

IQ Collaboratory III Empirical Dust Attenuation Models: Taking Hydrodynamical Simulations with a Grain of Dust

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ABSTRACT

We present the Framework for Attenuation by Dust Empirically (FADE) for applying dust attenuation to galaxies from theoretical models. FADE provides a flexible prescription for assigning realistic dust attenuation to simulated galaxies related to their physical properties (M_* , SSFR) and using the Noll et al. (2009) attenuation curve parameterization. Using the FADE, we forward model synthetic observations for a $M_r < -20$ complete galaxy sample for three state-of-the-art large-scale cosmological hydrodynamical simulations: SIMBA, IllustrisTNG, and EAGLE. We then compare the optical and UV color-magnitude relations, $(g-r) - M_r$ and $(FUV - NUV) - M_r$, for the forward modeled simulations to SDSS observations using likelihood-free inference. As expected, for all three of the simulations dust attenuation is necessary to match the observations. We find that we can accurately reproduce the color-magnitude relations of the observational sample for TNG and EAGLE. For SIMBA, we struggle to reproduce observations due to an overprediction of low-mass galaxies with high star-formation rates. Examining the attenuation curves predicted by FADE for TNG and EAGLE, we find good agreement with observed attenuation-slope relations and attenuation curves of star-forming galaxies. Additionally, FADE provides unprecedented predictions for the attenuation curves of quiescent galaxies, which are challenging to measure observationally. To match observations, simulated quiescent galaxies require significant UV and optical attenuation but with much shallower slopes than star-forming galaxies. Overall, we find that more massive galaxies in the simulations require higher dust attenuation, while galaxies with higher specific star formation rates have steeper attenuation curves. In addition to improving our understanding of dust in galaxies, our results underscore the advantages of FADE and the forward modeling approach.

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1. INTRODUCTION

Dust in the interstellar medium of a galaxy can dramatically impact its spectral energy distribution (SED). The combined effect of dust on a galaxy’s SED is typically described using an attenuation curve, $A(\lambda)$, which has now been broadly characterized by observations. In the UV, attenuation curves steeply rise due to absorptions by small grains. At 2175\AA , in the near-UV (NUV), there is an absorption bump referred to as the “UV dust bump”. At longer optical wavelengths, the curves take on a power-law shape. Finally, dust reemits the attenuated light in the optical and UV in the infrared (for an overview see Calzetti 2001; Draine 2003; Galliano et al. 2018). By impacting the SED, dust also affects the physical properties that are inferred from the SED, such as star formation rate (SFR), stellar mass (M_*), or stellar ages (see reviews by Walcher et al. 2011; Conroy 2013). Assumptions on dust attenuation can dramatically vary these properties (Kriek & Conroy 2013; Reddy et al. 2015; Salim et al. 2016; Salim & Narayanan 2020). Since these properties are the building blocks to our understanding of galaxies and how they evolve, a better understanding of dust not only provides insights into dust, but also underpins all galaxy studies.

To better understand dust in galaxies, many observational works have examined trends between dust attenuation and galaxy properties. For example, UV and optical attenuation are found to correlate with M_* , SFR, and metallicity in star-forming galaxies (Garn & Best 2010; Battisti et al. 2016). The slope of the attenuation curves in star-forming galaxies also correlate with galaxy properties, such as M_* , specific SFR (SSFR), metallicity, and axial ratio (Wild et al. 2011; Battisti et al. 2017). Recently, Salim et al. (2018) argue that these correlations stem from the underlying “attenuation-slope relation”, a trend between the amplitude of attenuation and slope. Despite the progress, there is still no clear consensus on the connection between attenuation curves and galaxy properties. Also, studies so far have focused solely on star-forming galaxies and little is known about dust attenuation in quiescent galaxies. Furthermore, galaxy properties and dust attenuation measured from galaxy SEDs are subject to variations, inconsistencies, and biases of different methodologies, which can be significant even for the same observations (*e.g.* Speagle et al. 2014; Katsianis et al. 2020). SED fitting can also impose undesirable priors on derived galaxy properties (Carnall et al. 2018; Leja et al. 2019) and suffer from parameter degeneracies that are poorly understood.

Significant progress has also been made in theoretically modeling dust. Simulations can now model the radiative transfer of stellar light through a dusty ISM for a wide range of configurations: from simple slab-like dust geometries (*e.g.* Witt & Gordon 1996, 2000; Seon & Draine 2016) to 3D hydrodynamic simulations of entire galaxies (*e.g.* Jonsson 2006; Rocha et al. 2008; Hayward & Smith 2015; Natale et al. 2015; Hou et al. 2017). Radiative transfer models have even been applied to cosmological hydrodynamical simulations (*e.g.* Camps & Baes 2015; Narayanan et al. 2018; Trayford et al. 2020). Dust has also been examined in a cosmological context using semi-analytic models (SAMs; *e.g.* Granato et al. 2000; Fontanot et al. 2009; Wilkins et al. 2012; Gonzalez-Perez et al. 2013; Popping et al. 2017). Yet there are still major limitations in modeling dust. Dust models in cosmological simulations currently do not reproduce the redshift evolution of dust properties (Somerville et al. 2012; Yung et al. 2019; Vogelsberger et al. 2020). Also, radiative transfer models produce attenuation-slope relations that are significantly steeper than observations. Many models also require significant hand-

tuning (*e.g.* propagating rays/photons into particular cells) and make assumptions on the underlying dust grain models (see Steinacker et al. 2013, for a review).

We take a different approach from the observational and theoretical works above — *we investigate dust attenuation using a forward modeling approach to compare simulations to observations*. Our “forward model” starts with three major large-scale hydrodynamical simulations: EAGLE, IllustrisTNG, and SIMBA. We use their outputs (*e.g.* star formation history) to build SEDs for each simulated galaxy. We then apply dust attenuation to all the SEDs using an Empirical Dust Attenuation framework, which we describe shortly. Finally, we apply a realistic noise model and survey selection function on the attenuated SEDs and construct synthetic photometric observations. Afterwards, we compare the synthetic observations from the forward model to actual observations. The comparisons are made in observational space, so they are not impacted by the inconsistencies of observational methods in measuring galaxy properties. Furthermore, since the forward models can directly include the selection functions and observational systematic effects, forward modeling makes it easier to account for these effects and to exploit the full observational data set.

An essential step in our forward model is applying the Empirical Dust Attenuation (FADE) framework, which provides a flexible and computationally inexpensive prescription for applying dust attenuation. The FADE first assigns attenuation curves to every simulated galaxy. In this work, we use the Noll et al. (2009) parameterization for the attenuation curves and determine the amplitude and slope of the curves from the simulated galaxy’s M_* and specific star formation rate (SSFR) as well as a randomly sampled inclination (i). We use the same parameterization as observational studies so that the FADE attenuation curves can easily be compared to observational constraints. Also, the M_* and SSFR dependence is motivated by observations (*e.g.* Garn & Best 2010; Wild et al. 2011; Battisti et al. 2016; Leja et al. 2017; Salim et al. 2018; Salim & Narayanan 2020) and allows us to easily explore the correlation between galaxy properties and dust attenuation. After the assignment, we simply apply the attenuation curves to the SEDs of the simulated galaxies. The FADE, unlike radiative transfer models, does not produce realistic dust attenuation for individual galaxies. However, as we later demonstrate, it produces realistic distributions of dust attenuation for galaxy populations. Unlike radiative transfer models, however, the FADE does not produce realistic dust attenuation for individual galaxies. The FADE provides an empirical mapping framework for dust attenuation, analogous to the halo occupation or abundance matching frameworks in galaxy formation (for a review see Wechsler & Tinker 2018).

In principle, a radiative transfer model can be used instead of the FADE in the forward modeling approach; however, radiative transfer models are computationally expensive. Applying a range of radiative transfer dust models to multiple simulations for comparisons would require huge computational resources. Using them with Monte Carlo methods for parameter exploration would be prohibitive. On the other hand, with the FADE, we can apply a wide range of realistic dust attenuation to simulated galaxies in a matter of seconds. We can easily explore and sample the dust parameter space and infer the relationship between dust attenuation and galaxy properties. That is the focus of this paper. Beyond investigating dust, the FADE also provides a framework where we can treat dust as *nuisance* parameters and tractably marginalize over dust attenuation. In the subse-



Figure 1. The stellar mass functions, Φ_{M_*} (left-most panel), and M_* –SFR relation (right panels) of galaxies in three cosmological hydrodynamic simulations: SIMBA (orange), TNG (blue), and EAGLE (green). For reference, we include Φ_{M_*} (black) and the M_* –SFR relation (black dashed) of from SDSS observations. Uncertainties for the SDSS Φ_{M_*} are derived using jackknife resampling. We describe the simulations and observations in Section 2. *Differences in Φ_{M_*} and the M_* –SFR relations among the hydrodynamic simulations highlight how they predict galaxy populations with significantly different physical properties.*

quent paper of the IQ series, Starkenburg et al. (in preparation), we will use the FADE framework to compare star formation quenching in cosmological galaxy formation models after marginalizing over dust attenuation.

In Section 2, we describe the three large-scale cosmological hydrodynamical simulations (SIMBA, IllustrisTNG, and EAGLE) that we use in our forward model. We also describe the observed SDSS galaxy sample used for the comparison. Next, we present the specific FADE prescription used in this work in Section 3 and the likelihood-free inference method for comparing the simulations to observations in Section 4. Finally, in Section 5, we present the results of our comparison and discuss their implications on dust attenuation and its connection to galaxy properties.

2. DATA

In this paper, we present the Empirical Dust Attenuation (FADE) model and demonstrate how it can be used in a forward modeling approach to compare galaxy populations in simulations and observations. For our simulations, we use three cosmological hydrodynamical simulations: the Illustris TNG (hereafter TNG), EAGLE, and SIMBA. For our observations, we use a galaxy sample derived from SDSS. Below, we briefly describe the hydrodynamical simulations and the SDSS observations used throughout this work.

In Figure 1, we present the stellar mass functions, Φ_{M_*} (left-most panel), and M_* –SFR relations (right panels) of galaxies in the SIMBA (orange), TNG (blue), and EAGLE (green) cosmological hydrodynamic simulations. For reference, we include Φ_{M_*} and the M_* –SFR relation for SDSS observations. For the simulations, M_* is the total stellar mass within the host halo, excluding any stellar mass in subhalos; SFR is the instantaneous SFR derived from dense and cold gas. **We do not impose any selection cuts on the simulations in Figure 1.** For SDSS, M_* is estimated using `kcorrect` (Blanton & Roweis 2007) assuming a Chabrier (2003) initial mass function and SFR is

from the current release of Brinchmann et al. (2004)¹. The uncertainties for the SDSS SMF are derived from jackknife resampling. Figure 1 illustrates that the hydrodynamical simulations predict significantly different SMFs and $M_* - \text{SFR}$ relations from each other. *This difference, which was also recently highlighted in Hahn et al. (2019c), demonstrates that the hydrodynamical simulations predict galaxy populations with significantly different physical properties from one another.*

2.1. IllustrisTNG100

The IllustrisTNG100 simulation² is a cosmological hydrodynamic simulation of comoving volume $(110.7 \text{ Mpc})^3$, with a particle mass resolution of $7.6 \times 10^6 M_\odot$ for dark matter and $1.4 \times 10^6 M_\odot$ for baryonic particles (Nelson et al. 2018; Pillepich et al. 2018; Springel et al. 2018). It improves on the original Illustris simulation³ (Vogelsberger et al. 2014; Genel et al. 2014; public data release by Nelson et al. 2015), by including magneto-hydrodynamics and updated treatments for galactic winds, metal enrichment, and AGN feedback. Most notably, TNG uses a new implementation for feedback from SMBH, where feedback energy is injected in the form of a kinetic AGN-driven wind at low SMBH accretion rates (Weinberger et al. 2018). This new implementation has been shown to alleviate discrepancies found between the original Illustris and observations for $> 10^{13-14} M_\odot$ massive halos.

