



# AAE2004 Introduction to Aviation Systems AAE Design of Path Planning Algorithm for Aircraft Operation

Path Planning Algorithm and Python Robotics

Dr Li-Ta Hsu and Dr Kam Hung NG
Assisted by

Miss Hiu Yi HO (Queenie), Miss Yan Tung LEUNG (Nikki)

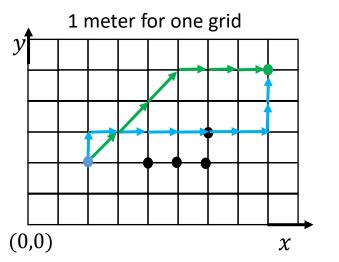


## A\* Path Planning Algorithm



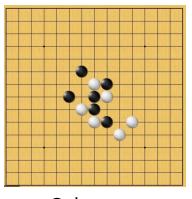


#### Definition of Path Planning



- Start node
- Goal node
- Route 1
- Route 2

- •Node All potential position you can go across with a unique position (x, y)
- •Search Space A collection of nodes, like all board positions of a board game.



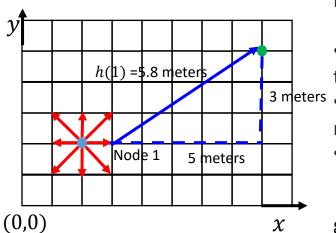
Gobang

•Objective of path planning— Find the shortest routes with smallest cost from start node to goal node.

How to find the shortest route!







- Start node
- Goal node

1 meter for one grid

Definition of cost:

$$f(x,y) = g(x,y) + h(x,y)$$

- •g(x,y) this represents the **exact cost** of the path from the **starting node** to node (x,y)
- •h(x,y) this represents the heuristic **estimated cost** from node (x,y) to the goal node.
  - f(x, y) —cost of the neighboring node (x, y)

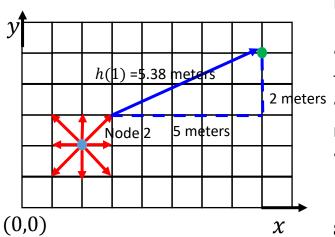
8 neighboring node and the cost can be calculated as follows!

Node 1:

$$f(3,2) = g(3,2) + h(3,2) = 6.8$$
 meters  
with  $g(3,2) = 1$  meter and  $h(3,2) = 5.8$  meters







- Start node
- Goal node

1 meter for one grid

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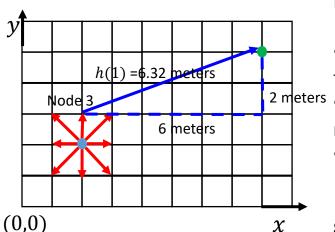
8 neighboring node and the cost can be calculated as follows!

Node 2:

$$f(3,3) = g(3,3) + h(3,3) = 6.79$$
 meters  
with  $g(3,3) = \sqrt{2}$  meter and  $h(3,3) = 5.38$  meters







Start node

Goal node

1 meter for one grid

Definition of cost:

$$f(x,y) = g(x,y) + h(x,y)$$

- •g(x,y) this represents the **exact cost** of the path from the **starting node** to node (x,y)
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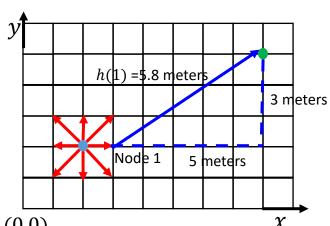
Node 3:

$$f(2,3) = g(2,3) + h(2,3) = 7.32$$
 meters  
with  $g(2,3) = 1$  meter and  $h(2,3) = 6.32$  meters

Similar cost calculation method for other 5 nodes







Definition of cost:

$$f(x,y) = g(x,y) + h(x,y)$$

- •g(x,y) this represents the **exact cost** of the path from the **starting node** to node (x,y)
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  - f(x, y) —cost of the neighboring node (x, y)

(0,0)

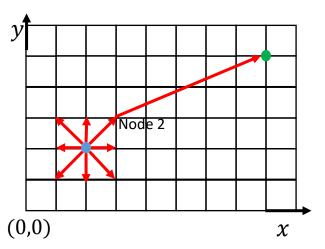
- Start node
- Goal node

1 meter for one grid

_	λ			_					
	Node $(x, y)$	Node 1 $(x, y)$	Node 2 ( <i>x</i> , <i>y</i> )	Node 3 ( <i>x</i> , <i>y</i> )	Node 4 ( <i>x</i> , <i>y</i> )	Node 5 ( <i>x</i> , <i>y</i> )	Node 6 ( <i>x</i> , <i>y</i> )	Node 7 ( <i>x</i> , <i>y</i> )	Node 8 ( <i>x</i> , <i>y</i> )
ŀ		(x,y)	L(x,y)	J(x,y)	$\tau(x,y)$	J(x,y)	$O(\lambda, y)$	$(\lambda, y)$	$\sigma(x,y)$
	g(x,y)	1	1.414	1	1.414	1	1.414	1	1.414
	h(x,y)	5.8	5.38	6.32	7.28	7.62	8.06	7.21	6.40
	f(x,y)	6.8	6.79	7.32	8.694	8.62	9.474	8.21	7.814







- Start node
- Goal node

1 meter for one grid

Definition of cost:

$$f(x,y) = g(x,y) + h(x,y)$$

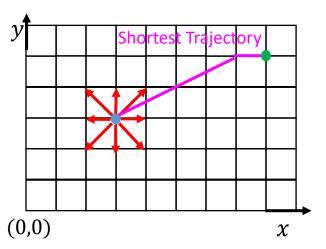
- •g(x,y) this represents the **exact cost** of the path from the **starting node** to node (x,y)
- •h(x,y) this represents the heuristic **estimated cost** from node (x,y) to the goal node.
- •f(x,y) —cost of the neighboring node (x,y)

8 neighboring node and the cost can be calculated as follows!

