

➤ **Motion, Distance, ...**

1. The acceleration of a particle moving along the  $x$ -axis at time  $t$  is given by  $a(t) = 2t - 6$ .

If at  $t = 1$ , the velocity of the particle is 3 and its position is  $\frac{1}{3}$ , then the position  $x(t) =$

(A)  $\frac{t^3}{3} - 6t^2 + 5t + \frac{1}{3}$

(B)  $\frac{t^3}{3} - 3t^2 + 8t - 5$

(C)  $\frac{t^3}{3} - 6t + 9$

(D)  $\frac{t^3}{3} - 3t^2 + 8t - \frac{7}{3}$

2. The velocity of a particle moving along the  $x$ -axis at any time  $t$  is given by  $v(t) = 3e^{-t} - t$ .

What is the average speed of the particle over the time interval  $0 \leq t \leq 3$ ?

(A) 0.873

(B) 1.096

(C) 1.273

(D) 1.482

3. A particle travels along a straight line with a velocity of  $v(t) = e^t(t^2 - 5t + 6)$  meters per second.

What is the average velocity of the particle over the time interval  $0 \leq t \leq 5$ ?

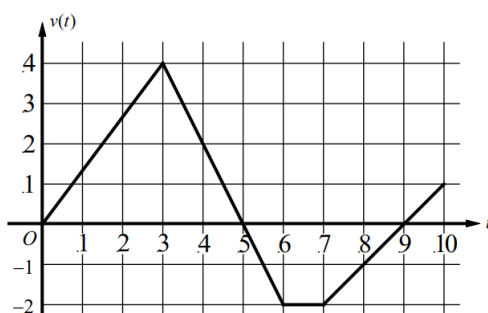
(A) 58.602

(B) 64.206

(C) 79.351

(D) 86.448

Questions 4-8 refer to the following situation.



A particle is moving along the  $x$ -axis. The velocity  $v$  of the particle at time  $t$ ,  $0 \leq t \leq 10$ , is given by the function whose graph is shown above.

4. At what value(s) of  $t$  does the particle change direction?

(A) 3 only

(B) 3 and 6

(C) 5 and 9

(D) 6 and 7

5. What is the total distance traveled by the particle over the time interval  $0 \leq t \leq 10$ ?

(A) 15.5

(B) 12

(C) 9.5

(D) 8

6. At what time  $t$  during the time interval  $0 \leq t \leq 10$  is the particle farthest to the right?

(A) 3

(B) 5

(C) 7

(D) 9

7. What is the velocity of the particle at time  $t = 4$ ?

(A) -2

(B) 2

(C) 5

(D) 7

8. What is the acceleration of the particle at time  $t = 4$ ?

(A) -2

(B) 2

(C) 5

(D) 7

9. A car is traveling on a straight road with position function given by  $s(t) = (4t^2 - 3)e^{-0.5t}$ , where  $s$  is measured in meters and  $t$  is measured in seconds. At time  $t = 0$  seconds the brakes are applied to stop the car. To the nearest meters, how far does the car travel from time  $t = 0$  to the moment the car stops?

(A) 9 (B) 10 (C) 11 (D) 12

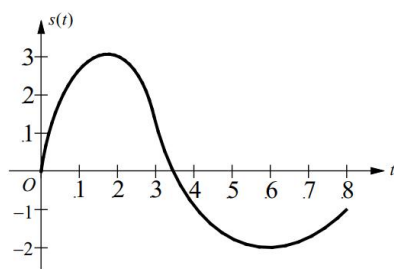
10. A particle moves along the  $x$ -axis with a velocity given by  $v(t) = t \cos(t^2 - 1)$  for  $t \geq 0$ .

- In which direction (left or right) is the particle moving at time  $t = 2$ ?
- Find the acceleration of the particle at time  $t = 2$ . Is the velocity of the particle increasing at time  $t = 2$ ? Justify your answer.
- Is the speed of the particle increasing at time  $t = 2$ ? Justify your answer.
- Given that  $x(t)$  is the position of the particle at time  $t$  and that  $x(0) = 4$ , find  $x(2.5)$ .
- During the time interval  $0 \leq t \leq 2.5$ , what is the greatest distance between the particle and the origin?
- Find the total distance traveled by the particle from  $t = 0$  to  $t = 2.5$ .

