



# Theorembeweiserpraktikum

Syntax & Macros

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THEOREM PROVER

# Quick Project Remarks

- prefer `induction` to manual recursion in tactic proofs
- prefer `induction/cases` on an inductive predicate to doing so on one of its parameters
- trust in `simp/simp_all` (in terminal position!)
  - for goals directly solvable by combinations of rewriting, injection, ex falso, ...

# We Have Dates!

- final presentations, part 1: Monday, July 12, 14:00–15:30
- final presentations, part 2: Friday, July 15, 14:00–15:30
- please tell us if your group *can't* make one of these dates!

# Syntax & Macros

```
...
syntax "[Com]" com* "]" : term

macro_rules
| `([Com])                => `(Com.skip)
| `([Com|$c $cs*])        => `(Com.seq `[Com|$c] `[Com|$cs*])
| `([Com|if ($b) { $cts* }]) => `([Com|if ($b) { $cts* } else {}])
...

def example1 := `[Com|
  x := 8;
  y := 10;
  if (x < y) {
    x := x + 1;
  } else {
    y := y + 3;
  }
}]
```

What is even going on here?

# The Lean 4 Frontend Pipeline

- parser:  $\approx$  String  $\rightarrow$  Syntax
- macro expansion: Syntax  $\rightarrow$  MacroM Syntax
  - actually interleaved with elaboration
- elaboration
  - terms: Syntax  $\rightarrow$  TermElabM Expr
  - commands: Syntax  $\rightarrow$  CommandElabM Unit
  - universes: Syntax  $\rightarrow$  TermElabM Level
  - tactics: Syntax  $\rightarrow$  TacticM Unit

Every part of the pipeline is extensible by users

# Notations

```
infixl:65 " + " => HAdd.hAdd -- left-associative
infix:50  " = "  => Eq      -- non-associative
infixr:80  " ^ "  => HPow.hPow -- right-associative
prefix:100 "- "   => Neg.neg
postfix:max "-1"  => Inv.inv
```

# Notations

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```

These are just macros.

```

notation:65 lhs:65 " + " rhs:66 => HAdd.hAdd lhs rhs
notation:50 lhs:51 " = " rhs:51 => Eq lhs rhs
notation:80 lhs:81 " ^ " rhs:80 => HPow.hPow lhs rhs
notation:100 "-" arg:100 => Neg.neg arg
notation:1024 arg:1024 "-1" => Inv.inv arg

```

# Mixfix Notations

notation:  $\max$  "(" e ")"  $\Rightarrow$  e

notation:  $\vdash$  " e " : "  $\tau \Rightarrow$  Typing  $\vdash$  e  $\tau$



# Mixfix Notations

```
notation:max " (" e " )" => e
notation:10  $\Gamma$  "  $\vdash$  " e " : "  $\tau$  => Typing  $\Gamma$  e  $\tau$ 
```

```
notation:50 a:51 " = " b:51 " = " c:51 => a = b  $\wedge$  b = c
#reduce 1 = 2 = 3 -- 1 = 2  $\wedge$  2 = 3
```

Overlapping notations are parsed with a (local) “longest parse” rule

See also <https://leanprover.github.io/lean4/doc/syntax.html>

# Syntax

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```

This is just a macro.

```
syntax:max "(" term ")" : term  
macro_rules ...
```

`term` is a *syntax category*

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`term` is a *syntax category*

```
declare_syntax_cat index
syntax ident : index
syntax ident ":" term : index
syntax term "<=" ident "<" term : index

syntax "Σ" index ", " term : term
```

# More Syntax

```
syntax binderIdent          := ident <|> "_"  
syntax unbracketedExplicitBinders := binderIdent+ (" : " term)?  
  
syntax "begin " tactic,*,? "end" : tactic
```

<https://github.com/leanprover/lean4/blob/master/src/Init/Notation.lean#L40>

# Summary: Parsing

Each syntax category is

- a precedence (Pratt) parser composed of a set of leading and trailing parsers
- with per-parser precedences
- following the longest parse rule

