Adult Mortality in the Metropolis of London 1100–1850

Supplement: Code structure, data source and processing

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Prerequisites

The calculations were made in R using R-Studio. The structure of the code is essentially based on the structure of the text. The raw code is in the file order_of_code.R. The file extended with Markdown is order_of_code-doc.RMD and the file order_of_code-doc.pdf is generated from it.

The code makes extensive use of the function **source** to call external code. Thus, the main part of the code remains slim, well structured and readable.

Note: The base path for rmd files is the folder in which they are located, not the r-project. Consequently, order_of_code.R and order_of_code-doc.RMD are both located in the root folder of the project.

Install required packages, set some options and link the sources for the helper functions.

Remark: The current version of osmplotr has to be installed from github using devtools::install_github ("ropensci/osmplotr").

require(pacman) | install.packages("pacman")

Lade nötiges Paket: pacman

[1] TRUE

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```
pacman::p_load(dplyr, fitdistrplus, flexsurv, ggplot2, gridExtra, kableExtra,
               mortAAR, nlme, osmplotr, reshape2, rgdal, HMDHFDplus, Metrics,
               svMisc, tibble, tidyr, cowplot, MortalityLaws, rio,
               coda, rjags, runjags, demogR, sf, rnaturalearth, readxl,
               ggrepel)
options(scipen = 999)
options(dplyr.summarise.inform = FALSE)
source("./functions/bayes_cat_poisson.R")
source("./functions/gomp_MLE.R")
source("./functions/gomp_MLE_adapted.R")
source("./functions/gomp_MLE_interval.R")
source("./functions/gomp anthr age.R")
source("./functions/gomp anthr age r.R")
source("./functions/gomp_bayes_known_age.R")
source("./functions/gomp_known_age_r.R")
source("./functions/helper_functions.R")
source("./functions/lt_MC.R")
source("./functions/lt_MC_Gomp.R")
RNGkind("L'Ecuyer-CMRG") # conservative random number generator to avoid periodicity
```

Important for saving time: Decide to run extensive code anew (app. 6~h~+). In addition, you can set the folder for preprocessed files.

```
runCodeNew <- FALSE
#runCodeNew <- TRUE

saveFileDir = "preprocessed_files"
if (saveFileDir %in% list.files(getwd()))
{}else{
    dir.create(file.path(".", saveFileDir), showWarnings = FALSE )
}</pre>
```

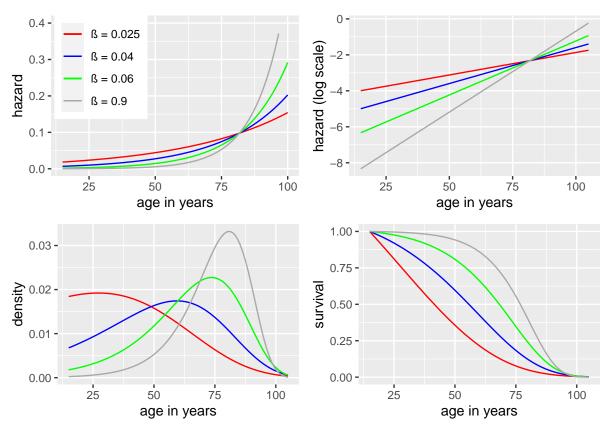
NULL

1 Chapter 01 Introduction

Figure 1: Exemplary life table curves generated by Gompertz functions with different β parameters.

source("./chapter_01_introduction/gompertz_distribution.R")

Saving 6.5×4.5 in image

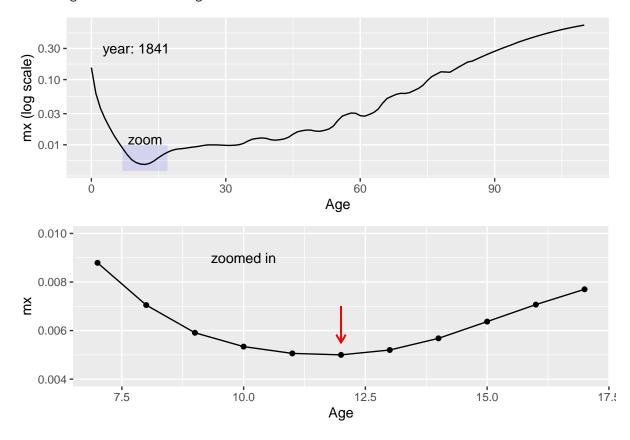


2 Chapter 02 Materials and methods

Figure 3: Hazard curve for HMD UK data of the year 1841.

source("./chapter_02_materials_and_methods/hazard_curve.R")

Saving 6.5 x 4.5 in image



3 Chapter 03 Data

Figure 4: Major cemeteries in Greater London 1100–1850 used in the present study.

source("./chapter_03_data/London_places.R")

Data (c) OpenStreetMap contributors, ODbL 1.0. https://www.openstreetmap.org/copyright
Saving 6.5 x 4.5 in image

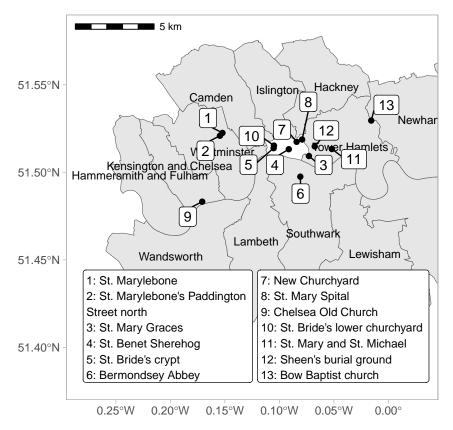
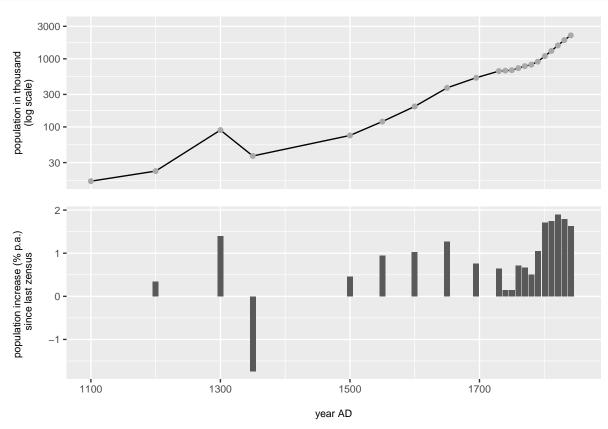


Figure 5: Population development of London, compiled from Finlay/Shearer (1986), 39 table 1; Landers (1993), 41; 179 table 5.7; Weinreb et al. (2008), 655–657.

```
source("./chapter_03_data/London_population.R")
grid::grid.newpage()
grid::grid.draw(rbind(london_pop1, london_pop2))
```



Footnote 6: Re-calculation of population increase rates of London from RAZZELL/SPENCE (2007). Calculated in $./chapter_03_data/London_population.R$

knitr::kable(razz_df, caption = "Re-calculation of population increase rates of London from Razzell/
kableExtra::kable_styling(latex_options = "HOLD_position")

Table 1: Re-calculation of population increase rates of London from Razzell/Spence 2007.

| date | population | rate.per.year |
|------|------------|---------------|
| 1520 | 55000 | NA |
| 1600 | 200000 | 0.016 |
| 1650 | 400000 | 0.014 |
| 1700 | 575000 | 0.007 |
| 1750 | 675000 | 0.003 |
| 1801 | 960000 | 0.007 |
| 1851 | 2685000 | 0.021 |
| | | |

4 Chapter 04 Results

Preprocessing of data used in figure 6: Estimated modal ages.

4.1 Historical life tables

4.1.1 Written sources and pre-processing

Basic statistics

The data is referenced and aggregated in "./chapter_04_results/historical_lifetables.R". In this file, all records from individual preprocessing files located in "./liftables_preprocessed/" are sourced. The corresponding data files are stored in "./data/".

English_Peers.R, russell.txt, Source: LA POUTRÉ/JANSSEN (2021), table 2

```
source("./chapter_04_results/historical_lifetables.R")
kable(peers_ranges, caption = "English Peers") %>%
kableExtra::kable_styling(latex_options = "HOLD_position")
```

Table 2: English Peers

| parameter | modes | HDI.ranges |
|-----------|---------|---------------|
| beta | 0.0613 | 0.0559-0.0660 |
| M | 58.1758 | 56.4-59.8 |
| e20 | 33.4148 | NA |
| e25 | 29.4926 | NA |

Medieval England.R, Christ church monks.txt, Source: HATCHER et al. (2006), 28 table 2

```
kable(monks_ranges, caption = "Christ Church monks") %>%
kableExtra::kable_styling(latex_options = "HOLD_position")
```

Table 3: Christ Church monks

| parameter | modes | HDI.ranges |
|-----------|---------|---------------|
| beta | 0.0461 | 0.0398-0.0523 |
| M | 52.7659 | 48.9-56.0 |
| e20 | 31.0948 | NA |
| e25 | 27.7530 | NA |

 $\label{london_1728_1840.R} London_1728_1840.R, \ Mortality_bills_1728_1840.txt, \ Source: \ Roberts/Cox\ (2003),\ 304\ Table\ 6.5; > 100\ years\ and\ < 1\ year\ collapsed$

Table 4: London Mortality bills 1728-1840.

| parameter | ranges |
|-----------|---------------|
| beta | 0.0326-0.0418 |
| M | 43.3-54.8 |

Table 5: London Mortality bills 1728-1840, corrected for population growth.

| parameter | ranges |
|-----------|--------------|
| beta_r | 0.034-0.0507 |
| r | 46-64.3 |
| r | 0.002-0.019 |

London_1841_raw_all.R, London_1841_raw.txt, Source: Graham (1842), 19 table q.

Table 6: Census data for London from 1841.

| parameter | modes | HDI.ranges |
|-----------|---------|---------------|
| beta | 0.0547 | 0.0510-0.0585 |
| M | 60.4164 | 58.9-61.7 |

English_Mortality.R, wrigley_et_al_1997_england_1640-1809.txt, Source: WRIGLEY et al. (1997), 290 table 6.19

Table 7: English mortality data.

| parameter | ranges |
|-----------|---------------|
| beta | 0.0438-0.0608 |
| M | 52.2-67.4 |

HMD_UK_ranges.R

The data from the Human Mortality Database (https://mortality.org/) were retrieved with a personal account using the R package HMDHFDplus. Therefore, we only provide the processed data here.

