Writing a qi function

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1 Introduction

For any Zelig module, the qi function is ultimately the most important piece of code that must be written; it describes the actual process which simulates the quantities of interest. Because of the nature of this process - and the gamut of statistical packages and their underlying statistical model - it is rare that the simulation process can be generalized for arbitrary fitted models. Despite this, it is possible to break down the simulation process into smaller steps.

2 Notable Features of qi Function

The typical qi function has several basic procedures:

- 1. Call the param function: This is entirely optional but sometimes important for the clarity of your algorithm. This step typically consists of taking random draws from the fitted model's underlying probability distribution.
- 2. Compute the Quantity of Interest: Depending on your model, there are several ways to compute necessary quantities of interest. Typical methods for computing quantities of interest include:
 - (a) Using the 'predict' method of your given linear model.
 - (b) Using the sample provided by 'param' to generate simulations of the $Quantities\ of\ Interest.$
 - (c) Using a Maximum-likelihood estimate on the fitted model.
- 3. Create a list of titles for your Quantities of Interest:
- 4. Generate the Quantity of Interest Object: Finally, with the computed Quantities of Interest, you must

3 Basic Layout of a qi Function

Now with the general outline of a qi function defined, it is important to discuss the expected procedures and specifics of implementation.

3.1 The Function's Signature

The qi function's signature accepts 4 parameters:

- **@z:** An object of type "zelig". This wraps the fitted model in the slot "result".
- **@x:** An object of type "setx". This object is used to compute important coefficients, parameters, and features of the data frame passed to the function call.
- **@x1:** Also an object of type "setx". This object is used in a similar fashion, however its presence allows a variety of quantities of interest to be computed. Notably, this is a necessary parameter to compute first-differences.

@num: The number of simulations to compute

3.2 Code Example: qi Function Signature

```
qi.your_model_name <- function(z, x=NULL, x1=NULL, num=1000) {
# start typing your code here
# ...
# ...</pre>
```

Note: In the above example, the function name "qi.your_model_name" is merely a placeholder. In order to register a qi function with zelig, the developer must follow the naming convention qi.your mode name, where your_model_name is the name of the developer's module. For example, if a developer titled his or her zelig module "logit", then the corresponding qi function is titled "qi.logit".

3.3 Call to the param Function

This step is common in many zelig models, however, its existence - though highly recommended - is purely optional. Typically, during this step, samples are taken from the distribution governing the statistical model. This is then used to simulate values for the *quantities of interest*.

3.4 The Function Body

The function body of qi function varies largely from model to model. As a result, it is impossible to create general guidelines to simulate quantities of interest - or even determine what the quantity of interest is. Typical methods for computing quantities of interest include:

- Implementing sampling algorithms based on the underlying fitted model, or
- "Predicting" a large number of values from the fitted model

3.5 The Return Value

In order for Zelig to process the simulations, they must be returned in one of several formats:

```
• list(
    "TITLE OF QI 1" = val1,
    "TITLE OF QI 2" = val2,
    # any number of title-val pairs
    # ...
    "TITLE OF QI N" = val.n
)
• make.qi(
    titles = list(title1, title2),
    stats = list(val1, val2)
)
```

In the above example, val1, val2 are data.frames, matrices, or lists representing the simulations of the quantities of interests, and title1, title2 - and any number of titles - are character-strings that will act as human-readable descriptions of the quantities of interest. Once results are returned in this format, Zelig will convert the results into a machine-readable format and summarize the simulations into a comprehensible format.

NOTE: Because of its readability, it is suggested that the first method is used when returning *quantities of interest*.

4 Example qi function (qi.logit.R)

```
qi.ls <- function(z, x=NULL, x1=NULL, num=1000) {
  # error-catching
  if (missing(x))
    stop("x cannot be missing while computing the 'ls' model")
  # get 'parameters'
  # In this example, this amounts to sampling
  # a multivariate normal distribution
  coefs <- param(z, num=num)</pre>
  # compute expected values using X
  ev <- coefs %*% t(x$matrix)</pre>
  ev1 <- NA
  fd <- NA
  # if x1 exists:
  # compute expected values using X1
  # compute finite differences
  if (!is.null(x1)) {
    ev1 <- coefs %*% t(x1$matrix)</pre>
    fd <- ev1 - ev
  }
  # return
  list("Expected Value: E(Y|X)" = ev,
       "Expected Value (of X1): E(Y|X1)" = ev1,
       "First Difference in Expected Values: E(Y|X1) - E(Y|X)" = fd
}
```

5 The qi API

 $In\ Development$