11. A particle moves along the  $y$ -axis with a velocity given by  $v(t) = 3t^2 - 14t + 8$  for  $t \geq 0$ .

At time  $t = 0$ , the position of the particle is  $y(0) = 2$ .

- Find the minimum acceleration of the particle.
- For what values of  $t$  is the particle moving downward?
- What is the average velocity of the particle on the closed interval  $[0, 3]$ ?
- What is the average acceleration of the particle on the closed interval  $[0, 3]$ ?
- Find the position of the particle at time  $t = 3$ .
- Find the total distance traveled by the particle from  $t = 0$  to  $t = 3$ .



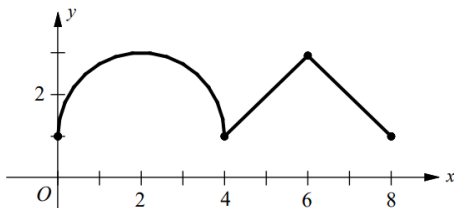
12. A particle moves along a horizontal line. The graph of the particle's position  $s(t)$  at time  $t$  is shown above for  $0 < t < 8$ . The graph has horizontal tangents at  $t = 2$  and  $t = 6$  and has a point of inflection at  $t = 3$ .

- What is the velocity of the particle at time  $t = 6$ ?
- The slope of tangent to the graph (not shown) at  $t = 4$  is  $-1$ . What is the speed of the particle at time  $t = 4$ ?
- For what values of  $t$  is the particle moving to the left?
- For what values of  $t$  is the velocity of the particle decreasing?
- On the interval  $2 < t < 3$ , is the speed of the particle increasing or decreasing? Give a reason for your answer.
- During what time intervals, if any, is the acceleration of the particle positive? Justify your answer.

➤ **Average value of a function**

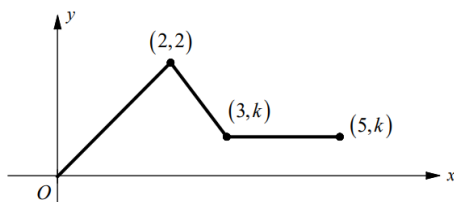
1. What is the average value of  $f(x) = \sqrt{x}(4-x)$  on the closed interval  $[0, 4]$ ?

- (A)  $\frac{7}{3}$       (B)  $\frac{21}{5}$       (C)  $\frac{32}{15}$       (D)  $\frac{35}{4}$



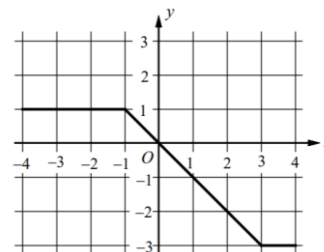
2. The graph of  $y = f(x)$  consists of a semicircle and two line segments. What is the average value of  $f$  on the interval  $[0, 8]$ ?

- (A)  $\frac{\pi+2}{4}$       (B)  $\frac{\pi+3}{4}$       (C)  $\pi+1$       (D)  $\frac{\pi+6}{4}$



3. The graph of  $y = f(x)$  consists of three line segments as shown above. If the average value of  $f$  on the interval  $[0, 5]$  is 1 what is the value of  $k$ ?