2.2. EAGLE

The Virgo Consortium’s EAGLE project⁴ (Schaye et al. 2015; Crain et al. 2015; McAlpine et al. 2016) is a publicly available suite of cosmological hydrodynamic simulations constructed using AN-ARCHY (Dalla Vecchia et al. in prep.; see also Appendix A of Schaye et al. 2015), a modified version of the GADGET-3 code (Springel 2005). We use the L0100Ref simulation, which has a comoving volume of $(100 \text{ Mpc})^3$, and a baryonic mass resolution of $1.81 \times 10^6 M_\odot$. EAGLE has subgrid models for star formation, stellar mass loss, metal enrichment and stellar feedback that stochastically inject thermal energy in the ISM as in (Dalla Vecchia & Schaye 2012). The feedback energy from AGN is also added to surrounding gas stochastically (Booth & Schaye 2009). Parameters of the stellar feedback and SMBH accretion are calibrated to broadly reproduce the $z = 0$ stellar mass function and galaxy stellar size-stellar mass relation. Meanwhile, the AGN feedback efficiency is calibrated to match the SMBH-galaxy mass relation.

2.3. SIMBA

The SIMBA simulation suite (Davé et al. 2019), the successor to MUFASA (Davé et al. 2016, 2017a,b), is a cosmological hydrodynamical simulation constructed using GIZMO, a meshless finite mass hydrodynamics code (Hopkins 2015; Hopkins et al. 2017). Of the simulations, we use ‘m100n1024’, which has a box size of $(100 h^{-1} \text{ Mpc})^3$ and baryonic mass resolution of $1.82 \times 10^7 M_\odot$. The simulation uses the same subgrid models as MUFASA for H_2 based star formation, decoupled two-phase winds for star formation driven galactic winds, and feedback from Type I supernovae

¹ <http://www.mpa-garching.mpg.de/SDSS/DR7/>

² <https://www.tng-project.org/>

³ <http://www.illustris-project.org>

⁴ <http://www.eaglesim.org>

and AGB stars. SIMBA uses a two-mode SMBH accretion model, torque-limited accretion for cold gas (Anglés-Alcázar et al. 2017) and Bondi-based accretion for hot gas, and two-mode AGN feedback.

2.4. SDSS Galaxies

For our observations, we use a galaxy sample derived from SDSS observations. We impose a $M_r < -20$ completeness limit on a volume-limited sample from Tinker et al. (2011). The Tinker et al. (2011) sample is derived from the SDSS DR7 (Abazajian et al. 2009) NYU Value-Added Galaxy Catalog (VAGC; Blanton et al. 2005) and has a $M_* > 10^{9.4} h^{-2} M_\odot$ completeness limit. In total, our SDSS sample has 16,970 galaxies. In this work, we focus on observables that can be consistently defined and derived in both simulations and observations: the r -band absolute magnitude, M_r , the optical $g-r$ color, and the $FUV-NUV$ color. For the SDSS sample, we use FUV , NUV , r and g band absolute magnitudes from the NASA-Sloan Atlas⁵, which is re-reduction of SDSS DR8 (Aihara et al. 2011) that includes an improved background subtraction (Blanton et al. 2011) and near and far UV photometry from GALEX. These absolute magnitudes are derived using `kcorrect` (Blanton & Roweis 2007), assuming a Chabrier (2003) initial mass function.

2.5. Forward Modeling Observations

One of the main goals of this work is to conduct an “apples-to-apples” comparison between the simulations and observations. A crucial step in this comparison is to *forward model* the observables for the simulations. The simulations can then be directly compared to observations in observational-space. This means that the comparison does not rely on measured galaxy properties, which are impacted by variations, inconsistencies, and biases of different methods. The comparison can also include selection functions and systematic effects of the observations through the forward model. In this work, we use r -band luminosity (M_r), optical color ($g-r$), and UV color ($FUV-NUV$) as our observables.

As the first step in our forward model, we construct SEDs for all of the simulated galaxies based on their star formation and metallicity histories (SFH and ZH) using the Flexible Stellar Population Synthesis model (FSPS; Conroy et al. 2009, 2010). For each simulated galaxy, we bin the total stellar mass formed by age (t) and metallicity (Z). We use a consistent t , Z grid for all of the simulations to account for the variable time and mass resolutions. For each point in the t , Z grid, we generate a spectrum assuming a simple stellar population (SSP) using FSPS and take the mass-weighted linear combination of them to produce the galaxy SED. We use a Chabrier (2003) initial mass function. For further details on how we construct the SEDs, we refer readers to Starkenberg et al. (in prep.).

Next, we apply dust attenuation to the SEDs. We use the FADE prescription to assign dust attenuation curves for each simulated galaxy based on its physical properties, a randomly sampled inclination, and FADE model parameters. We describe the FADE framework in detail later in Section 3. We measure the observables by convolving the attenuated SEDs with transmission curves of the GALEX FUV , GALEX NUV , SDSS g , and SDSS r broadband filters. We add realistic noise to M_r , $g-r$, and $FUV-NUV$ by sampling from the observed uncertainty distributions of the NASA

⁵ <http://nsatlas.org/>

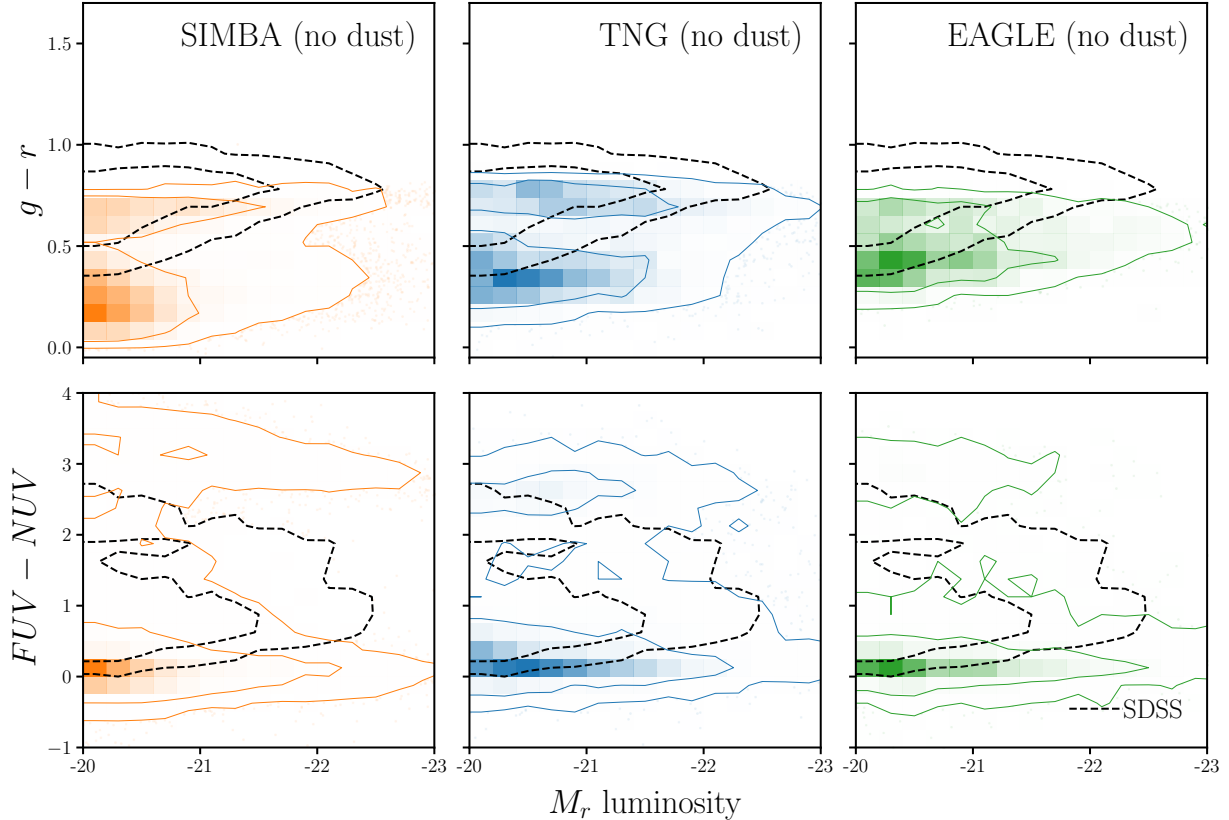


Figure 2. We present the forward modeled optical and UV color-magnitude relations of SIMBA (left), TNG (center), and EAGLE (right) galaxies *assuming no dust attenuation*. We present $(g-r) - M_r$ in the top panels and $(FUV-NUV) - M_r$ in the bottom panels. The contours represent the 68 and 95% of the distribution. We derive observables M_r , $g-r$, and $FUV-NUV$ for the simulations using our forward model (Section 2.5). For comparison, we include the color-magnitude relations of our SDSS sample (black dashed; Section 2.4). *Without dust attenuation, the hydrodynamical simulations do not reproduce the SDSS optical or UV color-magnitude relations.*

Sloan-Atlas. Lastly, we apply the $M_r < -20$ absolute magnitude completeness limit of our SDSS sample to the simulated galaxies.

In Figure 2, we present the forward modeled optical and UV color-magnitude relations, $(g-r) - M_r$ (top) and $(FUV-NUV) - M_r$ (bottom), for simulated galaxies in SIMBA (left), TNG (center) and EAGLE (right) *assuming no dust attenuation*. We mark the 68 and 95% contours and include, for reference, the optical and UV color-magnitude relations of our SDSS sample (black dashed). Comparison to SDSS observations clearly demonstrate that *without dust attenuation, the hydrodynamical simulations cannot reproduce the observed optical or UV color-magnitude relations.*

3. THE EMPIRICAL DUST ATTENUATION FRAMEWORK

In this section, we describe the Empirical Dust Attenuation (FADE) framework and present the FADE prescription we use in this work. The FADE is a flexible framework for applying dust attenuation curves to simulated galaxy populations. For each simulated galaxy, the FADE assigns a

dust attenuation curve that is parameterized as a function of the galaxy’s properties (M_* , SSFR), the FADE parameters, and randomly sampled inclination. With the FADE, we can apply a wide variety of dust attenuation that include correlation between dust attenuation and physical galaxy properties.

We begin by defining the dust attenuation curve, $A(\lambda)$, as

$$F_o(\lambda) = F_i(\lambda)10^{-0.4A(\lambda)} \quad (1)$$

where F_o is the observed flux and F_i is the intrinsic flux. We normalize the attenuation to the V band attenuation,

$$A(\lambda) = A_V \frac{k(\lambda)}{k_V} \quad (2)$$

so that A_V determines the amplitude of the attenuation, while $k(\lambda)$ determines the wavelength dependence.

