# Analyse\_modele

October 5, 2023

What *cluster\_alignment.py* does:

The goal is to learn a predictive model, which assigns to any cell (i.e., gene expression vector on the gene panel) its most probable cluster number among those determined on whole scRNA sequencing data.

**Model training** The training data is a subset of the whole scRNAseq gene expression matrix (on all samples, that is, all conditions and ages), restricted to genes which belong to the panel in targeted scRNA data (N = 46). The training pipeline and the model are implemented in Python 3.6, using package scikit-learn [1] (version 0.24.2).

**Data processing** Whole scRNAseq gene expression matrix is standardized using routine *StandardScaler* in scikit-learn, that is, if X is the matrix:

$$\tilde{X} := (X - \text{mean}(X))/\text{std}(X - \text{mean}(X))$$
,

where mean (resp., std) is the function computing the mean (resp., the standard deviation) on the array comprising of all values contained in the matrix in argument.

**Model** The considered model is a logistic (logit) model. If  $x = [x_1, x_2, ..., x_{L-1}, x_L]^{\top}$  is a gene expression vector on L = 46 genes, let us denote the set of L + 1 coefficients (including the intercept) in the model associated with any cluster  $C \in \{0, 1, 2, ..., 7\}$   $\beta_0^C$ ,  $\beta_1^C$ , ...,  $\beta_{L-1}^C$ ,  $\beta_L^C$ . Then the probability of the associated cell of belonging to cluster C is

$$Pr(x \text{ in } C|\beta_{\cdot}^{C}) := \frac{1}{1 + \exp(-(\beta_{0}^{C} + \beta_{1}^{C}x_{1} + \dots + \beta_{L-1}^{C}x_{L-1} + \beta_{L}^{C}x_{L}))}.$$

Model fitting Given a list of N whole scRNA gene expression vectors (from the standardized whole scRNAseq matrix) and associated cluster numbers  $(x^i, y^i), i = 1, 2, ...$  (training data), the model fitting step consists to estimating the values of the L = 46 coefficients  $\beta_0^C, \beta_1^C, ..., \beta_{L-1}^C, \beta_L^C$  for each cell cluster  $C \in \{0, 1, 2, ..., 7\}$ . We consider a  $l_1$  (also called lasso) regularization, that is, the estimated set of parameters  $\beta$  for all clusters and genes would minimize the following function

$$\operatorname{loss}(\beta_{\cdot}^{\cdot}) := -\sum_{\substack{\text{cluster } C\\ \text{s.t. cluster } y^i = C}} \sum_{\substack{\operatorname{log}(Pr(x^i \text{ in } C|\beta_{\cdot}^C)) + \sum \\ g = 1, 2, \dots, L}} \sum_{\substack{\text{gene} \\ g = 1, 2, \dots, L}} |\beta_g^C| \,.$$

 $L \times 8$  (#clusters) coefficients are estimated in total.

To perform model fitting, we have used the  $Logistic\_Regression$  class in scikit-learn, with tolerance parameter=  $10^{-4}$ , random seed= 0, maximum number of iterations= 2000, and the SAGA solver.

Training procedure We have split the samples in the whole scRNAseq gene expression matrix into two groups, the training and the testing sets, where the testing set represents 5 of the total number of samples. The logistic model is fitted on the training set, and the values of Area Under the Curve (AUC) and Adjusted Rand Score (ARI) reported below are computed on cluster predictions on the testing set, compared to the ground truth cluster numbers for samples in the testing set. We performed a 5-fold cross-validation procedure, and selected the model with the highest AUC across all cross-validation phases.

Application to targeted scRNA data Targeted scRNA gene expression matrix is restricted to the L=46 genes identified in the training phase. Then it is standardized (using routine StandardScaler in scikit-learn), and the fitted logistic model is run to get the cluster predictions for targeted scRNAseq samples.

**References** [1] Pedregosa, Fabian, et al. "Scikit-learn: Machine learning in Python." the Journal of machine Learning research 12 (2011): 2825-2830.

[2] Defazio, Aaron, Francis Bach, and Simon Lacoste-Julien. "SAGA: A fast incremental gradient method with support for non-strongly convex composite objectives." Advances in neural information processing systems 27 (2014).