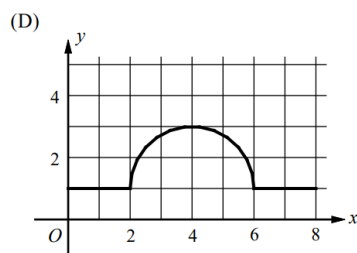
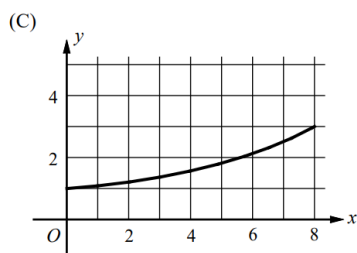
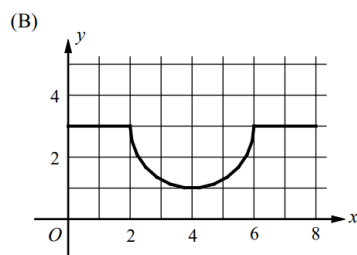
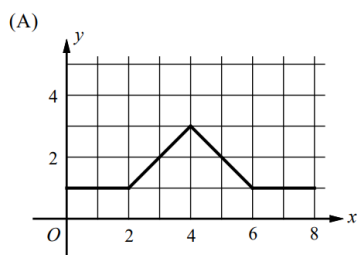
- (A)  $\frac{3}{5}$       (B)  $\frac{7}{10}$       (C)  $\frac{4}{5}$       (D)  $\frac{9}{10}$



Graph of  $f$

4. The function  $f$  is continuous for  $-4 \leq x \leq 4$ . The graph of  $f$  shown above consists of three line segments. What is the average value of  $f$  on the interval  $-4 \leq x \leq 4$ ?

5. On the closed interval  $[0, 8]$ , which of the following could be the graph of a function  $f$  with the property that  $\frac{1}{8-0} \int_0^8 f(t) dt > 2$ ?



6. Let  $f$  be the function defined by

$$f(x) = \begin{cases} \frac{1}{16}x^2 + 1 & \text{for } 0 \leq x \leq 4 \\ 3\sqrt{x} - x & \text{for } 4 < x \leq 9. \end{cases}$$

What is the average value of  $f$  on the closed interval  $0 \leq x \leq 9$ ?

- (A)  $\frac{65}{54}$       (B)  $\frac{35}{27}$       (C)  $\frac{85}{27}$       (D)  $\frac{55}{9}$

7. Let  $f$  be the function given by  $f(x) = x \cos(x^2)$ .

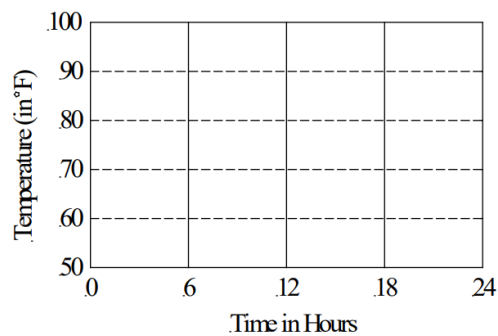
(a) Find the average rate of change of  $f$  on the closed interval  $[0, \sqrt{\pi}]$ .

(b) Find the average value of  $f$  on the closed interval  $[0, \sqrt{\pi}]$ .

(c) Find the average value of  $f'$  on the closed interval  $[0, \sqrt{\pi}]$ .

8. The temperature outside a house during a 24-hour period is given by  $F(t) = 75 + 15 \sin\left[\frac{\pi(t-6)}{12}\right]$ , for  $0 \leq t \leq 24$ , where  $F(t)$  is measured in degrees Fahrenheit and  $t$  is measured in hours.

(a) Sketch the graph of  $F$  on the grid below.



- (b) Find the average temperature, to the nearest degree, between  $t = 4$  and  $t = 10$ .
- (c) An air conditioner cooled the house whenever the outside temperature was 80 degrees or above. For what values of  $t$  was the air conditioner cooling the house?
- (d) The hourly cost of cooling the house is \$0.12 for each degree the outside temperature exceeds 80 degrees. What is the total cost, to the nearest cent, to cool the house for the 24 hour period?

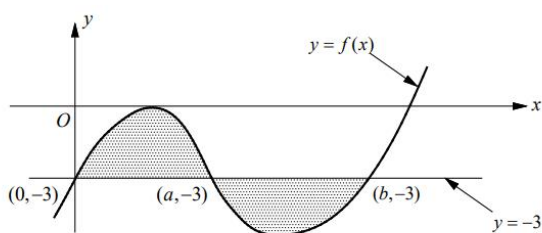
➤ **Area**

1. What is the area of the region enclosed by the graphs of  $f(x) = x + 2$  and  $g(x) = x^3 - 4x^2 + 6$ ?

- (A)  $\frac{193}{12}$       (B)  $\frac{218}{12}$       (C)  $\frac{253}{12}$       (D)  $\frac{305}{12}$

