

Report on Hyperbolic Community detection

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1 Introduction

The objective of this report is to give tools and insight to execute and run the current project. Learning embedding within the Poincaré model is a difficult task much more than Euclidean usual learning. Optimization in hyperbolic space often leads to machine precision issues and tweaking very precisely hyperparameters. Furthermore, coordinate of vectors is meaningful contrary to Euclidean, thus most centered element often means most general concept or in our work a most central nodes (e.g. nodes with high degree relatively to others). This last point is especially important when developing a cost function using negative sampling, indeed sampling negative nodes randomly will accentuate the initial behaviour while sampling nodes based on the degree will soften it.

In this document we will go through issues encountered, by showing examples of errors that can occur and behaviour depending on model tuning.

2 KMeans and EM algorithm within Poincaré model

2.1 Barycenter hyper-parameters

2.2 EM: Machine precision

What to do : never clamp unnormalised wik

2.3 EM: Updating parameters

Updating μ : Because of the gradient descent (or ascent) used for updating μ , this step is subject to failure or taking more or less time to process. Let be the two initialisations possible to start the gradient descent:

$$\begin{aligned} \circ \quad b_k &= \frac{1}{n} \sum_{i=1}^n x_i \\ \circ \quad b_k &= \frac{1}{\sum_{j=1}^n w_{jk}} \sum_{i=1}^n x_i w_{ik} \end{aligned}$$

Obviously the second initialisation will lead to make less iteration to reach the convergence.

3 Learning embeddings

3.1 Batch, Mini-batch, sum or mean

3.2 Negative sampling

3.3 Compareason of optimization methods

3.4 Going out of the ball border