```
kable(HMD_UK_ranges, caption = "Human Mortality Database UK.") %>%
kableExtra::kable_styling(latex_options = "HOLD_position")
```

Table 8: Human Mortality Database UK.

| parameter | ranges |
|-----------|-------------|
| beta | 0.05-0.0654 |
| M | 64.2-70.2 |

Marylebone.R

Data are hard coded in the code. Sources: MILES et al. (2008), 97–103 table 32 (St Marylebone); HENDERSON et al. (2015), 81 (St Marylebone north of Paddington street)

```
source("./lifetables_processing/Marylebone.R")
kable(Marylebone_ranges, caption = "St Marylebone.") %>%
  kableExtra::kable_styling(latex_options = "HOLD_position")
```

Table 9: St Marylebone.

| parameter | modes | HDI.ranges |
|-----------------------|---------|---------------|
| Marylebone beta | 0.0526 | 0.0435-0.0618 |
| Marylebone M | 54.2470 | 49.5-59.3 |
| Marylebone north beta | 0.0588 | 0.0496-0.0682 |
| Marylebone north M | 55.6570 | 51.3-59.9 |

Extended statistics

```
kable(peers_result, caption = "English Peers.") %>%
  kableExtra::kable_styling(latex_options = c("HOLD_position", "scale_down"))
```

Table 10: English Peers.

| | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|---|-----------------|-----------------|------------|------------|------------|---------|-----------|---------|------------|------------|
| a | 1.000356 | 1.001061 | 0.0044095 | 0.0043879 | 0.0043263 | 11315.3 | 0.0000044 | 0.95 | 0.0035238 | 0.0053575 |
| b | 1.000307 | 1.000854 | 0.0609452 | 0.0609518 | 0.0612976 | 11121.9 | 0.0000244 | 0.95 | 0.0559415 | 0.0660412 |
| M | 1.000196 | 1.000696 | 58.1500750 | 58.1648975 | 58.1757927 | 20660.4 | 0.0059675 | 0.95 | 56.4492001 | 59.8036275 |

```
kable(monks_result, caption = "Christ Church monks.") %>%
kableExtra::kable_styling(latex_options = c("HOLD_position", "scale_down"))
```

Table 11: Christ Church monks.

| start | end | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|-------|------|-----------|-----------------|-----------------|------------|------------|------------|---------|-----------|---------|------------|------------|
| 1395 | 1505 | alpha | 1.000569 | 1.001661 | 0.0102993 | 0.0102563 | 0.0100488 | 13991.9 | 0.0000096 | 0.95 | 0.0081076 | 0.0125497 |
| 1395 | 1505 | beta | 1.000498 | 1.001436 | 0.0459467 | 0.0459287 | 0.0461060 | 13623.6 | 0.0000273 | 0.95 | 0.0397953 | 0.0523389 |
| 1395 | 1505 | M | 1.000504 | 1.001504 | 52.5281106 | 52.6296486 | 52.7658924 | 15808.5 | 0.0143226 | 0.95 | 48.9344189 | 55.9631681 |

Table 12: London Mortality bills 1728-1840.

| | | DODE D. L. | DODE II OI | | 37.11 | 36.3 | Poo | MOOR | YYYNY | TTT TI | ****** |
|-------|-----------|-----------------|-----------------|------------|------------|------------|---------|-----------|---------|------------|------------|
| year | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
| X1728 | alpha | 1.000087 | 1.000306 | 0.0146842 | 0.0146345 | 0.0145833 | 17556.5 | 0.0000101 | 0.95 | 0.0121424 | 0.0173529 |
| X1728 | beta | 1.000115 | 1.000412 | 0.0349280 | 0.0349276 | 0.0347502 | 17418.0 | 0.0000202 | 0.95 | 0.0296810 | 0.0401486 |
| X1728 | M | 1.000083 | 1.000299 | 44.6441200 | 44.8860914 | 45.5314756 | 17327.3 | 0.0224261 | 0.95 | 38.6469401 | 50.0270569 |
| X1730 | alpha | 1.000130 | 1.000390 | 0.0156561 | 0.0155984 | 0.0155550 | 17707.3 | 0.0000113 | 0.95 | 0.0127651 | 0.0186532 |
| X1730 | beta | 1.000044 | 1.000181 | 0.0325647 | 0.0325599 | 0.0325660 | 17242.0 | 0.0000212 | 0.95 | 0.0271489 | 0.0380817 |
| X1730 | M | 1.000124 | 1.000377 | 42.2325103 | 42.5795321 | 43.3073366 | 17007.1 | 0.0285150 | 0.95 | 34.7635858 | 49.1029390 |
| X1740 | alpha | 1.000404 | 1.001423 | 0.0153988 | 0.0153491 | 0.0151995 | 17959.5 | 0.0000100 | 0.95 | 0.0128421 | 0.0180871 |
| X1740 | beta | 1.000376 | 1.001376 | 0.0337368 | 0.0337428 | 0.0337806 | 17712.7 | 0.0000192 | 0.95 | 0.0286838 | 0.0387413 |
| X1740 | M | 1.000496 | 1.001609 | 43.0631632 | 43.3280277 | 43.9606200 | 17454.0 | 0.0235235 | 0.95 | 36.6700553 | 48.6880952 |
| X1750 | alpha | 1.000135 | 1.000198 | 0.0151763 | 0.0151270 | 0.0150364 | 18259.1 | 0.0000101 | 0.95 | 0.0125377 | 0.0178563 |
| X1750 | beta | 1.000114 | 1.000178 | 0.0342964 | 0.0342869 | 0.0341703 | 18177.8 | 0.0000196 | 0.95 | 0.0290894 | 0.0394288 |
| X1750 | M | 1.000179 | 1.000275 | 43.5924225 | 43.8460270 | 44.4983607 | 17767.1 | 0.0230817 | 0.95 | 37.4073951 | 49.2703888 |
| X1760 | alpha | 1.000177 | 1.000629 | 0.0145817 | 0.0145330 | 0.0143877 | 17316.9 | 0.0000100 | 0.95 | 0.0120971 | 0.0172323 |
| X1760 | beta | 1.000136 | 1.000506 | 0.0350143 | 0.0350086 | 0.0350484 | 17001.2 | 0.0000202 | 0.95 | 0.0298241 | 0.0401131 |
| X1760 | M | 1.000187 | 1.000641 | 44.8612069 | 45.0945299 | 45.4484334 | 17136.0 | 0.0220610 | 0.95 | 39.0545641 | 50.2289914 |
| X1770 | alpha | 1.000210 | 1.000234 | 0.0143004 | 0.0142472 | 0.0140950 | 17376.2 | 0.0000100 | 0.95 | 0.0117447 | 0.0168976 |
| X1770 | beta | 1.000111 | 1.000112 | 0.0356448 | 0.0356520 | 0.0357779 | 17075.8 | 0.0000206 | 0.95 | 0.0303640 | 0.0408917 |
| X1770 | M | 1.000272 | 1.000317 | 45.4735868 | 45.7082853 | 46.2765443 | 17338.6 | 0.0215703 | 0.95 | 39.8841834 | 50.8485089 |
| X1780 | alpha | 1.000514 | 1.001561 | 0.0136096 | 0.0135643 | 0.0135416 | 17117.8 | 0.0000093 | 0.95 | 0.0112683 | 0.0160201 |
| X1780 | beta | 1.000465 | 1.001440 | 0.0367597 | 0.0367653 | 0.0367765 | 16987.0 | 0.0000198 | 0.95 | 0.0317257 | 0.0418630 |
| X1780 | M | 1.000566 | 1.001711 | 46.9184820 | 47.1022825 | 47.2254317 | 17138.4 | 0.0191612 | 0.95 | 41.9217381 | 51.6370888 |
| X1790 | alpha | 1.001017 | 1.003544 | 0.0126577 | 0.0126131 | 0.0125275 | 16575.3 | 0.0000091 | 0.95 | 0.0104144 | 0.0149800 |
| X1790 | beta | 1.000983 | 1.003179 | 0.0385025 | 0.0385094 | 0.0386019 | 16305.1 | 0.0000206 | 0.95 | 0.0333766 | 0.0437012 |
| X1790 | M | 1.000966 | 1.003389 | 48.8104699 | 48.9690668 | 49.1799758 | 17098.7 | 0.0174550 | 0.95 | 44.3144300 | 53.1380827 |
| X1800 | alpha | 1.000110 | 1.000420 | 0.0116860 | 0.0116468 | 0.0115927 | 16299.7 | 0.0000084 | 0.95 | 0.0096049 | 0.0137829 |
| X1800 | beta | 1.000087 | 1.000347 | 0.0399538 | 0.0399387 | 0.0396845 | 16015.0 | 0.0000202 | 0.95 | 0.0349411 | 0.0449695 |
| X1800 | M | 1.000108 | 1.000414 | 50.7157959 | 50.8389930 | 51.1834695 | 17252.3 | 0.0153333 | 0.95 | 46.6384629 | 54.4728117 |
| X1810 | alpha | 1.000243 | 1.000527 | 0.0115193 | 0.0114800 | 0.0114383 | 15734.5 | 0.0000082 | 0.95 | 0.0095164 | 0.0135694 |
| X1810 | beta | 1.000118 | 1.000358 | 0.0383935 | 0.0383896 | 0.0384657 | 15460.0 | 0.0000197 | 0.95 | 0.0335364 | 0.0431518 |
| X1810 | M | 1.000326 | 1.000622 | 51.2962821 | 51.4292427 | 51.6215562 | 16508.4 | 0.0161901 | 0.95 | 47.0977231 | 55.2320786 |
| X1820 | alpha | 1.000052 | 1.000181 | 0.0104841 | 0.0104445 | 0.0102781 | 15011.2 | 0.0000079 | 0.95 | 0.0086351 | 0.0124260 |
| X1820 | beta | 1.000027 | 1.000124 | 0.0403826 | 0.0403829 | 0.0404617 | 14970.0 | 0.0000204 | 0.95 | 0.0354909 | 0.0452688 |
| X1820 | M | 1.000055 | 1.000187 | 53.3587767 | 53.4706305 | 53.7399168 | 16366.7 | 0.0145839 | 0.95 | 49.6763807 | 56.9584942 |
| X1830 | alpha | 1.000258 | 1.000430 | 0.0098584 | 0.0098256 | 0.0097258 | 14395.4 | 0.0000077 | 0.95 | 0.0080812 | 0.0116651 |
| X1830 | beta | 1.000286 | 1.000581 | 0.0420293 | 0.0420238 | 0.0418237 | 14224.9 | 0.0000211 | 0.95 | 0.0371298 | 0.0469784 |
| X1830 | M | 1.000236 | 1.000371 | 54.4809550 | 54.5648372 | 54.7531694 | 16267.7 | 0.0133487 | 0.95 | 51.0810043 | 57.7147665 |
| X1840 | alpha | 1.000201 | 1.000590 | 0.0103011 | 0.0102629 | 0.0101990 | 14208.6 | 0.0000081 | 0.95 | 0.0084545 | 0.0122232 |
| X1840 | beta | 1.000209 | 1.000633 | 0.0409196 | 0.0409247 | 0.0410181 | 14009.2 | 0.0000213 | 0.95 | 0.0359043 | 0.0457889 |
| X1840 | M | 1.000202 | 1.000548 | 53.6779375 | 53.7846103 | 53.9681394 | 15624.6 | 0.0146214 | 0.95 | 50.0085204 | 57.1315996 |