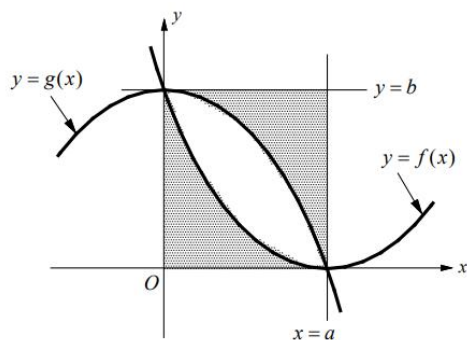
2. What is the area of the region in the first quadrant, bounded by the curve  $y = \sqrt[3]{x}$  and  $y = x$ ?

- (A)  $\frac{1}{5}$       (B)  $\frac{1}{4}$       (C)  $\frac{1}{3}$       (D)  $\frac{1}{2}$



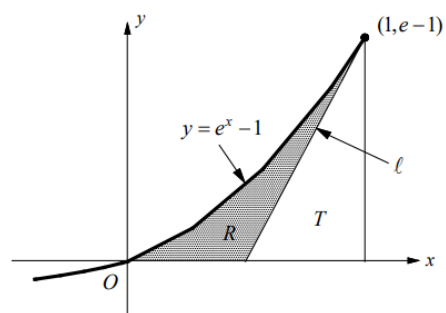
3. The curve  $y = f(x)$  and the line  $y = -3$ , shown in the figure above, intersect at the points  $(0, -3)$ ,  $(a, -3)$ , and  $(b, -3)$ . The sum of area of the shaded region enclosed by the curve and the line is given by

- (A)  $\int_0^a [3 - f(x)] dx + \int_a^b [-3 + f(x)] dx$   
 (B)  $\int_0^a [-3 + f(x)] dx + \int_a^b [3 - f(x)] dx$   
 (C)  $\int_0^a [f(x) + 3] dx + \int_a^b [-3 - f(x)] dx$   
 (D)  $\int_0^a [f(x) - 3] dx + \int_a^b [3 - f(x)] dx$



4. Which of the following is the area of the shaded region in the figure above?

- (A)  $\int_0^a [g(x) - f(x)] dx$   
 (B)  $\int_0^a [b + g(x) - f(x)] dx$   
 (C)  $\int_0^a [b - g(x) - f(x)] dx$   
 (D)  $\int_0^a [b - g(x) + f(x)] dx$



5. The figure above shows the graph of  $y = e^x - 1$  and the line  $\ell$  tangent to the graph at  $(1, e-1)$ .
- (a) Find the area of the triangular region  $T$ , which is bounded by the line  $x = 1$ , x-axis and  $\ell$ .
- (b) Find the area of region  $R$ , which is bounded by the graph of  $y = e^x - 1$ , x-axis and  $\ell$ .

➤ **Volume**

- The region in the first quadrant bounded by the graph of  $y = \sec x$ ,  $x = \frac{\pi}{3}$ , and the coordinate axes is rotated about the  $x$ -axis. What is the volume of the solid generated?  
  
 (A)  $\frac{\pi}{3}$                       (B)  $\frac{\pi}{2}$                       (C)  $\sqrt{3}\pi$                       (D)  $3\pi$
- The region enclosed by the graphs of  $y = e^{(x/2)}$  and  $y = (x-1)^2$  from  $x = 0$  to  $x = 1$  is rotated about the  $x$ -axis. What is the volume of the solid generated?  
  
