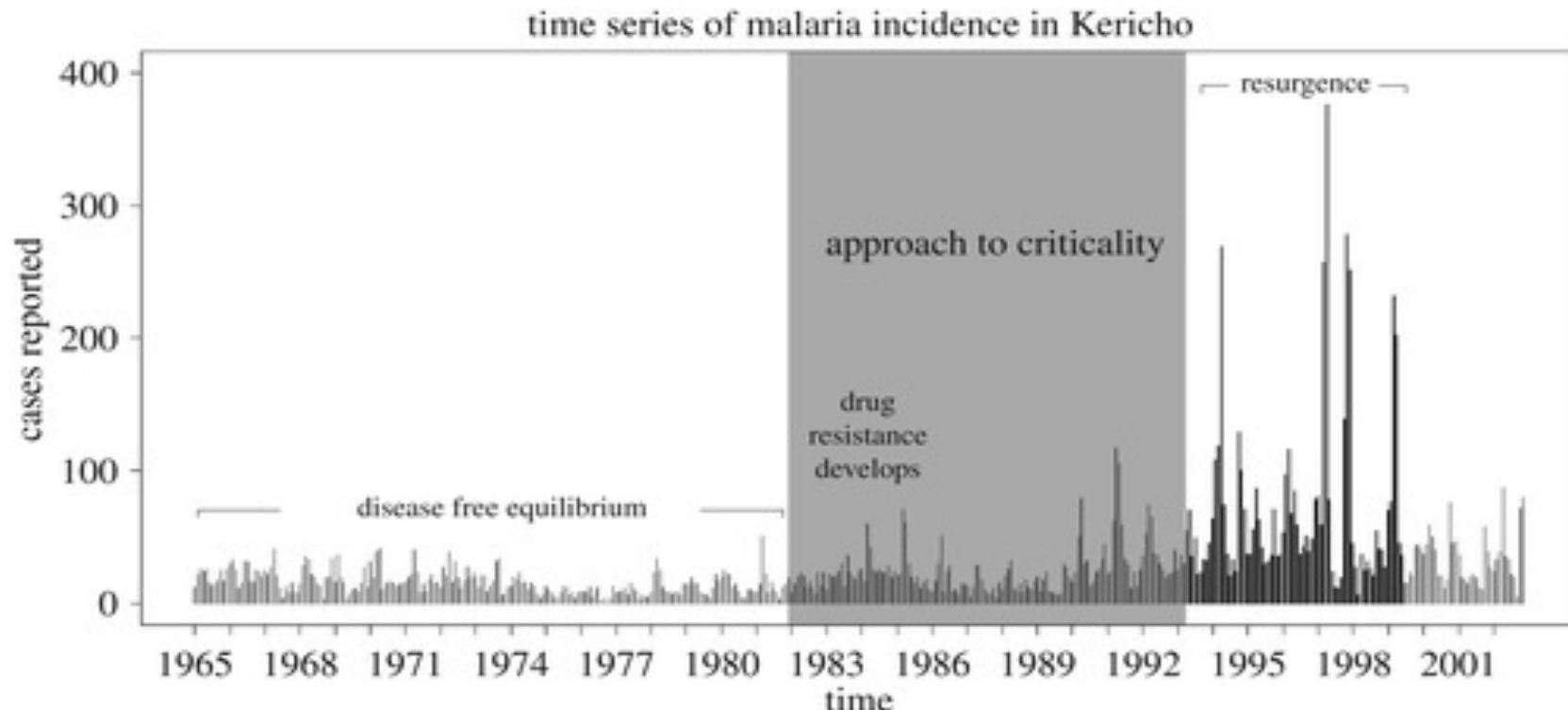
Critical transition in harvast

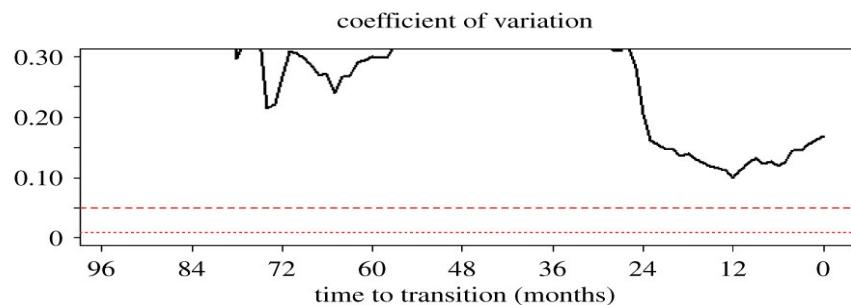
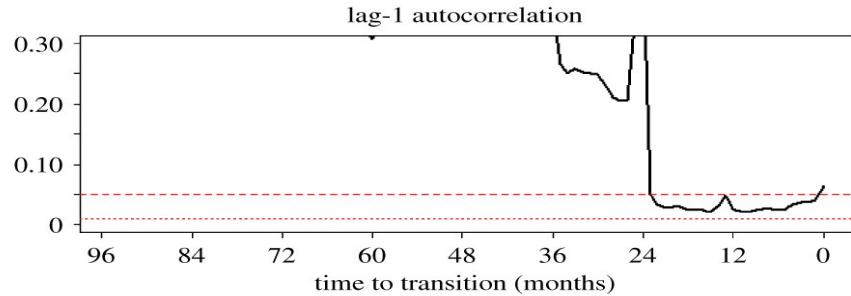
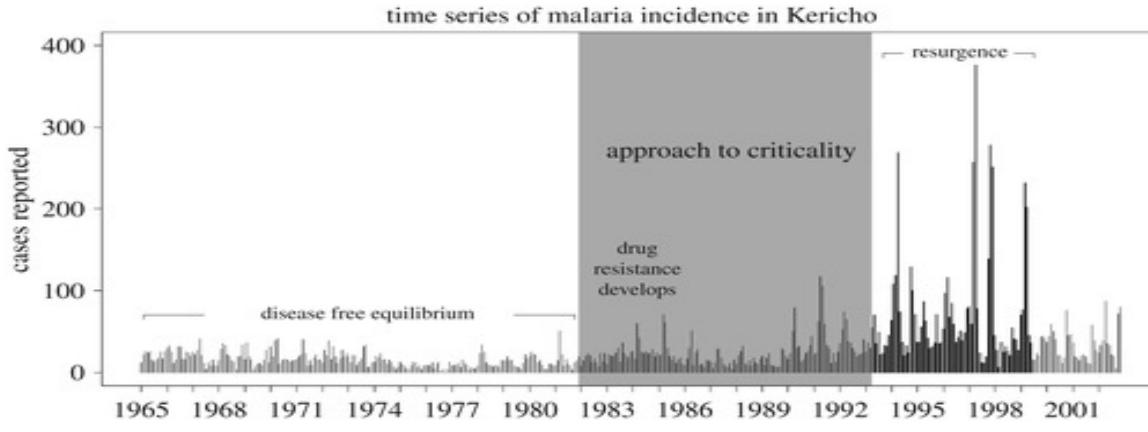


