# SUPPLEMENTAL MATERIALS

### Ground-truth of benchmark images/video



Fig. S1: Ground-truth of eight small benchmark images.



Fig. S2: Ground-truth of three high-resolution benchmark images.



Fig. S3: Ground-truth of the benchmark video.

### RSE curves of Large images inpainting

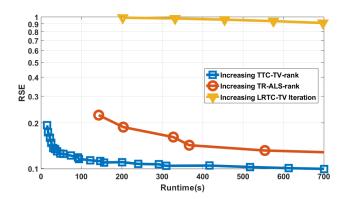


Fig. S4: Obtained RSE of TTC-TV, TR-ALS and LRTC-TV on the *Dolphin* benchmark image versus the total runtime for increasing TT-ranks or number of iterations.

### **Choice of tuning parameters**

All tuning parameters of the different methods used in Section 4 are listed below so that all reported results can be reproduced.

### TABLE S1: House

Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 140$
HaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 80, \epsilon = 1e-7, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 200, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(\mathbf{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{\rm adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 540
TMac-TT	thl = 0.03, tol = 1e-10, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [7, 7, 7, 7, 7, 7, 7]$
TTC	h = 22, Itr = 2, $R = [1, 6, 11, 11, 11, 17, 3]$
TTC-TV	$h=22, \lambda=0.2, \mathrm{Itr}=2, R=[1,6,11,11,11,17,3]$

### TABLE S2: River

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Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 140$
HaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 80, \epsilon = 1e-7, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 40, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(\mathcal{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{\rm adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 380
TMac-TT	thl = 0.03, tol = 1e-6, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [8, 8, 8, 8, 8, 8, 8]$
TTC	h = 22, Itr $= 2$ , $R = [1, 3, 14, 14, 14, 17, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = [1, 3, 14, 14, 14, 17, 3]$

#### TABLE S3: Bridge

Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 200$
HaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 180, \epsilon = 1e-7, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 180, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(\mathcal{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{\rm adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 480
TMac-TT	thl = 0.04, tol = 1e-5, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [7, 7, 7, 7, 7, 7, 7]$
TTC	h = 22, Itr $= 2$ , $R = [1, 5, 11, 11, 11, 17, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = [1, 5, 11, 11, 11, 17, 3]$

### TABLE S4: Man

Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 150$
HaLRTC	$\alpha = [1, 1, 1e-3], MaxItr = 240, \epsilon = 1e-7, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 40, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(A)}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\begin{array}{l} \lambda_1 = 0.5, \lambda_2 = 1000, \alpha = [\frac{1}{N}, \frac{1}{N}, \frac{1}{N}], \beta = [1, 1, 0] \\ \alpha_{\text{adj}} = 0, \text{rank}_{\text{adj}} = [2, 2, 2], \text{rank}_{\text{max}} = [8, 8, 8], \text{MaxItr} = 540 \end{array}$
TMac	$\alpha_{\rm adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 540
TMac-TT	thl = 0.04, tol = 1e-6, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [8, 8, 8, 8, 8, 8, 8]$
TTC	h = 22, Itr = 2, $R = [1, 2, 16, 16, 16, 19, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = [1, 2, 16, 16, 16, 19, 3]$

### TABLE S5: Lena

Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 110$
HaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 140, \epsilon = 1e-7, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 40, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(\mathcal{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 440
TMac-TT	thl = 0.05, tol = 1e-7, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [7, 7, 7, 7, 7, 7, 7]$
TTC	h = 22, Itr = 3, $R = [1, 2, 12, 14, 14, 26, 3]$
TTC-TV	h = 22, Itr = 2, $R = [1, 2, 12, 14, 14, 26, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = [1, 2, 12, 14, 14, 26, 3]$

## TABLE S6: Peppers

Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 120$
HaLRTC	$\alpha = [1, 1, 1e-3], MaxItr = 100, \epsilon = 1e-8, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 40, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(\mathbf{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [12, 12, 12], MaxItr = 540
TMac-TT	thl = 0.06, tol = 1e-7, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [9, 9, 9, 9, 9, 9, 9]$
TTC	h = 22, Itr $= 2$ , $R = [1, 2, 12, 16, 16, 25, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = [1, 2, 12, 16, 16, 25, 3]$

### TABLE S7: Baboon

	TABLE 57. Babbon
Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 120$
HaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 80, \epsilon = 1e-8, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 80, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{size}(\mathcal{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{\rm adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 460
TMac-TT	thl = 0.05, tol = 1e-8, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [6, 6, 6, 6, 6, 6, 6]$
TTC	h = 22, Itr $= 2$ , $R = [1, 2, 8, 8, 8, 20, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = [1, 2, 8, 8, 8, 20, 3]$

## TABLE S8: Airplane

Method	Tunning Parameters
TNN	$\alpha = 1, \rho = 0.01, \text{MaxItr} = 140$
HaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 160, \epsilon = 1e-7, \rho = 1e-6$
FaLRTC	$\alpha = [1, 1, 1e-3], \text{MaxItr} = 160, \epsilon = 1e-7, \mu = \frac{5\alpha}{\sqrt{\text{sizc}(\mathcal{A})}}, C = 0.6, L0 = 1e-6$
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TMac	$\alpha_{\rm adj} = 0$ , rank <sub>adj</sub> = [2, 2, 2], rank <sub>max</sub> = [8, 8, 8], MaxItr = 560
TMac-TT	thl = 0.06, tol = 1e-9, MaxItr = 1000
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [5, 5, 5, 5, 5, 5, 5]$
TTC	h = 22, Itr = 2, $R = [1, 3, 12, 12, 12, 16, 3]$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2, R = \begin{bmatrix} 1, 3, 12, 12, 12, 16, 3 \end{bmatrix}$

## TABLE S9: Dolphin

Method	Tunning Parameters
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2$

## TABLE S10: Water Nature Fall

Method	Tunning Parameters
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$
TTC-TV	$h = 22 \lambda = 0.2 \text{ Itr} = 2$

## TABLE S11: Orion nebula

Method	Tunning Parameters
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TR-ALS	$Max_{tot} = 1e - 3$ , $MaxItr = 300$
TTC-TV	$h = 22, \lambda = 0.2, \text{Itr} = 2$

## TABLE S12: Baseball Pitcher Mariano Rivera

Method	Tunning Parameters
LRTC-TV	$\lambda_1 = 0.5, \lambda_2 = 1000, \alpha = \left[\frac{1}{N}, \frac{1}{N}, \frac{1}{N}\right], \beta = [1, 1, 0]$
TR-ALS	$Max_{tot} = 1e-3$ , $MaxItr = 300$ , $R = [4, 4, 4, 4, 4, 4, 4, 4, 4, 4, 4]$
TTC	h = 22, Itr = 2, $R = [1, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5]$