

# 西安电子科技大学

## 研究生课程考试试题

(答案必须写在答题纸上或在答题卡上填涂)

考试科目: \_\_\_\_\_ 课程编号: \_\_\_\_\_

考试日期: 2016 年 1 月 22 日 考试时间: \_\_\_\_\_ 120

分

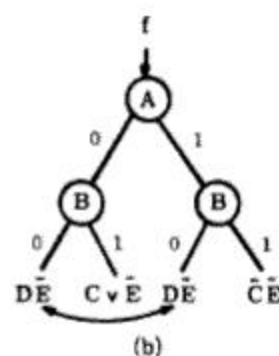
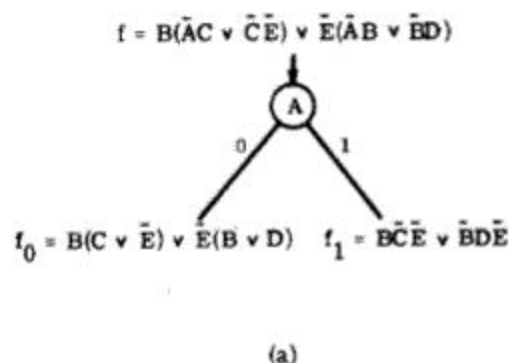
考试方式: (闭卷) 任课教师: \_\_\_\_\_ 班号 \_\_\_\_\_

学生姓名: \_\_\_\_\_ 学 号: \_\_\_\_\_

1. (20 分) Give the diagram deriving from the Shannon expansion formula of function  $f$  (using Binary Decision Diagrams).

$$f = B(\bar{A}C \vee \bar{C}\bar{E}) \vee \bar{E}(\bar{A}B \vee \bar{B}D)$$

### AKERS: BINARY DECISION DIAGRAMS



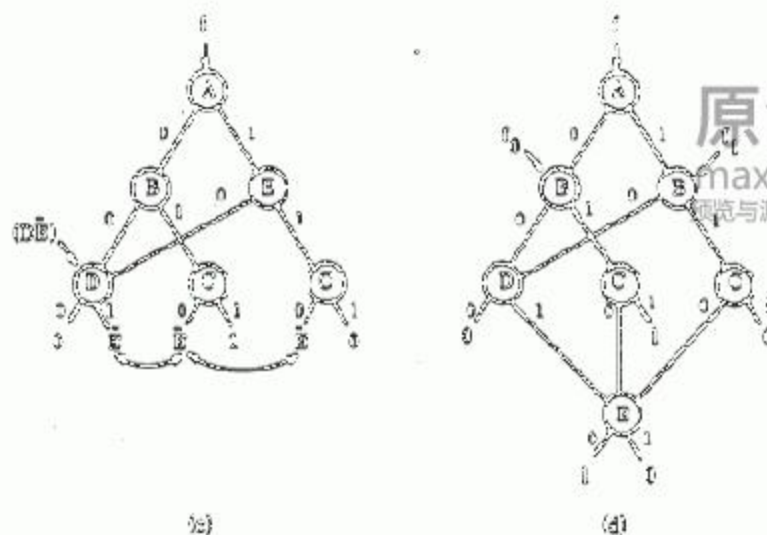
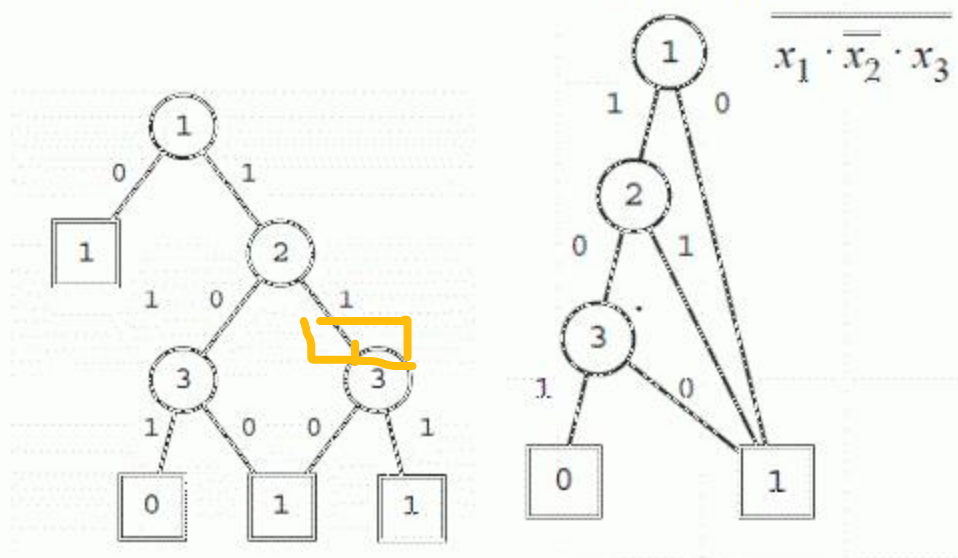


Fig. 5. Deriving a diagram by expansion.

