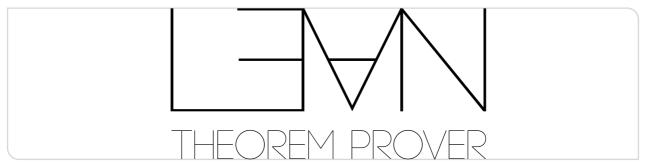




Theorembeweiserpraktikum

Metaprogramming in Lean

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Aesop News



- All our extensions but elimAny upstreamed and enabled by default
- Probability for unsafe now defaults to 50%

Tactics, How Do They Work?



- Tactics modify our proof goals and contexts to incrementally solve a problem.
- How is the final term proof assembled?
- Metavariables: Holes in term expressions which need to be filled.
- Example:

```
example {a b c : \alpha} (h : a = b) (h' : b = c) : a = c := by ...

creates a hole ?m1 : a = c . Using apply Eq.trans will fill this hole with ?m1 := Eq.trans ?m2 ?m3

while creating new holes ?m2 : a = ?m4 and ?m3 : ?m4 = c and ?m4 : \alpha .
```

 Tactics return unsolved metavariables as goals, so after the last goal is closed, no unsolved metavariables remain.

What are Monads?

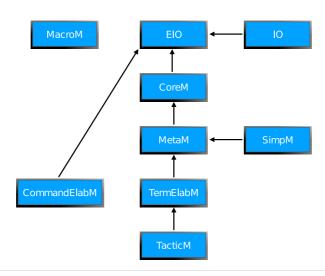


- Lean is a purely functional language (deterministic, no side-effects)!
- How to circumvent this in cases where we really need a state, like when writing tactics? \leadsto Replace functions $\alpha \to \beta$ by functions State $\times \alpha \to$ State $\times \beta$
- Monads are the abstract (and more general) concept behind this.
- Lean implements do notation to work "inside" monads:

```
example (a : StateM Nat \alpha) : StateM Nat \alpha := do let a' \leftarrow a StateT.set 5 return a'
```











- Given a hole ?m1 : (a : α) $\rightarrow \beta$ a we want to
 - ① solve this hole with ?m1 := fun (a : α) => ?m2 and
 - 2 return ?m2 as a new goal, where a : α is in the local context.





```
syntax (name := mvIntro) "mvIntro" : tactic
@[tactic myIntro] def elabMyIntro : Tactic -- `Tactic` is a shortcut for `Syntax → TacticM Unit`
   `(tactic|myIntro) => do -- We match the incoming suntax
   let mVarIds ← getUnsolvedGoals -- We get a List of unsolved goals
   match mVarIds with
    [] => throwNoGoalsToBeSolved -- If there are goals to be solved we throw an error
     mVarId :: otherGoals => -- Now we have the metavariable that we want to work on and "other goals"
     match ← getMVarType mVarId with -- Get the tupe of the metgygriable
       Expr.forallE n h b d => -- Match the type on a `V ...`, otherwise throw an error
       withLocalDecl n d.binderInfo h fun ld => do -- For the new metavar, we add a new declaration
         let bodyMVar ← mkFreshExprSyntheticOpaqueMVar (b.instantiate1 ld) -- Create the new metayar, instantiate `ld`
         let val ← mkLambdaFVars #[1d] bodyMVar -- Build the lambda term which we want to assign to the original metavar
         assignExprMVar mVarId val
         setGoals (bodyMVar.mvarId! :: otherGoals)
      _ => throwTacticEx `myIntro mVarId "tactic not applicable"
  => throwUnsupportedSyntax
```