Epileptic seizure



Resurgence of Malaria

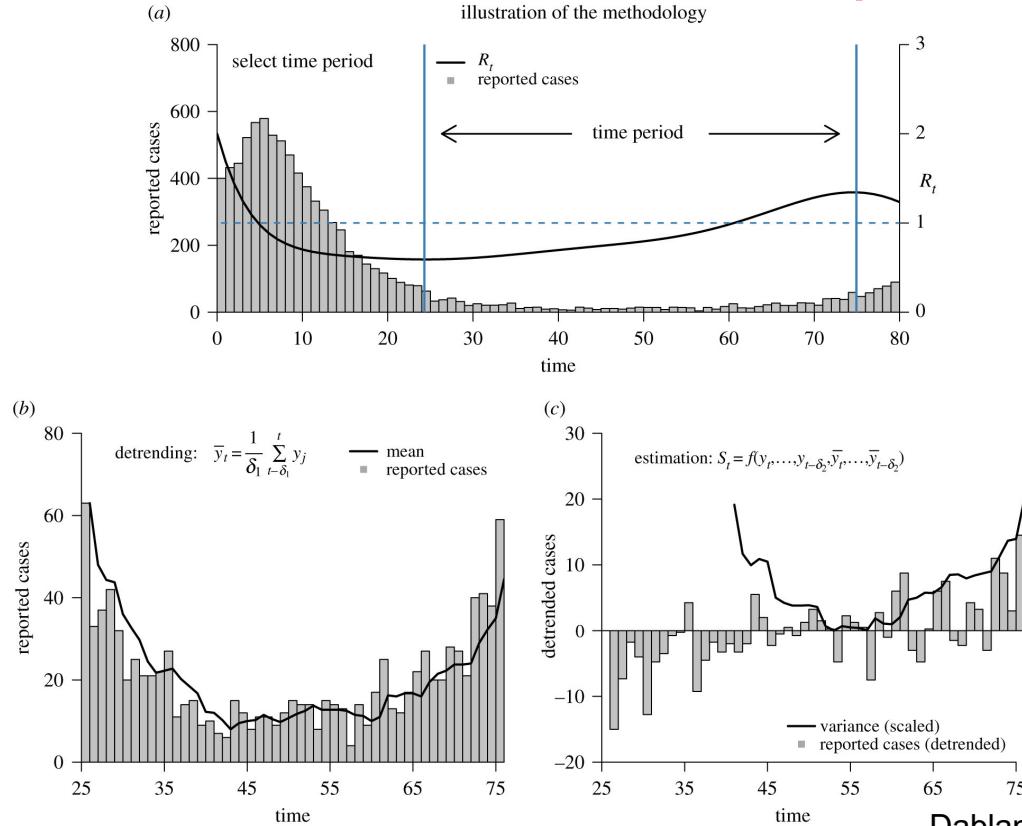


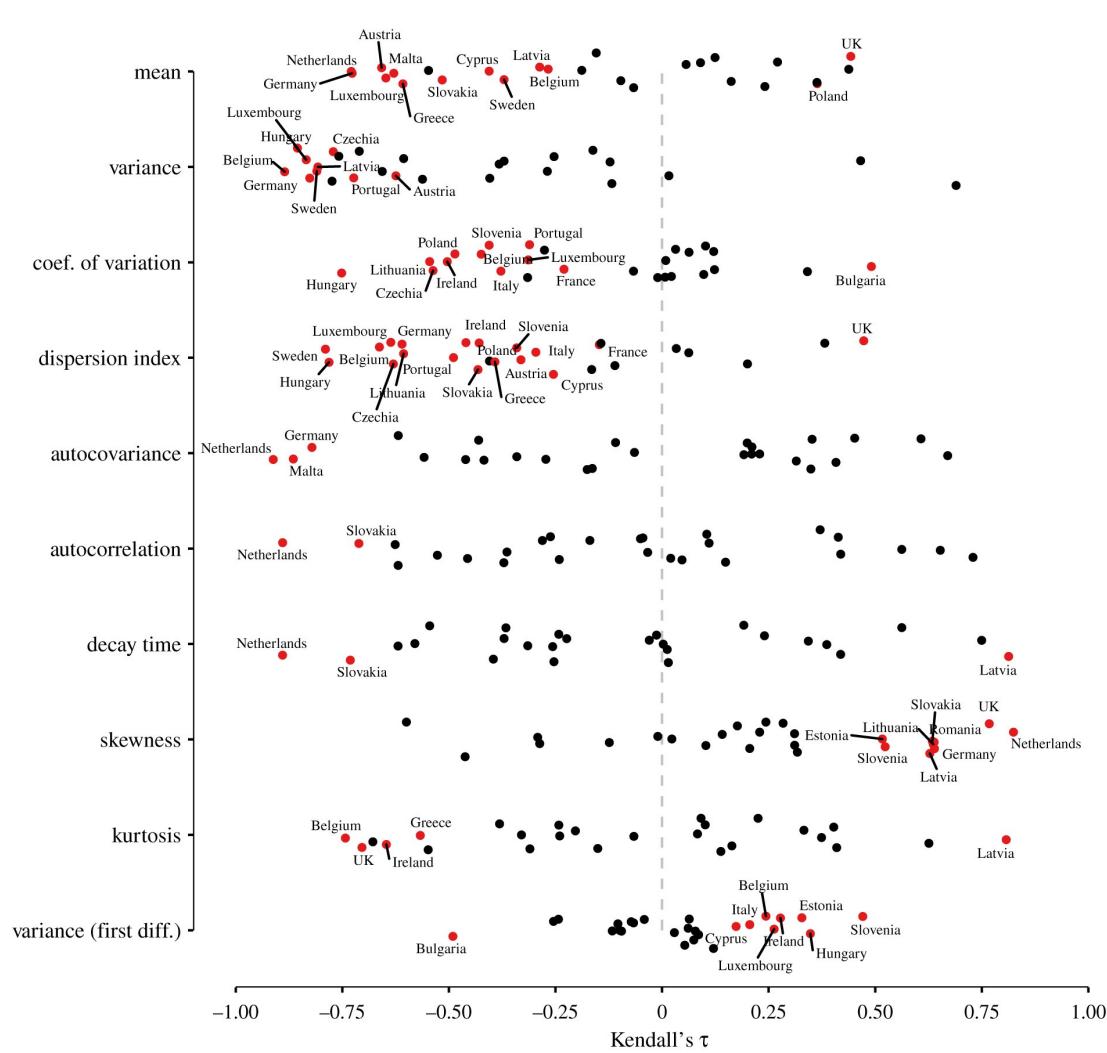


EWS for case data of COVID-19

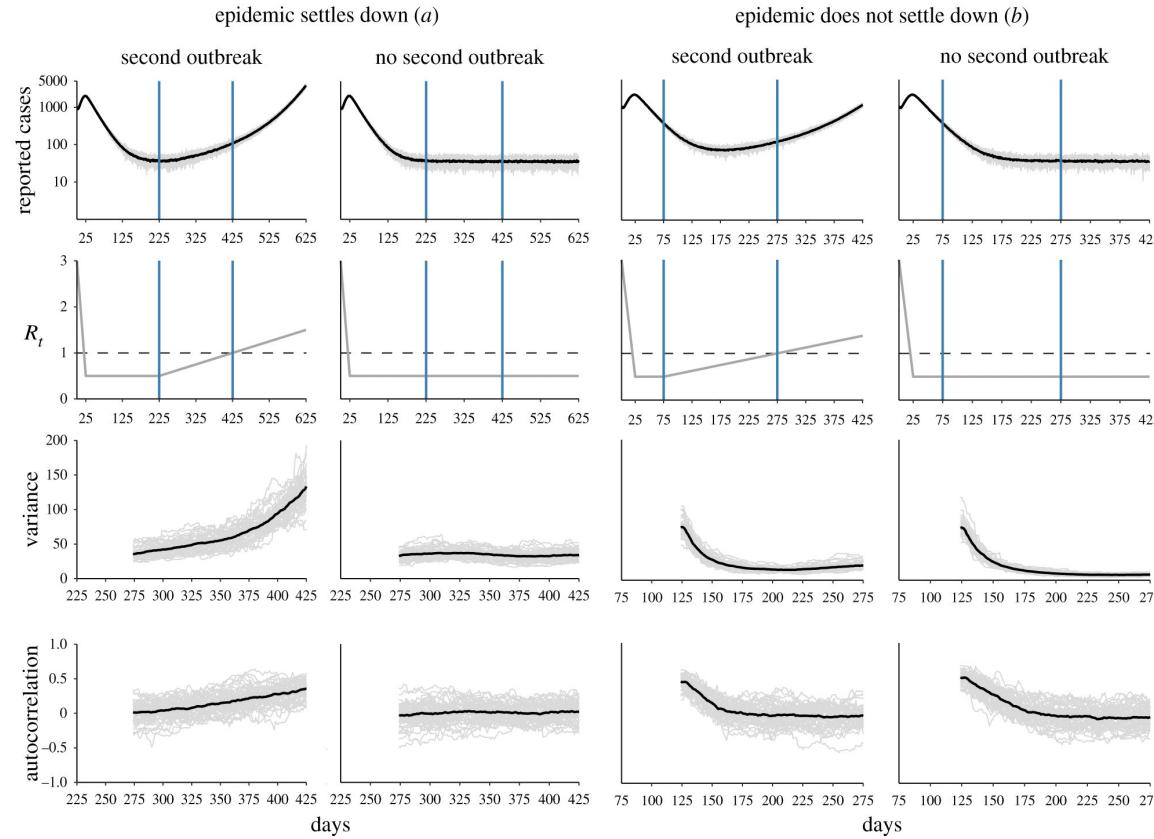
First Author	Main result	DOI
Dablander	Overlapping time-scales obscure EWS.	https://doi.org/ 10.1098/rsbl. 2021.1809
Proverbio	EWS can be useful for active monitoring of epidemic dynamics, but that their performance is sensitive to certain features of the underlying dynamics.	https://doi.org/ 10.1371/jour nal.pcbi.1009 58
O`brien	EWSs offer the opportunity for policymakers to improve the accuracy of urgent intervention decisions but best characterize hypothesized critical transitions.	https://doi.org/ 10.1098/rsbl. 2021.0487

Detecting the second wave in Europe





Detecting the second wave in Europe



EWS for other COVID-19 related data

First Author	Type of data	Main result	DOI
Bari	Google search queries & mobility data	Only very pre-liminary results	https://doi.org/10.1007/s13278-021-00723-5
Li	Visits to points of interest	Detects the behavioural response of the population to the COVID-19 pandemic	10.1109/ACCESS.2021.3058568