Node 2 leads to smallest cost



#### Calculate the cost of node



- Start node
- Goal node

1 meter for one grid

Definition of cost:

$$f(x,y) = g(x,y) + h(x,y)$$

- •g(x,y) this represents the **exact cost** of the path from the **starting node** to node (x,y)
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8 neighboring node and the cost can be calculated as follows!

Search from the neighbouring node with smallest cost until reaching the goal!

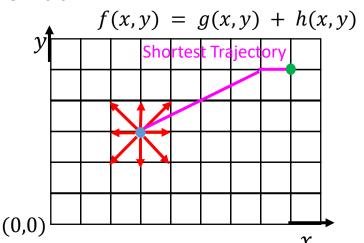




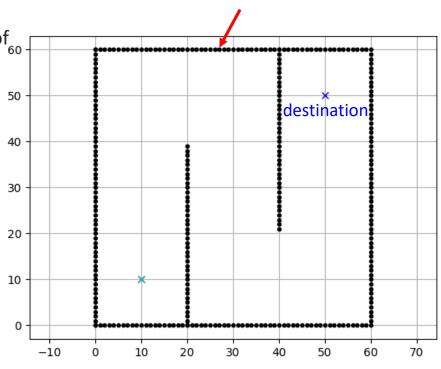
## A star method example

Each time A\* enters a node, it calculates the cost, f(n) (n being the neighboring node), to travel to all of  $_{60}$ the neighboring nodes, and then enters the node with the lowest value of f(n).

These values we calculate using the following formula:





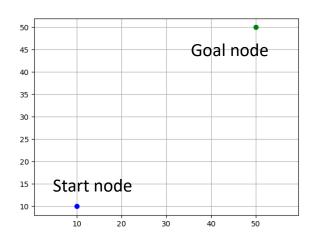


Source: PythonRobotics





## Code: set up start and goal node



Set up the start and goal nodes using the code

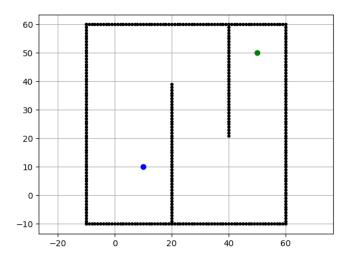
```
# start and goal position
sx = 10.0 # [m]
sy = 10.0 # [m]
gx = 50.0 # [m]
gy = 50.0 # [m]
grid_size = 2 # [m]
```

- Start node
- Goal node





#### Code: set up obstacle



- Start node
- Goal node

Obstacle (wall)

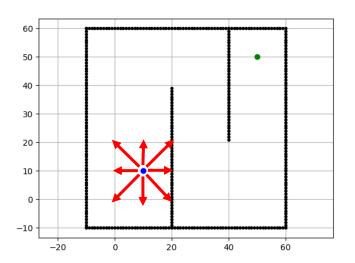
#### Set up the obstacle using the code

```
# set obstacle positions
ox, oy = [], []
for i in range(-10, 60): # draw the button border
   ox.append(i)
   oy.append(-10.0)
for i in range(-10, 60):
    ox.append(60.0)
   oy.append(i)
for i in range(-10, 61):
    ox.append(i)
   oy.append(60.0)
for i in range(-10, 61):
   ox.append(-10.0)
   oy.append(i)
for i in range(-10, 40):
    ox.append(20.0)
   oy.append(i)
for i in range(0, 40):
   ox.append(40.0)
   oy.append(60.0 - i)
```





## Code: neighboring node search



#### neighboring node search

```
get_neighbouring_node(): # the cost of the surrounding 8 points
motion = [[1, 0, 1],
          [0, 1, 1],
          [-1, 0, 1],
          [0, -1, 1],
          [-1, -1, math.sqrt(2)],
          [-1, 1, math.sqrt(2)],
          [1, -1, math.sqrt(2)],
          [1, 1, math.sqrt(2)]]
return motion
```

- Start node
- Goal node

Obstacle (wall)





#### Code: cost calculation

#### Heuristic cost g(x, y) calculation

```
def calc_heuristic(n1, n2):
    w = 1.0  # weight of heuristic
    d = w * math.hypot(n1.x - n2.x, n1.y - n2.y)
    return d
```

#### exact cost g(x, y) calculation





## Code: calculation of final path

```
def calc_final_path(self, goal_node, closed_set):
    # generate final course
    rx, ry = [self.calc_grid_position(goal_node.x, self.min_x)], [
        self.calc grid position(goal node.y, self.min y)] # save the goal node as the first point
    parent index = goal node.parent index
    while parent index != -1:
        n = closed_set[parent_index]
        rx.append(self.calc grid position(n.x, self.min x))
        ry.append(self.calc grid position(n.y, self.min y))
                                                                         50
        parent index = n.parent index
                                                                         40
    return rx, ry
                                                                         30
                                                                         20
                                                                         10
                                                                        -10
                                                                             -20
                                                                                                20
```