## 1 Analyse du modèle de prédiction de cluster cellulaire

#### 1.1 Model predictive power

Model achieved AUC = 0.923 (very good predictive power) and ARI = 0.452 (quite good clustering similarity) on the 5 perc. testing set

```
from cluster_alignment import data_normalisation
from sklearn.metrics import adjusted rand_score, roc_auc_score
from sklearn.preprocessing import LabelBinarizer
import numpy as np
with open(rfolder+"LogisticRegression_model.pck", "rb") as f:
   model = pkl.load(f)
clf = model["estimator"]
with open(rfolder+"gene_list.pck", "rb") as f:
   di = pkl.load(f)
whole_panel = di["whole_panel"]
info_experience = pd.read_csv(dfolder+"metadata_microglia.csv", index_col=0)
counts = pd.read_csv(rfolder+"raw_counts_subset_feature.csv", index_col=0)
counts = counts[info_experience.index].loc[whole_panel].dropna().T
## Clustering on whole data (true)
clustering_whole = pd.read_csv(dfolder+"info_experience.csv", index_col=0).
→loc[info_experience.index][["seurat_clusters"]].astype(str).values.flatten().
→ravel()
_, X_pred_fit = data_normalisation(counts, "standard", counts)
ids_microglia = np.array([i for i, c in enumerate(clustering_whole) if (c in_
→microglia)])
X_pred_fit_microglia = X_pred_fit[ids_microglia,:]
clustering_whole_microglia = clustering_whole[ids_microglia]
def print_metrics(Y, X_pred_fit, clf, type_):
   Y_pred = clf.predict(X_pred_fit).ravel()
   lab = LabelBinarizer().fit(Y)
   Y_bin, Y_predbin = lab.transform(Y), lab.transform(Y_pred)
   print("On clusters %s" % str(list(np.unique(Y))))
   auc = roc_auc_score(Y_bin, Y_predbin, multi_class="ovr",_
→average="weighted", labels=list(np.unique(Y)))
   ari = adjusted_rand_score(Y, Y_pred)
   return "(%s) ARI = %.3f, AUC = %.3f" % (type_, ari, auc)
## Clustering on whole data (predicted) on microglia
print(print_metrics(clustering_whole_microglia, X_pred_fit_microglia, clf, __
→"microglia"))
## Clustering on whole data (predicted) on microglia
print(print_metrics(clustering_whole, X_pred_fit, clf, "whole"))
```

Restricted to microglia clusters (/!\ on the WHOLE dataset, not only on testing

```
data)
On clusters ['0', '1', '2', '3', '5']
(microglia) ARI = 0.444, AUC = 0.818
On clusters ['0', '1', '2', '3', '4', '5', '6', '7']
(whole) ARI = 0.437, AUC = 0.815
```

#### 1.2 Gene panel in model

Targeted data gene panel (#genes = 46):

ApoE Bc1211 Cc112 Cc12 Cc13 Ccnd1 Cd14 Cd74 Cd9 Cldn5 Clec7a Colla2 Ctsd Fabp5 Gpnmb Gpr84 Hmgb2 Icam1 Ifngr1 Igfbp2

Il1b

```
I14Ra
Itgax
Jak3
Lyve1
Lyz2
Map3k8
Meg3
Mif
Mki67
Mrc1
Nfkb1
P2ry12
Pf4
Pim1
Ptprz1
Rab7b
Rgs5
S100a9
Socs3
Sparc
Spp1
Stat3
Tnfaip3
Ttr
Ube2c
Missing genes from initial panel (N=0) = []
```

## 1.3 Visualization of model coefficients

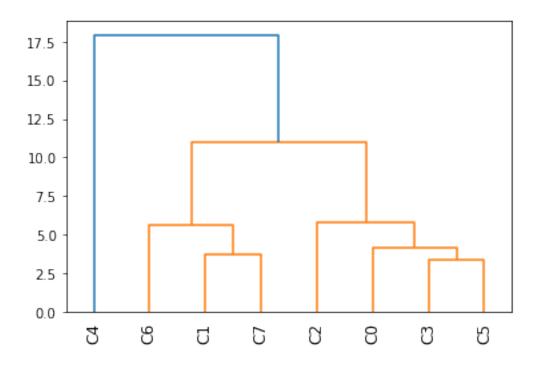
```
[4]: import matplotlib.pyplot as plt
     from copy import copy
     import matplotlib.cm as cm
     import seaborn as sns
     import numpy as np
     import pandas as pd
     from scipy.cluster.hierarchy import dendrogram, linkage
     def compute_cluster_dendrogram(clf, restrict_to=None, plot_it=False):
         classes = clf.classes_
         coefs = clf.coef_
         if (restrict_to is None):
             restrict_to = classes
         clusters_ids = [i for i,c in enumerate(classes) if (c in restrict_to)]
         ## sort columns by variance
         vars_clusters = np.var(coefs[clusters_ids], axis=0)
         gene_order = list(reversed(list(np.argsort(vars_clusters))))
```