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on the lower level: a combinatoric, non-monadic, lexer-less, memoizing recursive-descent parser

<https://github.com/leanprover/lean4/blob/master/src/Lean/Parser/Basic.lean#L7>

# Macros

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which can also be written as

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which can also be written as

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macro:max "(" e:term ")" : term => `($e)
```

or, in this case

```
macro:max "(" e:term ")" : term => pure e
```

# Quotations

```
`(let $id:ident $binders* $[: $ty?]? := $val; $body)
```

- has type `Syntax` in patterns
- has type `m Syntax` given `MonadQuotation m` in terms
- `id`, `val`, `body` have type `Syntax`
- `binders` has type `Array Syntax`
- `ty?` has type `Option Syntax`

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- `ts` in `$ts,*` has type `SepArray`

`syntax` `foo := ...` introduces a new *antiquotation kind* `$e:foo`

`declare_syntax_cat index` introduces a new antiquotation kind `$e:index` and a new *quotation kind*

```
`(index|...)
```

# Macros

Macros are extensible

```

syntax ident "|" term : index
macro_rules
  | `(_big [$op, $idx] ($i:ident | $p) $F) => `(bigop $idx (Enumerable.elems _) (fun $i:ident => ($i:ident, $op, $p, $F)))
#check  $\sum i \mid \text{myPred } i, i+i$ 
#check  $\prod i \mid \text{myPred } i, i+i$ 
  
```

(*Beyond Notations* supplement, <https://github.com/leanprover/lean4/blob/master/tests/lean/run/bigop.lean>)

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The newest macro is tried first, absent specific priorities

```

macro_rules (priority := high) ...

```

# Examples: Simple Web Server

```
import Webserver

GET / => redirect "/greet/stranger"

GET /greet/{name} => write
  <html>
    <h1>Hello, {name}!</h1>
  </html>

def main : IO Unit := do
  let hIn ← IO.stdin
  let hOut ← IO.stdout
  Webserver.run hIn hOut
```

<https://leanprover.github.io/talks/PLDI20>

```
notation "const" e => fun x => e
```

“Of course”  $e$  may not capture  $x$



# Hygiene

```
notation "const" e => fun x => e
```

“Of course” *e* may not capture *x*

```
macro "myDef" ... : command => do  
  `(def helper := ...)
```

“Of course” *helper* may not be captured from outside

Macro *hygiene*: macro expansion should be *capture-avoiding*

# Hygiene

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notation "const" e => fun x => e
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macro "myDef" ... : command => do  
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```

“Of course” *helper* may not be captured from outside

Macro *hygiene*: macro expansion should be *capture-avoiding*

The same principle applies to tactics: variables generated by `induction` are not visible outside it!

## Example: Tactic Macros

```
macro "bonk" x:ident : tactic => `(induction $x <|> simp_all)

example {as bs cs : List  $\alpha$ } : (as ++ bs) ++ cs = as ++ (bs ++ cs) := by
  bonk as
```

# Example: Tactic Macros

```

syntax "trivial" : tactic

macro_rules | `(tactic| trivial) => `(tactic| assumption)
macro_rules | `(tactic| trivial) => `(tactic| rfl)
macro_rules | `(tactic| trivial) => `(tactic| contradiction)
macro_rules | `(tactic| trivial) => `(tactic| apply True.intro)
macro_rules | `(tactic| trivial) => `(tactic| apply And.intro <;> trivial)

```

```

macro:1 x:tactic " <;> " y:tactic:0 : tactic => `(tactic| focus ($x:tactic; allGoals $y:tactic))

```

```

syntax "repeat " tacticSeq : tactic
macro_rules
| `(tactic| repeat $seq) => `(tactic| try (($seq); repeat $seq))

```

<https://github.com/leanprover/lean4/blob/master/src/Init/Notation.lean>

# Summary: Macros

Macros are syntax-to-syntax translations

- applied iteratively and recursively
- associated with a specific parser and tried in a specific order
- with “well-behaved” (hygienic) name capturing semantics