| | 1 | | | | | | | | | | |

Table 13: London Mortality bills 1728-1840, corrected for population growth.

| year | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|----------------|---------------|----------------------|----------------------|-------------------------|-------------------------|-------------------------|--------------------|------------------------|--------------|-------------------------|-------------------------|
| X1728 | alpha | 1.000216 | 1.000632 | 0.0117973 | 0.0117320 | 0.0118127 | 12703.3 | 0.0000126 | 0.95 | 0.0090855 | 0.0145984 |
| X1728 | beta | 1.000264 | 1.000811 | 0.0383802 | 0.0383752 | 0.0385662 | 13742.4 | 0.0000251 | 0.95 | 0.0326747 | 0.0441749 |
| X1728 | M | 1.000177 | 1.000534 | 50.6676878 | 50.8590788 | 51.5853562 | 13177.1 | 0.0252464 | 0.95 | 44.7887126 | 56.0258710 |
| X1728 | rate | 1.000032 | 1.000061 | 0.0067646 | 0.0067607 | 0.0067957 | 25886.2 | 0.0000155 | 0.95 | 0.0018885 | 0.0116701 |
| X1730 | alpha | 1.000179 | 1.000607 | 0.0143632 | 0.0142738 | 0.0140413 | 13423.4 | 0.0000148 | 0.95 | 0.0111303 | 0.0178349 |
| X1730 | beta | 1.000209 | 1.000645 | 0.0340807 | 0.0340719 | 0.0339992 | 14402.5 | 0.0000247 | 0.95 | 0.0282252 | 0.0398462 |
| X1730 | M | 1.000167 | 1.000545 | 45.1548428 | 45.5041559 | 46.1942144 | 13398.1 | 0.0340936 | 0.95 | 37.2310898 | 52.4481763 |
| X1730 | rate | 1.000100 | 1.000359 | 0.0021254 | 0.0021267 | 0.0023925 | 28508.1 | 0.0000148 | 0.95 | -0.0027647 | 0.0070247 |
| X1740 | alpha | 1.000250 | 1.000351 | 0.0143131 | 0.0142474 | 0.0141781 | 12578.6 | 0.0000142 | 0.95 | 0.0112583 | 0.0174506 |
| X1740 | beta | 1.000181 | 1.000319 | 0.0351166 | 0.0351062 | 0.0349517 | 13779.1 | 0.0000232 | 0.95 | 0.0297582 | 0.0404467 |
| X1740 | M | 1.000278 | 1.000415 | 45.4168492 | 45.6666273 | 45.9931494 | 12599.0 | 0.0307477 | 0.95 | 38.5335175 | 51.8684034 |
| X1740 | rate | 1.000068 | 1.000120 | 0.0016517 | 0.0016515 | 0.0015142 | 25567.8 | 0.0000156 | 0.95 | -0.0031950 | 0.0065573 |
| X1750 | alpha | 1.000044 | 1.000069 | 0.0122439 | 0.0121749 | 0.0120834 | 13261.9 | 0.0000125 | 0.95 | 0.0094963 | 0.0150957 |
| X1750 | beta | 1.000071 | 1.000205 | 0.0376537 | 0.0376479 | 0.0373656 | 14801.1 | 0.0000236 | 0.95 | 0.0320020 | 0.0432862 |
| X1750 | M | 1.000031 | 1.000056 | 49.7546558 | 49.9590937 | 50.2151068 | 13705.5 | 0.0254226 | 0.95 | 43.7054776 | 55.2902303 |
| X1750 | rate | 1.000077 | 1.000111 | 0.0067105 | 0.0067114 | 0.0065398 | 27317.4 | 0.0000151 | 0.95 | 0.0018180 | 0.0115565 |
| X1760 | alpha | 1.000225 | 1.000700 | 0.0116585 | 0.0115897 | 0.0114879 | 12463.7 | 0.0000123 | 0.95 | 0.0090429 | 0.0144036 |
| X1760 | beta | 1.000110 | 1.000420 | 0.0385112 | 0.0385024 | 0.0386022 | 13804.0 | 0.0000244 | 0.95 | 0.0328832 | 0.0441388 |
| X1760 | M | 1.000236 | 1.000723 | 50.9671802 | 51.1574788 | 51.4559256 | 12906.8 | 0.0247727 | 0.95 | 45.4374663 | 56.3675483 |
| X1760 | rate | 1.000227 | 1.000754 | 0.0069377 | 0.0069444 | 0.0071785 | 25388.2 | 0.0000156 | 0.95 | 0.0020562 | 0.0118077 |
| X1770 | alpha | 1.000913 | 1.002565 | 0.0119572 | 0.0118855 | 0.0116788 | 12401.3 | 0.0000128 | 0.95 | 0.0092493 | 0.0148011 |
| X1770 | beta M | 1.000842 | 1.002526 | 0.0385160 | 0.0385119 50.5009459 | 0.0385913 50.9360513 | 13729.2 12779.1 | 0.0000249 0.0255623 | 0.95 0.95 | 0.0328861 | 0.0442661 55.7354351 |
| X1770 X1770 | | 1.000933 1.000327 | 1.002591 1.001024 | 50.3026157 0.0054059 | 0.0053991 | 0.0053967 | 26694.8 | 0.0255623 | 0.95 | 44.5382288 0.0005155 | 0.0103390 |
| X1770 X1780 | rate | 1.000327 | 1.001024 | 0.0054059 | 0.0053991 | 0.0053967 | 12144.8 | 0.0000153 | 0.95 | 0.0076036 | 0.0103390 |
| X1780 X1780 | alpha beta | 1.000024 | 1.000332 | 0.0098947 | 0.0098373 | 0.0097623 | 13529.3 | 0.0000109 | 0.95 | 0.0076036 | 0.0122021 |
| X1780 | M | 1.000009 | 1.000332 | 54.5099445 | 54.6330090 | 54.9472107 | 13234.3 | 0.0000249 | 0.95 | 49.7839622 | 58.9932689 |
| X1780 | rate | 1.00003 | 1.000054 | 0.0101105 | 0.0101157 | 0.0102186 | 23262.7 | 0.0203360 | 0.95 | 0.0051865 | 0.0149529 |
| X1790 | alpha | 1.000780 | 1.002619 | 0.0074628 | 0.0074099 | 0.0072730 | 12511.4 | 0.0000086 | 0.95 | 0.0056365 | 0.0093699 |
| X1790 | beta | 1.000634 | 1.002266 | 0.0465156 | 0.0465133 | 0.0464524 | 13814.5 | 0.0000257 | 0.95 | 0.0405791 | 0.0524046 |
| X1790 | M | 1.000594 | 1.002037 | 59.3920496 | 59.4676688 | 59.6465203 | 15210.4 | 0.0154250 | 0.95 | 55.6352570 | 63.0795140 |
| X1790 | rate | 1.000364 | 1.001370 | 0.0165769 | 0.0165808 | 0.0166141 | 24083.9 | 0.0000160 | 0.95 | 0.0116026 | 0.0213767 |
| X1800 | alpha | 1.000673 | 1.001733 | 0.0067061 | 0.0066571 | 0.0065314 | 12303.3 | 0.0000078 | 0.95 | 0.0050738 | 0.0084373 |
| X1800 | beta | 1.000450 | 1.001205 | 0.0482926 | 0.0482882 | 0.0482750 | 13472.8 | 0.0000254 | 0.95 | 0.0425605 | 0.0540970 |
| X1800 | M | 1.000481 | 1.001391 | 60.9494935 | 61.0079704 | 61.2925933 | 16004.8 | 0.0138784 | 0.95 | 57.4654475 | 64.3420718 |
| X1800 | rate | 1.000147 | 1.000554 | 0.0172842 | 0.0172863 | 0.0173351 | 24114.8 | 0.0000161 | 0.95 | 0.0123533 | 0.0221326 |
| X1810 | alpha | 1.000778 | 1.002825 | 0.0061205 | 0.0060764 | 0.0060231 | 11885.0 | 0.0000073 | 0.95 | 0.0046308 | 0.0077169 |
| X1810 | beta | 1.000722 | 1.002651 | 0.0477278 | 0.0477231 | 0.0477969 | 12935.3 | 0.0000252 | 0.95 | 0.0421088 | 0.0533294 |
| X1810 | M | 1.000533 | 1.001967 | 63.1111594 | 63.1645788 | 63.3883652 | 15759.0 | 0.0139295 | 0.95 | 59.6818113 | 66.5370162 |
| X1810 | rate | 1.000355 | 1.001232 | 0.0188379 | 0.0188404 | 0.0189439 | 21465.1 | 0.0000169 | 0.95 | 0.0139210 | 0.0236200 |
| X1820 | alpha | 1.000095 | 1.000132 | 0.0055976 | 0.0055572 | 0.0054458 | 11229.6 | 0.0000070 | 0.95 | 0.0041772 | 0.0070725 |
| X1820 | beta | 1.000042 | 1.000144 | 0.0497736 | 0.0497549 | 0.0494675 | 11848.9 | 0.0000269 | 0.95 | 0.0440723 | 0.0555463 |
| X1820 | M | 1.000089 | 1.000100 | 63.9900524 | 64.0294417 | 64.0859524 | 15792.1 | 0.0130000 | 0.95 | 60.7385660 | 67.1324448 |
| X1820 | rate | 1.000054 | 1.000169 | 0.0184286 | 0.0184243 | 0.0183352 | 20638.3 | 0.0000173 | 0.95 | 0.0136164 | 0.0233407 |
| X1830 | alpha | 1.000685 | 1.002323 | 0.0055328 | 0.0054915 | 0.0053316 | 10784.7 | 0.0000071 | 0.95 | 0.0041241 | 0.0069785 |
| X1830 | beta | 1.000541 | 1.001972 | 0.0507604 | 0.0507524 | 0.0506613 | 11479.7 | 0.0000273 | 0.95 | 0.0450068 | 0.0564989 |
| X1830 | M | 1.000452 | 1.001586 | 63.7527679 | 63.7940673 | 63.8373687 | 14596.3 | 0.0130407 | 0.95 | 60.6000558 | 66.7627670 |
| X1830 | rate | 1.000340 | 1.001284 | 0.0170084 | 0.0170011 | 0.0170444 | 20042.5 | 0.0000176 | 0.95 | 0.0121792 | 0.0219144 |
| X1840 | alpha | 1.000307 | 1.001096 | 0.0054664 | 0.0054244 | 0.0053739 | 11068.3 | 0.0000069 | 0.95 | 0.0040888 | 0.0069308 |
| X1840 | beta | 1.000429 | 1.001483 | 0.0504923 | 0.0504880 | 0.0504433 | 12336.9 | 0.0000266 | 0.95 | 0.0445658 | 0.0561736 |
| X1840 | M | 1.000118 | 1.000460 | 64.1209693 | 64.1581002 | 64.3153799 | 15983.6 | 0.0125993 | 0.95 | 61.0149913 | 67.2673873 |
| X1840 | rate | 1.000057 | 1.000244 | 0.0185439 | 0.0185336 | 0.0183673 | 20908.7 | 0.0000172 | 0.95 | 0.0136249 | 0.0233586 |

Table 14: Census data for London from 1841.

| | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|---|-----------------|-----------------|------------|------------|------------|---------|-----------|---------|------------|------------|
| a | 1.000227 | 1.000481 | 0.0045780 | 0.0045654 | 0.0045126 | 15366.4 | 0.0000030 | 0.95 | 0.0038745 | 0.0053284 |
| b | 1.000173 | 1.000361 | 0.0547652 | 0.0547581 | 0.0546507 | 15261.7 | 0.0000155 | 0.95 | 0.0510256 | 0.0585294 |
| M | 1.000098 | 1.000288 | 60.3512664 | 60.3640713 | 60.4164328 | 26323.3 | 0.0044223 | 0.95 | 58.9378882 | 61.7484732 |