 (A)  $\frac{11}{4}\pi$                       (B)  $2(e-1)\pi$                       (C)  $(e-\frac{3}{2})\pi$                       (D)  $(e-\frac{6}{5})\pi$
- Let  $R$  be the region between the graphs of  $y = 1 + \sin(\pi x)$  and  $y = x^3$  from  $x = 0$  to  $x = 1$ . The volume of the solid obtained by revolving  $R$  about the  $x$ -axis is given by

- (A)  $\pi \int_0^1 [1 + \sin(\pi x) - x^3] dx$   
 (B)  $\pi \int_0^1 [(1 + \sin(\pi x))^2 - x^6] dx$   
 (C)  $\pi \int_0^1 [1 + \sin(\pi x) - x^3]^2 dx$   
 (D)  $2\pi \int_0^1 [1 + \sin(\pi x) - x^3] dx$

- The region  $R$  is enclosed by the graph of  $y = \sqrt{x+1}$ , the line  $y = x-1$ , and the  $y$ -axis. The volume of the solid generated when is  $R$  rotated about the line  $y = 2$  is

- (A)  $\frac{13}{2}\pi$                       (B)  $\frac{20}{3}\pi$                       (C)  $\frac{49}{6}\pi$                       (D)  $9\pi$

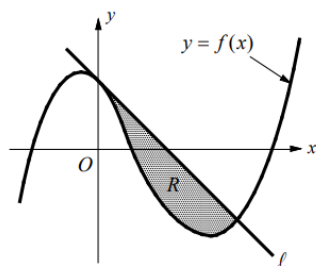
- The region  $R$  is enclosed by the graph of  $y = 3x - x^2$  and the line  $y = x$ . If the region  $R$  is rotated about the line  $y = -1$ , the volume of the solid that is generated is represented by which of the following integrals?

- (A)  $\pi \int_0^2 [3x - x^2 - x + 1]^2 dx$   
 (B)  $\pi \int_0^2 [(3x - x^2 + 1)^2 - (x+1)^2] dx$   
 (C)  $\pi \int_0^2 [(3x - x^2 + 1) - (x+1)]^2 dx$   
 (D)  $\pi \int_0^2 [(3x - x^2 - 1)^2 - (x-1)^2] dx$

- The region  $R$  is enclosed by the graph of  $y = x + \frac{3}{x}$  and the line  $y = 4$ . The volume of the solid generated when is  $R$  rotated about the  $x$ -axis is

- (A)  $\frac{16}{3}\pi$                       (B)  $4\pi$                       (C)  $6\pi$                       (D)  $\frac{15\pi}{2}$

7. The volume of the solid generated by revolving the region enclosed by the ellipse  $x^2 + 9y^2 = 36$  about the  $x$ -axis is
- (A)  $14\pi$                       (B)  $16\pi$                       (C)  $24\pi$                       (D)  $32\pi$
8. The volume of the solid generated by revolving the region bounded by the graphs of  $y = \sqrt{x}$ ,  $y = 2$ , and  $y$ -axis about the  $y$ -axis is
- (A)  $\frac{32}{5}\pi$                       (B)  $\frac{16}{3}\pi$                       (C)  $\frac{10}{3}\pi$                       (D)  $\frac{8}{3}\pi$



9. Let  $f$  be the function given by  $f(x) = x^3 - 2x^2 - x + \cos x$ . Let  $R$  be the shaded region bounded by the graph of  $f$  and the line  $\ell$ , which is the line tangent to the graph of  $f$  at  $x = 0$ , as shown above.
- (a) Find the equation of the line  $\ell$ .
- (b) Find the area of  $R$ .
- (c) Set up, but do not evaluate, an integral expression for the volume of the solid generated when  $R$  is revolved about the line  $y = 2$ .



➤ **Known Cross Section**

1. The base of a solid is the region enclosed by the graph of  $y = e^x$ , the coordinate axes, and the line  $x = 1$ . If the cross sections of the solid perpendicular to the  $x$ -axis are squares, what is the volume of the solid?

(A)  $\frac{e^2}{4}$       (B)  $\frac{e^2 - 1}{2}$       (C)  $\frac{e^2 + 1}{2}$       (D)  $e^2 - \frac{1}{2}$

2. The base of a solid is the region enclosed by the graph of  $y = \sqrt{x}$ , the  $x$ -axis, and the line  $x = 2$ . If each cross section perpendicular to the  $x$ -axis is an equilateral triangle, what is the volume of the solid?

