Common data structures

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Implementation and complexity

What's a data structure?

(Wikipedia) "a collection of **data values**, the **relationships** among them, and the functions or **operations** that can be applied to the data"

- an **abstraction** of data that is easy for a programmer to work with
- contains more than data: the data is organized in a specific way
- well-defined operations can be applied to the data
 - → it is important to know what data structures exist and which operations can be applied on them

Dynamic arrays (Python lists)

Goal: quickly access indexed items in a container and append new ones (or remove the last one)

Implementation:

- the language uses more room than needed
- while there is room, appending costs nothing
- when there is no more room, create a new array with more room and copy everything

```
|1|3|8
Logical size
    Capacity
```

Dynamic arrays (Python lists)

What's the complexity of adding a new item?

if you reach the capacity c_1 and extend the size to $c_2 = 2 * c_1$, the cost is c_1 only once but then the cost will be const for the next c_1 append operations

 \rightarrow on average, the cost is O(1)

What's the complexity of accessing an item?

O(1), position in RAM deduced from its index

2

2 7

2 7 1

2 7 1 3

27138

2 7 1 3 8 4

Logical size

Capacity

Dynamic arrays: in Python and C++

Common operations:

| эншин орегацоня: | Python | C++ | Complexity |
|------------------------|------------------|------------------|----------------------|
| Access the i-th item | arr[i] | arr[i] | 0(1) |
| Add v at the end | arr.append(v) | arr.push_back(v) | 0(1) avg 0(n) max |
| Insert v at position i | arr.insert(i, v) | arr.insert(i, v) | 0(n) |
| Find the position of v | arr.index(v) | std::find() | 0(n) |

When to use:

There are all kinds of use cases. If you often need to perform operations that are not O(1), check if another data structure matches your needs

Double-ended queues

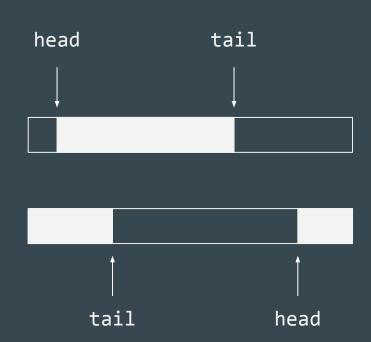
Goal: quickly access, remove and add items on both ends

Multiple implementations are used



Double-ended queues - with a ring buffer

- the queue is stored in an array
- head and tail indices are updated when removing or adding an item
- when too big, the queue is copied in a bigger array



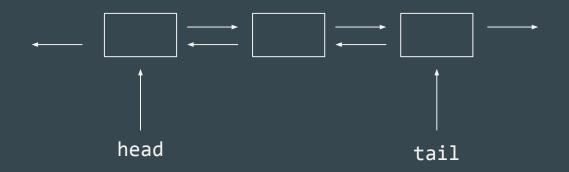
Double-ended queues - with a linked list

type Element
value

→ previous
→ next

type LinkedList

- \rightarrow head
- ightarrow tail



No direct access to other elements than head and tail but this is a very fast implementation

Double-ended queues - linked list of fixed-size subarrays

```
type Element
   values[]
   nb_used
    → previous
    → next
    head
   tail
```

 \rightarrow head

 \rightarrow tail

Still very fast, uses less memory

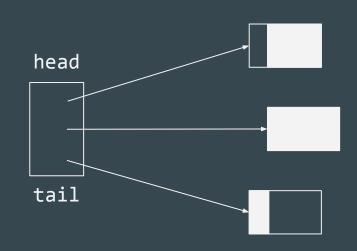
 \rightarrow used in Python

Double-ended queues - d.e-queue of fixed-size subarrays

C++ guys decided to implement double-ended queues... with a double-ended queue

The top-level queue is an array (e.g ring buffer)

- allows O(1) random-access
- adding and removing is now amortized
 O(1) it sometimes costs size / chunk_size



Double-ended queues - in Python and C++

Python: deque in collections

C++: deque (list is a linked list, Boost also offers a circular buffer)

| | Drubbass | Cu doque | Complexity | |
|---------------------------------|-----------------------------|--------------------|------------|----------|
| | Python | C++ deque | Python | C++ |
| Access the i-th element | dq[i] | dq[i] | O(n) | O(1) |
| Add v at the head | <pre>dq.appendleft(v)</pre> | dq.push_front(v) | O(1) | O(1) avg |
| Remove the head and put it in v | <pre>v = dq.popleft()</pre> | v = dq.pop_front() | O(1) | O(1) avg |
| Add v at the tail | dq.append(v) | dq.push_back(v) | O(1) | O(1) avg |
| Remove the tail and put it in v | v = dq.pop() | v = dq.pop_back() | O(1) | O(1) avg |

Double-ended queues - in Python and C++

When to use:

whenever you need a **queue** (e.g in *breadth-first search* algorithm)