```
kable(eng_mort_result, caption = "English mortality data.") %>%
kableExtra::kable_styling(latex_options = c("HOLD_position","scale_down"))
```

Table 15: English mortality data.

| year | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|----------------|---------------|----------------------|----------------------|-------------------------|-------------------------|-------------------------|--------------------|------------------------|--------------|-------------------------|-------------------------|
| X1640 | alpha | 1.000116 | 1.000213 | 0.0109640 | 0.0109440 | 0.0108724 | 20086.8 | 0.0000055 | 0.95 | 0.0094508 | 0.0125183 |
| X1640 | beta | 1.000128 | 1.000219 | 0.0473794 | 0.0473646 | 0.0471615 | 19457.0 | 0.0000160 | 0.95 | 0.0430271 | 0.0517521 |
| X1640 | M | 1.000098 | 1.000168 | 55.8790864 | 55.9257645 | 56.0762781 | 22766.9 | 0.0074788 | 0.95 | 53.6542245 | 58.0607633 |
| X1650 | alpha | 1.000196 | 1.000699 | 0.0086495 | 0.0086305 | 0.0086386 | 17477.0 | 0.0000050 | 0.95 | 0.0073694 | 0.0099516 |
| X1650 | beta | 1.000238 | 1.000818 | 0.0534298 | 0.0534191 | 0.0532174 | 17097.8 | 0.0000176 | 0.95 | 0.0488730 | 0.0579356 |
| X1650 | M | 1.000122 | 1.000456 | 59.0892102 | 59.1180884 | 59.1222939 | 22875.6 | 0.0058105 | 0.95 | 57.3707403 | 60.8059797 |
| X1660 | alpha | 1.000538 | 1.001899 | 0.0091323 | 0.0091133 | 0.0090836 | 17736.5 | 0.0000051 | 0.95 | 0.0078190 | 0.0104985 |
| X1660 | beta | 1.000442 | 1.001588 | 0.0507107 | 0.0507012 | 0.0506517 | 17263.0 | 0.0000172 | 0.95 | 0.0463039 | 0.0551739 |
| X1660 | M | 1.000484 | 1.001711 | 58.8100849 | 58.8427992 | 58.8427140 | 22595.3 | 0.0063824 | 0.95 | 56.9061034 | 60.6611103 |
| X1670 | alpha | 1.000280 | 1.000678 | 0.0109726 | 0.0109471 | 0.0109033 | 20090.3 | 0.0000056 | 0.95 | 0.0094600 | 0.0125515 |
| X1670 | beta | 1.000338 | 1.000812 | 0.0444972 | 0.0445019 | 0.0446316 | 19399.7 | 0.0000157 | 0.95 | 0.0402542 | 0.0488448 |
| X1670 | M | 1.000211 | 1.000529 | 56.4443366 | 56.5061422 | 56.5992418 | 22544.4 | 0.0083487 | 0.95 | 53.9239107 | 58.8183187 |
| X1680 | alpha | 1.000560 | 1.001531 | 0.0134499 | 0.0134251 | 0.0133309 | 22339.5 | 0.0000061 | 0.95 | 0.0116869 | 0.0152420 |
| X1680 | beta | 1.000479 | 1.001399 | 0.0435646 | 0.0435605 | 0.0437501 | 21337.1 | 0.0000151 | 0.95 | 0.0392159 | 0.0478531 |
| X1680 | M | 1.000597 | 1.001611 | 51.9412993 | 52.0117614 | 52.1884363 | 23152.8 | 0.0091727 | 0.95 | 49.1667363 | 54.6014009 |
| X1690 | alpha | 1.000203 | 1.000424 | 0.0100036 | 0.0099815 | 0.0099278 | 19068.4 | 0.0000053 | 0.95 | 0.0085828 | 0.0114492 |
| X1690 | beta | 1.000217 | 1.000487 | 0.0457255 | 0.0457144 | 0.0457837 | 18458.1 | 0.0000160 | 0.95 | 0.0414631 | 0.0499716 |
| X1690 | M | 1.000156 | 1.000323 | 58.2265512 | 58.2748183 | 58.3311613 | 22552.3 | 0.0076819 | 0.95 | 55.9044003 | 60.4191960 |
| X1700 | alpha | 1.000247 | 1.000813 | 0.0097904 | 0.0097696 | 0.0097670 | 19048.9 | 0.0000052 | 0.95 | 0.0083976 | 0.0112137 |
| X1700 | beta | 1.000228 | 1.000792 | 0.0469162 | 0.0469091 | 0.0468449 | 18524.9 | 0.0000160 | 0.95 | 0.0426635 | 0.0512282 |
| X1700 | M | 1.000210 | 1.000697 | 58.3940436 | 58.4388608 | 58.4010030 | 22362.5 | 0.0073779 | 0.95 | 56.2165699 | 60.5292073 |
| X1710 | alpha | 1.000629 | 1.002202 | 0.0076344 | 0.0076175 | 0.0075883 | 16583.9 | 0.0000046 | 0.95 | 0.0064833 | 0.0088178 |
| X1710 | beta | 1.000810 | 1.002798 | 0.0547320 | 0.0547184 | 0.0547561 | 16149.3 | 0.0000181 | 0.95 | 0.0502213 | 0.0592441 |
| X1710 | M | 1.000354 | 1.001230 | 61.0059909 | 61.0278089 | 61.0396872 | 23904.2 | 0.0053119 | 0.95 | 59.3643989 | 62.5807876 |
| X1720 | alpha | 1.000438 | 1.001584 | 0.0080028 | 0.0079824 | 0.0079301 | 17173.5 | 0.0000047 | 0.95 | 0.0068173 | 0.0092105 |
| X1720 | beta | 1.000453 | 1.001645 | 0.0560063 | 0.0560001 | 0.0558861 | 16622.0 | 0.0000179 | 0.95 | 0.0514205 | 0.0604697 |
| X1720 | M | 1.000297 | 1.001094 | 59.7548666 | 59.7785061 | 59.8227855 | 23615.5 | 0.0051845 | 0.95 | 58.1648789 | 61.2877274 |
| X1730 | alpha | 1.000128 | 1.000485 | 0.0067962 | 0.0067781 | 0.0067500 | 15125.2 | 0.0000045 | 0.95 | 0.0057413 | 0.0078882 |
| X1730 | beta | 1.000132 | 1.000481 | 0.0561362 | 0.0561233 | 0.0561525 | 14537.5 | 0.0000193 | 0.95 | 0.0516431 | 0.0607418 |
| X1730 | M | 1.000086 | 1.000325 | 62.6345173 | 62.6558894 | 62.6742840 | 23395.6 | 0.0050475 | 0.95 | 61.1122439 | 64.1406077 |
| X1740 | alpha | 1.000185 | 1.000678 | 0.0067863 | 0.0067674 | 0.0067507 | 15383.6 | 0.0000045 | 0.95 | 0.0057019 | 0.0078702 |
| X1740 | beta | 1.000260 | 1.000953 | 0.0566936 | 0.0566911 | 0.0568096 | 15043.4 | 0.0000191 | 0.95 | 0.0520709 | 0.0612724 |
| X1740 | M | 1.000063 | 1.000245 | 62.4655115 | 62.4849711 | 62.4345863 | 22893.7 | 0.0051037 | 0.95 | 60.9419302 | 63.9688404 |
| X1750 | alpha | 1.000389 | 1.001407 | 0.0053793 | 0.0053645 | 0.0053635 | 13451.8 | 0.0000040 | 0.95 | 0.0044682 | 0.0062959 |
| X1750 | beta | 1.000443 | 1.001627 | 0.0595510 | 0.0595305 | 0.0594825 | 12966.5 | 0.0000210 | 0.95 | 0.0548610 | 0.0642515 |
| X1750 | M | 1.000167 | 1.000607 | 65.4071998 | 65.4213962 | 65.4642394 | 24607.7 | 0.0044311 | 0.95 | 64.0354191 | 66.7582250 |
| X1760 | alpha | 1.000180 | 1.000387 | 0.0080565 | 0.0080378 | 0.0079359 | 17802.8 | 0.0000047 | 0.95 | 0.0068516 | 0.0092887 |
| X1760 | beta | 1.000187 | 1.000346 | 0.0488550 | 0.0488417 | 0.0488743 | 16840.4 | 0.0000169 | 0.95 | 0.0445037 | 0.0531121 |
| X1760 | M | 1.000119 | 1.000328 | 61.9016665 | 61.9336352 | 62.0050035 | 23618.5 | 0.0063598 | 0.95 | 59.9327761 | 63.7618010 |
| X1770 | alpha | 1.000469 | 1.001234 | 0.0067654 | 0.0067476 | 0.0066997 | 14881.8 | 0.0000045 | 0.95 | 0.0057073 | 0.0078687 |
| X1770 | beta | 1.000501 | 1.001341 | 0.0538935 | 0.0538804 | 0.0536262 | 14373.8 | 0.0000192 | 0.95 | 0.0494452 | 0.0584665 |
| X1770 X1780 | M | 1.000270 | 1.000709 | 63.5277738 | 63.5489910 | 63.4921572 | 22585.6 | 0.0054864 | 0.95 | 61.9173469 | 65.1383522 |
| | alpha | 1.000347 | 1.001235 | 0.0066384 | 0.0066225 | 0.0066110 | 15713.1 | 0.0000043 | 0.95 | 0.0055976 | 0.0076907 |
| X1780 | beta | 1.000349 | 1.001303 | 0.0570824 | 0.0570677 | 0.0571475 | 15127.7 | 0.0000188 | 0.95 | 0.0526292 | 0.0616896 |
| X1780 | M | 1.000195 | 1.000710 | 62.7166530 | 62.7352113 | 62.7235429 | 24154.0 | 0.0048243 | 0.95 | 61.2201635 | 64.1540268 |
| X1790 | alpha | 1.000180 | 1.000376 | 0.0058127 | 0.0057951 | 0.0057825 | 13899.0 | 0.0000042 | 0.95 | 0.0048677 | 0.0068164 |
| X1790 | beta M | 1.000229 | 1.000478 | 0.0580897 | 0.0580826 | 0.0579337 | 13447.1 | 0.0000206 | 0.95 | 0.0533856 | 0.0627649 |