(A)  $\frac{\sqrt{3}}{8}$       (B)  $\frac{\sqrt{3}}{6}$       (C)  $\frac{\sqrt{3}}{4}$       (D)  $\frac{\sqrt{3}}{2}$

4. The base of a solid  $S$  is the semicircular region enclosed by the graph of  $y = \sqrt{9 - x^2}$  and the  $x$ -axis. If the cross sections of  $S$  perpendicular to the  $x$ -axis are semicircles, what is the volume of the solid?

(A)  $\frac{20\pi}{3}$       (B)  $6\pi$       (C)  $\frac{9\pi}{2}$       (D)  $\frac{7\pi}{2}$

7. Let  $R$  be the region enclosed by the graph of  $y = 3\sqrt{x} - x$  and the  $x$ -axis. The region  $R$  models the surface of a small pond. At all points in  $R$  at a distance  $x$  from the  $y$ -axis, the depth of the water is given by  $g(x) = \frac{1}{\sqrt{x}}$ . What is the volume of the water in the pond?

(A)  $2\sqrt{3}$       (B) 6      (C)  $4\sqrt{3}$       (D) 9

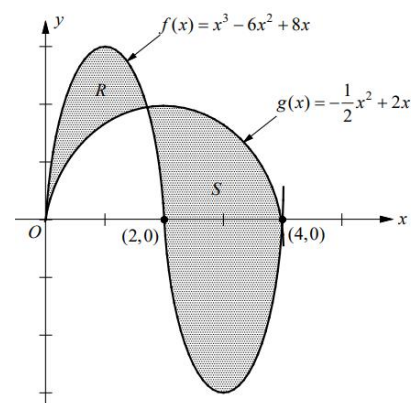
$x$ (meters)	0	2	4	6	8	10	12
$D(x)$ (meters)	.17	.15	.146	.142	.15	.138	.121

9. A 12 meter long tree trunk with circular cross sections of varying diameter is represented in the table above. The distance,  $x$ , of the tree trunk is measured from the ground and  $D(x)$  represents the diameter at that point.

- (a) Write an integral expression in terms of  $D(x)$  that represents the volume of the tree trunk between  $x = 0$  and  $x = 12$ .
- (b) Approximate the volume of the tree trunk between  $x = 0$  and  $x = 12$  using the data from the table and a midpoint Riemann sum with three subintervals of equal length.
- (c) Explain why there must be a value  $x$  for  $0 < x < 12$  such that  $D'(x) = 0$ ?

10. Let  $R$  and  $S$  be the region bounded by the graphs of  $f(x) = x^3 - 6x^2 + 8x$  and  $g(x) = -\frac{1}{2}x^2 + 2x$  as shown in the figure above.

- (a) Write, but do not evaluate, an integral expression that can be used to find the area of  $R$ .
- (b) Write, but do not evaluate, an integral expression that can be used to find the area of  $S$ .
- (c) The region  $R$  is the base of a solid. At all points in  $R$  at a distance  $x$  from the  $y$ -axis, the height of the solid is given by  $g(x) = 4e^{-x}$ . Find the volume of this solid.
- (d) The region  $S$  models the surface of a small pond. At all points in  $S$  at a distance  $x$  from the  $y$ -axis, the depth of the water is given by  $h(x) = 4 - \sqrt{x}$ . Find the volume of water in the pond.



➤ **Application of FTC**

- Oil is pumped out from a tank at the rate of  $\frac{20e^{(-0.1t)}}{1+e^{-t}}$  gallons per minute, where  $t$  is measured in minutes. To the nearest gallon, how many gallons of oil are pumped out from a tank during the time interval  $0 \leq t \leq 6$  ?  
  
 (A) 62                      (B) 78                      (C) 85                      (D) 93
- Pollutant is released into a lake at the rate of  $\frac{50e^{-t/2}}{\sqrt{t+1}}$  gallons per hour. To the nearest gallon, how many gallons of pollutant are released during the time interval  $0 \leq t \leq 12$  ?  
  