2. (20 分) Transform the following arbitrary function graph into a reduced graph denoting the same function.

After Reduction



3. (15 分) Judge if there are conflicting clauses in the following CNFs. If not, write all feasible assignments.

不行就画个真值表..

$$(1) (x \vee y \vee z)(x \vee \bar{y})(y \vee \bar{z})(z \vee \bar{x})(\bar{x} \vee \bar{y} \vee \bar{z})$$

假设  $x=0$ ,  $(x \vee \bar{y}) \Rightarrow y=0 + (y \vee \bar{z}) \Rightarrow z=0$

$$x=0, y=0, z=0 \Rightarrow (x \vee y \vee z)=0$$

假设  $x=1$ ,  $(z \vee \bar{x}) \Rightarrow z=1 + (y \vee \bar{z}) \Rightarrow y=1$

$$x=1, y=1, z=1, (\bar{x} \vee \bar{y} \vee \bar{z}) \Rightarrow 0$$

所以说, 所有的值都使得这个语句结果为 0, 根据定义, 是冲突语句

$$(2) (\bar{x} \vee y \vee \bar{z})(x \vee \bar{y} \vee z)(x \vee y \vee z)(\bar{x} \vee \bar{y})$$

$$(x \vee \bar{y} \vee z)(x \vee y \vee z) \Rightarrow x \vee z$$

$$(\bar{x} \vee \bar{y})(\bar{x} \vee y \vee \bar{z}) \Rightarrow (\bar{x} \vee \bar{z})$$

所以,  $x, z$  一个为 1

$$a. x=1, z=0, \bar{x} \vee \bar{y} \Rightarrow y=0$$

$$b. x=0, z=1, y \text{ 随便}$$

存在  $x, y, z$  的值, 使得这个语句结果不为 0, 所以不是冲突语句。

$$(3) (\bar{x} \vee y \vee z)(\bar{y} \vee z)(x \vee y)(y \vee z)(\bar{x} \vee y \vee \bar{z})$$

$$(y \vee z)(\bar{x} \vee y \vee \bar{z}) \Rightarrow y \vee z$$

$$(\bar{x} \vee y \vee \bar{z})(\bar{x} \vee y \vee z) \Rightarrow \bar{x} \vee y$$

$$(\bar{y} \vee z)(x \vee y) \Rightarrow x \vee z$$

$$x=0, x \vee z, x \vee y \Rightarrow z=1, y=1$$

$$x=1, \bar{x} \vee y \Rightarrow y=1, \bar{y} \vee z \Rightarrow z=1$$

存在  $x, y, z$  的值, 使得这个语句结果不为 0, 所以不是冲突语句。

4. (10 分) Prove the following equation.

$$(x + y)(y' + z) \equiv (x + y)(y' + z)(x + z)$$

画个真值表

x	y	z	x+y	y' + z	左	x+z	右
0	0	0	0	1	0	0	0
0	0	1	0	1	0	1	0
0	1	0	1	0	0	0	0
0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1
1	0	1	1	1	1	1	1
1	1	0	1	0	0	1	0
1	1	1	1	1	1	1	1

由真值表可知,  $(x + y)(y' + z) \equiv (x + y)(y' + z)(x + z)$

5. (15 分) Translate the following program into logical formula.

Program:

$x, y: \text{natural initially } x = y = 0$	
$\left[ \begin{array}{l} l_0: \text{ if } x = 0 \text{ do} \\ \quad [l_1: y := y + 2] \\ l_2: \text{ while } x = 1 \text{ do} \\ \quad [l_3:] \end{array} \right]$	$\parallel \left[ \begin{array}{l} m_0: x := 1 \\ m_1: \end{array} \right]$
- P <sub>1</sub> -	- P <sub>2</sub> -