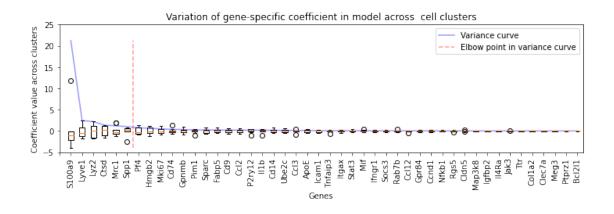
```
mat = logit_model.coef_[clusters_ids, :]
   mat = mat[:,gene_order]
    ## sort rows by cluster proximity
   linkage_data = linkage(mat, method='ward', metric='euclidean')
    cluster_order = list(dendrogram(linkage_data,
                    labels=["C%s"%classes[i] for i in clusters_ids],
                    leaf_rotation=90)["leaves"])
   if (plot_it):
       plt.show()
   plt.close()
   mat = mat[cluster order,:]
   return mat, vars_clusters, gene_order, cluster_order, linkage_data
def plot_feature_by_variance(mat, vars_clusters, gene_order, targeted_panel,u
\rightarrowname="", figsize=(12,3), ylim=(-5,25)):
   plt.figure(figsize=figsize)
   plt.title("Variation of gene-specific coefficient in model across %s cell__
⇔clusters" % name)
   plt.boxplot(mat)
   plt.plot(range(1,mat.shape[1]+1), vars_clusters[gene_order], "b-", alpha=0.
plt.plot([6.5,6.5], [np.min(mat), np.max(vars_clusters)], "r--", alpha=0.4,
→label="Elbow point in variance curve")
   plt.xticks(range(mat.shape[1]+1), [""]+[targeted_panel[i] for i in_
 ⇒gene_order], rotation=90)
   plt.ylabel("Coefficient value across clusters")
   plt.xlabel("Genes")
   plt.ylim(ylim)
   plt.legend()
   plt.show()
   plt.close()
   print("\t".join(["Gene"]+[targeted panel[i] for i in gene order[:6]]))
   print('\t'.join(["Var."]+[str(i) for i in np.
 →round(vars_clusters[gene_order[:6]],2)]))
def plot_feature_coefficient(mat, vars_clusters, gene_order, cluster_order,_u
→targeted_panel, name="", figsize=(12,12)):
   plt.figure(figsize=figsize)
   plt.title("Gene-specific coefficient in model across %s cell clusters" %L
⇒name)
    c_map = copy(cm.get_cmap("coolwarm"))
    c_map.set_over('k')
   plt.imshow(mat, cmap=c_map, vmin=-2.5, vmax=2.5, interpolation='none')
   plt.xlabel("Genes")
   plt.ylabel("Clusters")
```

```
plt.xticks(range(mat.shape[1]), [targeted_panel[i] for i in gene_order],_
 →rotation=90)
   plt.yticks(range(mat.shape[0]), ["C%s"%i for i in cluster_order])
   plt.colorbar(shrink=0.25, extend='max')
   plt.show()
   plt.close()
def plot cluster heatmap(mat, vars clusters, gene order, targeted panel,
→linkage_data, figsize=(5,5)):
   genes = [targeted_panel[i] for i in gene_order]
   clusters = ["C%s" %i for i in cluster_order]
   clusters df = pd.DataFrame(mat, columns=genes, index=clusters)
   clusters_df = clusters_df.loc[list(sorted(clusters_df.index))]
   plt.figure(figsize=figsize)
   cg = sns.clustermap(clusters_df.T.corr(method="pearson"),
              figsize=figsize, cbar_kws=None, row_linkage=linkage_data,_
cmap="coolwarm", vmin=-1, vmax=1, cbar_pos=(1, .2, .03, .4))
   cg.ax_col_dendrogram.set_visible(False)
   plt.show()
   plt.close()
```

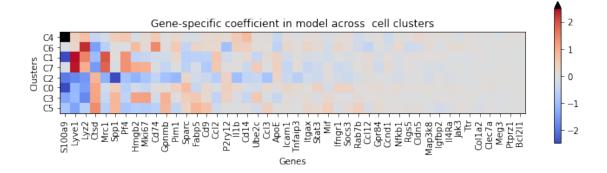
Strength of coefficient for each pair (gene, cell cluster). Genes are ordered by decreasing variance in coefficient across cell clusters. Clusters are by similarity (from hierarchical clustering) on coefficients across genes.