 (A) 53                      (B) 58                      (C) 66                      (D) 75
- Oil is pumped into an oil tank at the rate of  $S(t)$  gallons per hour during the time interval  $0 \leq t \leq 8$  hours. During the same time interval, oil is removed from the tank at the rate of  $R(t)$  gallons per hour. If the oil tank contained 200 gallons of oil at time  $t = 0$ , which of the following expressions shows the amount of oil in the tank at time  $t = 6$  hours?  
  
 (A)  $200 + S(6) - R(6)$   
 (B)  $200 + S'(6) - R'(6)$   
 (C)  $200 + \int_0^6 (S(t) - R(t)) dt$   
 (D)  $200 + \int_0^6 (S'(t) - R'(t)) dt$
- The rate at which people enter a supermarket, measured in people per hour on a given day, is modeled by the function  $S$  defined by  $S(t) = \frac{720}{t^2 - 28t + 205}$ , for  $6 \leq t \leq 22$ . To the nearest whole number, how many people entered the supermarket from time  $t = 6$  to  $t = 22$  ?  
  
 (A) 426                      (B) 475                      (C) 524                      (D) 582
- The height of the water in a cylindrical storage tank is modeled by a differential function  $h(t)$ , where  $h$  is measured in meters and  $t$  is measured in hours. At time  $t = 0$  the height of the water in the tank is 8 meters. During the time interval  $0 \leq t \leq 20$  hours, the height is changing at the rate  $h'(t) = 0.01t^3 - 0.3t^2 + 2.2t - 1.5$  meters per hour. What is the maximum height of the water in meters during the time period  $0 \leq t \leq 20$  ?  
  
 (A) 28.156                      (B) 30.108                      (C) 32.654                      (D) 33.975
- Water is pumped into a tank at a constant rate of 8 gallons per minute. Water leaks out of the tank at the rate of  $\frac{1}{2}t^{2/3}$  gallons per minute, for  $0 \leq t \leq 90$  minutes. At time  $t = 0$ , the tank contains 50 gallons of water.  
  
 (a) How many gallons of water leak out of the tank from time  $t = 0$  to  $t = 10$  minutes?  
 (b) How many gallons of water are in the tank at time  $t = 10$  minutes?  
 (c) Write an expression for  $f(t)$ , the total number of gallons of water in the tank at time  $t$ .  
 (d) At what time  $t$ , for  $0 \leq t \leq 90$ , is the amount of water in the tank a maximum?

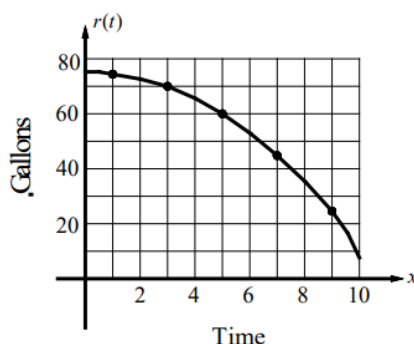
7. The rate at which the amount of granules of plastic at a toy factory is changing during a workday is modeled by  $P(t) = 5 - 2\sqrt{x} - 4\sin(\frac{x^2}{12})$  tons per hour, where  $0 \leq t \leq 8$ . At the beginning of the workday ( $t = 0$ ), the factory has 6 tons of granules of plastic.

- Find  $P'(3)$ . Using correct unit, interpret your answer in the context of the problem.
- At what time during the 8 hours was the amount of granules of plastic decreasing most rapidly?
- What was the maximum amount of granules of plastic at the factory during the 8 working hours?

8. For  $0 \leq t \leq 60$ , the rate of change of the number of mosquitoes at time  $t$  days is modeled by  $f(t) = 6\sqrt{t} \sin(\frac{t}{6})$  mosquitoes per day. There are 1200 mosquitoes at time  $t = 0$ .

- At time  $t = 20$ , is the number of mosquitoes increasing or decreasing?
- According to the model, how many mosquitoes will be there at time  $t = 60$ .
- To the nearest whole number, what is the maximum number of mosquitoes for  $0 \leq t \leq 60$ ?

9. Water leaks from a tank at a rate of  $r(t)$  gallons per hour. The graph of  $r$ , for the time interval  $0 \leq t \leq 10$  hours, is shown at the right. Use the midpoint Riemann sum with five intervals of equal length to estimate the total amount of water leaked out during the first 10 hours.