The FADE framework assigns $A(\lambda)$ to every galaxy in the simulations using some flexible prescription. For the FADE prescription in this work, we assign A_V for each galaxy using the slab model, where A_V is a function of galaxy inclination, i , and its optical depth, τ_V (*e.g.* Somerville & Primack 1999; Somerville et al. 2012):

$$A_V = -2.5 \log \left[\frac{1 - e^{-\tau_V \sec i}}{\tau_V \sec i} \right]. \quad (3)$$

Since observations have established that A_V correlates with galaxy properties (*e.g.* Garn & Best 2010; Battisti et al. 2016; Salim & Narayanan 2020), we include correlations between A_V and galaxy M_* and SSFR through τ_V (see Appendix A for details). We parameterize τ_V using a linear M_* and SSFR dependence:

$$\tau_V(M_*, \text{SFR}) = m_{\tau, M_*} \log \left(\frac{M_*}{10^{10} M_\odot} \right) + m_{\tau, \text{SSFR}} \log \left(\frac{\text{SSFR}}{10^{-10} \text{yr}^{-1}} \right) + c_\tau. \quad (4)$$

m_{τ, M_*} , $m_{\tau, \text{SSFR}}$, and c_τ represent the M_* dependence, the SSFR dependence, and amplitude of τ_V . Since τ_V is optical depth, we impose a $\tau_V \geq 0$ limit. For each galaxy, we uniformly sample $\cos i$ from 0 to 1. By sampling $\cos i$, our FADE prescription includes significant variance in $A(\lambda)$ so galaxies with the same galaxy properties do not have the same dust attenuation.

We use the slab model primarily as a flexible prescription for A_V that depend on a randomly sampled i , with *loose* physical motivations. For star-forming galaxies, which typically have disc-like morphologies, the slab model produces A_V that is correlated with i in a way consistent with observations: edge-on galaxies have higher A_V than face-on galaxies (*e.g.* Conroy et al. 2010; Wild et al. 2011; Battisti et al. 2017; Salim & Narayanan 2020). Nevertheless, the slab model is a naive approximation; in reality, A_V depends on the detailed star-to-dust geometry. Furthermore, all galaxies in the simulations are assigned A_V from the slab model. For quiescent galaxies, which typically have elliptical morphologies, the slab model serves only as an *empirical* prescription for statistically sampling A_V . However, the purpose FADE is to assign an accurate distribution of dust attenuation

curves for the galaxy population — *not* to accurately model dust attenuation for individual galaxies. In Appendix A, we demonstrate that the slab model based FADE can produce A_V values that match $p(A_V)$ of observations, which include quiescent galaxies. Hence, the slab model is a sufficiently flexible prescription for sampling A_V for all galaxies.

For the wavelength dependence of the attenuation curve, $k(\lambda)$, we use the Noll et al. (2009) parameterization:

$$k(\lambda) = (k_{\text{Cal}}(\lambda) + D(\lambda)) \left(\frac{\lambda}{\lambda_V} \right)^\delta. \quad (5)$$

Here $k_{\text{Cal}}(\lambda)$ is the Calzetti (2001) curve:

$$k_{\text{Cal}}(\lambda) = \begin{cases} 2.659(-1.857 + 1.040/\lambda) + R_V, & 6300A \leq \lambda \leq 22000A \\ 2.659(-2.156 + 1.509/\lambda - 0.198/\lambda^2 + 0.011/\lambda^3) + R_V & 1200A \leq \lambda \leq 6300A \end{cases}$$

where $\lambda_V = 5500A$ is the V band wavelength and δ is the slope offset of the attenuation curve from k_{Cal} . Since δ correlates with galaxy properties (*e.g.* Wild et al. 2011; Battisti et al. 2016; Leja et al. 2017; Salim et al. 2018, ; see also Appendix A), we parameterize δ with a similar M_* and SSFR dependence as τ_V :

$$\delta(M_*, \text{SFR}) = m_{\delta, M_*} \log \left(\frac{M_*}{10^{10} M_\odot} \right) + m_{\delta, \text{SFR}} \log \left(\frac{\text{SSFR}}{10^{-10} \text{yr}^{-1}} \right) + c_\delta. \quad (6)$$

$D(\lambda)$ in Eq. 5 is the UV dust bump, which we parameter using the standard Lorentzian-like Drude profile:

$$D(\lambda) = \frac{E_b(\lambda \Delta\lambda)^2}{(\lambda^2 - \lambda_0^2)^2 + (\lambda \Delta\lambda)^2} \quad (7)$$

where λ_0 , $\Delta\lambda$, and E_b are the central wavelength, full width at half maximum, and strength of the bump, respectively. We include the UV dust bump since we use UV color as one of our observables.

We assume fixed $\lambda_0 = 2175A$ and $\Delta\lambda = 350A$. Kriek & Conroy (2013) and Tress et al. (2018) find that E_b correlates with the δ for star-forming galaxies $z \sim 2$. Narayanan et al. (2018) confirmed this dependence in simulations. However, we assume a fixed relation between E_b and δ from Kriek & Conroy (2013): $E_b = -1.9 \delta + 0.85$. Allowing the slope and amplitude of the E_b and δ relation to vary does *not* impact our results; however, we also do not derive any meaningful constraints on them. In Table 1, we list and describe all of the free parameters of the FADE.

SSFR of galaxies are used to calculate τ_V and δ in Eqs. 4 and 6. However, due to mass and temporal resolutions, some galaxies in the simulations have $\text{SFR} = 0$ — *i.e.* an unmeasurably low SFR (Hahn et al. 2019c). They account for 17, 19, 9% of galaxies in SIMBA, TNG, and EAGLE, respectively. Since Eqs. 4 and 6 depend on $\log \text{SSFR}$, they cannot be used in the equations to derive τ_V and δ for these galaxies. To account for this issue, we assign SFR_{min} , the minimum non-zero SFR in the simulations, to $\text{SFR} = 0$ galaxies when calculating τ_V and δ . For SIMBA, TNG, and EAGLE, $\text{SFR}_{\text{min}} = 0.000816, 0.000268, \text{ and } 0.000707 M_\odot/\text{yr}$. Although this assumes that $\text{SFR} = 0$ galaxies have similar dust properties as the galaxies with $\text{SFR} = \text{SFR}_{\text{min}}$, since the simulations have very low

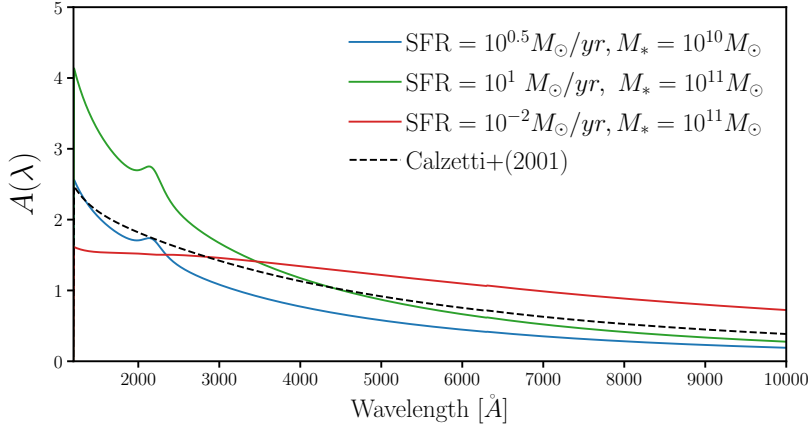


Figure 3. Attenuation curves, $A(\lambda)$, assigned by our Empirical Dust Attenuation (FADE) prescription to edge-on galaxies with different SFR and M_* values for an arbitrary set of FADE parameters. We include $A(\lambda)$ for star-forming galaxies with $\{M_*, \text{SFR}\} = \{10^{10} M_\odot, 10^{0.5} M_\odot/\text{yr}\}$ (blue), $\{10^{11} M_\odot, 10^1 M_\odot/\text{yr}\}$ (green) and a quiescent galaxy with $\{10^{11} M_\odot, 10^{-2} M_\odot/\text{yr}\}$ (red). We set $i = 0$ for all the galaxies in the figure for simplicity but in practice the FADE uniformly samples $\cos i$ from 0 to 1 for each galaxy. For comparison, we include the Calzetti (2001) attenuation curve. The FADE provides a flexible prescription for assigning dust attenuation to galaxies based on their inclination, physical properties (M_* and SSFR), and the FADE parameters.

SFR_{\min} we expect galaxies with $\text{SFR} = \text{SFR}_{\min}$ to have little recent star-formation and low gas mass, similar to $\text{SFR} = 0$ galaxies.

In practice, to apply the FADE to a simulated galaxy population, we first assign a randomly sampled inclination, i , to each galaxy ($\cos i$ uniformly sampled from 0 to 1). τ_V and δ are calculated for the galaxy based on its M_* , SSFR and the FADE parameters. We then combine A_V from i and τ_V with $k(\lambda)$ from δ to determine $A(\lambda)$ for each galaxy. Afterwards, we attenuate the galaxy SEDs using Eq. 1 and use the attenuated SEDs to calculate the observables: g , r , NUV , and FUV absolute magnitudes. In Figure 3, we present attenuation curves, $A(\lambda)$, generated by the FADE for galaxies with different SFR and M_* values. We include star-forming galaxies with $\{M_*, \text{SFR}\} = \{10^{10} M_\odot, 10^{0.5} M_\odot/\text{yr}\}$ (blue), $\{10^{11} M_\odot, 10^1 M_\odot/\text{yr}\}$ (green) and a quiescent galaxy with $\{10^{11} M_\odot, 10^{-2} M_\odot/\text{yr}\}$ (red). We use an arbitrarily set of FADE parameters (m_{τ, M_*} , $m_{\tau, \text{SSFR}}$, c_τ , m_{δ, M_*} , $m_{\delta, \text{SFR}}$, c_δ) within the prior range listed in Table 1. We set $i = 0$ (edge-on) for all $A(\lambda)$ in Figure 3 for simplicity. In practice the FADE uniformly samples $\cos i$ from 0 to 1 for each galaxy. For comparison, we include the Calzetti (2001) attenuation curve. Even when we set $i = 0$, the FADE produces attenuation curves with a wide range of amplitude and slope to galaxies based on their physical properties.

4. LIKELIHOOD-FREE INFERENCE: APPROXIMATE BAYESIAN COMPUTATION

With our forward model, which includes the FADE prescription for dust attenuation, we can now generate synthetic observations for simulated galaxies and make an “apples-to-apples” comparison to SDSS. Next, we want to use this comparison to infer the posterior probability distribution of the FADE parameters. Typically in astronomy, this inference is done assuming a Gaussian likelihood to compare the “summary statistic” (e.g. SMF) of the model to observations and some sampling

Table 1. Free parameters of the Empirical Dust Attenuation Model

Parameter	Definition	prior
m_{τ, M_*}	M_* dependence of the optical depth, τ_V	flat $[-5., 5.]$
$m_{\tau, \text{SSFR}}$	SSFR dependence of τ_V	flat $[-5., 5.]$
c_τ	amplitude of τ_V	flat $[0., 6.]$
m_{δ, M_*}	M_* dependence of δ , the attenuation curve slope offset	flat $[-4., 4.]$
$m_{\delta, \text{SSFR}}$	SSFR dependence of δ	flat $[-4., 4.]$
c_δ	amplitude of δ	flat $[-4., 4.]$

method (*e.g.* Markov Chain Monte Carlo) to estimate the posterior distribution. The functional form of the likelihood, however, depends on the summary statistic and assuming an incorrect form of the likelihood can significantly bias the inferred posteriors (*e.g.* Hahn et al. 2019b). In this work, we use the optical and UV color-magnitude relations as our summary statistic. Since the statistic is three-dimensional histogram, its likelihood is *not* Gaussian but rather a Poisson distribution.