Model coefficients: 8 cell categories/clusters x 46 genes from panel



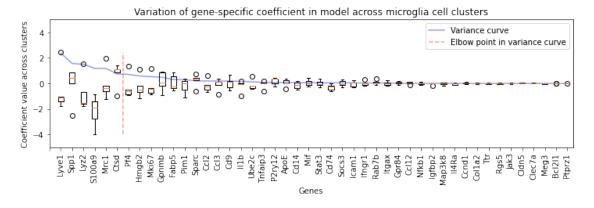


Gene S100a9 Lyve1 Lyz2 Ctsd Mrc1 Spp1 Var. 21.23 2.45 2.19 1.36 1.21 1.01



According to those two plots, the genes which are most critical (with largest variance across cell clusters) to identify the cell cluster are S100a9, Lyve1, Lyz2, Ctsd, Mrc1 and Spp1.

#### 1.3.1 Variation of coefficients in microglia cell clusters



```
Gene Lyve1 Spp1 Lyz2 S100a9 Mrc1 Ctsd
Var. 2.38 1.56 1.5 1.19 1.18 0.75
```

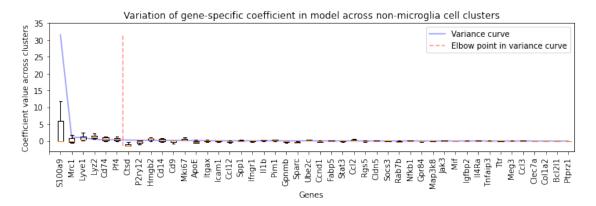
#### 1.3.2 Variation of coefficients in non-microglia cell clusters

```
[7]: mat, vars_clusters, gene_order, _, _ = compute_cluster_dendrogram(logit_model, _ 

→restrict_to=["4","6","7"])

plot_feature_by_variance(mat, vars_clusters, gene_order, targeted_panel,
```

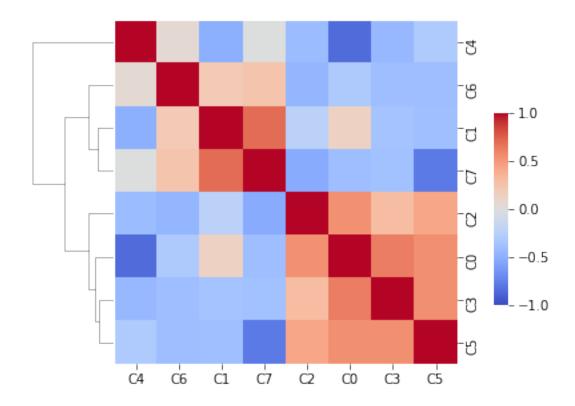
```
name="non-microglia", figsize=(12,3), ylim=(-3,35))
```



```
Gene S100a9 Mrc1 Lyve1 Lyz2 Cd74 Pf4
Var. 31.54 1.14 0.98 0.48 0.39 0.33
```

