```
## Load libraries
library(splines)
library(MASS)
library(FDRreg)
## Loading required package: fda
## Loading required package: Matrix
## Attaching package: 'fda'
## The following object is masked from 'package:graphics':
##
      matplot
##
## Loading required package: BayesLogit
## Loading required package: mutnorm
## Warning: package 'mvtnorm' was built under R version 3.3.2
library(curl)
library(doParallel) ##to make cluster (on Windows)
## Warning: package 'doParallel' was built under R version 3.3.2
## Loading required package: foreach
## Loading required package: iterators
## Loading required package: parallel
library(foreach) ##to use foreach function that does the parallel processing
library(doRNG) ##for reproducible seeds when doing parallel processing
## Loading required package: rngtools
## Loading required package: pkgmaker
## Loading required package: registry
##
## Attaching package: 'pkgmaker'
## The following object is masked from 'package:base':
##
##
      isNamespaceLoaded
```

### 1 Probability of being a false positive as a linear function of time

Load simulations and (re)define some variables:

```
load("simResults_1.RData")

nSims <- length(pValuesSims)</pre>
```

```
ntest <- length(pValuesSims[[1]])
## Set up the time vector and the probability of being null
tme <- seq(-1,2,length=ntest)
pi0 <- 1/4*tme+1/2</pre>
```

### Perform estimation and save estimates:

```
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMat <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorhandling
       \#\#first\ transform\ the\ p-values\ into\ z-scores
       ##randomly assign positive or negative sign
      zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2) ##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2) ##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim
      fdr <- FDRreg(zScores, matrix(tme, ncol=1),</pre>
                                                     nulltype = 'empirical',
                                                      control=list(lambda=1));
      piOhatScott.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
dim(pi0hatScottMat)
## [1] 8761 1000
pi0hatScottMean <- colMeans(pi0hatScottMat)</pre>
piOhatScottVar <- apply(piOhatScottMat,2,var)</pre>
length(pi0hatScottMean)
## [1] 1000
##save results
save(file="simResults_pi0x_Scott_1.RData",
                 list=c("tme", "pi0",
                                         "pi0hatScottMean","pi0hatScottVar"))
```

## 2 Probability of being a false positive as a smooth function of time

Load simulations and (re)define some variables:

```
load("simResults_2.RData")

nSims <- length(pValuesSims)
ntest <- length(pValuesSims[[1]])

## Set up the time vector and the probability of being null
tme <- seq(-1,2,length=ntest)
pi0 <- pnorm(tme)

splineMat <- ns(tme,df=3)</pre>
```

Perform estimation and save estimates:

```
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMatFitLin <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorham
  zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2)##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)##
  fdr <- FDRreg(zScores, tme,</pre>
                 nulltype = 'empirical',
                 control=list(lambda=1));
  piOhatScottMatFitLin.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMatFitSpl <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorham
  zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2)##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)
  fdr <- FDRreg(zScores, splineMat,</pre>
                 nulltype = 'empirical',
                 control=list(lambda=1));
  piOhatScottMatFitSpl.sim <- 1-fdr$priorprob</pre>
```

```
##close the cluster
stopCluster(cl)
dim(pi0hatScottMatFitLin)
## [1] 8703 1000
dim(piOhatScottMatFitSpl)
## [1] 8703 1000
pi0hatLin.ScottMean <- colMeans(pi0hatScottMatFitLin)</pre>
piOhatLin.ScottVar <- apply(piOhatScottMatFitLin,2,var)</pre>
pi0hatSpl.ScottMean <- colMeans(pi0hatScottMatFitSpl)</pre>
pi0hatSpl.ScottVar <- apply(pi0hatScottMatFitSpl,2,var)</pre>
length(pi0hatLin.ScottMean)
## [1] 1000
length(pi0hatSpl.ScottMean)
## [1] 1000
##save results
save(file="simResults_pi0x_Scott_2.RData",
     list=c("tme", "pi0",
            "piOhatLin.ScottMean", "piOhatLin.ScottVar",
            "piOhatSpl.ScottMean", "piOhatSpl.ScottVar"))
```

# 3 Probability of being a false positive as a sine + step function

Load simulations and (re)define some variables:

```
load("simResults_3.RData")

nSims <- length(pValuesSims)
ntest <- length(pValuesSims[[1]])

## Set up the time vector and the probability of being null</pre>
```

```
tme1 <- seq(-1*pi,2*pi,length=ntest)
tme2 <- rep(1:0, each=ntest/2)

pi0 <- 1/4*sin(tme1) + tme2/4 + 1/2
range(pi0)

## [1] 0.2500028 0.9999972

splineMat3 <- cbind(ns(tme1,df=3), tme2)
splineMat20 <- cbind(ns(tme1,df=20), tme2)</pre>
```