Loprete	Twitter data	Unexpected levels of concerns about pneumonia had been raised for several weeks before the frst cases of infection were ofcially announced	https://www.nature.com/articles/s41598-021-01333-1

EWS are not unique to critical transitions

EWS without Critical Transitions

EWS can occur prior to smooth transitions between stable states (Drake & Griffen, 2010; Kéfi et al., 2013).

EWS can occur when there is no transition (e.g., Wagner & Eisenman, 2015).

Critical Transitions without EWS

Strong external perturbations can lead to transitions without EWS (Ditlevsen & Johnsen, 2010; van Nes et al., 2016).

EWS may not occur prior to critical transitions in systems with non-smooth potentials (Hastings & Wysham, 2010).

Not all variables in a system generally express EWS equally strongly or at all (Boerlijst et al., 2013; Patterson et al., 2021).

EWS may not occur under correlated or extrinsic noise (Dakos et al., 2012b; O'Regan & Burton, 2018; Qin & Tang, 2018).

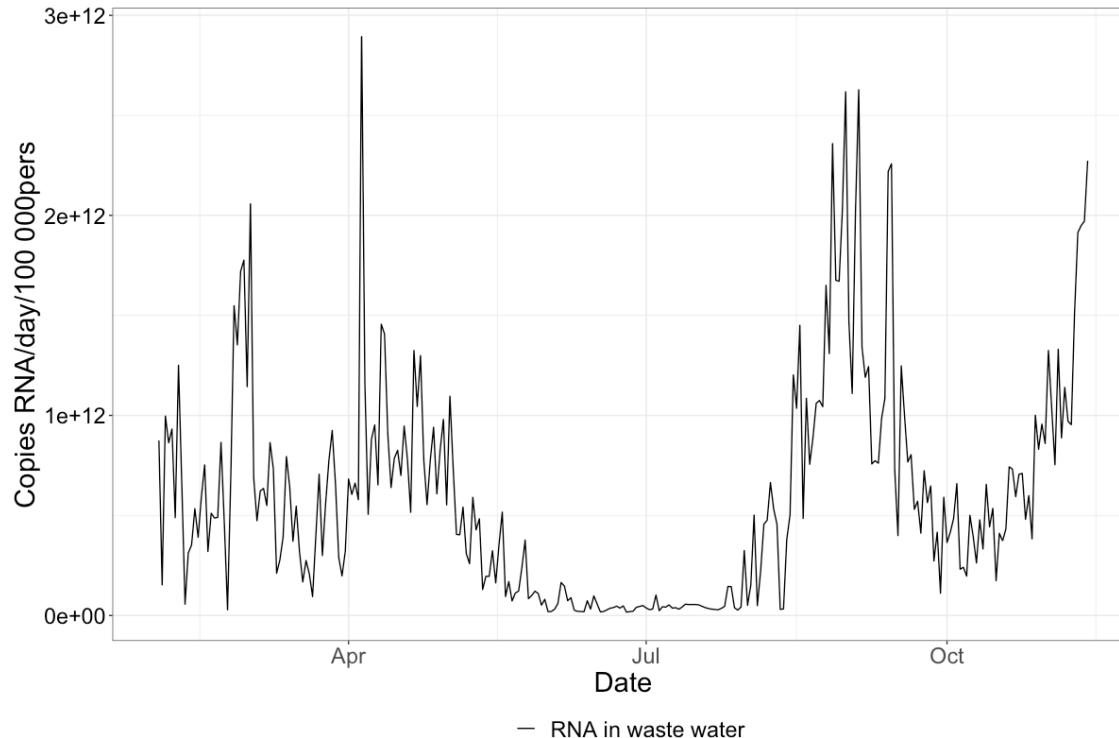
Other challenges

- Seasonality of the data
- Type of detrending used
- Availability of negative control data
- Overlapping time scales
- Co-occurring variants with different R_0 values