| X1790 X1800 | | 1.000055 1.000697 | 1.000174 1.002167 | 64.6577738 0.0046142 | 64.6756380 0.0045977 | 64.7246120 0.0045567 | 23430.8 12391.5 | 0.0047208 0.0000037 | 0.95 0.95 | 63.2361972 0.0038253 | 66.0657933 0.0054317 |
| | alpha beta | | 1.002167 | | | | 12391.5 | 0.0000037 | 0.95 | 0.0038253 | 0.0054317 |
| X1800 X1800 | M | 1.000709 1.000239 | 1.002222 | 0.0608363 67.4325112 | 0.0608357 67.4451148 | 0.0608310 67.4486965 | 26907.8 | 0.0000219 | 0.95 | 66.1359322 | 68.6958522 |
| A1000 | 171 | 1.000239 | 1.000622 | 01.4020112 | 01.4401140 | 01.4400500 | 20301.0 | 0.0033010 | 0.99 | 00.1309322 | 00.0900022 |

kable(HMD_UK_result, caption = "Human Mortality Database UK.") %>%
 kableExtra::kable_styling(latex_options = c("HOLD_position","scale_down"))

Table 16: Human Mortality Database UK.

| year | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|-------|-----------|-----------------|-----------------|------------|------------|------------|---------|-----------|---------|------------|------------|
| X1841 | alpha | 1.000163 | 1.000417 | 0.0036316 | 0.0036148 | 0.0035704 | 13786.9 | 0.0000032 | 0.95 | 0.0029186 | 0.0043694 |
| X1841 | beta | 1.000156 | 1.000468 | 0.0519888 | 0.0519880 | 0.0522191 | 13557.1 | 0.0000185 | 0.95 | 0.0476828 | 0.0561015 |
| X1841 | M | 1.000083 | 1.000148 | 66.2542881 | 66.2748935 | 66.3111134 | 25227.7 | 0.0056085 | 0.95 | 64.4997322 | 67.9878895 |
| X1845 | alpha | 1.000079 | 1.000297 | 0.0042938 | 0.0042780 | 0.0042669 | 14758.1 | 0.0000036 | 0.95 | 0.0034647 | 0.0051540 |
| X1845 | beta | 1.000067 | 1.000247 | 0.0498996 | 0.0498859 | 0.0500069 | 14606.7 | 0.0000180 | 0.95 | 0.0455985 | 0.0541474 |
| X1845 | M | 1.000065 | 1.000255 | 64.2120906 | 64.2353737 | 64.2258466 | 24443.1 | 0.0062539 | 0.95 | 62.2412879 | 66.0782225 |
| X1850 | alpha | 1.000973 | 1.003549 | 0.0037558 | 0.0037391 | 0.0036783 | 13963.2 | 0.0000033 | 0.95 | 0.0030110 | 0.0045196 |
| X1850 | beta | 1.000868 | 1.003159 | 0.0517607 | 0.0517548 | 0.0515669 | 13902.2 | 0.0000185 | 0.95 | 0.0475374 | 0.0561228 |
| X1850 | M | 1.000670 | 1.002447 | 65.7445767 | 65.7656894 | 65.8470383 | 24788.4 | 0.0057544 | 0.95 | 63.9683713 | 67.5152044 |
| X1855 | alpha | 1.000156 | 1.000325 | 0.0034310 | 0.0034165 | 0.0034148 | 13071.2 | 0.0000031 | 0.95 | 0.0027387 | 0.0041407 |
| X1855 | beta | 1.000111 | 1.000252 | 0.0533405 | 0.0533264 | 0.0532089 | 12901.9 | 0.0000193 | 0.95 | 0.0489858 | 0.0575821 |
| X1855 | M | 1.000055 | 1.000176 | 66.5070750 | 66.5214941 | 66.5377049 | 24496.9 | 0.0055156 | 0.95 | 64.7810996 | 68.1628553 |
| X1860 | alpha | 1.000103 | 1.000169 | 0.0034785 | 0.0034615 | 0.0034062 | 13432.3 | 0.0000031 | 0.95 | 0.0027794 | 0.0041924 |
| X1860 | beta | 1.000118 | 1.000200 | 0.0532621 | 0.0532640 | 0.0532106 | 13350.6 | 0.0000189 | 0.95 | 0.0490210 | 0.0575846 |
| X1860 | M | 1.000016 | 1.000032 | 66.2956647 | 66.3134949 | 66.3500169 | 24949.1 | 0.0054798 | 0.95 | 64.5756127 | 67.9675086 |
| X1865 | alpha | 1.000093 | 1.000333 | 0.0035991 | 0.0035837 | 0.0035330 | 13810.1 | 0.0000031 | 0.95 | 0.0028932 | 0.0043267 |
| X1865 | beta | 1.000108 | 1.000353 | 0.0530530 | 0.0530491 | 0.0530859 | 13658.1 | 0.0000185 | 0.95 | 0.0488013 | 0.0572954 |
| X1865 | M | 1.000045 | 1.000177 | 65.7780212 | 65.7953467 | 65.8802464 | 25507.4 | 0.0054316 | 0.95 | 64.0717897 | 67.4665740 |
| X1870 | alpha | 1.000077 | 1.000191 | 0.0035027 | 0.0034908 | 0.0034765 | 13760.3 | 0.0000030 | 0.95 | 0.0028292 | 0.0042127 |
| X1870 | beta | 1.000110 | 1.000242 | 0.0536849 | 0.0536587 | 0.0535650 | 13616.9 | 0.0000184 | 0.95 | 0.0495385 | 0.0579499 |
| X1870 | M | 1.000013 | 1.000070 | 65.9071237 | 65.9205478 | 65.8577523 | 25746.8 | 0.0052524 | 0.95 | 64.2645935 | 67.5678728 |
| X1875 | alpha | 1.000092 | 1.000343 | 0.0030605 | 0.0030478 | 0.0030211 | 12815.0 | 0.0000028 | 0.95 | 0.0024475 | 0.0036823 |
| X1875 | beta | 1.000131 | 1.000471 | 0.0568401 | 0.0568279 | 0.0568980 | 12685.7 | 0.0000193 | 0.95 | 0.0526071 | 0.0611415 |
| X1875 | M | 1.000031 | 1.000141 | 66.4668857 | 66.4785272 | 66.5086127 | 26537.0 | 0.0047162 | 0.95 | 64.9506366 | 67.9602202 |
| X1880 | alpha | 1.000119 | 1.000291 | 0.0027376 | 0.0027242 | 0.0026867 | 12292.1 | 0.0000026 | 0.95 | 0.0021904 | 0.0033047 |
| X1880 | beta | 1.000171 | 1.000388 | 0.0580794 | 0.0580802 | 0.0580583 | 12275.9 | 0.0000195 | 0.95 | 0.0538930 | 0.0623071 |
| X1880 | M | 1.000016 | 1.000046 | 67.6639684 | 67.6752899 | 67.6594434 | 26763.5 | 0.0045057 | 0.95 | 66.2138218 | 69.0997903 |
| X1885 | alpha | 1.000329 | 1.000699 | 0.0024297 | 0.0024169 | 0.0023954 | 11472.9 | 0.0000024 | 0.95 | 0.0019319 | 0.0029532 |
| X1885 | beta | 1.000279 | 1.000617 | 0.0605593 | 0.0605577 | 0.0605172 | 11375.3 | 0.0000207 | 0.95 | 0.0561612 | 0.0648427 |
| X1885 | M | 1.000124 | 1.000309 | 68.1749533 | 68.1842585 | 68.1928238 | 26834.9 | 0.0042250 | 0.95 | 66.8018933 | 69.5153058 |
| X1890 | alpha | 1.000121 | 1.000451 | 0.0024118 | 0.0023997 | 0.0023802 | 11867.7 | 0.0000024 | 0.95 | 0.0019247 | 0.0029285 |
| X1890 | beta | 1.000146 | 1.000531 | 0.0614665 | 0.0614588 | 0.0613662 | 11669.1 | 0.0000205 | 0.95 | 0.0571518 | 0.0657954 |
| X1890 | M | 1.000045 | 1.000148 | 67.7519542 | 67.7613179 | 67.8037905 | 28081.6 | 0.0040695 | 0.95 | 66.4069818 | 69.0759956 |
| X1895 | alpha | 1.000328 | 1.001210 | 0.0019825 | 0.0019735 | 0.0019634 | 10586.6 | 0.0000021 | 0.95 | 0.0015598 | 0.0024219 |
| X1895 | beta | 1.000267 | 1.000994 | 0.0637922 | 0.0637712 | 0.0636859 | 10594.5 | 0.0000217 | 0.95 | 0.0594245 | 0.0681856 |
| X1895 | M | 1.000224 | 1.000819 | 69.4924393 | 69.4994274 | 69.5249671 | 28489.7 | 0.0038280 | 0.95 | 68.2103261 | 70.7410684 |
| X1900 | alpha | 1.000051 | 1.000194 | 0.0017882 | 0.0017794 | 0.0017686 | 10113.1 | 0.0000020 | 0.95 | 0.0013975 | 0.0021792 |
| X1900 | beta | 1.000061 | 1.000247 | 0.0653147 | 0.0653019 | 0.0653664 | 10036.7 | 0.0000222 | 0.95 | 0.0609626 | 0.0696771 |
| X1900 | M | 1.000007 | 1.000020 | 70.1656919 | 70.1713832 | 70.1615274 | 28126.0 | 0.0036879 | 0.95 | 68.9548389 | 71.3801825 |

4.2 London cemeteries

The data is manly hard coded in the file ./chapter_04_results/Wellcome_DB.R.

Only St. Bride's crypt is excluded but available from the Museum of London upon request. For general information: https://www.museumoflondon.org.uk go for: Collections > Archaeology at the Museum of London > Wellcome Osteological Research Database > St. Bride's Church Fleet Street. If runCodeNew == TRUE the file ./lifetables_processing/stbrides_crypt.R will ask for the location of the retrieved dataset (Excel sheet) and process the data. In any other case pre-processed data will be loaded.