#### Perform estimation and save estimates:

```
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMat3 <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorhandling
      zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2)##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)##
     fdr <- FDRreg(zScores, splineMat3,</pre>
                                                 nulltype = 'empirical',
                                                  control=list(lambda=1));
     piOhatScottMat3.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMat20 <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorhandling")
      zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2) ##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2) ##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim
      fdr <- FDRreg(zScores, splineMat20,</pre>
                                                 nulltype = 'empirical',
                                                 control=list(lambda=1));
     piOhatScottMat20.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
dim(pi0hatScottMat3)
```

```
## [1] 8900 1000
dim(pi0hatScottMat20)
## [1] 8900 1000
pi0hat3.ScottMean <- colMeans(pi0hatScottMat3)</pre>
pi0hat3.ScottVar <- apply(pi0hatScottMat3,2,var)</pre>
pi0hat20.ScottMean <- colMeans(pi0hatScottMat20)</pre>
pi0hat20.ScottVar <- apply(pi0hatScottMat20,2,var)</pre>
length(pi0hat3.ScottMean)
## [1] 1000
length(pi0hat20.ScottMean)
## [1] 1000
##save results
save(file="simResults_pi0x_Scott_3.RData",
     list=c("tme1", "tme2", "pi0",
             "pi0hat3.ScottMean", "pi0hat3.ScottVar",
            "pi0hat20.ScottMean", "pi0hat20.ScottVar"))
```

### Session info:

```
devtools::session_info()
## Session info -----
## setting value
## version R version 3.3.1 (2016-06-21)
## system x86_64, mingw32
       RTerm
## ui
## language (EN)
## collate English_United States.1252
## tz America/New_York
## date
         2017-01-02
## Packages -----
## package * version date
## assertthat 0.1 2013-12-06
## BayesLogit * 0.5.1 2014-07-21
## codetools 0.2-14 2015-07-15
## colorspace 1.2-6 2015-03-11
```

```
curl
              * 1.0
                        2016-07-24
##
##
   DBI
                 0.4-1
                        2016-05-08
##
   devtools
                1.12.0
                        2016-06-24
##
   digest
                 0.6.9
                         2016-01-08
   doParallel * 1.0.10 2015-10-14
##
##
   doRNG
               * 1.6
                         2014-03-07
##
   dplyr
                0.5.0
                        2016-06-24
##
    evaluate
                0.10
                        2016-10-11
##
              * 2.4.4
                        2014-12-16
   fda
              * 0.2-1
##
   FDRreg
                        2016-08-30
##
   foreach
              * 1.4.3
                        2015-10-13
##
   ggdendro
               0.1-20 2016-04-27
                2.1.0
                        2016-03-01
##
    ggplot2
##
    gridExtra
                2.2.1
                        2016-02-29
##
                0.2.0
                        2016-02-26
   gtable
##
   highr
                0.6
                        2016-05-09
   iterators * 1.0.8
                        2015-10-13
##
##
   knitr
              * 1.15.1 2016-11-22
##
   lattice
                0.20-33 2015-07-14
   lazyeval
               0.2.0
                        2016-06-12
##
               1.5
                         2014-11-22
##
   magrittr
##
   MASS
               * 7.3-45
                        2016-04-21
##
   Matrix
              * 1.2-6
                        2016-05-02
##
   memoise
                1.0.0
                        2016-01-29
##
   mosaic
                0.14.4 2016-07-29
##
   mosaicData 0.14.0 2016-06-17
##
   munsell
                0.4.3
                        2016-02-13
##
   mvtnorm
              * 1.0-5
                        2016-02-02
                        2014-05-14
              * 0.22
##
   pkgmaker
##
               1.8.4
                        2016-06-08
   plyr
##
   R6
               2.1.2
                        2016-01-26
               0.12.6 2016-07-19
##
   Rcpp
##
   registry
              * 0.3
                        2015-07-08
## rngtools
             * 1.2.4
                        2014-03-06
   scales
               0.4.0
                        2016-02-26
##
   stringi
##
                1.1.1
                        2016-05-27
##
   stringr
                1.0.0
                         2015-04-30
##
   tibble
                1.1
                        2016-07-04
   tidyr
                0.5.1
                        2016-06-14
##
##
   withr
                1.0.2
                        2016-06-20
                1.8-2
##
   xtable
                        2016-02-05
##
   source
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.0)
   CRAN (R 3.3.1)
```

```
## CRAN (R 3.3.1)
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   CRAN (R 3.3.1)
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    CRAN (R 3.3.1)
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    CRAN (R 3.3.2)
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    CRAN (R 3.3.1)
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    CRAN (R 3.3.1)
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    CRAN (R 3.3.2)
##
    CRAN (R 3.3.1)
##
    Github (jgscott/FDRreg@8025d1a)
    CRAN (R 3.3.1)
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##
    CRAN (R 3.3.1)
   CRAN (R 3.3.1)
```