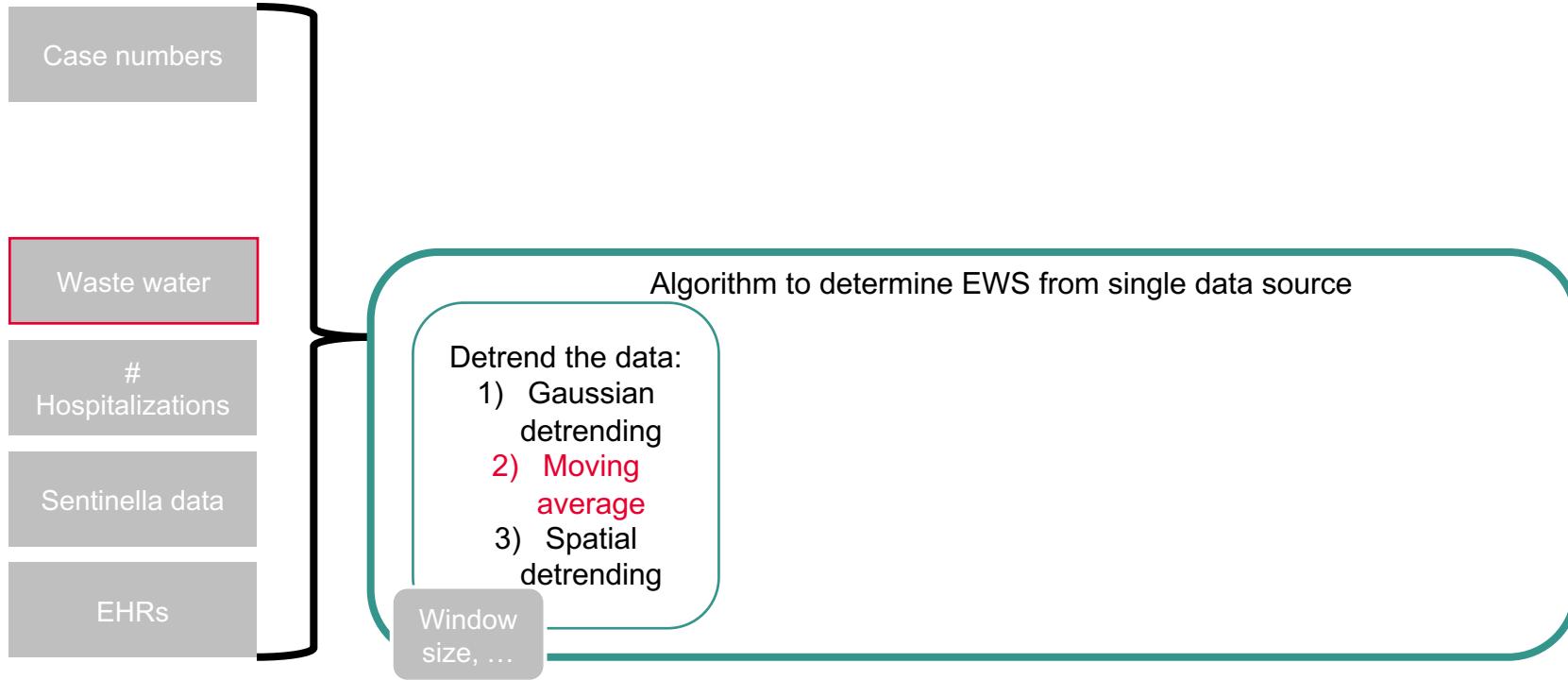
EWS in the MCID C-19 monitoring project



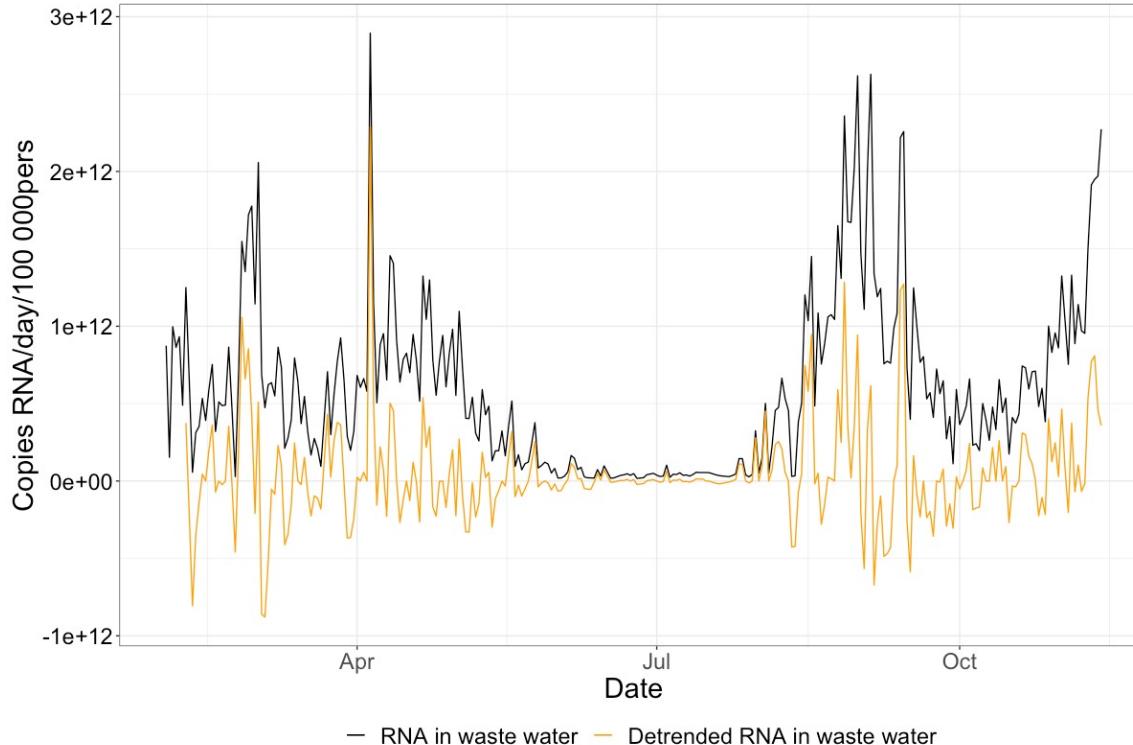
Preliminary analysis of Waste-water data