```
source("./lifetables_processing/stbrides_crypt.R")
source("./chapter_04_results/Wellcome_DB.R")
```

4.2.1 Pre-processing and extended results

```
kable(wellcome_result, caption = "London cemeteries data") %>%
kableExtra::kable_styling(latex_options = c("HOLD_position","scale_down"))
```

Table 17: London cemeteries data

| cemetery | start | end | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|--|-------|------|---------------|-----------------|-----------------|------------|------------|------------|---------|------------|---------|------------|------------|
| Bermondsey Abbey | 1089 | 1538 | alpha | 1.000095 | 1.000352 | 0.0119872 | 0.0118695 | 0.0117349 | 26882.4 | 0.0000115 | 0.95 | 0.0084108 | 0.0157410 |
| Bermondsey Abbey | 1089 | 1538 | beta | 1.000115 | 1.000319 | 0.0410531 | 0.0410516 | 0.0413654 | 23098.5 | 0.0000312 | 0.95 | 0.0318561 | 0.0503895 |
| Bermondsey Abbey | 1089 | 1538 | M | 1.000071 | 1.000266 | 41.8366810 | 42.1437778 | 42.5664355 | 29309.6 | 0.0207896 | 0.95 | 34.6719658 | 48.4310632 |
| St. Mary Graces | 1350 | 1540 | alpha | 1.000196 | 1.000732 | 0.0197808 | 0.0196850 | 0.0195223 | 35662.0 | 0.0000118 | 0.95 | 0.0154857 | 0.0241619 |
| St. Mary Graces | 1350 | 1540 | beta | 1.000244 | 1.000894 | 0.0346722 | 0.0346636 | 0.0349129 | 29450.8 | 0.0000239 | 0.95 | 0.0266567 | 0.0427213 |
| St. Mary Graces | 1350 | 1540 | M | 1.000288 | 1.000951 | 27.6620555 | 28.2853721 | 29.0829030 | 31343.0 | 0.0275212 | 0.95 | 17.7908628 | 36.1544161 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | alpha | 1.000021 | 1.000058 | 0.0249328 | 0.0248411 | 0.0247596 | 47240.6 | 0.0000108 | 0.95 | 0.0203838 | 0.0295337 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | beta | 1.000010 | 1.000041 | 0.0363031 | 0.0363142 | 0.0366087 | 42155.0 | 0.0000184 | 0.95 | 0.0288655 | 0.0437148 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | M | 1.000014 | 1.000048 | 21.9000883 | 22.4278307 | 23.6171674 | 41316.5 | 0.0217592 | 0.95 | 12.9358328 | 29.6933479 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | alpha | 1.000142 | 1.000479 | 0.0299501 | 0.0298832 | 0.0296347 | 50227.8 | 0.0000103 | 0.95 | 0.0254561 | 0.0345077 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | beta | 1.000145 | 1.000390 | 0.0356927 | 0.0356959 | 0.0355017 | 44544.0 | 0.0000163 | 0.95 | 0.0288836 | 0.0423855 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | M | 1.000138 | 1.000388 | 16.4726206 | 16.9685941 | 17.8228768 | 43773.7 | 0.0209091 | 0.95 | 7.6941741 | 24.3391668 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | alpha | 1.000058 | 1.000230 | 0.0183232 | 0.0182986 | 0.0182568 | 30711.1 | 0.0000060 | 0.95 | 0.0162397 | 0.0203837 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | beta | 1.000039 | 1.000160 | 0.0580756 | 0.0580643 | 0.0577145 | 27569.9 | 0.0000162 | 0.95 | 0.0529190 | 0.0634424 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | M | 1.000056 | 1.000226 | 31.8403051 | 31.8802975 | 31.9815271 | 32452.4 | 0.0050096 | 0.95 | 30.0460798 | 33.5688087 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | alpha | 1.000184 | 1.000413 | 0.0262455 | 0.0261845 | 0.0258468 | 45106.6 | 0.0000098 | 0.95 | 0.0222297 | 0.0303974 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | beta | 1.000202 | 1,000384 | 0.0374668 | 0.0374646 | 0.0373648 | 37992.2 | 0.0000178 | 0.95 | 0.0307176 | 0.0443176 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | M | 1.000255 | 1,000509 | 21.1562579 | 21.5422484 | 22.2118499 | 38394.6 | 0.0188420 | 0.95 | 13,7317283 | 27.8355824 |
| New Churchyard | 1569 | 1739 | alpha | 1.000100 | 1.000375 | 0.0257447 | 0.0256826 | 0.0256229 | 40693.9 | 0.0000097 | 0.95 | 0.0219664 | 0.0296497 |
| New Churchyard | 1569 | 1739 | beta | 1.000143 | 1.000447 | 0.0365472 | 0.0365523 | 0.0364771 | 33659.4 | 0.0000185 | 0.95 | 0.0298776 | 0.0431955 |
| New Churchyard | 1569 | 1739 | M | 1.000167 | 1,000489 | 21.2258180 | 21.6422371 | 22.4873708 | 34065.6 | 0.0202506 | 0.95 | 13.6829257 | 27.9012158 |
| St. Benet Sherehog | 1670 | 1740 | alpha | 1.000103 | 1,000388 | 0.0159324 | 0.0158024 | 0.0157241 | 35332.7 | 0.0000126 | 0.95 | 0.0114989 | 0.0206750 |
| St. Benet Sherehog | 1670 | 1740 | beta | 1,000166 | 1.000541 | 0.0354819 | 0.0354675 | 0.0352938 | 29914.9 | 0.0000268 | 0.95 | 0.0265131 | 0.0446216 |
| St. Benet Sherehog | 1670 | 1740 | M | 1.000123 | 1.000414 | 34.0694974 | 34.7174821 | 36.0672253 | 33191.8 | 0.0286473 | 0.95 | 23.6417236 | 43.3454393 |
| Chelsea Old church | 1712 | 1842 | alpha | 1.000120 | 1.000284 | 0.0083989 | 0.0083033 | 0.0082201 | 24055.1 | 0.0000095 | 0.95 | 0.0056545 | 0.0113658 |
| Chelsea Old church | 1712 | 1842 | beta | 1.000107 | 1.000363 | 0.0422444 | 0.0421520 | 0.0421527 | 20068.2 | 0.0000343 | 0.95 | 0.0327982 | 0.0517568 |
| Chelsea Old church | 1712 | 1842 | M | 1.000066 | 1.000214 | 50.2412943 | 50.4255236 | 50.6944550 | 32126.8 | 0.0173728 | 0.95 | 43.9580757 | 56.1242381 |
| St. Marylebone | 1742 | 1817 | alpha | 1.000026 | 1.000095 | 0.0125953 | 0.0125006 | 0.0123046 | 29334.6 | 0.0000102 | 0.95 | 0.0092608 | 0.0160318 |
| St. Marylebone | 1742 | 1817 | beta | 1.000020 | 1.000034 | 0.0420937 | 0.0420895 | 0.0423370 | 23957.1 | 0.0000291 | 0.95 | 0.0331445 | 0.0508272 |
| St. Marylebone | 1742 | 1817 | M | 1.000036 | 1.000085 | 40.5179648 | 40.7766676 | 41.3760128 | 31991.5 | 0.0170220 | 0.95 | 34.3796076 | 46.1332104 |
| St. Marylebone Paddington Street north | 1772 | 1853 | alpha | 1.000045 | 1.000166 | 0.0099037 | 0.0098127 | 0.0096774 | 27403.8 | 0.0000087 | 0.95 | 0.0071709 | 0.0127837 |
| St. Marylebone Paddington Street north | 1772 | 1853 | beta | 1.000015 | 1.000206 | 0.0488613 | 0.0488575 | 0.0485839 | 23270.2 | 0.0000301 | 0.95 | 0.0398523 | 0.0578266 |
| St. Marylebone Paddington Street north | 1772 | 1853 | M | 1.000039 | 1,000116 | 44.6690555 | 44.7919466 | 45,0496301 | 37001.7 | 0.0116510 | 0.95 | 40.1953904 | 48.9817326 |
| St. Bride's lower churchyard | 1770 | 1849 | alpha | 1.000035 | 1.000113 | 0.0061790 | 0.0061316 | 0.0059751 | 14779.1 | 0.0000071 | 0.95 | 0.0045330 | 0.0078754 |
| St. Bride's lower churchyard | 1770 | 1849 | beta | 1.000155 | 1.000339 | 0.0510752 | 0.0510280 | 0.0511331 | 11203.6 | 0.0000422 | 0.95 | 0.0423814 | 0.0598976 |
| St. Bride's lower churchyard | 1770 | 1849 | M | 1.000130 | 1.000460 | 53.4368072 | 53.4511152 | 53.4536777 | 46992.7 | 0.0074618 | 0.95 | 50.2090353 | 56.5697935 |
| Sheen's burial ground | 1763 | 1854 | alpha | 1.000130 | 1.000400 | 0.0129642 | 0.0128270 | 0.0124596 | 28565.8 | 0.00014018 | 0.95 | 0.0089230 | 0.0173233 |
| Sheen's burial ground | 1763 | 1854 | beta | 1.00031 | 1.000320 | 0.0353994 | 0.0353305 | 0.0350479 | 24673.6 | 0.0000300 | 0.95 | 0.0262620 | 0.0446735 |
| Sheen's burial ground | 1763 | 1854 | M | 1.000171 | 1.000430 | 39.9956498 | 40.5717091 | 41.5741951 | 29050.5 | 0.0299067 | 0.95 | 29.5817256 | 49.0658033 |
| Bow Baptist Church | 1816 | 1854 | alpha | 1.000120 | 1.000420 | 0.0177742 | 0.0176655 | 0.0171967 | 37363.4 | 0.0233007 | 0.95 | 0.0135868 | 0.0221462 |
| Bow Baptist Church | 1816 | 1854 | beta | 1.000037 | 1.000121 | 0.0344658 | 0.0344556 | 0.0344680 | 30272.0 | 0.0000114 | 0.95 | 0.0150000 | 0.0429301 |
| Bow Baptist Church | 1816 | 1854 | M | 1.000013 | 1.000063 | 30.6580796 | 31.3283020 | 32.6360138 | 33171.9 | 0.0000249 | 0.95 | 20.3999444 | 39.3695617 |
| St. Mary and St. Michael | 1843 | 1853 | alpha | 1.000523 | 1.001826 | 0.0186478 | 0.0185639 | 0.0182508 | 41699.1 | 0.00000099 | 0.95 | 0.0148267 | 0.0227130 |
| St. Mary and St. Michael | 1843 | 1853 | beta | 1.000323 | 1.001320 | 0.0130473 | 0.0402172 | 0.0404972 | 35162.0 | 0.0000039 | 0.95 | 0.0148207 | 0.0481568 |
| St. Mary and St. Michael | 1843 | 1853 | M | 1.000441 | 1.001467 | 30.8426109 | 31.1889790 | 31.6656994 | 38394.2 | 0.0000216 | 0.95 | 24.1587401 | 36.9724139 |
| St. Bride's crypt (known age) | 1740 | 1853 | alpha | 1.001301 | 1.001944 | 0.0048650 | 0.0048100 | 0.0046364 | 11054.4 | 0.0171194 | 0.95 | 0.0033513 | 0.0064885 |
| | 1740 | 1853 | aipna beta | 1.001301 | 1.004385 | 0.0048650 | 0.0048100 | 0.0046364 | 10034.4 | 0.0000077 | 0.95 | 0.0033513 | 0.0064885 |
| St. Bride's crypt (known age) | | | | | | | | | | | | | |
| St. Bride's crypt (known age) | 1740 | 1853 | M | 1.000820 | 1.002819 | 59.1168993 | 59.1961001 | 59.4409448 | 16528.6 | 0.0139187 | 0.95 | 55.5069567 | 62.4858268 |
| St. Bride's crypt (estimates) | 1740 | 1853 | alpha | 1.000250 | 1.000942 | 0.0050511 | 0.0049857 | 0.0049500 | 13935.6 | 0.0000077 | 0.95 | 0.0033266 | 0.0068431 |
| St. Bride's crypt (estimates) | 1740 | 1853 | beta | 1.000251 | 1.000919 | 0.0461973 | 0.0460966 | 0.0460772 | 11655.0 | 0.0000408 | 0.95 | 0.0375863 | 0.0548062 |
| St. Bride's crypt (estimates) | 1740 | 1853 | M | 1.000110 | 1.000431 | 60.0918241 | 60.1324772 | 60.2370171 | 29765.3 | 0.0137390 | 0.95 | 55.4315320 | 64.7329115 |

kable(wellcome_result_r, caption = "London cemeteries data, rate") %>%
kableExtra::kable_styling(latex_options = c("HOLD_position", "scale_down"))

Table 18: London cemeteries data, rate

| cemetery | start | end | parameter | PSRF Point est. | PSRF Upper C.I. | Mean | Median | Mode | ESS | MCSE | HDImass | HDIlow | HDIhigh |
|---|-------|------|-----------|-----------------|-----------------|---------------|---------------|---------------|----------|-----------|---------|---------------|--------------|
| Bermondsey Abbey | 1089 | 1538 | alpha | 1.0001999 | 1.0007416 | 0.0105288 | 0.0104025 | 0.0101065 | 26895.4 | 0.0000111 | 0.95 | 0.0071225 | 0.0141935 |
| Bermondsey Abbey | 1089 | 1538 | beta | 1.0003786 | 1.0010986 | 0.0429176 | 0.0429090 | 0.0434181 | 24113.7 | 0.0000308 | 0.95 | 0.0335341 | 0.0522185 |
| Bermondsey Abbey | 1089 | 1538 | M | 1.0001327 | 1.0004472 | 44.7061829 | 44.9293082 | 45.3226906 | 30386.5 | 0.0198385 | 0.95 | 37.7940665 | 51.2834230 |
| Bermondsey Abbey | 1089 | 1538 | rate | 1.0000303 | 1.0000756 | 0.0039098 | 0.0039108 | 0.0039733 | 106914.0 | 0.0000076 | 0.95 | -0.0009505 | 0.0088325 |
| St. Mary Graces | 1350 | 1540 | alpha | 1.0001410 | 1.0003568 | 0.0169749 | 0.0168588 | 0.0167558 | 33748.3 | 0.0000119 | 0.95 | 0.0128271 | 0.0213266 |
| St. Mary Graces | 1350 | 1540 | beta | 1.0000433 | 1.0001007 | 0.0372463 | 0.0372464 | 0.0370084 | 30177.8 | 0.0000242 | 0.95 | 0.0289760 | 0.0454249 |
| St. Mary Graces | 1350 | 1540 | M | 1.0001281 | 1.0002492 | 32.7675640 | 33.2209124 | 33.9417464 | 31746.8 | 0.0236912 | 0.95 | 24.2993787 | 40.4275089 |