➤ **Length of a curve**

1. What is the length of the curve of  $y = \frac{1}{3}(x^2 + 2)^{3/2}$  from  $x = 1$  to  $x = 2$ ?  
  
(A)  $\frac{8}{3}$                       (B)  $\frac{10}{3}$                       (C) 4                      (D)  $\frac{14}{3}$
2. Which of the following integrals gives the length of the graph of  $y = \ln(\sin x)$  between  $x = \frac{\pi}{3}$  to  $x = \frac{2\pi}{3}$ ?  
  
(A)  $\int_{\pi/3}^{2\pi/3} \csc^2 x \, dx$   
(B)  $\int_{\pi/3}^{2\pi/3} \sqrt{1 + \cot x} \, dx$   
(C)  $\int_{\pi/3}^{2\pi/3} \csc x \, dx$   
(D)  $\int_{\pi/3}^{2\pi/3} \sqrt{1 + \csc^2 x} \, dx$
3. Which of the following integrals gives the length of the graph of  $y = \frac{1}{3}x^{3/2} - x^{1/2}$  between  $x = 1$  to  $x = 4$ ?  
  
(A)  $\frac{1}{2} \int_1^4 \left( \sqrt{x} + \frac{1}{\sqrt{x}} \right) dx$   
(B)  $\frac{1}{2} \int_1^4 \left( \sqrt{x} - \frac{1}{\sqrt{x}} \right) dx$   
(C)  $\frac{1}{2} \int_1^4 \left( 1 + \sqrt{x} + \frac{1}{\sqrt{x}} \right) dx$   
(D)  $\frac{1}{2} \int_1^4 \left( 1 + \sqrt{x} - \frac{1}{\sqrt{x}} \right) dx$
4. What is the length of the curve of  $y = \ln(x^2 + 1) - x$  from  $x = 0$  to  $x = 3$ ?  
  
(A) 1.026                      (B) 1.826                      (C) 2.227                      (D) 3.135
5. If the length of a curve from  $(0, -3)$  to  $(3, 3)$  is given by  $\int_0^3 \sqrt{1 + (x^2 - 1)^2} \, dx$ , which of the following could be an equation for this curve?  
  
(A)  $y = \frac{x^3}{3} - \frac{x}{3} - 3$   
(B)  $y = \frac{x^3}{3} - 3x - 3$   
(C)  $y = \frac{x^3}{3} - x - 3$   
(D)  $y = \frac{x^3}{3} + x - 3$

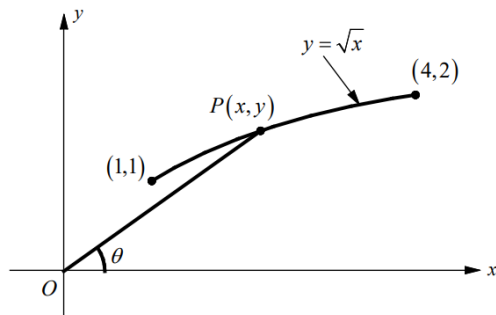
6. If  $F(x) = \int_1^{x^2} \sqrt{t+1} \, dt$ , what is the length of the curve of from  $x = 1$  to  $x = 2$ ?

(A)  $\frac{8}{3}$

(B)  $\frac{10}{3}$

(C)  $\frac{15}{3}$

(D)  $\frac{17}{3}$



7. The figure above shows a point,  $P(x,y)$ , moving on the curve of  $y = \sqrt{x}$ , from the point  $(1,1)$  to the point  $(4,2)$ . Let  $\theta$  be the angle between  $\overline{OP}$  and the positive  $x$ -axis.

(a) Find the  $x$ - and  $y$ -coordinates of point  $P$  in terms of  $\cot \theta$ .

(b) Find the length of the curve from the point  $(1,1)$  to the point  $(4,2)$ .

(c) If the angle  $\theta$  is changing at the rate of  $-0.1$  radian per minute, how fast is the point  $P$  moving along the curve at the instant it is at the point  $(3,\sqrt{3})$ ?