Tries

Specialized and misspelled trees

(Aka prefix trees)

Sample problem : how to store a phone directory

06 00 00 00 00 : John

06 00 22 45 86 : Dany

06 01 21 45 67 : Cersei

06 01 22 43 68 : Sansa

06 02 43 88 88 : Arya

07 10 11 12 13 : Night King

Sample problem : how to store a phone directory

06 0<mark>0 00 00 00 : John</mark>

06 01 21 45 67 : Cersei

06 0<mark>1 22 43 68 : Sansa</mark>

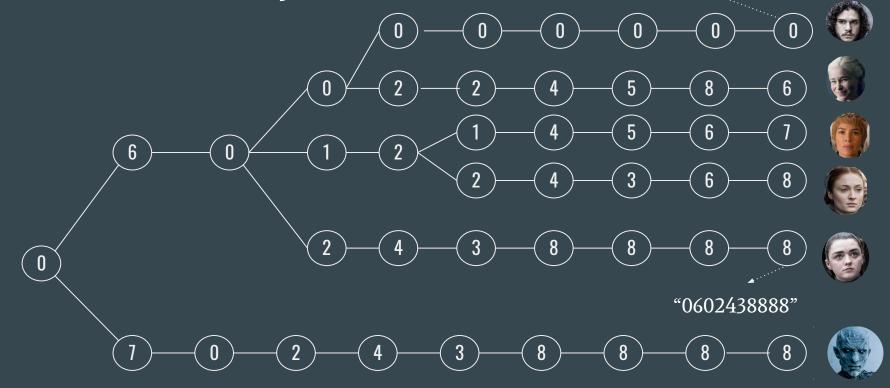
06 0<mark>2 43 88 88 : A</mark>rya

07 10 11 12 13 : Night King

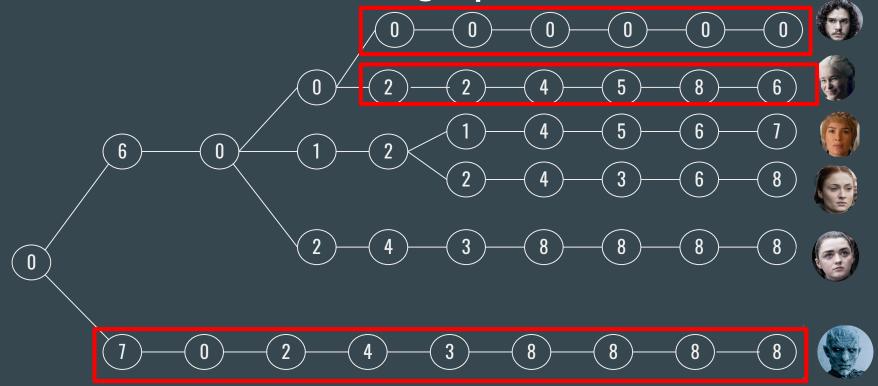
Do we really need that information 5 times?

Much better that way!

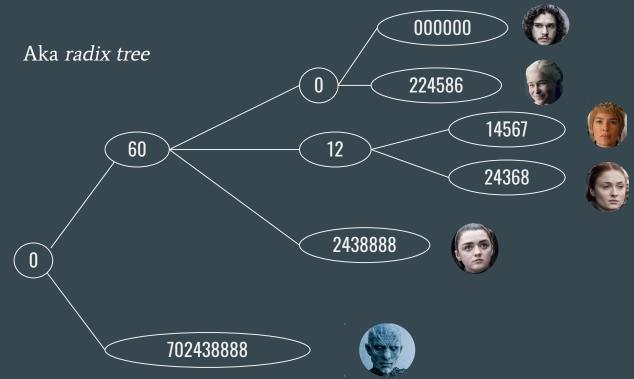
"0600000000"



That's a lot of nodes for a straight path



A compressed version



Prefix & suffix tries

• Same principle of construction, but this time the elements of the collection are prefixes/suffixes of a string

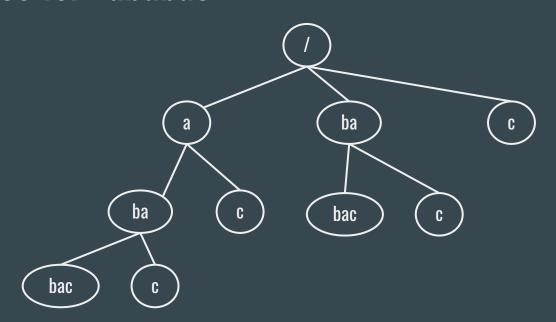
What is a suffix?

A substring that contains the last character of a string

```
"INSAlgo" → { "o", "go", " lgo", "Algo", "SAlgo", "NSAlgo", "INSAlgo"}
```

```
"ababac" \rightarrow { "c", "ac", "bac", "abac", "babac", "ababac"}
```

Suffix tree for "ababac"



"ababac" → { "c", "ac", "bac", "abac", "babac", "ababac"}

How to build a suffix tree?

With n the size of the string the tree represents:

- Naive implementation runs in O(n²)
 - \circ Generate every suffix (O(n)), then insert them into the tree (O(n²))
- An algorithm exists to build them in O(n)!
 - Ukkonen Algorithm
 - "The proof is left to the reader"!

What are tries effective for?

- Data compression, auto completion
- String manipulation
 - Longest palindromic substring
 - Pattern searching
 - Longest substring common to a set of strings
 - Shortest unique substring
 - Many more!

Credits

Author: Arthur Tondereau

Sources:

Wikipedia: https://en.wikipedia.org/wiki/Suffix_tree

https://en.wikipedia.org/wiki/Trie

THE Algorithm design MANUAL, 12.3 . S.S. Skiena

Edited by Emma Neiss