| St. Mary Graces | 1350 | 1540 | rate | 1.0001305 | 1.0004837 | 0.0051616 | 0.0051627 | 0.0052870 | 100496.1 | 0.0000078 | 0.95 | 0.0003122 | 0.0100454 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | alpha | 1.0000331 | 1.0001286 | 0.0228885 | 0.0227897 | 0.0226513 | 43799.9 | 0.0000115 | 0.95 | 0.0183155 | 0.0276638 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | beta | 1.0000350 | 1.0001314 | 0.0379869 | 0.0379887 | 0.0379277 | 41935.6 | 0.0000186 | 0.95 | 0.0304787 | 0.0454167 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | M | 1.0000459 | 1.0001549 | 24.9940336 | 25.4195077 | 26.1632091 | 39863.2 | 0.0202351 | 0.95 | 16.8860536 | 32.3216380 |
| St. Mary Hospital, 1120-1200 | 1120 | 1200 | rate | 1.0000328 | 1.0000475 | 0.0028308 | 0.0028305 | 0.0028200 | 115634.2 | 0.0000073 | 0.95 | -0.0021173 | 0.0076306 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | alpha | 1.0000810 | 1.0003099 | 0.0230203 | 0.0229469 | 0.0229048 | 50830.0 | 0.0000094 | 0.95 | 0.0189207 | 0.0272159 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | beta | 1.0001545 | 1.0005234 | 0.0398856 | 0.0398998 | 0.0399483 | 51029.8 | 0.0000157 | 0.95 | 0.0328956 | 0.0468336 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | M | 1.0000928 | 1.0003558 | 25.5429589 | 25.8389492 | 26.4616904 | 46661.4 | 0.0149967 | 0.95 | 19.0144549 | 31.4789393 |
| St. Mary Hospital, 1200-1250 | 1200 | 1250 | rate | 1.0000406 | 1.0000908 | 0.0129320 | 0.0129281 | 0.0127274 | 107875.9 | 0.0000076 | 0.95 | 0.0080676 | 0.0177871 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | alpha | 1.0000497 | 1.0001170 | 0.0184492 | 0.0184122 | 0.0182888 | 23215.0 | 0.0000084 | 0.95 | 0.0159587 | 0.0209832 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | beta | 1.0000407 | 1.0001310 | 0.0588094 | 0.0588085 | 0.0589706 | 23589.8 | 0.0000177 | 0.95 | 0.0534970 | 0.0641442 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | M | 1.0000497 | 1.0001156 | 31.6963826 | 31.7396954 | 31.8464384 | 24117.1 | 0.0070508 | 0.95 | 29.5007009 | 33.7824781 |
| St. Mary Hospital, 1250-1400 | 1250 | 1400 | rate | 0.9999962 | 0.9999989 | -0.0026207 | -0.0026209 | -0.0027932 | 56055.6 | 0.0000104 | 0.95 | -0.0073601 | 0.0022509 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | alpha | 1.0000223 | 1.0000549 | 0.0231055 | 0.0230308 | 0.0230113 | 41925.6 | 0.0000104 | 0.95 | 0.0190097 | 0.0273502 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | beta | 1.0000087 | 1.0000259 | 0.0399576 | 0.0399616 | 0.0400633 | 39732.1 | 0.0000178 | 0.95 | 0.0330820 | 0.0469712 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | M | 1.0000141 | 1.0000391 | 25.4683995 | 25.7644549 | 26.3462367 | 38317.9 | 0.0165837 | 0.95 | 18.9737587 | 31.4815633 |
| St. Mary Hospital, 1400-1539 | 1400 | 1539 | rate | 1.0000340 | 1.0000951 | 0.0050553 | 0.0050563 | 0.0051778 | 103432.2 | 0.0000077 | 0.95 | 0.0001496 | 0.0098918 |
| New Churchyard | 1569 | 1739 | alpha | 1.0001279 | 1.0002871 | 0.0211766 | 0.0211136 | 0.0212054 | 37764.5 | 0.0000100 | 0.95 | 0.0174176 | 0.0249711 |
| New Churchyard | 1569 | 1739 | beta | 1.0000753 | 1.0001933 | 0.0400944 | 0.0400933 | 0.0400801 | 35294.2 | 0.0000185 | 0.95 | 0.0332312 | 0.0468600 |
| New Churchyard | 1569 | 1739 | M | 1.0001440 | 1.0003447 | 27.7108539 | 27.9722139 | 28.4872019 | 35217.0 | 0.0160479 | 0.95 | 21.6010226 | 33.2292167 |
| New Churchyard | 1569 | 1739 | rate | 1.0000620 | 1.0001365 | 0.0082621 | 0.0082646 | 0.0083576 | 87104.3 | 0.0000084 | 0.95 | 0.0033814 | 0.0131413 |
| St. Benet Sherehog | 1670 | 1740 | alpha | 1.0001805 | 1.0006101 | 0.0132861 | 0.0131411 | 0.0129458 | 34008.4 | 0.0000119 | 0.95 | 0.0091934 | 0.0176933 |
| St. Benet Sherehog | 1670 | 1740 | beta | 1.0001190 | 1.0003512 | 0.0381719 | 0.0381737 | 0.0382241 | 31530.9 | 0.0000266 | 0.95 | 0.0289791 | 0.0474535 |
| St. Benet Sherehog | 1670 | 1740 | M | 1.0002037 | 1.0006791 | 39.3972135 | 39.8401136 | 40.1526185 | 34591.5 | 0.0241655 | 0.95 | 30.3535344 | 47.6481468 |
| St. Benet Sherehog | 1670 | 1740 | rate | 1.0000344 | 1.0000931 | 0.0059873 | 0.0059983 | 0.0060528 | 119114.7 | 0.0000072 | 0.95 | 0.0011010 | 0.0108270 |
| Chelsea Old church | 1712 | 1842 | alpha | 1.0002873 | 1.0010299 | 0.0058789 | 0.0057818 | 0.0055736 | 24844.5 | 0.0000075 | 0.95 | 0.0036917 | 0.0082560 |
| Chelsea Old church | 1712 | 1842 | beta | 1.0002128 | 1.0007988 | 0.0472765 | 0.0472197 | 0.0472248 | 21617.0 | 0.0000341 | 0.95 | 0.0374445 | 0.0571072 |
| Chelsea Old church | 1712 | 1842 | M | 1.0001776 | 1.0006011 | 56.3070206 | 56.3582529 | 56.7461356 | 44134.7 | 0.0138780 | 0.95 | 50.5873981 | 62.0866861 |
| Chelsea Old church | 1712 | 1842 | rate | 1.0000451 | 1.0001660 | 0.0100601 | 0.0100643 | 0.0101297 | 89138.8 | 0.0000084 | 0.95 | 0.0051571 | 0.0149469 |
| St. Marylebone | 1742 | 1817 | alpha | 1.0000748 | 1.0001372 | 0.0095679 | 0.0094649 | 0.0091973 | 30628.4 | 0.0000087 | 0.95 | 0.0067098 | 0.0125807 |
| St. Marylebone | 1742 | 1817 | beta | 1.0000415 | 1.0001241 | 0.0459357 | 0.0459208 | 0.0457528 | 27451.1 | 0.0000277 | 0.95 | 0.0370076 | 0.0549197 |
| St. Marylebone | 1742 | 1817 | M | 1.0000736 | 1.0001274 | 46.1751078 | 46.2984132 | 46.3570171 | 40003.8 | 0.0136968 | 0.95 | 40.7083583 | 51.4616051 |
| St. Marylebone | 1742 | 1817 | rate | 1.0000683 | 1.0002323 | 0.0095688 | 0.0095712 | 0.0093581 | 99214.5 | 0.0000079 | 0.95 | 0.0047434 | 0.0145099 |
| St. Marylebone Paddington Street north | 1772 | 1853 | alpha | 1.0000358 | 1.0000900 | 0.0065801 | 0.0065013 | 0.0064360 | 29127.9 | 0.0000066 | 0.95 | 0.0044463 | 0.0087891 |
| St. Marylebone Paddington Street north | 1772 | 1853 | beta | 1.0001415 | 1.0004460 | 0.0544281 | 0.0544209 | 0.0547945 | 26218.3 | 0.0000292 | 0.95 | 0.0452271 | 0.0637787 |
| St. Marylebone Paddington Street north | 1772 | 1853 | M | 0.9999975 | 1.0000085 | 50,9632692 | 50.9739902 | 50.9618065 | 49233.1 | 0.0098106 | 0.95 | 46.6741737 | 55.2372052 |
| St. Marylebone Paddington Street north | 1772 | 1853 | rate | 1.0000364 | 1.0001074 | 0.0144206 | 0.0144255 | 0.0141691 | 101071.9 | 0.0000078 | 0.95 | 0.0094983 | 0.0192607 |
| St. Bride's lower churchyard | 1770 | 1849 | alpha | 1.0011697 | 1.0042730 | 0.0037341 | 0.0036868 | 0.0036269 | 16620.6 | 0.0000049 | 0.95 | 0.0025631 | 0.0049982 |
| St. Bride's lower churchyard | 1770 | 1849 | beta | 1.0015090 | 1.0051365 | 0.0582705 | 0.0582224 | 0.0580684 | 12836.2 | 0.0000410 | 0.95 | 0.0491681 | 0.0672636 |
| St. Bride's lower churchyard | 1770 | 1849 | M | 1.0003029 | 1.0011116 | 59.3567949 | 59.3049875 | 59.1753323 | 40772.1 | 0.0095119 | 0.95 | 55.5901301 | 63.1117920 |
| St. Bride's lower churchyard | 1770 | 1849 | rate | 1.0003038 | 1.0011395 | 0.0143225 | 0.0143172 | 0.0141355 | 52696.3 | 0.0000108 | 0.95 | 0.0094154 | 0.0191705 |
| Sheen's burial ground | 1763 | 1854 | alpha | 1.0001549 | 1.0002068 | 0.0081112 | 0.0079857 | 0.0076079 | 28990.1 | 0.0000095 | 0.95 | 0.0051656 | 0.0113978 |
| Sheen's burial ground | 1763 | 1854 | beta | 1.0000827 | 1.0001417 | 0.0418442 | 0.0418050 | 0.0417337 | 27930.4 | 0.0000294 | 0.95 | 0.0322170 | 0.0514367 |
| Sheen's burial ground | 1763 | 1854 | M | 1.0001259 | 1.0001599 | 51.3035346 | 51.4719153 | 51.7458183 | 37127.6 | 0.0196709 | 0.95 | 43.8156221 | 58.7122226 |
| Sheen's burial ground | 1763 | 1854 | rate | 1.0000471 | 1,0000606 | 0.0143440 | 0.0143429 | 0.0142681 | 101954.9 | 0.0000078 | 0.95 | 0.0093921 | 0.0191445 |
| Bow Baptist Church | 1816 | 1854 | alpha | 1.0000751 | 1.0002591 | 0.0110080 | 0.0109048 | 0.0107115 | 41439.7 | 0.0000082 | 0.95 | 0.0078878 | 0.0143335 |
| Bow Baptist Church | 1816 | 1854 | beta | 1.0000831 | 1.0003245 | 0.0409501 | 0.0409441 | 0.0407475 | 36617.2 | 0.0000234 | 0.95 | 0.0322211 | 0.0497674 |
| Bow Baptist Church | 1816 | 1854 | M | 1.0000690 | 1.000210 | 44.0086393 | 44.2046299 | 44.6069317 | 46933.1 | 0.0152560 | 0.95 | 37.4300374 | 50.3741413 |
| Bow Baptist Church | 1816 | 1854 | rate | 1.0000216 | 1.0000239 | 0.0174851 | 0.0174851 | 0.0173758 | 106259.5 | 0.0000076 | 0.95 | 0.0125967 | 0.0223740 |
| St. Mary and St. Michael | 1843 | 1853 | alpha | 1.0001563 | 1.0005720 | 0.0122807 | 0.0121938 | 0.0120196 | 46093.7 | 0.0000074 | 0.95 | 0.0092409 | 0.0154457 |
| St. Mary and St. Michael | 1843 | 1853 | beta | 1.0002253 | 1.0007624 | 0.0459562 | 0.0459699 | 0.0456100 | 42613.3 | 0.0000011 | 0.95 | 0.0378149 | 0.0541866 |
| St. Mary and St. Michael | 1843 | 1853 | M | 1.0002203 | 1.0007024 | 40.6794124 | 40.8054593 | 41.3726101 | 51800.7 | 0.0109648 | 0.95 | 35.7481079 | 45.5245164 |
| St. Mary and St. Michael | 1843 | 1853 | rate | 1.0001423 | 1.0003033 | 0.0176425 | 0.0176439 | 0.0178219 | 111336.5 | 0.0103045 | 0.95 | 0.0128415 | 0.0226355 |
| St. Bride's crypt (known age) | 1740 | 1853 | alpha | 11.3187848 | 26,7160198 | 0.0062628 | 0.0058303 | 0.0034420 | 1.5 | 0.0018915 | 0.95 | 0.0031442 | 0.0102527 |
| St. Bride's crypt (known age) | 1740 | 1853 | beta | 11.7161168 | 22.9647008 | 0.0510415 | 0.0510591 | 0.0509381 | 1.4 | 0.0013313 | 0.95 | 0.0443241 | 0.0572525 |
| St. Bride's crypt (known age) | 1740 | 1853 | M | 11.7488400 | 23,5976438 | 53.9513110 | 54.4984270 | 54.3621152 | 1.4 | 4.7419679 | 0.95 | 44.8901900 | 62.3280593 |
| St. Bride's crypt (known age) | 1740 | 1853 | rate | 1.0001302 | 1.0004858 | -0.9898864 | -0.9898864 | -0.9898825 | 68206.5 | 0.0000004 | 0.95 | -0.9900793 | -0.9896890 |
| St. Bride's crypt (known age) St. Bride's crypt (estimates) | 1740 | 1853 | alpha | 1.0010883 | 1.0036469 | 0.8089951 | 0.8096464 | 0.8091857 | 3141.3 | 0.0003460 | 0.95 | 0.7708209 | 0.8467743 |
| St. Bride's crypt (estimates) | 1740 | 1853 | beta | 1.001033 | 1.0035453 | 0.0049692 | 0.0049308 | 0.0048867 | 3152.0 | 0.0000100 | 0.95 | 0.0036820 | 0.0063247 |
| St. Bride's crypt (estimates) | 1740 | 1853 | M | 1.00011031 | 1.0039337 | -1038.5780551 | -1022.5151667 | -1000.6858905 | 3228.3 | 3.1452459 | 0.95 | -1405.8300586 | -716.0579775 |
| St. Bride's crypt (estimates) | 1740 | 1853 | rate | 1.0000135 | 1.0000707 | -0.9873975 | -0.9873961 | -0.9874078 | 123992.2 | 0.0000071 | 0.95 | -0.9922468 | -0.9824618 |
| co crype (commeco) | 1110 | 1000 | | 1.0000200 | 1.0000101 | 0.0010010 | 0.0010001 | 0.0011010 | -20002.2 | 5.0000011 | 5.50 | 0.0022100 | 0.0021010 |

4.3 Modal ages from historical and osteological data

Figure 6: Modal ages from historical and osteological data