Rather than *incorrectly* assuming a Gaussian likelihood or attempting to estimate the true Poisson likelihood of the optical and UV color-magnitude relations, we use Approximate Bayesian Computation (hereafter ABC; Diggle & Gratton 1984; Tavaré et al. 1997; Pritchard et al. 1999; Beaumont et al. 2009; Del Moral et al. 2012) for our inference. ABC is a likelihood-free (or “simulation-based”) parameter inference framework that approximates the posterior probability distribution, $p(\theta | \text{data})$, without requiring evaluations of the likelihood. Instead, ABC only requires a forward model of the observed data, a prior that can be sampled, and a distance metric that quantifies the “closeness” to the observed data. Since ABC does not require evaluating the likelihood, it does not assume any functional form of the likelihood and so we avoid any biases from such assumptions. Furthermore, it also allows us to infer the posterior using summary statistics with likelihoods that are difficult or intractable to directly estimate (Hahn et al. 2017a).

In the simplest version of ABC, with a rejection sample framework (Pritchard et al. 1999), a proposal set of parameter values are drawn from the prior. The forward model is run with the proposal parameter values. The output of the forward model is then compared to the observed data using a distance metric that quantifies the “closeness” of the forward model output to the observed data. If the distance is within some small threshold, we keep the proposed parameters; otherwise, we discard them. Proposals are drawn until enough pass the threshold to sample the posterior. A rejection sampling framework requires a large number of evaluations of the forward model, which can be computationally costly. Many variations of ABC with more efficient sampling strategies have now been applied to astronomy and cosmology (*e.g.* Cameron & Pettitt 2012; Weyant et al. 2013; Ishida et al. 2015; Lin et al. 2016; Alsing et al. 2018). Among these methods, we use ABC with Population Monte Carlo (PMC) importance sampling (Hahn et al. 2017a,b, 2019a).

ABC-PMC begins with an arbitrarily large threshold ϵ_1 and N proposals $\bar{\theta}_1$ sampled from the prior distribution. Each proposal is assigned a weight $w_1^i = 1/N$. Then for subsequent iterations ($n > 1$),

the threshold, ϵ_n , is set to the median distance of the previous iteration’s proposals. New proposals are drawn from the previous iteration’s proposals perturbed by a kernel and kept if their distance is below ϵ_n . This is repeated until we assemble a new set of N proposals $\bar{\theta}_n$. The entire process is repeated for the next iteration until convergence is confirmed. We use the Python implementation of Akeret et al. (2015)⁶. For further details on the ABC-PMC implementation, we refer readers to Hahn et al. (2017b) and Hahn et al. (2019a).

In this work, we use ABC-PMC with uninformative uniform priors on each of the FADE parameters and choose ranges that encompass constraints in the literature. The prior ranges of $m_{\tau, M_*}, m_{\tau, \text{SSFR}}, c_{\tau}$ are chosen to conservatively include the A_V range and M_* and SFR dependence of Narayanan et al. (2018) and Salim & Narayanan (2020). Meanwhile, the prior ranges of $m_{\delta, M_*}, m_{\delta, \text{SFR}}, c_{\delta}$ are chosen to conservatively include the δ range and M_* and SFR dependence of Leja et al. (2017) and Salim et al. (2018). We list the range of the priors in Table 1. For our forward model, we use the model described in Section 2.5: we construct SEDs for every simulated galaxies from the hydrodynamic simulations, apply dust attenuation with our FADE, calculate the observables (M_r , $g-r$, and $FUV-NUV$), add uncertainties to them, and apply a $M_r < -20$ completeness limit. We use the optical and UV color-magnitude relation, $(g-r) - M_r$ and $(FUV-NUV) - M_r$ as our summary statistic to fully exploit the $(M_r, g-r, FUV-NUV)$ observational-space. We measure the color-magnitude relations by calculating the number density in bins of $(g-r, FUV-NUV, M_r)$ with widths (0.0625, 0.25, 0.5) mags. For our distance metric, ρ , we use the L2 norm between the summary statistics of the SDSS observation, X^{SDSS} and of our forward model, $X^{\text{FM}}(\theta_{\text{FADE}})$:

$$\rho(\theta_{\text{FADE}}) = [X^{\text{SDSS}} - X^{\text{FM}}(\theta_{\text{FADE}})]^2. \quad (8)$$

In Figure 4, we present the posterior distributions of the FADE parameters derived using ABC-PMC for the SIMBA (orange), TNG (blue), and EAGLE (green) hydrodynamical simulations. The contours mark the 68 and 95 percentiles of the distributions.

5. RESULTS

Without dust attenuation, all of the hydrodynamical simulations struggle to reproduce the $(g-r) - M_r$ and $(FUV-NUV) - M_r$ relations of SDSS (Figure 2). In the optical, the simulations predict significantly bluer colors and find broader differences in color, ~ 0.5 mag, between star-forming and quiescent galaxies. In the UV, they predict quiescent galaxies with $\text{SSFR} < 10^{-12} \text{yr}^{-1}$ that have redder $FUV-NUV$ colors beyond SDSS observations. Meanwhile, for the rest of the galaxies, the simulations predict significantly bluer UV colors than SDSS.

With our FADE prescription, however, all three simulations reproduce the color-magnitude relations of SDSS observations. In Figure 5, we present the optical and UV color-magnitude relations predicted by the FADE for the SIMBA (orange), TNG (blue), and EAGLE (green) simulations. For the FADE parameters, we use the median of the posterior distributions inferred using ABC (Figure 4). We include the color-magnitude relations of SDSS observations (black-dashed) comparison. The contours mark the 68 and 95 percentiles of the distributions.

⁶ <https://abcpmc.readthedocs.io/en/latest/index.html>

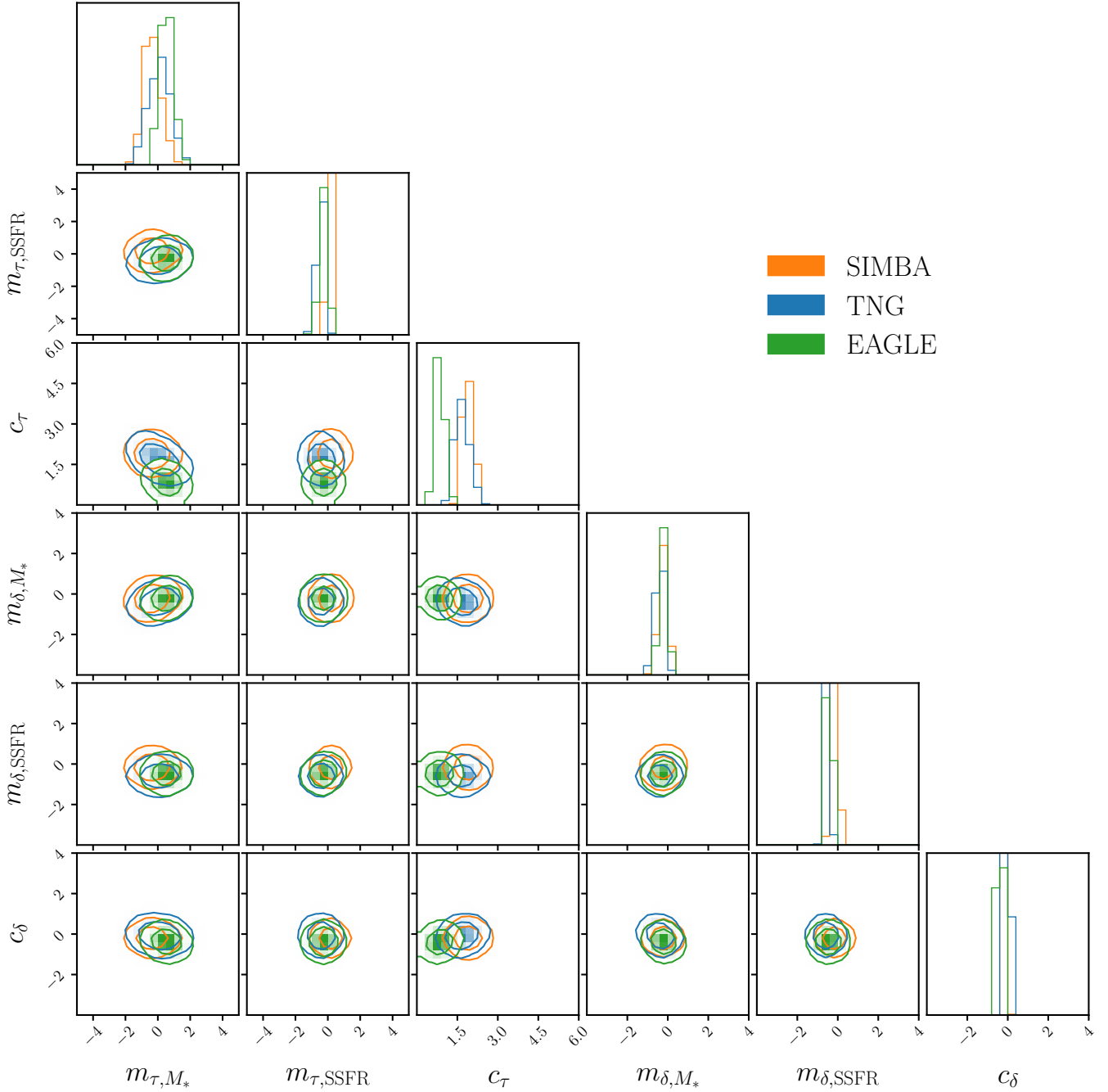


Figure 4. Posterior distributions of the FADE parameters for the SIMBA (orange), TNG (blue), and EAGLE (green) hydrodynamical simulations. The contours mark the 68 and 95 percentiles of the distributions. The posteriors are derived using the likelihood-free inference method: Approximate Bayesian Computation with Population Monte Carlo (Section 4). We focus on the FADE posteriors for TNG and EAGLE since the FADE struggles to reproduce SDSS observations with SIMBA, which predicts an overabundance of starburst galaxies. Based on the posteriors, we find that *galaxies with higher M_* have overall higher dust attenuation and galaxies with higher SSFR have steeper attenuation curves.*