## 1.4 Cluster similarity based on coefficients

<Figure size 360x360 with 0 Axes>



#### 1.5 Signatures for microglia clusters

Using whole data on **predicted** (not ground truth!) clusters by the model, and applying a differential analysis

```
#! pip install qit+https://qithub.com/Maayanlab/qeode.qit
     from geode import chdir
     res_df_ls = []
     for s in list(np.unique(Y_pred)):
         annotation = list((Y_pred==s).astype(int)+1)
         chdir_res = chdir(X_fit.T, annotation, whole_panel, calculate_sig=1,__
      →nnull=10000, sig_only=1)
         res_df = pd.DataFrame({"Statistic C%s" % s: {x[1]:x[0] for x in chdir_res}})
         res_df_ls.append(res_df)
     res_df = res_df_ls[0].join(res_df_ls[1:], how="outer")
     res_df
    Number of significant genes: 30
    Number of significant genes: 6
    Number of significant genes: 41
    Number of significant genes: 4
    Number of significant genes: 7
    Number of significant genes: 10
    Number of significant genes: 6
    Number of significant genes: 5
[9]:
              Statistic CO
                             Statistic C1
                                            Statistic C2 Statistic C3
                                                                          Statistic C4
                  -0.132651
     Cc12
                                  0.196295
                                                                    NaN
                                                0.055466
                                                                                    NaN
     Cc13
                                                                    NaN
                   0.153458
                                       NaN
                                               -0.182139
                                                                                    NaN
                  -0.147615
     Cd14
                                       NaN
                                               -0.024717
                                                                    NaN
                                                                              0.194470
     Cd9
                                                                    NaN
                   0.086696
                                       NaN
                                               -0.131152
                                                                                   NaN
     Clec1a
                  0.078496
                                       NaN
                                                0.129389
                                                                    NaN
                                                                                   NaN
     Ctsd
                                       NaN
                                                                    NaN
                                                                                   NaN
                  0.101190
                                               -0.044343
     Fabp5
                  -0.247859
                                       NaN
                                                                    NaN
                                                                                   NaN
                                                0.034000
     Gpr84
                   0.093508
                                       NaN
                                                0.038351
                                                                    NaN
                                                                                   NaN
     Hmgb2
                                       NaN
                                                               0.428646
                                                                                   NaN
                  -0.110875
                                               -0.203829
                                               -0.093973
     Icam1
                   0.213932
                                       NaN
                                                                    NaN
                                                                                   NaN
     Ifngr1
                  0.215454
                                       NaN
                                               -0.143127
                                                                    NaN
                                                                                   NaN
     Il4ra
                                                                    NaN
                  0.067208
                                       NaN
                                                      NaN
                                                                                   NaN
     Lyve1
                  -0.209359
                                 0.470689
                                               -0.150369
                                                                    NaN
                                                                                   NaN
                                               -0.201182
                                                                    NaN
                                                                                   NaN
     Lyz2
                  -0.289889
                                 0.354955
     Map3k8
                                                                    NaN
                                                                                   NaN
                   0.102472
                                       NaN
                                                      NaN
     Mif
                  -0.145485
                                       NaN
                                                0.128322
                                                                    NaN
                                                                                   NaN
                                                               0.717253
     Mki67
                  -0.339764
                                       NaN
                                               -0.130964
                                                                                   NaN
     Mrc1
                  -0.143086
                                 0.458088
                                               -0.215117
                                                                    NaN
                                                                                   NaN
                                                                    NaN
     Nfkb1
                  0.099611
                                       NaN
                                               -0.043158
                                                                                   NaN
     Pf4
                  -0.153995
                                 0.383312
                                               -0.151327
                                                                    NaN
                                                                                   NaN
     Pim1
                  0.165707
                                       NaN
                                               -0.214916
                                                                    NaN
                                                                                   NaN
     Rab7b
                  -0.081107
                                       NaN
                                                                    NaN
                                                      NaN
                                                                                   NaN
     Rgs5
                  0.086749
                                       NaN
                                                0.295996
                                                                    NaN
                                                                             -0.126292
     S100a9
                                 -0.358090
                                                              -0.260491
                                                                              0.906180
                  -0.317980
                                                0.195165
     Socs3
                   0.249172
                                       NaN
                                               -0.101065
                                                                    NaN
                                                                                   NaN
```