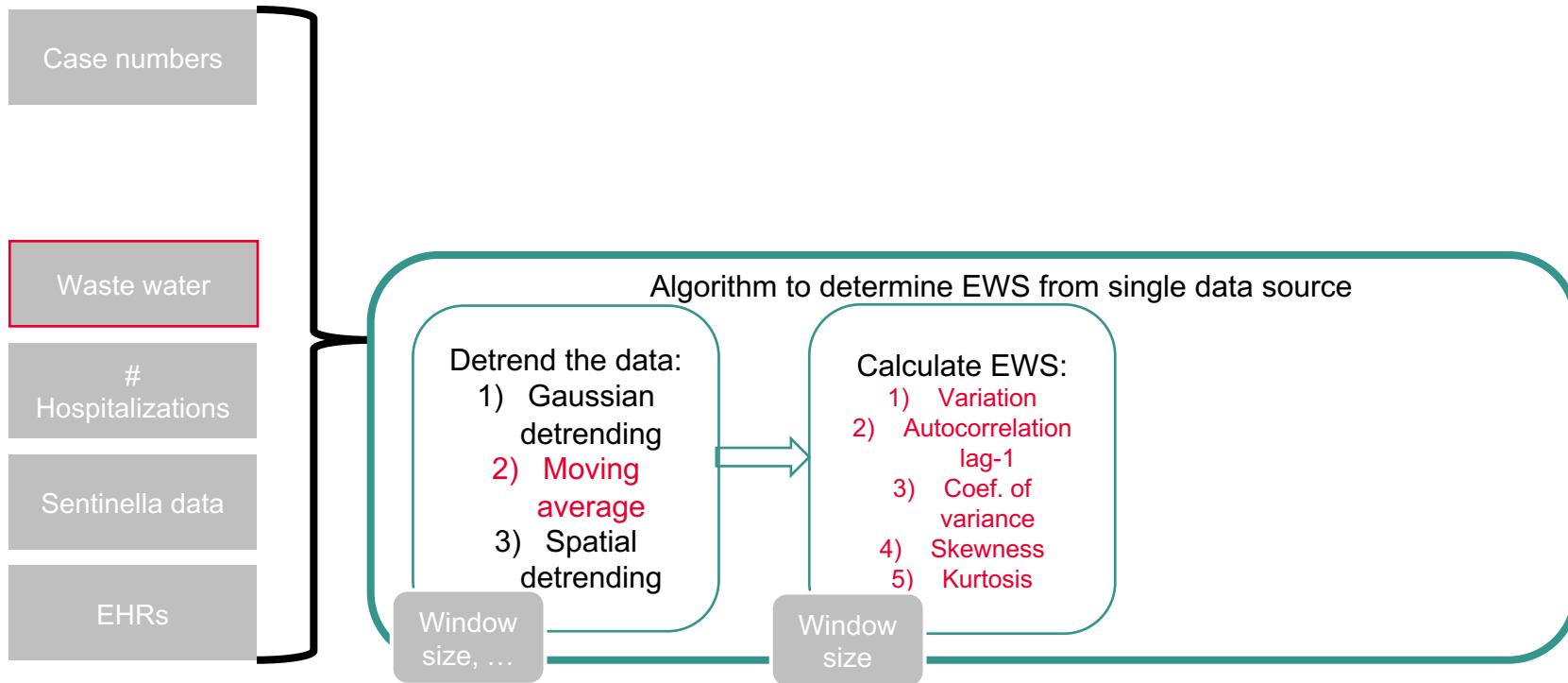
Step 1

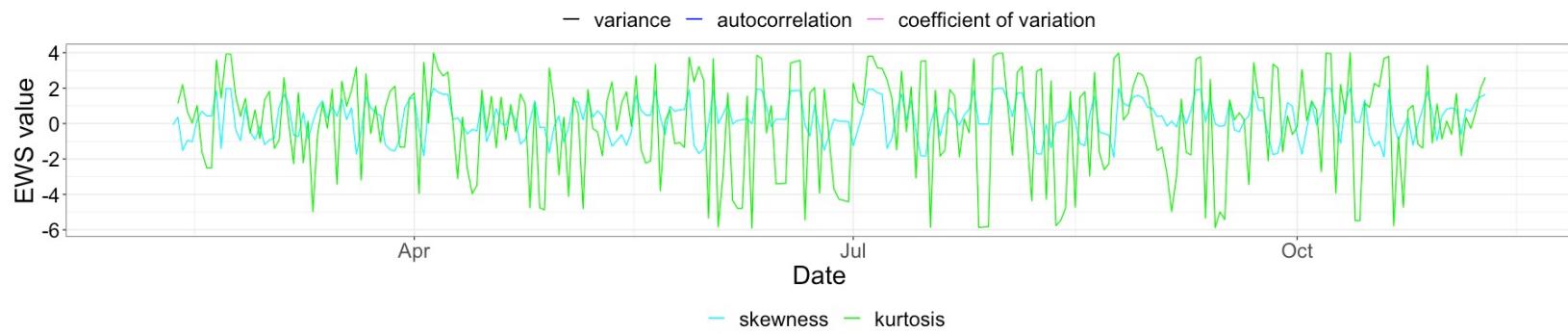
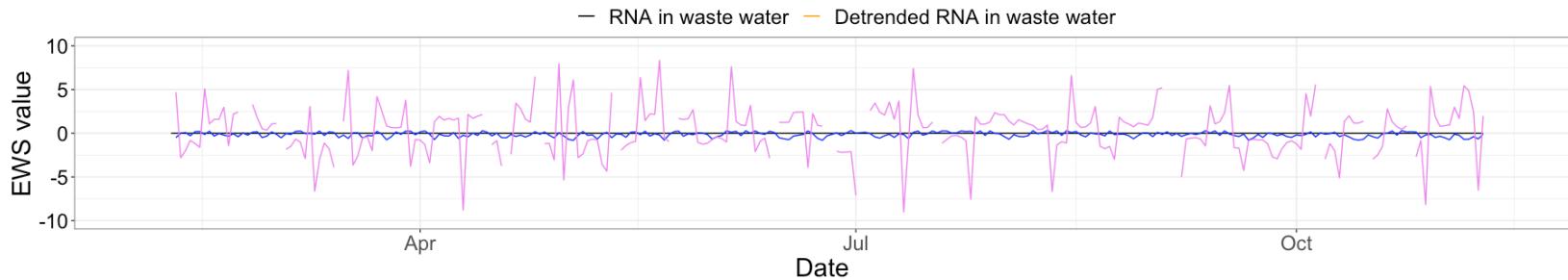
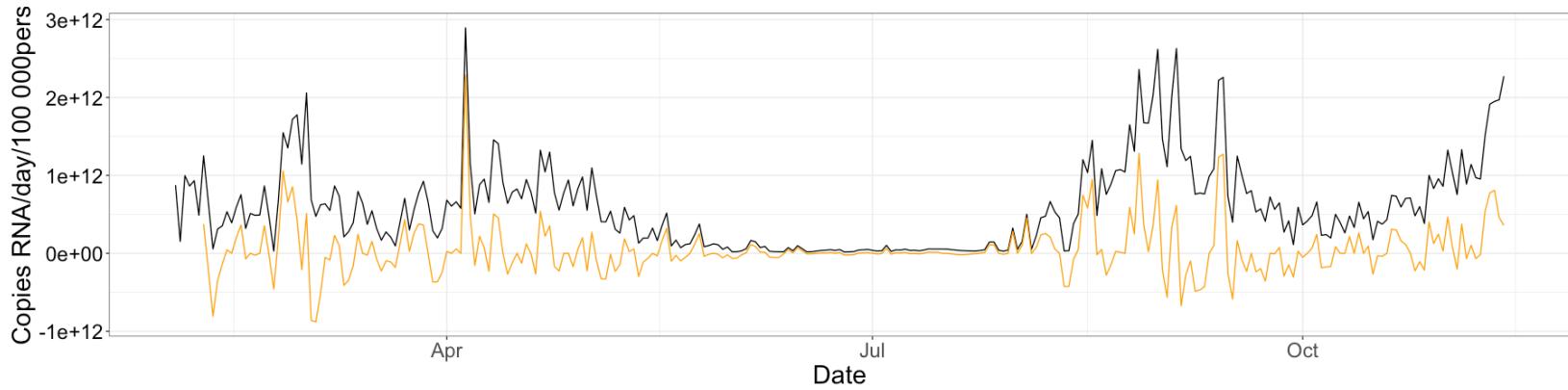


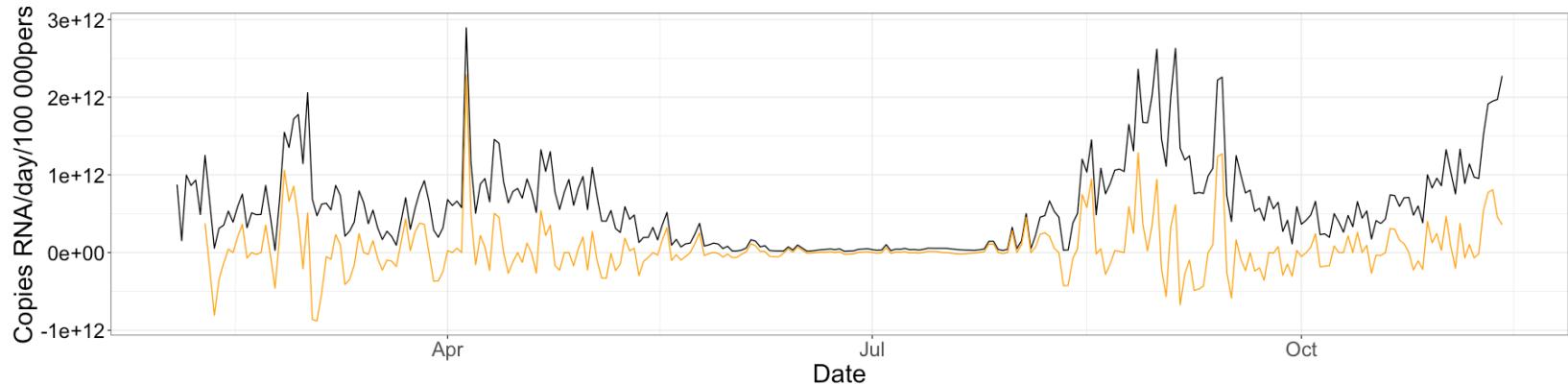
Preliminary analysis of Waste-water data



