

# Problem Set 1: Path simulation

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## 1 Exercise 1

Generate 10000 Wiener process paths in the interval  $[0, 1]$  with 100 equal simulation steps.

Draw the first 10 paths

## 2 Exercise 2

Generate 10000 Wiener process paths in the interval  $[0, 1]$  with 100 equal simulation steps using the cumsum from the numpy package.

Draw the first 10 paths.

## 3 Exercise 3

Generate 10000 paths of geometric Brownian motion (Black-Scholes model) on the interval  $[0, 3]$  (i.e. up to three years) with 12 simulation steps per year with three methods (accurate discretization, Euler scheme and Milstein scheme) based on the same samples from the normal distribution while considering  $r = 0.02$ ,  $\sigma = 0.25$ .

Compare the first paths obtained by each method in one drawing.

## 4 Exercise 4

Generate 10000 CIR process paths in the interval with 252 simulation steps (Euler and Milstein Scheme) based on of the same samples from the normal distribution while considering  $\kappa = 10.0$ ,  $\theta = 0.03$ ,  $r_0 = 0.05$ ,  $\sigma = 0.25$ .

Compare the first paths obtained by each method in one drawing.

## 5 Exercise 5

Generate 10000 paths of two correlated Wiener processes on the interval  $[0, 2]$  with 252 simulation steps per year and 0.9 correlation.

Draw the first paths of both processes in one drawing.

## 6 Exercise 6

Generate 100 paths of three correlated Wiener processes on the interval  $[0, 1]$  with 252 simulation steps per year and correlations  $\rho(W1, W2) = 0.9$ ,  $\rho(W1, W3) = -0.7$ ,  $\rho(W2, W3) = -0.7$ .

Draw the first paths of three processes in one drawing.