## Writing a qi function

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#### 1 Introduction

For any Zelig module, the qi function is ultimately the most important piece of code that must be written; it describes the actual process which simulates the quantities of interest. Because of the nature of this process - and the gamut of statistical packages and their underlying statistical model - it is rare that the simulation process can be generalized for arbitrary fitted models. Despite this, it is possible to break down the simulation process into smaller steps.

### 2 Notable Features of qi Function

The typical qi function has several basic procedures:

- 1. Call the param function: This is entirely optional but sometimes important for the clarity of your algorithm. This step typically consists of taking random draws from the fitted model's underlying probability distribution.
- 2. Compute the Quantity of Interest: Depending on your model, there are several ways to compute necessary quantities of interest. Typical methods for computing quantities of interest include:
  - (a) Using the 'predict' method of your given linear model.
  - (b) Using the sample provided by 'param' to generate simulations of the  $\it Quantities~of~Interest.$
  - (c) Using a Maximum-likelihood estimate on the fitted model.
- 3. Create a list of titles for your Quantities of Interest:
- 4. Generate the Quantity of Interest Object: Finally, with the computed Quantities of Interest, you must

## 3 Basic Layout of a qi Function

Now with the general outline of a qi function defined, it is important to discuss the expected procedures and specifics of implementation.

#### 3.1 The Function's Signature

The qi function's signature accepts 4 parameters:

- **@z:** An object of type "zelig". This wraps the fitted model in the slot "result".
- **@x:** An object of type "setx". This object is used to compute important coefficients, parameters, and features of the data frame passed to the function call.
- **@x1:** Also an object of type "setx". This object is used in a similar fashion, however its presence allows a variety of quantities of interest to be computed. Notably, this is a necessary parameter to compute first-differences.

**@num:** The number of simulations to compute

#### 3.2 Code Example: qi Function Signature

```
qi.your_model_name <- function(z, x=NULL, x1=NULL, num=1000) {
# start typing your code here
# ...
# ...</pre>
```

Note: In the above example, the function name "qi.your\_model\_name" is merely a placeholder. In order to register a qi function with zelig, the developer must follow the naming convention qi.your mode name, where your\_model\_name is the name of the developer's module. For example, if a developer titled his or her zelig module "logit", then the corresponding qi function is titled "qi.logit".

#### 3.3 Call to the param Function

This step is common in many zelig models, however, its existence - though highly recommended - is purely optional. Typically, during this step, samples are taken from the distribution governing the statistical model. This is then used to simulate values for the *quantities of interest*.

#### 3.4 The Function Body

The function body of qi function varies largely from model to model. As a result, it is impossible to create general guidelines to simulate quantities of interest - or even determine what the quantity of interest is. Typical methods for computing quantities of interest include:

- Implementing sampling algorithms based on the underlying fitted model, or
- "Predicting" a large number of values from the fitted model

#### 3.5 The Return Value

In order for Zelig to process the simulations, they must be returned in one of several formats:

```
• list(
    "TITLE OF QI 1" = val1,
    "TITLE OF QI 2" = val2,
    # any number of title-val pairs
    # ...
    "TITLE OF QI N" = val.n
)
• make.qi(
    titles = list(title1, title2),
    stats = list(val1, val2)
)
```

In the above example, val1, val2 are data.frames, matrices, or lists representing the simulations of the quantities of interests, and title1, title2 - and any number of titles - are character-strings that will act as human-readable descriptions of the quantities of interest. Once results are returned in this format, Zelig will convert the results into a machine-readable format and summarize the simulations into a comprehensible format.

NOTE: Because of its readability, it is suggested that the first method is used when returning *quantities of interest*.

## 4 Example qi function (qi.logit.R)

```
qi.ls <- function(z, x=NULL, x1=NULL, num=1000) {
  # error-catching
  if (missing(x))
    stop("x cannot be missing while computing the 'ls' model")
  # get 'parameters'
  # In this example, this amounts to sampling
  # a multivariate normal distribution
  coefs <- param(z, num=num)</pre>
  # compute expected values using X
  ev <- coefs %*% t(x$matrix)</pre>
  ev1 <- NA
  fd <- NA
  # if x1 exists:
  # compute expected values using X1
  # compute finite differences
  if (!is.null(x1)) {
    ev1 <- coefs %*% t(x1$matrix)</pre>
    fd <- ev1 - ev
  }
  # return
  list("Expected Value: E(Y|X)" = ev,
       "Expected Value (of X1): E(Y|X1)" = ev1,
       "First Difference in Expected Values: E(Y|X1) - E(Y|X)" = fd
}
```

# 5 The qi API

 $In\ Development$