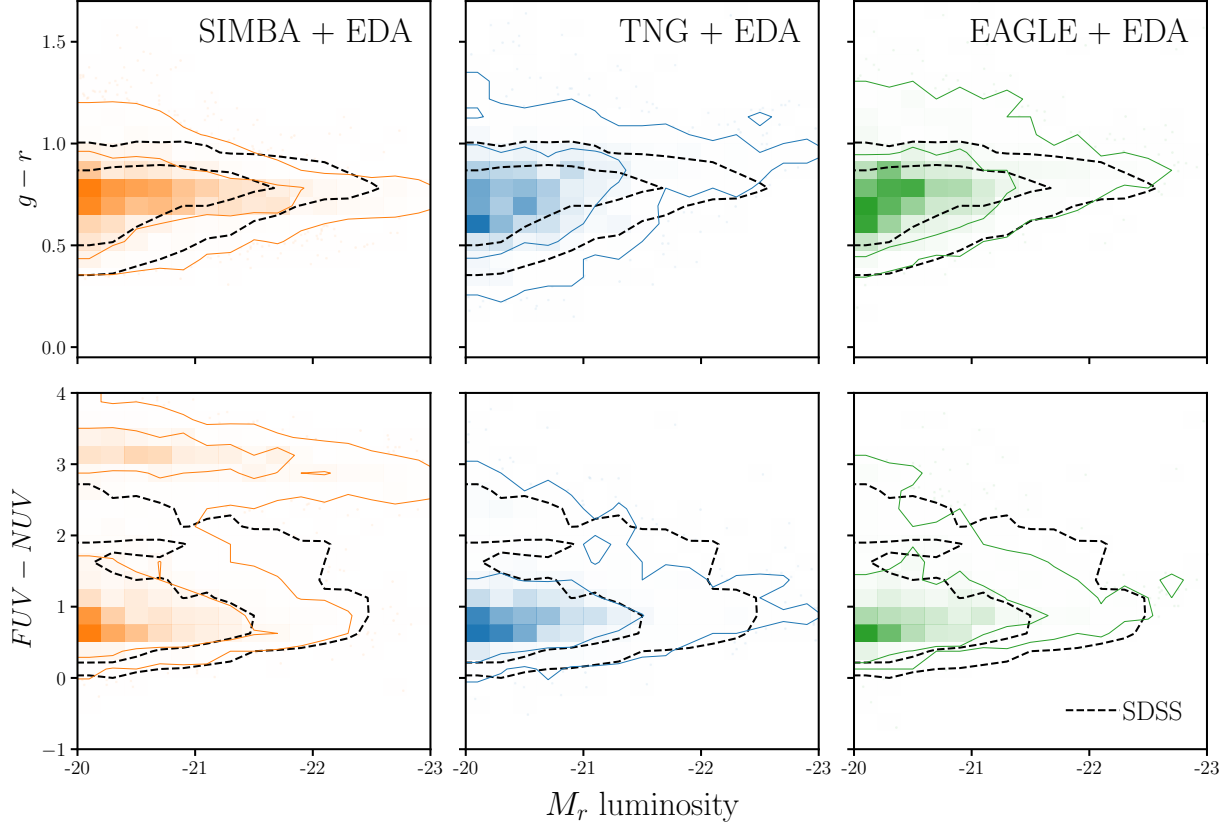


Figure 5. The optical ($(g-r) - M_r$; top) and UV ($(FUV-NUV) - M_r$; bottom panels) color-magnitude relations predicted by our FADE prescription for the SIMBA (orange), TNG (blue), and EAGLE (green) hydrodynamical simulations. For the FADE parameters of each simulation, we use the median of the posterior distributions inferred using ABC. For comparison, we include the color-magnitude relations of SDSS (black dashed). Comparing the color-magnitude relations above to those without dust attenuation in Figure 2, we see that dust *dramatically* impacts the color-magnitude relations. Therefore, dust attenuation must be accounted for when interpreting and comparing simulations. Furthermore, with our FADE prescription, all three simulations reproduce the color-magnitude relations of SDSS observations. *Since the different simulations can reproduce observations just by varying dust, dust significantly limits our ability to constrain the underlying physical processes of galaxy formation models.*

Dust dramatically impacts the observables of simulations. The FADE affects the the optical and UV color-magnitude relations in three major ways to produce good agreement with SDSS. First, the FADE significantly reddens simulated galaxies in both the optical and UV. Overall, $g-r$ colors are ~ 0.25 mag redder and $FUV-NUV$ colors are ~ 0.5 mag redder. Second, the FADE significantly attenuates (~ 0.5 mag) intrinsically blue galaxies (*i.e.* star-forming galaxies with $\log \text{SSFR} > -10.5$). As a result, there are no luminous optically blue galaxies ($M_r < -21$ and $g-r < 0.5$) — consistent with observations. Lastly, in the UV, the FADE attenuates low SSFR quiescent galaxies that are intrinsically red in the UV ($FUV-NUV \sim 3$ mag) by ~ 1 mag. Thus, unlike in Figure 2, the UV color-magnitude relations from the FADE do not have a significant number of galaxies with high $FUV-NUV$, in agreement with SDSS.

For SIMBA, although the FADE prescription predicts optical and UV color-magnitude relations consistent with observations, there are still some discrepancies in the color-magnitude relations with SDSS. Furthermore, the overall agreement is significantly worse than TNG and EAGLE: the median ABC distance metric (Eq. 8) of the posterior $\rho = 3.7 \times 10^{-3}, 3.2 \times 10^{-3}$ for TNG and EAGLE while $\rho = 6.8 \times 10^{-3}$ for SIMBA. SIMBA+FADE produces a $g-r$ color distribution that is narrower and a $FUV-NUV$ distribution that is broader than SDSS. The inferred FADE parameters for SIMBA also differ significantly from the parameters of TNG and EAGLE (Figure 4). These discrepancies are primarily driven by the excess of high $\log \text{SSFR} > -9.5$ “starburst” galaxies with $M_* < 10^{10} M_\odot$ that lie significantly above the SFS, which are *only* present in SIMBA (Figure 1). This starburst population, which has also been identified in Davé et al. (2019) (see their Figures 5 and 6) is caused by excess gas in low-mass galaxies at $z = 0$. If we exclude $\log \text{SSFR} > -9.5 \text{ yr}^{-1}$ starburst galaxies and run the FADE for SIMBA using median values of the TNG and EAGLE posteriors for the FADE parameters, we find similar level of agreement with SDSS as TNG and EAGLE.

Without dust attenuation, the excess starburst galaxies in SIMBA are blue $g-r \sim 0.1$ and have high luminosity, $M_r < -22$. Since such high luminosity blue galaxies do not exist in observations, they need to be both strongly attenuated and reddened. In our FADE prescription, dust attenuation and reddening is a linear function of $\log \text{SSFR}$ so it cannot strongly attenuate and redden the starburst population in particular. Although we can increase the flexibility of our FADE prescription, the attenuation and reddening necessary for the starburst galaxies conflict with the attenuation-slope relation well-established in observations and simulations (Inoue 2005; Chevallard et al. 2013; Salim et al. 2018; Salim & Narayanan 2020; Trayford et al. 2020). The SIMBA starbursts require both high attenuation and steeper slopes but, based on the attenuation-slope relations, galaxies with higher attenuation have shallower slopes. We therefore do not explore extending our FADE prescription and focus on the TNG and EAGLE simulations for the rest of the paper.

Previous works in the literature have also compared simulations with different dust prescriptions to observations in color-magnitude space. For EAGLE, Trayford et al. (2015) calculate colors and luminosities with the GALAXEV population synthesis models and a two-component screen model for dust. More recently, Trayford et al. (2017) calculated optical colors for EAGLE using SKIRT, a Monte Carlo radiative transfer code (Camps & Baes 2015), to model the dust. At stellar masses and luminosities comparable to our SDSS sample, both Trayford et al. (2015) and Trayford et al. (2017) produce red sequences bluer than in GAMA observations. Also, Trayford et al. (2015) predict an excess of luminous blue galaxies. Although a detailed comparison is difficult since both works compare to different observations, we note that with the FADE, EAGLE is able to successfully reproduce the position of the SDSS red sequence and does not predict a significant excess of luminous blue galaxies. Also using EAGLE and SKIRT, Baes et al. (2019) find that they overestimate the observed cosmic SED (CSED) in the UV regime and produce significantly higher $FUV-NUV$ color than GAMA. The FADE predicts $FUV-NUV$ in good agreement with SDSS. For TNG, Nelson et al. (2018) calculate optical colors using a dust model that includes attenuation due to dense gas birth clouds surrounding young stellar populations and also due to simulated distribution of neutral gas and metals. They find bluer red sequence peaks and a narrower blue cloud compared to SDSS. We find neither of these

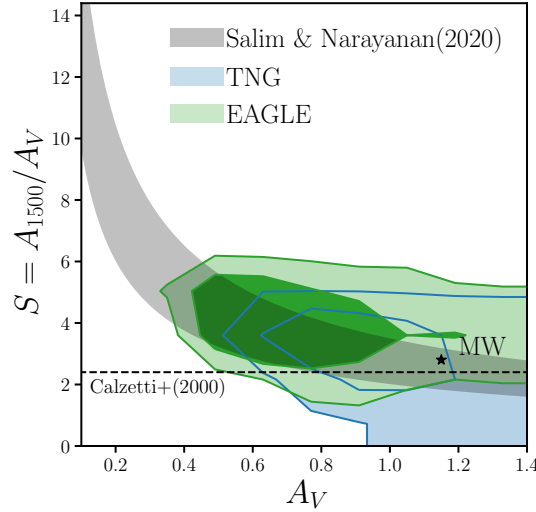


Figure 6. The attenuation-slope relation of the attenuation curves predicted by our FADE prescription for the median posterior parameter values of TNG (blue) and EAGLE (green). For comparison, we include the observed attenuation-slope relation from GSWLC2 (Salim & Narayanan 2020). We also include the Milky Way (star) and mark the slope of the Calzetti (2001) curve (dashed). We use A_V and $S = A(1500\text{\AA})/A_V$ as measurements of attenuation and slope, respectively. We derived the posteriors of the FADE parameters from comparing the UV and optical color-magnitude relation and do not fit any observed dust attenuation measurements. Yet, *we find excellent agreement between the attenuation-slope relation predicted by the FADE and observations.*

discrepancies for the TNG+FADE. The FADE provides a simpler empirical framework for applying dust attenuation than the dust models in these works. Yet, with its flexibility, we are able to produce optical and UV color-magnitude relations that are in good agreement with observations. Furthermore, with its low computation costs we were able to fully explore our dust parameters.

5.1. Reproducing Dust Observations

With our FADE prescription, we are able to accurately reproduce the observed optical and UV color-magnitude relations with our simulations. In addition to reproducing observations, since the FADE assigns dust attenuation curves for each simulated galaxies, we can also compare the FADE dust attenuation curves to dust attenuation measured from observations. We begin with the well-established attenuation-slope relation: galaxies with higher dust attenuations have shallower attenuation curves. This relation is a consequence of dust scattering dominating absorption at low attenuation while dust absorption dominating at high attenuation (Gordon et al. 1994; Witt & Gordon 2000; Draine 2003; Chevillard et al. 2013). In Figure 6, we present the attenuation-slope relation of the dust attenuation curves predicted by the FADE for the median posteriors of TNG (blue) and EAGLE (green). For comparison, we include the observed attenuation-slope relations of GSWLC2 galaxies (grey shaded; Salim & Narayanan 2020), the Milky Way (star), and mark the slope of the Calzetti (2001) curve (dashed). For attenuation we use A_V and for slope we use the UV-optical slope, $S = A(1500\text{\AA})/A_V$, commonly found in the literature. The contours mark the 68 and 95 percentiles. We note that the different in the A_V ranges is due to the M_r completeness limit imposed by our

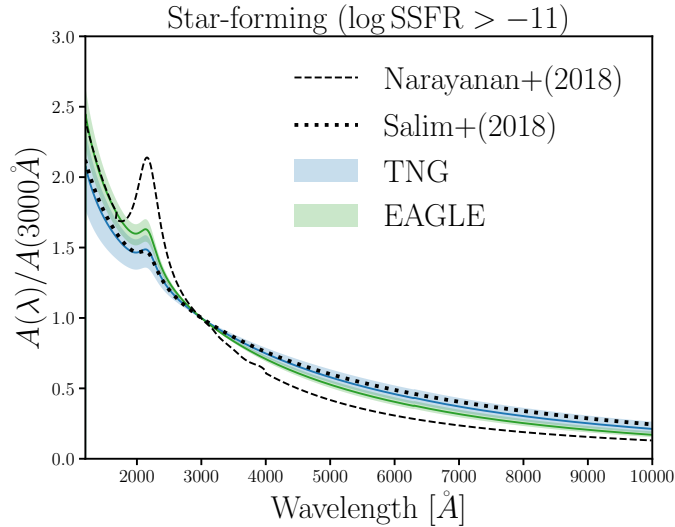


Figure 7. The normalized attenuation curves of star-forming galaxies predicted by the FADE for median posterior parameter values of TNG (blue) and EAGLE (green). Galaxies are classified as star-forming using a $\log \text{SSFR} > -11 \text{ yr}^{-1}$ cut. The attenuation curves are normalized at 3000\AA and we mark the 1σ standard deviation of the attenuation curves with the shaded region. For comparison, we include $A(\lambda)/A(3000\text{\AA})$ measurements from the (Narayanan et al. 2018) radiative transfer simulation (dashed) and Salim et al. (2018) observations (dotted). *The FADE predict attenuation curves of star-forming galaxies that are in good agreement with the attenuation curves measured from the simulation and observations.*

forward model (Section 2.5). The Salim & Narayanan (2020) GSWLC2 sample extends down to $M_* \sim 10^{8.5} M_\odot$; however, the TNG and EAGLE samples do not extend below $M_* \sim 10^{10} M_\odot$. *The FADE predicts attenuation-slope relations for TNG and EAGLE that are in excellent agreement with observations.*