```
source("./chapter_04_results/english_wellcome.R")

## `geom_smooth()` using method = 'loess' and formula = 'y ~ x'

## `geom_smooth()` using method = 'loess' and formula = 'y ~ x'

## `geom_smooth()` using method = 'loess' and formula = 'y ~ x'

plot(modal_ages_plot)
```

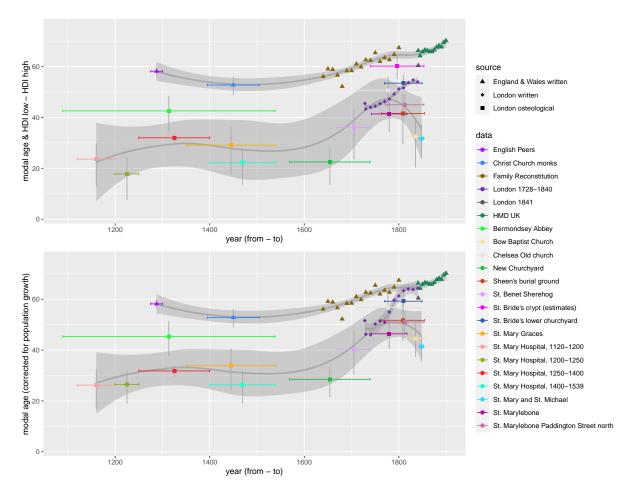


Table 2: Overview of modelled osteological data from London cemeteries

The data overview is build during pre-processing in ./chapter_04_results/Wellcome_DB.R and saved to a textfile (sep = $\setminus t$).

wellcome_overview_all

```
kable(wellcome overview all, caption = "London cemeteries overview") %>%
 kableExtra::kable_styling(latex_options = c("HOLD_position", "scale_down"))
```

M M_range ex20 ex25 M M_range beta beta_range beta beta_range ex20 ex25 cemetery 25.5 22.7 Bermondsey Abbey 0.0414 0.0319-0.0504 42.6 34.7-48.4 22.7 0.0434 0.0335-0.0522 45.3 37.8-51.3 26.8 23.8 Bow Baptist Church Chelsea Old church 0.0345 0.026-0.0429 32.6 20.4-39.4 20.4 0.0407 0.0322-0.0498 44.6 37.4-50.4 27.1 24.2 50.7 44-56.1 30.4 27.3 0.0472 50.6-62.1 33.9 30.4 0.0422 0.0328-0.0518 0.0374-0.0571 New Churchyard 0.0365 0.0299-0.0432 22.5 13.7-27.9 17.0 15.0 0.0401 0.0332-0.0469 28.5 21.6-33.2 18.3 16.1 Sheen's burial ground 0.0350 0.0263-0.0447 41.6 29.6-49.1 27.3 24.6 0.0417 0.0322-0.0514 51.7 43.8-58. 31.8 28.6 St. Benet Sherehog 0.029-0.0475 36.1 23.6-43.3 23.7 21.2 0.0382 40.2 25.3 22.7 0.0353 0.0265-0.0446 30.4-47.6 St. Bride's crypt (estimates) 60.2 55.4-64.7 36.4 32.8 -1405.8-716 1.2 1.2 0.0461 0.0376-0.0548 0.0049 0.0037-0.0063 1000.7 St. Bride's crypt (known age) St. Bride's lower churchyard 0.0491 0.0423-0.0565 59.4 55.5-62.5 50.2-56.6 35.7 32.0 0.0509 0.0443-0.0573 54.4 44 9-62 3 39.3 35.4 55.6-63.1 0.0424-0.0599 53.5 31.0 27.5 0.0492-0.0673 59.2 0.0511 0.0581 34.8 30.9 22.2 29.1 17.8-36.2 20.8 18.6 33.9 24.3-40.4 19.8 St. Mary Graces 0.0349 0.0267-0.0427 0.0370 St. Mary Hospital, 1120-1200
St. Mary Hospital, 1200-1250 0.0366 0.0289-0.0437 23.6 12.9-29.7 17.4 15.4 0.0379 0.0305-0.0454 26.2 16.9-32.3 18.1 16.0 7.7-24.3 17.5 15.3 0.0355 0.0289-0.0424 15.7 13.8 0.0329-0.0468 26.5 19-31.5 0.0399 St. Mary Hospital, 1250-1400 32.0 30-33.6 13.4 31.8 29.5-33.8 13.1 0.0577 0.0529-0.0634 16.0 0.0590 14.7 St. Mary Hospital, 1400-1539 0.0374 0.0307-0.0443 22.2 13.7-27. 0.0323-0.0482 31.7 24.2-37 13.7-27.8 16.7 0.0401 0.0331-0.047 26.3 19-31.5 17.4 15.2 23.6 20.8 20.0 17.6 0.0456 St. Mary and St. Michael 0.0378-0.0542 41.4 35.7-45.5 0.040541.4 34.4-46.1 24.5 21.7 27.2 24.1 0.0331-0.0508 St. Marylebone Paddington Street north 0.0486 0.0399-0.0578 45.0 40.2-49 25.4 22.4 0.0548 0.0452-0.0638 51.0 46.7-55.2 28.5 25.0

Table 19: London cemeteries overview

Figure 7: St. Bride's Crypt. Density of actual ages and Bayesian model of Gompertz distribution of actual ages and osteological estimates (without correction for population growth).

The plot is build in ./lifetables_processing/stbrides_crypt.R within the if-statement on runCodeNew (s. data limitations above).

plot(stbrides_crypt_plot)

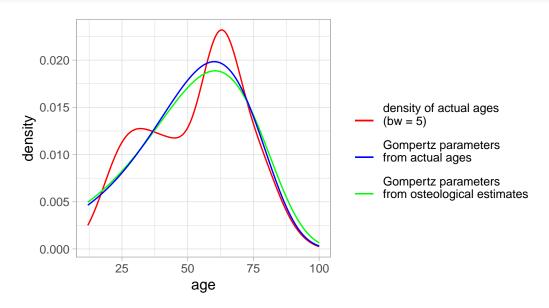
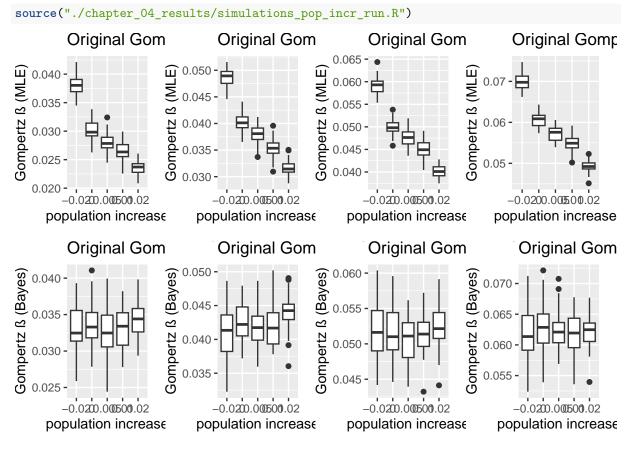


Figure 8: Simulation of population increase with known age-at-death and Maximum Likelihood Estimation (MLE) (top four) and osteological estimates, Bayesian model and including rate of increase (bottom four).



5 Supplements

The chapter 'Supporting informations' provides details about the London cemeteries included in the study.

5.1 The Coale & Demeny life tables

Calculation of the lowest β -value for any of their life tables is 0.0391 (the female table "West", level 1).

```
source("./chapter_supplement/coale_demeny_life_tables_gompertz.R")
min(gompertz_df$Gompertz_shape)
```

[1] 0.03913138

5.2 Gompertz parameters

Simulations for evaluation of algorithms for retrieving Gompertz parameters. The file simulations_run.R provides various tests and plots from the evaluation process. Plot the results of methods with known age-at-death.

```
source("./chapter_supplement/simulations_run.R")
## Scale for y is already present.
## Adding another scale for y, which will replace the existing scale.
gridExtra::grid.arrange(grobs = plot_list_shapes, ncol = 3)
                                                WOLS
                                                                                      WNLS
           OLS
 estimated \Bar{k} estimated \Bar{k} estimated \Bar{k} estimated
                                                                            estimated
                                       estimated
     8:458 =
             0.025 0.050 0.075 0.100
                                                   0.025 0.050 0.075 0.100
                                                                                        0.025 0.050 0.075 0.100
                  original ß
                                                        original ß
                                                                                             original ß
                                                                            estimated ß
                                       ~
                                                                                      survival (10y-cat)
           survival
                                       estimated
                                                survival (5y-cat)
             0.025 0.050 0.075 0.100
                                                   0.025 0.050 0.075 0.100
                                                                                        0.025 0.050 0.075 0.100
                  original ß
                                                        original ß
                                                                                             original ß
                                                                            estimated ß
                                      estimated ß
           MLE
                                                 MLE (5y-cat)
                                                                                      MLE (10y-cat)
                                                                                        0.025 0.050 0.075 0.100
             0.025 0.050 0.075 0.100
                                                   0.025 0.050 0.075 0.100
                  original ß
                                                        original ß
                                                                                             original ß
                                                                            estimated ß
                                      estimated ß
                                                 Bayes (5y-cat)
                                                                                      Bayes (10y-cat)
           Bayes
             0.025 0.050 0.075 0.100
                                                   0.025 0.050 0.075 0.100
                                                                                        0.025 0.050 0.075 0.100
                  original ß
                                                        original ß
                                                                                             original ß
           Bayes poisson
             0.025 0.050 0.075 0.100
                  original ß
```

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