

# Applications and Examples

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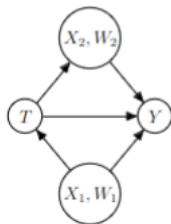
IPL

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# Common Driver example



# Double Machine Learning



$$Y = \theta(X) \cdot T + g(X, W). \quad (1)$$

The parameter  $\theta$  describes the direct effect of some variable  $T$  on the outcome variable  $Y$ .

$$Y = \theta(X) \cdot T + g(X, W) + \epsilon \quad \mathbb{E}[\epsilon|X, W] = 0 \quad (2)$$

$$T = m(X, W) + \eta \quad \mathbb{E}[\eta|X, W] = 0 \quad (3)$$

$$\mathbb{E}[\eta \cdot \epsilon|X, W] = 0. \quad (4)$$

We proceed according to the partialling out method of the double machine learning framework Chernozhukov et al. [2018]:

1. Fit an estimator  $\mathbb{E}[Y|X, W]$  of  $Y$  on  $X$  and  $W$ ,
2. fit an estimator  $\mathbb{E}[T|X, W]$  of  $T$  on  $X$  and  $W$ ,
3. compute residuals over  $\tilde{Y} = Y - \mathbb{E}[Y|X, W]$  and  $\tilde{T} = T - \mathbb{E}[T|X, W]$  and
4. estimate  $\hat{\theta} = \arg \min_{\theta \in \Theta} \sum_i (\tilde{Y} - \theta(X) \cdot \tilde{T})^2$ .

# The Q10 model

$$R_{eco}(X, T) = R_b(X, T) \cdot Q_{10}^{(T - T_{ref})/10}, \quad (5)$$

Following the example of Reichstein et al. [2022], we used data from the EC tower in Neustift, Austria, from 2003 to 2007 of the FLUXNET2015 dataset and generated the data similarly.

## Synthetic data

$$RECO_{syn} = Rb_{syn} \cdot Q_{10}^{0.1 \cdot (T - 15)}, \quad (6)$$

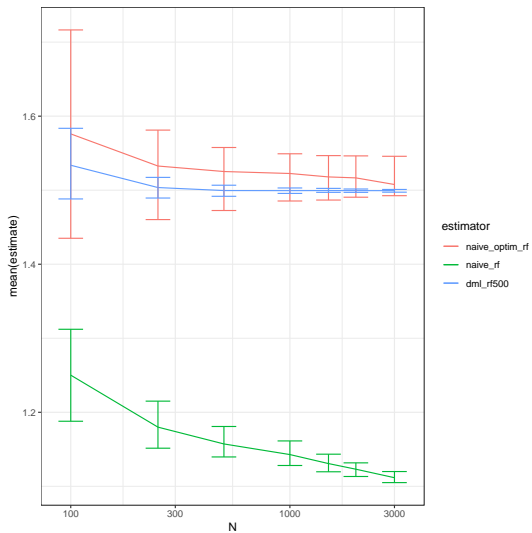
$$Rb_{syn} = 0.75 \cdot (\tilde{R}_b^{syn} - \min(\tilde{R}_b^{syn}) + 0.1 \cdot \pi), \quad (7)$$

$$\tilde{R}_b^{syn} = 0.01 \cdot SWPOT_{sm} - 0.005 \cdot SWPOT_{smdiff}, \quad (8)$$

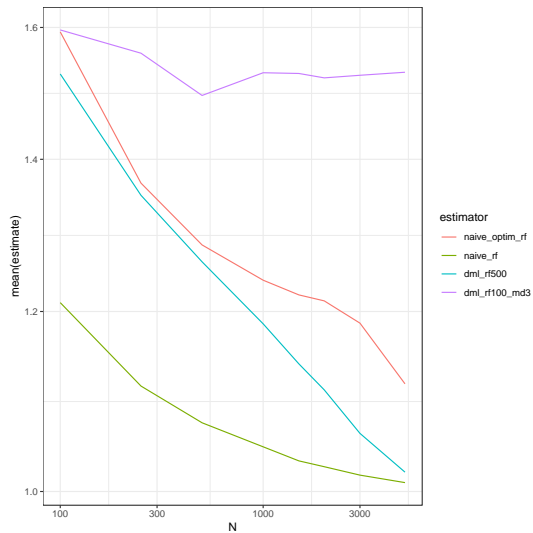
- ▶  $Rb^{syn}$  describes the base respiration
- ▶ The smooth incoming potential radiation  $SWPOT_{sm}$  and its smoothed difference quotient  $SWPOT_{smdiff}$  are computed by averaging moving windows of 10 days over the incoming potential radiation  $SW_{POT}$ .
- ▶ The  $Q_{10}$  temperature coefficient is set to 1.5.

Ecosystem respiration is not directly observed at flux towers during the day. It is a latent flux that can only be measured under controlled conditions such as a sealed chamber. At night, however, we assume *GPP* to be zero as there is no photosynthesis occurring, and all carbon flow stems from respiration. From all measured data, the ones that do not fulfill a certain quality criterion are filtered out and gap filled. We will work with measured data only. Only about 10% of the nighttime data is observed. Thus, we estimate  $Q_{10}$  on 4331 data points. As predictors we will use the day of the year to account for seasonality, vapor pressure deficit *VPD*, and soil water content *SWC*.

# Bootstrapped results for synthetic data



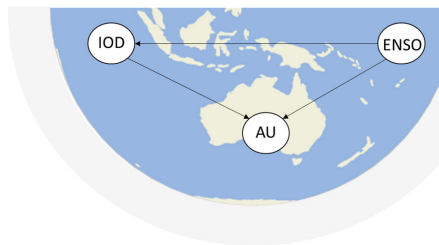
# Bootstrapped results for real data





# ENSO Effects on Spring Precipitation in Australia

- ▶ Effect of El Niño Southern Oscillation (ENSO) on Australian precipitation (AU) during spring, and the possible mediation of the Indian Ocean Dipole (IOD) [Kretschmer et al., 2021]
- ▶ monthly NCEP reanalyses covering 1949–2019
- ▶ ENSO (Niño, neutral, Niña), IOD into positive (+), neutral (0) and negative (-) phases; and AU into above (high) and below (low) average values



Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters. *The Econometrics Journal*, 21(1):C1–C68, 01 2018. ISSN 1368-4221. doi: 10.1111/ectj.12097. URL <https://doi.org/10.1111/ectj.12097>.

M. Kretschmer, S. V. Adams, A. Arribas, R. Prudden, N. Robinson, E. Saggioro, and T. G. Shepherd. Quantifying causal pathways of teleconnections. *Bulletin of the American Meteorological Society*, 102(12):"E2247–E2263, 2021.

M. Reichstein, B. Ahrens, B. Kraft, G. Camps-Valls, N. Carvalhais, F. Gans, P. Gentine, and A. Winkler. Combining system modeling and machine learning into hybrid ecosystem modeling. In *Knowledge-Guided Machine Learning*. 2022. doi: <https://doi.org/10.1201/9781003143376-14>.