In addition to the attenuation-slope relation, we can also directly compare the attenuation curves predicted by the FADE to measurements from observations for star-forming galaxies. In Figure ??, we present the normalized attenuation curves of star-forming galaxies predicted by the FADE for the median posterior parameter values of TNG (blue) and EAGLE (green). We define galaxies with $\log \text{SSFR} > -11 \text{ yr}^{-1}$ as star-forming. The attenuation curves are normalized at 3000\AA and we present the variation in the attenuation curves in the shaded region, 1σ standard deviation about the median. For comparison, we include $A(\lambda)/A(3000\text{\AA})$ from the Narayanan et al. (2018) radiative transfer simulation (dashed) and observations (Salim et al. 2018, ; dotted). The attenuation curve from Salim et al. (2018) correspond to star-forming galaxies with $M_* > 10^{10.5} M_\odot$, a similar M_* range as our forward modeled TNG and EAGLE samples. Since we do not vary the UV bump in our FADE prescription, we ignore any discrepancies in the amplitudes of UV dust bump. *Overall, we find good agreement between the FADE attenuation curves for star-forming galaxies and the attenuation curves from observations and simulations.*

In this section, we show that FADE predicts dust attenuation curves that are in good agreement with the well-established attenuation-slope relation and the attenuation curves of star-forming galaxies from observations and simulations. The FADE predictions are derived solely from matching the

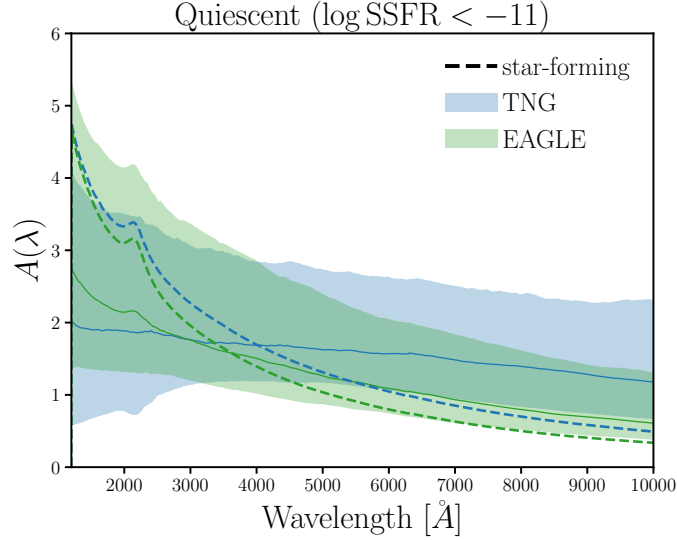


Figure 8. The attenuation curves of quiescent galaxies predicted by the FADE for median posterior parameter values of TNG (blue) and EAGLE (green). Galaxies are classified as quiescent using a $\log \text{SSFR} < -11 \text{ yr}^{-1}$ cut. We mark the 1σ standard deviation of the attenuation curves with the shaded region and include the predicted attenuation curves of star-forming galaxies for comparison (dashed). For both TNG and EAGLE, the FADE predicts significant UV and optical dust attenuation in quiescent galaxies with an overall shallow attenuation curve.

SDSS UV and optical color-magnitude relations — without fitting any observed dust attenuation measurements. The overall agreement demonstrates the robustness of the FADE framework and the specific parameterization of our FADE prescription.

5.2. The Attenuation Curves of Quiescent Galaxies

We have demonstrated so far that the FADE can reproduce the observed UV and optical color-magnitude relations. In doing so, it also predicts attenuation-slope relation and dust attenuation curves of star-forming galaxies that are in good agreement with observations and radiative transfer simulations. Beyond reproducing previous work, the FADE also makes predictions on the dust attenuation of quiescent galaxies, which is still poorly constrained by observations. There are many challenges to measuring the attenuation curves of quiescent galaxies directly from observations. Methods that rely on IR luminosities can be contaminated by MIR emission from AGN heating nearby dust (Kirkpatrick et al. 2015). SED fitting methods must also account for AGN MIR emission (Salim et al. 2016; Leja et al. 2018; Salim et al. 2018) and struggle to tightly constrain dust attenuation for quiescent galaxies due to the degeneracies with star formation history and metallicity.

With a forward modeling approach, we circumvent these challenges. Instead, we derive the attenuation curves necessary for the simulated quiescent population to reproduce the observed optical and UV photometry. In Figure 8, we present the attenuation curves of quiescent galaxies predicted by the FADE for the median posterior parameter values of TNG (blue) and EAGLE (green). Quiescent galaxies are classified using a $\log \text{SSFR} < -11 \text{ yr}^{-1}$ cut. Unlike Figure 7, the attenuation curves are *not* normalized at 3000\AA . For comparison, we include $A(\lambda)$ of star-forming galaxies predicted

by the FADE (dotted). Both TNG+FADE and EAGLE+FADE predict significant dust attenuation in quiescent galaxies: $A(\lambda) \gtrsim 1$ throughout the UV and optical. Their attenuation curves are also significantly shallower than the attenuation curves of star-forming galaxies.

The quiescent galaxy dust attenuation we predict is not a consequence of the parameterization of our FADE prescription. Without dust both TNG and EAGLE predict quiescent galaxies that are too luminous and bluer in the optical than SDSS observations (Figure 2). Therefore, to match the SDSS color-magnitude relations, significant attenuation is necessary to lower their luminosities but with a shallow slope that reddens their $g-r$ colors while maintaining their $FUV-NUV$ colors. This is also the reason why TNG has a shallower slope than EAGLE: without dust, TNG has a quiescent population that is redder in both UV and optical.

Dust attenuation in quiescent galaxies, which is typically neglected, has significant implications. For instance, it strengthens the evidence for the UV upturn phenomenon, the unexpected detections of UV flux in quiescent galaxies (*e.g.* ?????). Better constraints on the attenuation in quiescent galaxies may help discern among the different hypotheses: residual star formation activity (*e.g.* ?), post-main-sequence stellar evolutionary phases (*e.g.* ?), or binary systems (*e.g.* ?). Since the attenuation curves of quiescent galaxies are difficult to measure from observations, the FADE predictions highlight the advantages of a forward modeling approach and its complementarity with standard approaches. We, however, note that since we only vary the FADE parameters in our forward model, we do not explore whether the discrepancy between the quiescent populations in simulations and observations is due to shortcomings of the galaxy formation models. In principle, and in future work, we can vary both the FADE parameters and the parameters of the galaxy formation models and infer them simultaneously with a forward modeling approach.

5.3. The Galaxy – Dust Connection

With the FADE framework, we can also shed light on the connection between the physical properties of the simulated galaxies and dust attenuations. In our FADE prescription, we included a flexible M_* and SSFR dependence in both the amplitude and slope of the attenuation curve (Eqs 4 and 6). Hence, we can reveal the M_* and SSFR dependence of dust attenuation through both the FADE parameter constraints (Figure 4) and the predicted attenuation curves.

Focusing first on the amplitude of dust attenuation, we find that TNG has little M_* dependence in τ_V : $m_{\tau, M_*} = 0.14^{+0.64}_{-0.58}$. EAGLE has a more significant positive M_* dependence: $m_{\tau, M_*} = 0.53^{+0.36}_{-0.36}$. Though neither TNG nor EAGLE has a strong dependence, V -band dust attenuation is higher for more massive galaxies. Meanwhile, we find significant SSFR dependences in both TNG ($m_{\tau, \text{SSFR}} = -0.42^{+0.2}_{-0.18}$) and EAGLE ($m_{\tau, \text{SSFR}} = -0.24^{+0.22}_{-0.19}$): galaxies with higher SSFR have lower V -band dust attenuation. For the slope of the dust attenuation, we find some M_* dependence in both TNG ($m_{\delta, M_*} = -0.36^{+0.23}_{-0.19}$) and EAGLE ($m_{\delta, M_*} = -0.2^{+0.16}_{-0.16}$). More massive galaxies have slightly steeper attenuation curves. We also find significant SSFR dependence in both TNG ($m_{\delta, \text{SSFR}} = -0.55^{+0.08}_{-0.08}$) and EAGLE ($m_{\delta, \text{SSFR}} = -0.43^{+0.08}_{-0.08}$). Galaxies with higher SSFR have steeper attenuation curves.

Next, we take a closer look at the M_* and SSFR dependence of the attenuation curve in Figure 9. We present dust attenuation at 1500\AA (A_{1500} ; top) and 5500\AA (A_V ; bottom) as a function of $\log M_*$ and $\log \text{SFR}$ predicted by the FADE for TNG (left) and EAGLE (right). For each hexbin, the colormap