When not to use:

- if you want to access very often elements in the middle of the sequence
- you don't need it when inserting and removing elements only on one side (e.g a a stack). Just don't do that on the left side

Dictionaries / hash maps

Goals:

- associate **values** to **keys**
- retrieve the value associated to a key in O(1) time
- → unlike real-life dictionaries, these ones are **not ordered**

(in real life, finding a word in a dictionary is O(log n) unless you have forgotten the alphabetical order)

Dictionaries / hash maps

The underlying structure is called a **hash table**

- a hash function turns the keys into an index
- the keys and values are stored in the data structure based on this index
- multiple strategies exist to manage collisions (cf next slides)

Example of hash function: sum of the ASCII codes for a string, modulo 42

"hello" \rightarrow 28

"world" \rightarrow 6

"INSAlgo" \rightarrow 33

Dictionaries / hash maps - separate chaining

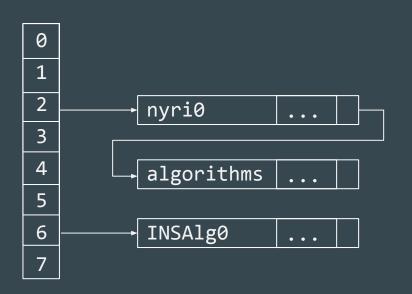
(key, value) couples where keys have the same hash are stored in a common data structure

These structures are kept small enough to have O(1) time access. When too filled, the table is re-created bigger

Often used:

- linked lists
- trees

With sum of ASCII codes modulo 8, and using linked lists:



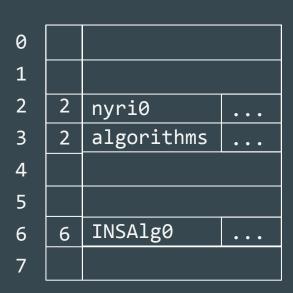
Dictionaries / hash maps - Open adressing

- No other data structure behind the array
- Collisions are solved with probing
- When the fill rate becomes too big, copy the data in a bigger hash table

Linear probing = put at next cell available

Randomized probing: follow a random sequence which seed is given by the hash

 \rightarrow used in Python



(sum of ASCII codes modulo 8, open adressing with linear probing)

Dictionaries / hash maps - in Python and C++

Python: open adressing with randomized probing (congruential RNG)

initial size 8, resized when ²/₃ full

C++: unordered map is a hash table, map a red-black tree

(we will talk about trees later in the year)

Common operations:

| | Python | C++ unordered_map | Complexity |
|--|------------|-------------------|----------------------|
| Find or set the value associated to key | dic[key] | dic[key] | 0(1) avg 0(n) max |
| Check if key exists in the dictionary | key in dic | dic.find(key) | 0(1) avg 0(n) max |

Dictionaries / hash maps - in Python and C++

When to use:

Whenever you need to associate a value to a key.

In Python, the ease of use and high performance make the dictionaries a **very powerful tool**.

When not to use:

When your keys are 0, 1, ..., n You're better than that.

Sets

Goals:

- store unique values
- quickly check if a value is in the set or not

Two common implementations:

- tree-based sets are ordered
- hash sets are faster but unordered (they're basically hash tables without values)

Sets - in Python and C++

Python: set is a hash set

C++: unordered_set is a hash table, set a tree

| Common operations: | Python | C++ set and unordered_set | Complexity | Complexity - C++ set |
|---------------------------------|-------------|---------------------------|----------------------|-------------------------|
| Add the value v to the set | s.add(v) | s.emplace(v) | 0(1) avg 0(n) max | O(log n) |
| Remove the value v from the set | s.remove(v) | s.erase(v) | 0(1) avg 0(n) max | O(log n) |
| Check if v is in the set | v in s | s.find(v) | 0(1) avg 0(n) max | O(log n) |

Set arithmetics in Python

| | | Average complexity |
|-------------------|--|---------------------|
| s1 <= s2, s1 < s2 | check if s1 is a [proper] subset of s2 | O(n1) |
| s1 >= s2, s1 > s2 | check if s1 is a [proper] superset of s2 | O(n2) |
| s1 s2 sk | union of s1, s2,, sk | O(n1 + n2 + + sk) |
| s1 & s2 & & sk | intersection of s1, s2, …, sk | O(min(n1, n2,, sk)) |
| s1 - s2 | all elements of s1 that are not in s2 | O(n1) |
| s1 ^ s2 | all elements of s1 or s2 but not both | O(n1 + n2) |

Sets too are cool:)

Sets - in Python and C++

When to use:

- to mark values already seen
- to keep a collection of unordered unique elements

When not to use:

• to make coffee (you just can't)

To be continued...

You probably want to hear about red-black trees, heaps (priority queues), etc...

Well, see you in 2019!

Slides: Louis Sugy for INSAlgo Schema of dynamic arrays: Wikipedia