1 logit.net: Network Logistic Regression for Dichotomous Proximity Matrix Dependent Variables

Use network logistic regression analysis for a dependent variable that is a binary valued proximity matrix (a.k.a. sociomatricies, adjacency matrices, or matrix representations of directed graphs).

1.0.1 Syntax

```
> z.out <- zelig(y ~ x1 + x2, model = "logit.net", data = mydata)
> x.out <- setx(z.out)
> s.out <- sim(z.out, x = x.out)</pre>
```

1.0.2 Examples

1. Basic Example

Load the sample data (see **?friendship** for details on the structure of the network dataframe):

> data(friendship)

Estimate model:

```
> z.out <- zelig(friends ~ advice + prestige + perpower, model = "logit.net",
+ data = friendship)
> summary(z.out)
```

Setting values for the explanatory variables to their default values:

```
> x.out <- setx(z.out)</pre>
```

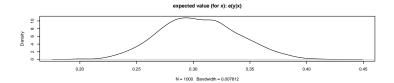
Simulating quantities of interest from the posterior distribution.

```
> s.out <- sim(z.out, x = x.out)
> summary(s.out)
> plot(s.out)
```

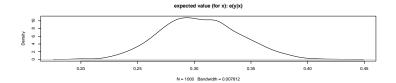
2. Simulating First Differences

Estimating the risk difference (and risk ratio) between low personal power (25th percentile) and high personal power (75th percentile) while all the other variables are held at their default values.

```
> x.high <- setx(z.out, perpower = quantile(friendship$perpower,
+     prob = 0.75))
> x.low <- setx(z.out, perpower = quantile(friendship$perpower,
+     prob = 0.25))</pre>
```



```
> s.out2 <- sim(z.out, x = x.high, x1 = x.low)
> summary(s.out2)
> plot(s.out2)
```



1.0.3 Model

The logit.net model performs a logistic regression of the proximity matrix \mathbf{Y} , a $m \times m$ matrix representing network ties, on a set of proximity matrices \mathbf{X} . This network regression model is directly analogous to standard logistic regression element-wise on the appropriately vectorized matrices. Proximity matrices are vectorized by creating Y, a $m^2 \times 1$ vector to represent the proximity matrix. The vectorization which produces the Y vector from the \mathbf{Y} matrix is performed by simple row-concatenation of \mathbf{Y} . For example, if \mathbf{Y} is a 15×15 matrix, the $\mathbf{Y}_{1,1}$ element is the first element of Y, and the $\mathbf{Y}_{2,1}$ element is the second element of Y and so on. Once the input matrices are vectorized, standard logistic regression is performed.

Let Y_i be the binary dependent variable, produced by vectorizing a binary proximity matrix, for observation i which takes the value of either 0 or 1.

• The stochastic component is given by

$$Y_i \sim \text{Bernoulli}(y_i|\pi_i)$$

= $\pi_i^{y_i} (1 - \pi_i)^{1-y_i}$

where $\pi_i = \Pr(Y_i = 1)$.

• The *systematic component* is given by:

$$\pi_i = \frac{1}{1 + \exp(-x_i \beta)}.$$

where x_i is the vector of k covariates for observation i and β is the vector of coefficients.

1.0.4 Quantities of Interest

The quantities of interest for the network logistic regression are the same as those for the standard logistic regression.

 The expected values (qi\$ev) for the logit.net model are simulations of the predicted probability of a success:

$$E(Y) = \pi_i = \frac{1}{1 + \exp(-x_i \beta)},$$

given draws of β from its sampling distribution.

- The predicted values (qi\$pr) are draws from the Binomial distribution with mean equal to the simulated expected value π_i .
- The first difference (qi\$fd) for the network logit model is defined as

$$FD = \Pr(Y = 1|x_1) - \Pr(Y = 1|x)$$

1.0.5 Output Values

The output of each Zelig command contains useful information which you may view. For example, you run z.out <- zelig(y ~ x, model = "logit.net", data), then you may examine the available information in z.out by using names(z.out), see the coefficients by using z.out\$coefficients, and a default summary of information through summary(z.out). Other elements available through the \$ operator are listed below.

- From the zelig() output stored in z.out, you may extract:
 - coefficients: parameter estimates for the explanatory variables.
 - fitted.values: the vector of fitted values for the explanatory variables.

- residuals: the working residuals in the final iteration of the IWLS fit
- linear.predictors: the vector of $x_i\beta$.
- aic: Akaikeś Information Criterion (minus twice the maximized loglikelihood plus twice the number of coefficients).
- bic: the Bayesian Information Criterion (minus twice the maximized log-likelihood plus the number of coefficients times $\log n$).
- df.residual: the residual degrees of freedom.
- df.null: the residual degrees of freedom for the null model.
- zelig.data: the input data frame if save.data = TRUE
- From summary(z.out)(as well as from zelig()), you may extract:
 - mod.coefficients: the parameter estimates with their associated standard errors, p-values, and t statistics.
 - cov.scaled: a $k \times k$ matrix of scaled covariances.
 - cov.unscaled: a $k \times k$ matrix of unscaled covariances.
- From the sim() output stored in s.out, you may extract:
 - qi\$ev: the simulated expected probabilities for the specified values of x.
 - qi\$pr: the simulated predicted values for the specified values of x.
 - qi\$fd: the simulated first differences in the expected probabilities simulated from x and x1.

How to Cite Network Log-Log Regeression

Olivia Lau Matt Owen, Kosuke Imai and Gary King. logit.net: Logistic Regression for Dichotomous Dependent Variables, 2011

How to Cite the Zelig Software Package

To cite Zelig as a whole, please reference these two sources:

Kosuke Imai, Gary King, and Olivia Lau. 2007. "Zelig: Everyone's Statistical Software," http://GKing.harvard.edu/zelig.

Imai, Kosuke, Gary King, and Olivia Lau. (2008). "Toward A Common Framework for Statistical Analysis and Development." Journal of Computational and Graphical Statistics, Vol. 17, No. 4 (December), pp. 892-913.

See also

The network logistic regression is part of the netglm package by Skyler J. Cranmer and is built using some of the functionality of the sna package by Carter T. Butts [1].In addition, advanced users may wish to refer to help(netgamma). Sample data are fictional.

References

- [1] C.T. Butts and K.M. Carley. Multivariate methods for interstructural analysis. Technical report, CASOS working paper, Carnegie Mellon University, 2001.
- [2] Olivia Lau Matt Owen, Kosuke Imai and Gary King. logit.net: Logistic Regression for Dichotomous Dependent Variables, 2011.