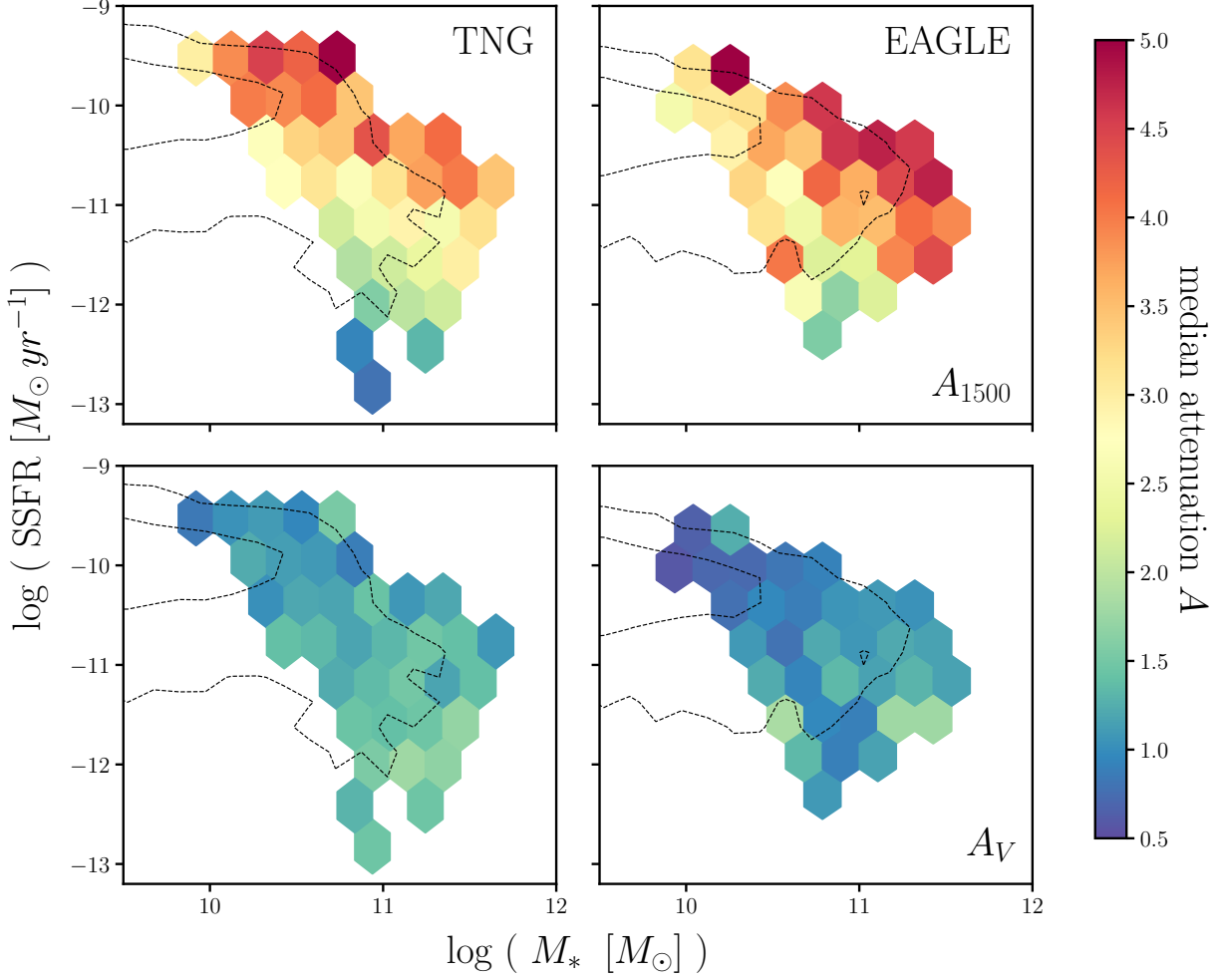


Figure 9. M_* and SSFR dependence of dust attenuation at 1500Å (A_{1500} ; top) and at 5500Å (A_V bottom) predicted by the FADE for TNG (left) and EAGLE (right). The colormap in each hexbin represents the median attenuation for all simulated galaxies in the bin (right color bar). We only include bins with more than 10 galaxies that satisfy our $M_r < -20$ completeness limit. For reference, we mark $\log \text{SSFR} = -11 \text{ yr}^{-1}$ (dashed). The bottom panels illustrate that, overall, more massive galaxies have higher A_V while galaxies with higher SSFR have lower A_V .

represents the median attenuation for all simulated galaxies in the bin. We only include bins with more than 10 galaxies that satisfy our $M_r < -20$ completeness limit. For reference, we include the line where $\log \text{SSFR} = -11 \text{ yr}^{-1}$ (dashed); galaxies above and below this line can roughly be classified as star-forming and quiescent. In both the top and bottom panels of Figure 9, we find that TNG and EAGLE galaxies with higher M_* have higher dust attenuation. This M_* dependence is consistent with the literature. Burgarella et al. (2005), for instance, found significant positive M_* dependence in FUV attenuation in NUV-selected and FIR-selected samples. Garn & Best (2010) and Battisti et al. (2016) also find higher attenuation in more massive SDSS star-forming galaxies. Most recently, Salim et al. (2018) find higher V and FUV attenuation for more massive star-forming galaxies in GSWLC2.

For the SSFR dependence, we find that galaxies with higher SSFR have higher A_{1500} (top) but lower A_V (bottom). The opposite SSFR dependence in A_{1500} versus A_V is a result of the significant SSFR dependence on the slope of the attenuation curve. Galaxies with higher SSFR have significantly steeper slopes so even though they have lower A_V , they have higher A_{1500} . At the lowest SSFR end, quiescent galaxies in TNG and EAGLE have nearly flat attenuation curves. Since observations have only focused on star-forming galaxies due to the difficulty in measuring dust attenuation in quiescent galaxies, the FADE predictions provide new insight into the SSFR dependence of dust attenuation. In summary, from the FADE predictions, we find that *TNG and EAGLE galaxies with higher M_* have overall higher dust attenuation and galaxies with higher SSFR have steeper attenuation curves.*

5.4. Discussion

We make a number of assumptions and choices in our FADE prescription. First, we use the slab model (Eq. 3) to assign A_V as a function of the randomly sampled i and τ_V . This choice is based on the fact that the slab model reproduces the correlation between attenuations and inclination found in observations (Conroy 2010; Wild et al. 2011; Battisti et al. 2017; Salim & Narayanan 2020) as well as simulations (*e.g.* Chevallard et al. 2013; Narayanan et al. 2018; Trayford et al. 2020). It can also reproduce the SDSS A_V distribution (Figure 11). If we replace the slab model with a more flexible model for sampling A_V using truncated normal distributions, we find that our results are not significantly impacted (see Appendix A for details). Therefore, we conclude that our results do not significantly depend on our choice of the slab model. In our FADE, we also use a parameterization of τ_V and δ that depend linearly on $\log M_*$ and $\log \text{SSFR}$. While the M_* and SSFR dependence of A_V is well-motivated and is found in, for instance, the Salim et al. (2018) GSWLC2 catalog (Appendix A), the linear dependence was chosen primarily for its simplicity. The FADE framework can be easily extended to more flexible parameterizations. In fact, a more flexible parameterization would likely reduce some of the discrepancies with the SDSS color-magnitude relations. The FADE produces broader distributions of optical colors than SDSS. Few galaxies in SDSS have $g-r > 1$, while some galaxies in the FADE broadly extend beyond this cut-off. In the UV, the FADE struggles to accurately reproduce the redder portions ($FUV-NUV > 1.5$) of the UV color-magnitude relation. The main challenges for a more flexible parameterization would be model selection and finding a well-motivated parameterization. Notwithstanding, for SDSS observations, our FADE prescription using parameter values from the TNG and EAGLE posteriors find good agreement.

We demonstrate in this work that accounting for dust attenuation is essential when comparing simulations to observations. None of the simulations reproduce the UV and optical color-magnitude relation without dust attenuation (Figure 2). Furthermore, the fact that we can use the FADE to reproduce SDSS observations for different hydrodynamical simulations highlights how our current lack of understanding of dust limits our ability to closely compare galaxy formation models. Our FADE prescription is built on our current understanding of dust attenuation in galaxies: *e.g.* the Noll et al. 2009 parameterization, the UV bump, the slab model, etc. Yet with the FADE, two simulations that predict galaxy populations with significantly different physical properties (Figure 1) can reproduce the same SDSS observations. This suggests that dust is highly degenerate with the differences between simulations. Put another way — if we were to marginalize over dust in our

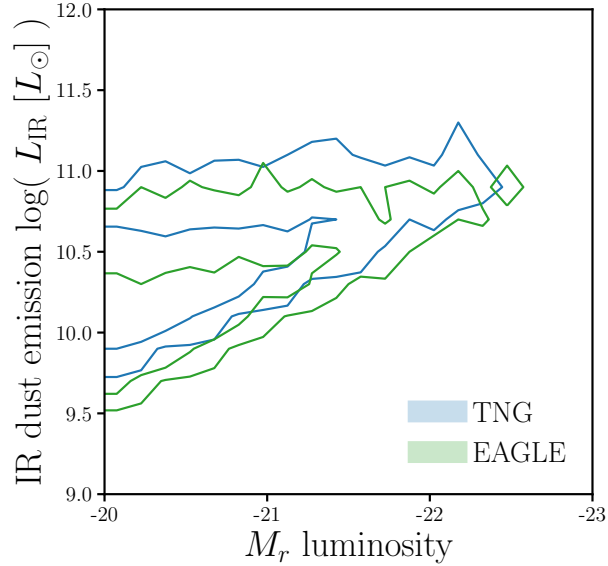


Figure 10. IR dust emission luminosity predicted by the FADE with median parameter values of the TNG (blue) and EAGLE (green) posteriors as a function of M_r . The dust emission is estimated assuming the [da Cunha et al. \(2008\)](#) energy balance. Despite reproducing the same SDSS UV and optical color-magnitude relations, *the FADE predicts significantly different IR dust emission for TNG and EAGLE*. Therefore, including IR observations will significantly improve the constraints on FADE parameters and allow us to better differentiate galaxy formation models.

comparison to observations, we would not be able to differentiate between the different galaxy physics prescriptions in the simulations. Hence, current limitations in our understanding of dust is a major bottleneck for investigating galaxy formation using simulations. *In the next paper of the series, Starkenburg et al. (in preparation), we will examine whether we can compare the prescriptions for star formation quenching in different galaxy formation models once we include the FADE framework.*

Fortunately, there are many avenues for improving our understanding of dust with a forward modeling approach. In this work, we used a restrictive $M_r < -20$ complete SDSS galaxy sample. *Figure 9 illustrates that our completeness cut limits the number of quiescent galaxies below $M_* < 10^{11} M_\odot$.* Instead of imposing a completeness limit, we can include the actual SDSS selection function in the forward model (*e.g.* [Dickey et al. 2020](#)). *This would allow us to compare the simulations with FADE to the entire SDSS sample, a substantially larger sample with a wider range of galaxies.*

Upcoming surveys, such as the Bright Galaxy Survey (BGS) of the Dark Energy Spectroscopic Instrument (DESI; [DESI~Collaboration et al. 2016](#); [Ruiz-Macias et al. 2020](#)) and galaxy evolution survey of the Prime Focus Spectrograph (PFS; [Takada et al. 2014](#); [Tamura et al. 2016](#)), will also vastly expand galaxy observations. *BGS, for instance, will measure $10\times$ the number of galaxy spectra as SDSS out to $z \sim 0.4$ and with its $r \sim 20$ magnitude limit will probe a significant number of low redshift dwarf galaxies. Such an observational sample will allow us to place tighter constraints on the FADE parameters, which may enable comparisons of the underlying galaxy formation models, and shed light on dust in a broader range of galaxies.*

In this work, we also only used observables derived from UV and optical photometry, which means that we have only examined one side of the impact that dust has on galaxy spectra. While dust attenuates light in the optical and UV, it emits light in IR. In fact, even though the TNG and EAGLE simulations reproduce the same UV and optical color-magnitude relations with the FADE, they predict significantly different dust emission in the IR. In Figure 10, we present IR dust emission luminosity, L_{IR} , predicted by the FADE with median parameter values of the TNG (blue) and EAGLE (green) posteriors as a function of the r -band absolute magnitude, M_r . The dust emissions are estimated using the standard energy balance assumption — *i.e.* all starlight attenuated by dust is reemitted in the IR (da Cunha et al. 2008).

Despite reproducing the same SDSS UV and optical color-magnitude relations, the FADE predicts significantly different IR dust emission for TNG and EAGLE. For TNG, the FADE predicts an overall ~ 0.3 dex ($2\times$) higher dust emissions than for EAGLE. Higher dust emission for TNG is consistent with the higher c_τ we infer for TNG (Figure 4). It is also consistent with the fact that TNG predicts bluer galaxies and more luminous quiescent galaxies with red $FUV-NUV$ color than EAGLE (Figure 2). Since IR dust emission measures the total dust attenuation, IR observations would specifically constrain the FADE and therefore break degeneracies between dust and the galaxy physics in simulations. Upcoming will provide crucial observation on this front. BGS, for instance, will have IR photometry from NEOWISE (Meisner et al. 2018). James Webb Space Telescope (JWST) will also provide valuable IR observations.