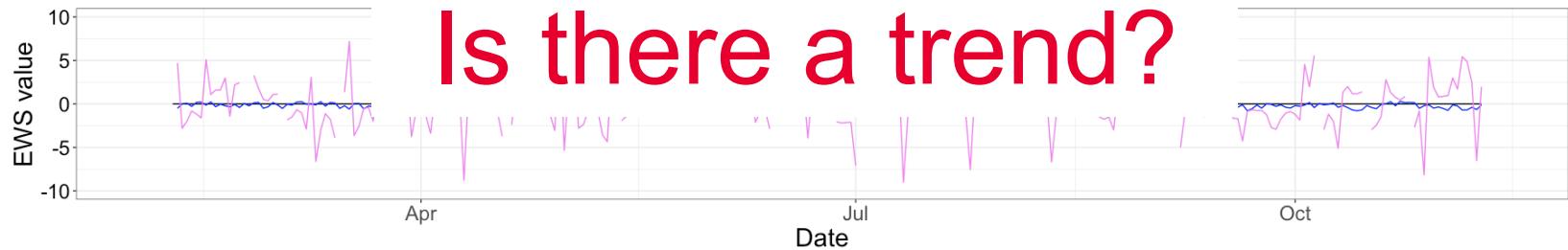
Step 2



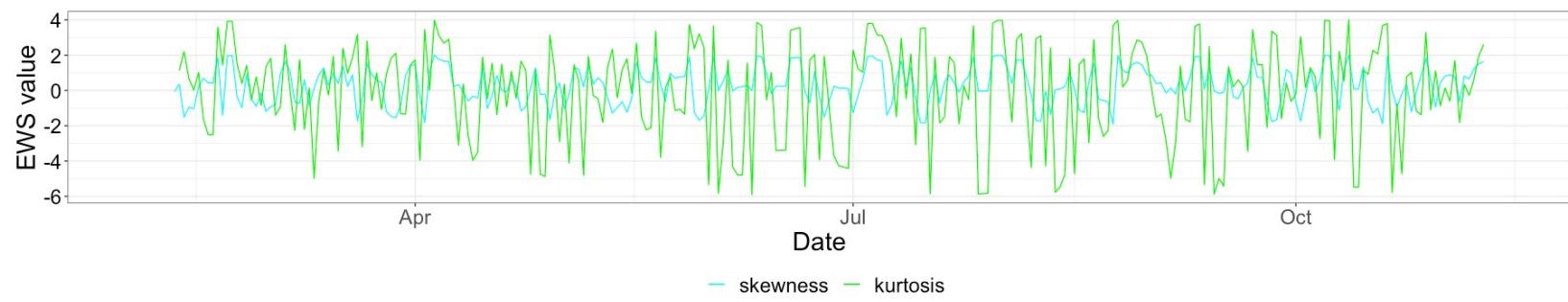




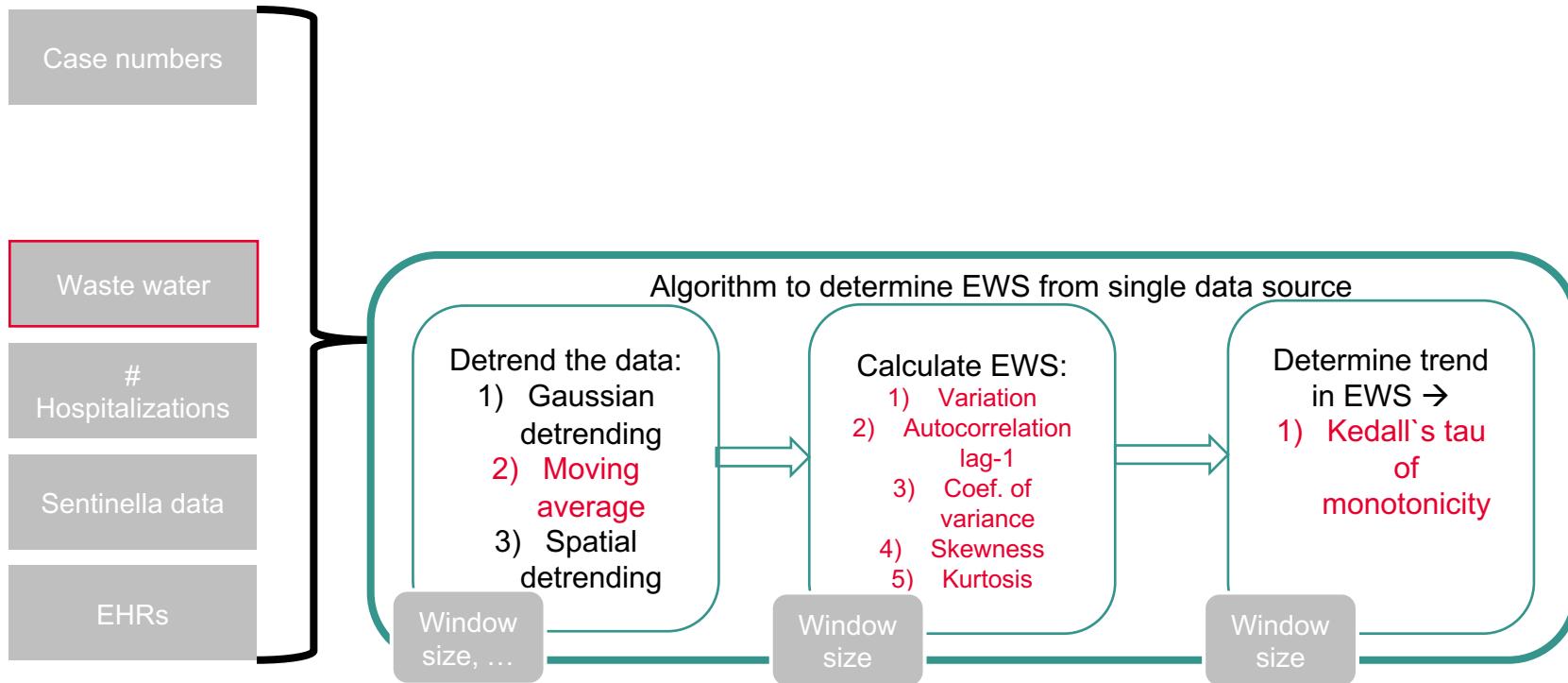
Is there a trend?