Sparc	0.269514	NaN	-0.127994	NaN	NaN
Spp1	-0.073966	NaN	-0.119963	NaN	NaN
Stat3	0.260570	NaN	-0.174188	NaN	NaN
Tnfaip3	0.155578	NaN	-0.096640	NaN	NaN
Ube2c	-0.129065	NaN	-0.059675	0.379733	NaN
Apoe	NaN	NaN	0.034318	NaN	NaN
Bc1211	NaN	NaN	0.100960	NaN	NaN
Ccl12	NaN	NaN	0.048993	NaN	NaN
Cd74	NaN	NaN	0.212247	NaN	-0.168130
Cldn5	NaN	NaN	0.071985	NaN	NaN
Col1a2	NaN	NaN	0.154939	NaN	NaN
Gpnmb	NaN	NaN	0.066496	NaN	-0.124086
Igfbp2	NaN	NaN	0.442392	NaN	-0.175270
Il1b	NaN	NaN	-0.119863	NaN	0.152262
Jak3	NaN	NaN	0.082153	NaN	NaN
Meg3	NaN	NaN	0.142381	NaN	NaN
P2ry12	NaN	NaN	0.060512	NaN	NaN
Ptprz1	NaN	NaN	0.160588	NaN	NaN
Ttr	NaN	NaN	0.265173	NaN	NaN
Itgax	NaN	NaN	NaN	NaN	NaN
	Statistic C5	Statistic C6	Statistic C7		
Ccl2	NaN	NaN	NaN		
Cc13	NaN	NaN	NaN		
Cd14	NaN	NaN	NaN		
Cd9	0.206786	NaN	NaN		
Clec1a	NaN	NaN	NaN		
Ctsd	NaN	NaN	NaN		
Fabp5	0.471414	NaN	NaN		
Gpr84	NaN	NaN	NaN		
Hmgb2	NaN	NaN	0.544891		
Icam1	NaN	NaN	NaN		
Ifngr1	NaN	NaN	NaN		
Il4ra	NaN	NaN	NaN		
Lyve1	NaN	NaN	NaN		
Lyz2	NaN	0.314001	NaN		
Map3k8	NaN	NaN	NaN		
Mif	NaN	NaN	NaN		
Mki67	NaN	NaN	0.606353		
Mrc1	NaN	NaN	NaN		
Nfkb1	NaN	NaN	NaN		
Pf4	NaN	NaN	0.236722		
Pim1	NaN	NaN	NaN		
Rab7b	0.257480	NaN	NaN		
Rgs5	-0.178343	-0.120462	NaN		
S100a9	-0.200794	-0.343953	-0.214476		
Socs3	NaN	NaN	NaN		

Sparc	NaN	NaN	NaN
Spp1	0.484868	NaN	NaN
Stat3	NaN	NaN	NaN
Tnfaip3	NaN	NaN	NaN
Ube2c	NaN	NaN	0.191943
Apoe	NaN	NaN	NaN
Bc1211	NaN	NaN	NaN
Ccl12	NaN	NaN	NaN
Cd74	-0.236294	0.833718	NaN
Cldn5	NaN	NaN	NaN
Col1a2	NaN	NaN	NaN
Gpnmb	0.236981	-0.109043	NaN
Igfbp2	-0.313405	-0.154700	NaN
Il1b	NaN	NaN	NaN
Jak3	NaN	NaN	NaN
Meg3	NaN	NaN	NaN
P2ry12	NaN	NaN	NaN
Ptprz1	NaN	NaN	NaN
Ttr	NaN	NaN	NaN
Itgax	0.214470	NaN	NaN

# 1.5.1 Is the quality of the gene panel for cluster identification stronger in microglia clusters?

#### 0.4390570399587614

[10]:			#significant genes	is microglia
	Statistic	C2	41	1
	Statistic	CO	30	1
	Statistic	C5	10	1
	Statistic	C4	7	0
	Statistic	C1	6	0
	Statistic	C6	6	0

Statistic	C7	5	0
Statistic	C3	4	1

There is a quite large positive correlation ( $\rho > 0.4$ ) between having a lot of significant genes (for identification against other clusters among the 8) in the gene panel and being a microglia cell cluster, which seems to confirm what we visually observed when comparing non-microglia clusters and microglia clusters in the first heatmap, and in the last two boxplots.

#### 1.5.2 Visualization

```
[11]: def plot_predicted_foldchange(res_df,cluster_order,figsize=(12,12), maxval=0.7):
          plt.figure(figsize=figsize)
          plt.title("Genewise 'fold-change' (one-vs-other clusters) across,
       →model-predicted cell clusters")
          res_df_copy = res_df.copy().dropna(how="all")
          res_df_copy.columns = [x.split(" ")[1] for x in res_df_copy.columns]
          res_df_copy = res_df_copy[res_df_copy.columns[cluster_order]]
          gene_order = res_df_copy.var(axis=1, skipna=True).dropna().sort_values()
          res df copy = res df copy.loc[list(reversed(gene order.index))]
          c_map = copy(cm.get_cmap("coolwarm"))
          c_map.set_bad("lightgray")
          c_map.set_over("k")
          plt.imshow(res_df_copy.values.T, cmap=c_map, interpolation='none',_
       →vmin=-maxval, vmax=maxval)
          plt.xlabel("Genes")
          plt.ylabel("Clusters")
          plt.xticks(range(res_df_copy.shape[0]), res_df_copy.index, rotation=90)
          plt.yticks(range(res_df_copy.shape[1]), res_df_copy.columns)
          plt.colorbar(shrink=0.25, extend="max")
          plt.show()
          plt.close()
```

# [12]: plot\_predicted\_foldchange(res\_df,cluster\_order,figsize=(12,12))