6. SUMMARY

In this work, we present the FADE, a framework for statistically applying dust attenuation to simulated galaxy populations. It uses a parameterization of the attenuation curves motivated from observations (Noll et al. 2009) and a flexible method for sampling the attenuation curve parameters that includes correlations with galaxy properties (M_* and SSFR). We apply the FADE to three state-of-the-art hydrodynamical simulations (SIMBA, TNG, and EAGLE) and forward model the optical and UV color-magnitude relations. We then compare the forward modeled simulations to a $M_r < -20$ complete SDSS galaxy sample using likelihood-free inference. Based on this comparison, we find the following results:

- Dust attenuation is essential for simulations to reproduce observations. Without dust attenuation, all of the hydrodynamical simulations struggle to reproduce the observed UV and optical color-magnitude relation.
- With the FADE, the TNG and EAGLE simulations are able to produce UV and optical color-magnitude relations in good agreement with SDSS observations. SIMBA, however, overpredicts a substantial starburst galaxy population and in order to reproduce observations, these galaxies require both high attenuation and reddening, which goes against the observed attenuation-slope relation.
- The attenuation curves predicted by the FADE for TNG and EAGLE are in excellent agreement with the observed attenuation-slope relation. They also closely reproduce the observed

attenuation curves of star-forming galaxies. The success of the FADE in reproducing these observations, which were not included in the comparison, highlights the advantages of a forward modeling approach.

- Lastly, the FADE sheds light on dust attenuation in quiescent galaxies, which remains poorly understood due to observations challenges. **We find that simulated quiescent galaxies require significant UV and optical attenuation with shallow attenuation curves.** For all galaxies, we find that more massive galaxies have higher overall dust attenuation while galaxies with higher SSFR have steeper attenuation curves.

Our results clearly demonstrate that the FADE and a forward modeling approach provides key insights into dust attenuation. For those uninterested in dust, the FADE also provides a framework for marginalizing over dust when comparing simulations to observations. In the case of SIMBA, we found that the FADE dust attenuation is insufficient to accurately reproduce observations due to its excess starburst population. For TNG and EAGLE, however, dust attenuation is highly degenerate with differences in their galaxy physics prescriptions. Even though TNG and EAGLE predict galaxy populations with significantly different physical properties, there is enough uncertainty in our understanding of dust that by adjusting attenuation alone both TNG and EAGLE can reproduce the same SDSS observations. This also suggests that any comparisons across simulations must marginalize over dust attenuation or run the risk of overinterpretation. Therefore, our current understanding of dust, or lack of, limit our ability to distinguish between the various hydrodynamical models and is a major bottleneck for investigating galaxy formation using simulations.

The forward modeling approach we present offers many avenues for improving on our understanding of dust. In this paper, we used a relatively restrictive M_r complete SDSS galaxy sample. Comparison to a larger observed galaxy sample will place tighter constraints on FADE parameters and enable better differentiation between the simulations. One way to expand the observed galaxy sample would be to remove the M_r completeness limit by including the selection function to our forward model. Upcoming surveys, such as the DESI Bright Galaxy Survey and the PFS Galaxy Evolution Survey, will also soon provide much larger galaxy samples. Furthermore, IR observations, which measure dust emission and trace dust attenuation, also have the potential to tightly constrain the FADE parameters and therefore break degeneracies between dust and the galaxy physics in simulations. In future works, we will apply the FADE and a forward modeling approach to more statistically powerful samples and include IR observables in order to tightly constrain and reveal new insights into dust attenuation.

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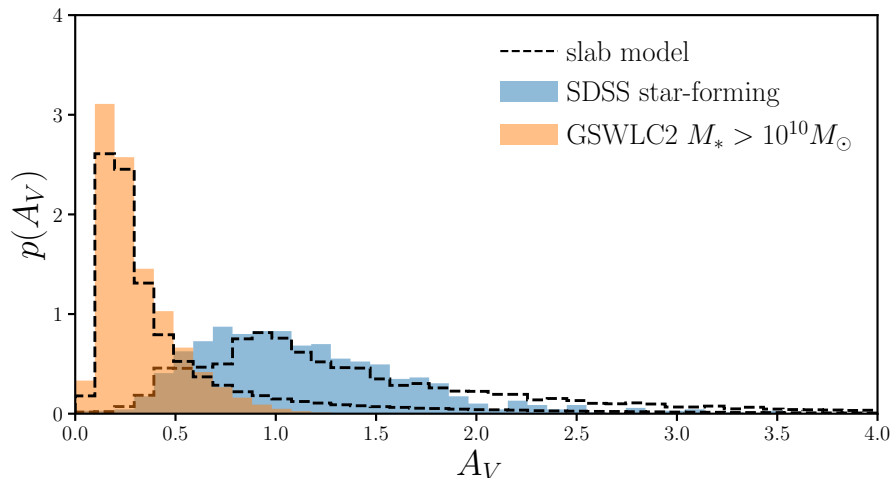


Figure 11. The A_V distributions generated from the slab model (Eq. 3; black dash) compared to $p(A_V)$ of star-forming galaxies in SDSS (blue) and of $M_* > 10^{10} M_\odot$ galaxies in the Salim et al. (2018) GSWLC2 sample (orange). The A_V values for both observations are derived using SED fitting (Brinchmann et al. 2004; Salim et al. 2018) while the A_V values for the slab model are generated using Eq. 3 with M_* and SSFR for SDSS and GSWLC2 also measured from SED fitting. The slab model is able to produce $p(A_V)$ in good agreement with $p(A_V)$ from both observations. Hence, it provides a sufficiently flexible prescription for our FADE.

APPENDIX

A. THE SLAB MODEL BASED EDA

In our FADE prescription, we use the slab model to determine A_V , the amplitude of attenuation, as a function of a randomly sampled inclination, i , and τ_V (see Eq. 3 in Section 3). The slab model is based on the assumption that dust in galaxies in slab-like geometry and illuminated by the stellar radiation source (Somerville & Primack 1999). For a given τ_V , the attenuation depends solely on the orientation of the galaxy. While this simplification reproduces the correlation between A_V and i found in observed star-forming galaxies (*e.g.* Conroy et al. 2010; Wild et al. 2011; Battisti et al. 2017; Salim & Narayanan 2020), it ignores the detailed star-to-dust geometry that impacts the attenuation curve. It also does not provide a well-motivated prescription for quiescent galaxies, which typically have elliptical morphologies. Despite its limitations, the slab model provides a robust empirical prescription that allows us to produce realistic distributions of A_V .

In Figure 11, we compare the A_V distributions, $p(A_V)$, of star-forming galaxies in SDSS (blue) and galaxies in the Salim et al. (2018) GSWLC2 sample (orange) to the $p(A_V)$ generated from the slab model (black dashed). The A_V values of the SDSS are derived using SED fitting from the Brinchmann et al. (2004) MPA-JHU catalog. The A_V values of the GSWLC2 galaxies are also derived from SED fitting UV and optical photometry from GALEX and SDSS observations as well as mid-IR photometry from WISE. We include all GSWLC2 galaxies, including quiescent galaxies, above $M_* > 10^{10} M_\odot$. We include slab model A_V distributions for SDSS and GSWLC2 individually. We

sample A_V for each SDSS and GSWLC2 galaxy: we uniformly sample $\cos i$ from 0 to 1 and derive τ_V (Eq. 4) with M_* and SSFR measured from SED fitting. We pick $m_{\tau, M_*}, m_{\tau, \text{SSFR}}, c_\tau$ values within the prior range (Table 1) to reproduce the SDSS and GSWLC2 $p(A_V)$ distributions by eye. The comparison reveals that the slab model can produce $p(A_V)$ in good agreement with both observed distributions. We therefore conclude that the slab model provides a sufficiently flexible prescription to sample a realistic distribution of A_V .

In addition to assuming the slab model, in the FADE, we also assume a linear dependence on M_* and SSFR in the V band optical depth, τ_V (see Eq. 4). This parameterization is motivated by observations that find significant correlation between A_V and M_* and SSFR (*e.g.* Garn & Best 2010; Battisti et al. 2016; Salim & Narayanan 2020). We take a closer look at this correlation using the GSWLC2 sample in Figure 12. We present the dependence of A_V on M_* (left panel) and SSFR (right panel). In the left panel, we divide the GSWLC2 galaxies by SSFR: $-11 < \log \text{SSFR} < -10.5$ (purple), $-10.5 < \log \text{SSFR} < -10$ (red), and $-10 < \log \text{SSFR}$ (orange). For each of the SSFR bins, we find significant $\log M_*$ dependence in A_V . Galaxies with higher SSFR have a stronger M_* dependence. In the right, we divide the galaxies by M_* : $9.5 < \log M_* < 10.5$ (blue) and $10.5 < \log M_* < 11.5$ (green). Although both M_* bins have some SSFR dependence, the dependence is stronger for galaxies with $M_* > 10^{10.5} M_\odot$. This stellar mass limit roughly corresponds to galaxies that are included in our forward model (see Figure 9). The M_* and SSFR dependence we find in A_V from the GSWLC2 sample is consistent with previous observations. Moreover, the M_* and SSFR dependence we find further motivates our FADE prescription.

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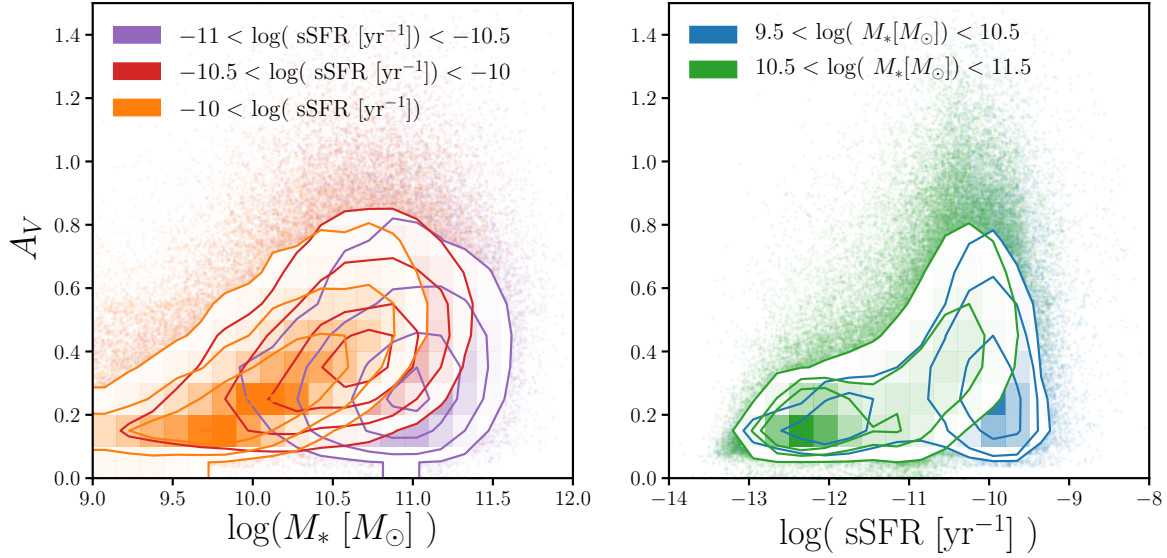


Figure 12. Dependence of A_V on M_* (left) and SSFR (right) for the Salim et al. (2018) GSWLC2 sample. In the left panel, we divide the GSWLC2 sample into bins of SSFR: $-11 < \log \text{SSFR} < -10.5$ (purple), $-10.5 < \log \text{SSFR} < -10$ (red), and $-10 < \log \text{SSFR}$ (orange). There is a significant M_* dependence in all of the SSFRbins. In the right panel, we divide the sample into bins of M_* : $9.5 < \log M_* < 10.5$ (blue) and $10.5 < \log M_* < 11.5$ (green). In the $\log M_* > 10.5$ bin, which roughly corresponds to our SDSS sample, we find significant SSFR dependence. The M_* and SSFR dependence in A_V we find in GSWLC2, which is consistent with previous observations, provides further motivation for our FADE prescription.

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