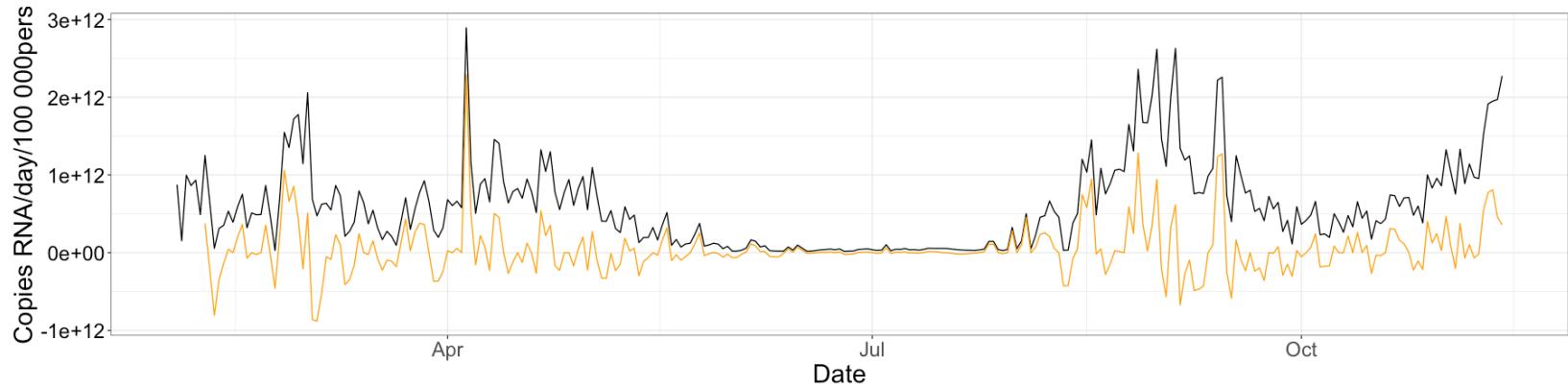


— variance — autocorrelation — coefficient of variation

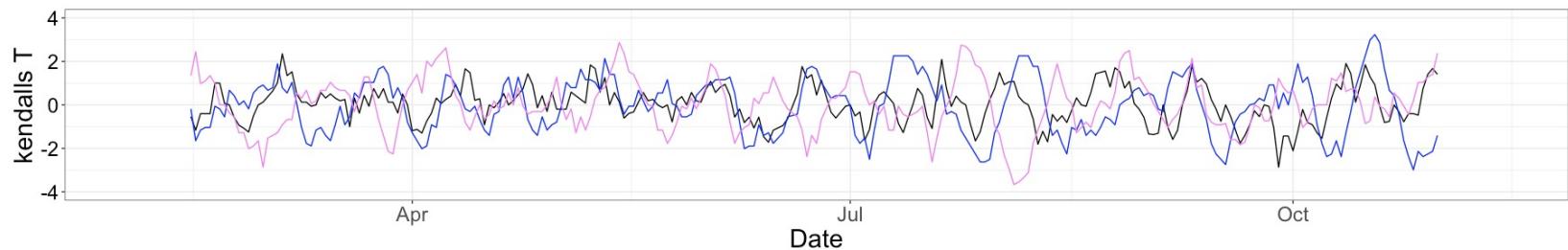


Step 3

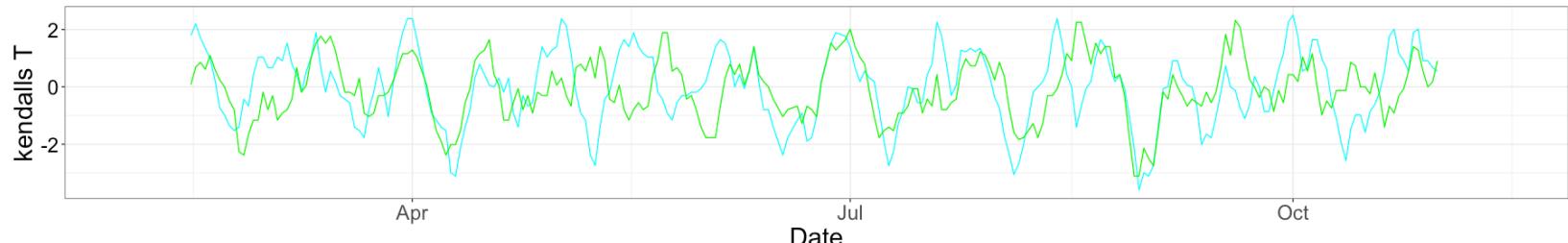




— RNA in waste water — Detrended RNA in waste water

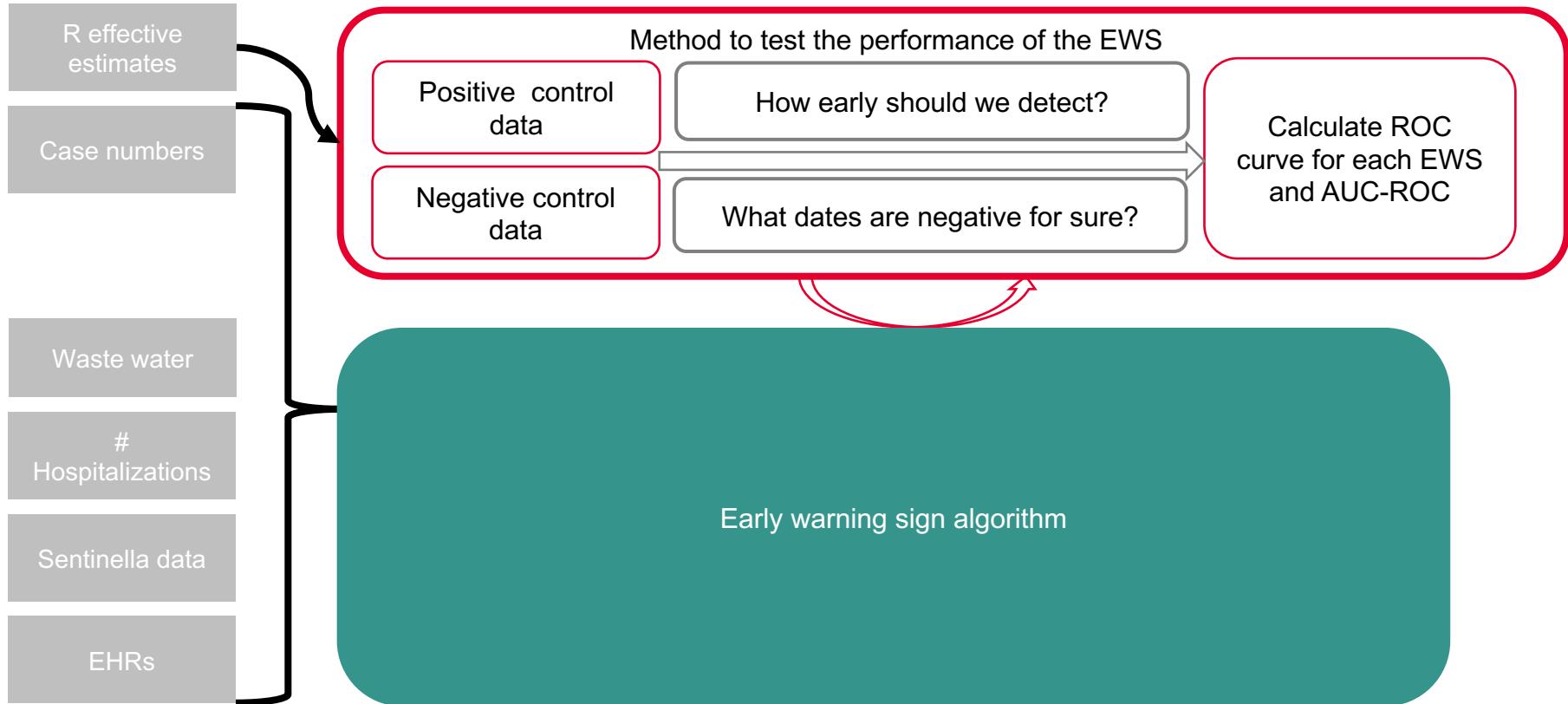


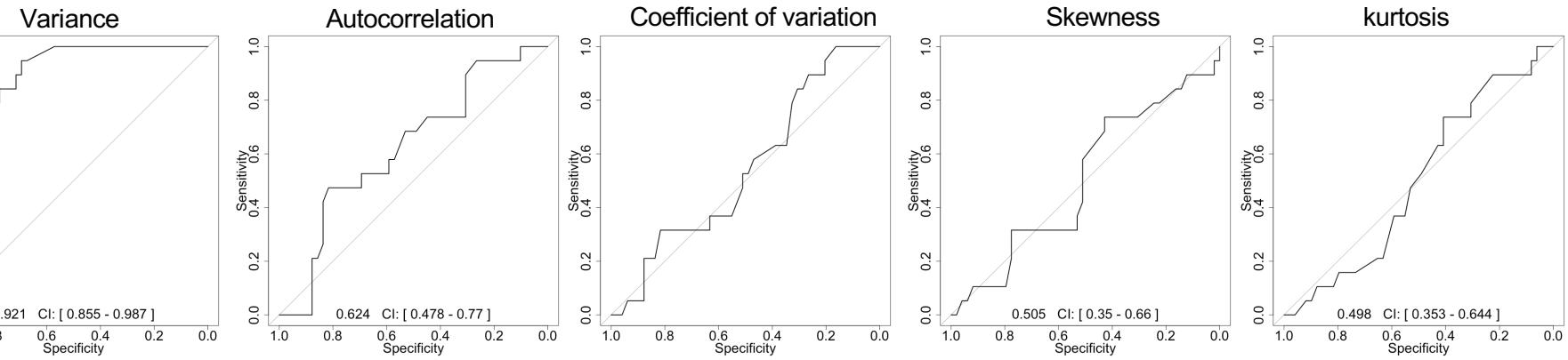
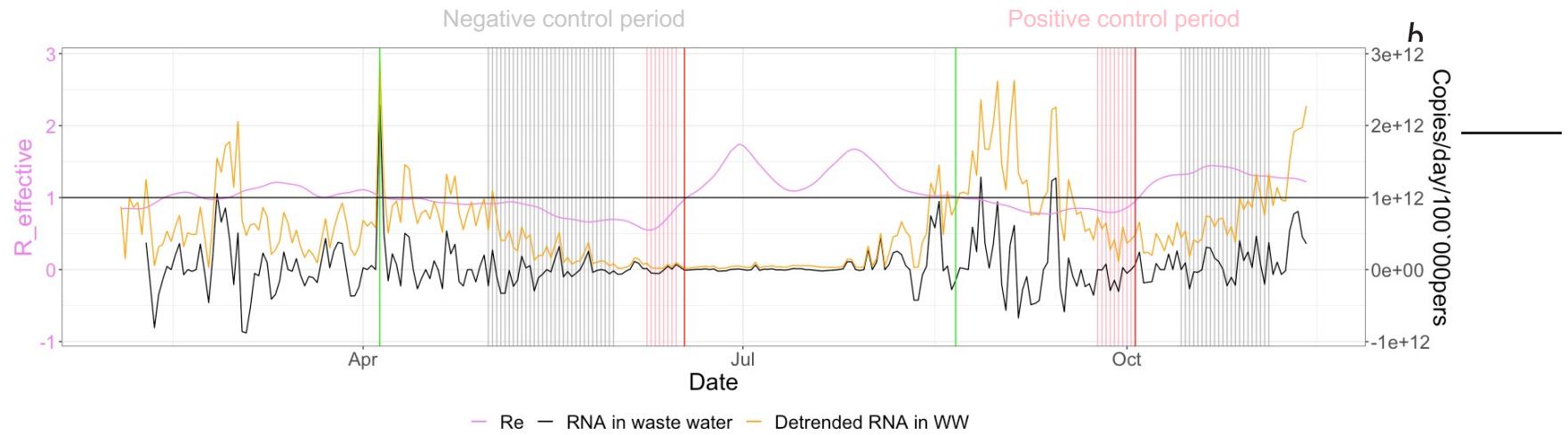
— variance — autocorrelation — coefficient of variation

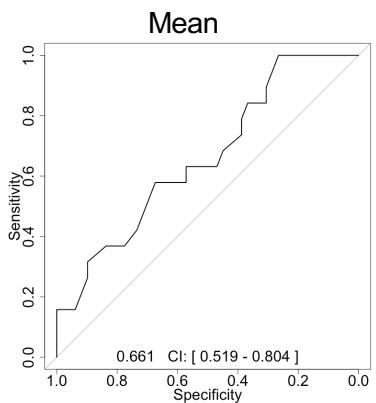
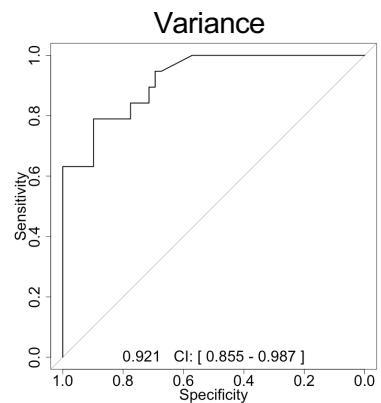
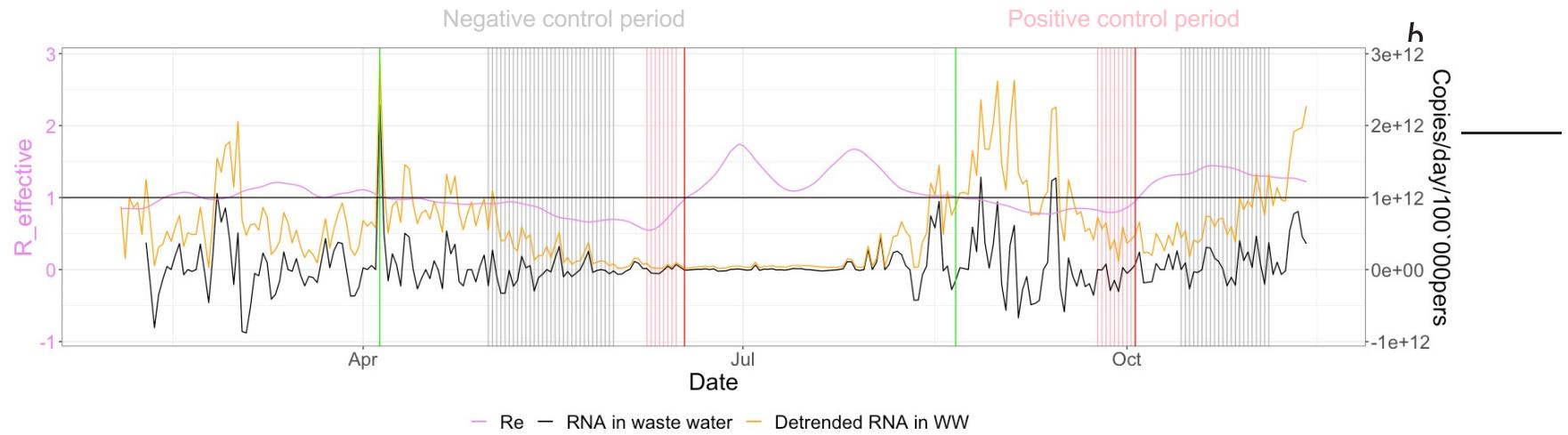


— skewness — kurtosis

What value predicts a transition?







Challenges and possible solutions

1. Too few data, especially in times where there are no transitions.
 2. The truth is unknown, R_e estimates also depend on the data.
 3. The power of the analysis is low.
1. Possible solutions:
 - a) Use data from multiple locations.
 - b) Use EHR, which were collected long before COVID started.
 - c) Validate the methods and test their performance with simulated data using the transmission model
 2. Use the R_e estimates from our transmission model rather than those calculated directly from case data.
 3. Possible solutions:
 - a) Combine several types of EWS.
 - b) Combine EWSs from multiple data sources.
 - c) Consider a different type of warning sign
 1. distribution of passing a threshold?
 2. Deep learning on simulated data and then apply to real data?

Resources

u^b

b
UNIVERSITÄT
BERN

<https://fabiandablander.com/>



Input research meeting

16 September 2022, ISPM, Bern