```
## Load libraries
library(splines)
library(MASS)
library(FDRreg)
## Loading required package: fda
## Loading required package: Matrix
## Attaching package: 'fda'
## The following object is masked from 'package:graphics':
##
      matplot
##
## Loading required package: BayesLogit
## Loading required package: mutnorm
library(curl)
library(doParallel) ##to make cluster (on Windows)
## Warning: package 'doParallel' was built under R version 3.3.2
## Loading required package: foreach
## Loading required package: iterators
## Loading required package: parallel
library(foreach) ##to use foreach function that does the parallel processing
library(doRNG) ##for reproducible seeds when doing parallel processing
## Loading required package: rngtools
## Loading required package: pkgmaker
## Loading required package: registry
## Attaching package: 'pkgmaker'
## The following object is masked from 'package:base':
##
##
      is Names pace Loaded
```

1 Probability of being a false positive as a linear function of time

Load simulations and (re)define some variables:

```
load("simResults_1.RData")

nSims <- length(pValuesSims)
ntest <- length(pValuesSims[[1]])</pre>
```

```
## Set up the time vector and the probability of being null
tme <- seq(-1,2,length=ntest)
pi0 <- 1/4*tme+1/2</pre>
```

Perform estimation and save estimates:

```
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMat <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorhandling
       \#\#first\ transform\ the\ p-values\ into\ z-scores
       ##randomly assign positive or negative sign
       zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2) \# **sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)) \# **sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)) # 
      fdr <- FDRreg(zScores, matrix(tme, ncol=1),</pre>
                                                     nulltype = 'empirical',
                                                      control=list(lambda=1));
      piOhatScott.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
dim(pi0hatScottMat)
## [1] 8883 1000
piOhatScottMean <- colMeans(piOhatScottMat)</pre>
piOhatScottVar <- apply(piOhatScottMat,2,var)</pre>
length(pi0hatScottMean)
## [1] 1000
##save results
save(file="simResults_pi0x_Scott_1.RData",
                list=c("tme", "pi0",
                                         "pi0hatScottMean","pi0hatScottVar"))
```

2 Probability of being a false positive as a smooth function of time

Load simulations and (re)define some variables:

```
load("simResults_2.RData")

nSims <- length(pValuesSims)
ntest <- length(pValuesSims[[1]])

## Set up the time vector and the probability of being null
tme <- seq(-1,2,length=ntest)
pi0 <- pnorm(tme)

splineMat <- ns(tme,df=3)</pre>
```

Perform estimation and save estimates:

```
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMatFitLin <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorham
      zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2)##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)##
     fdr <- FDRreg(zScores, tme,</pre>
                                                 nulltype = 'empirical',
                                                  control=list(lambda=1));
     piOhatScottMatFitLin.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMatFitSpl <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorham</pre>
      zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2) ##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2) ##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim
     fdr <- FDRreg(zScores, splineMat,</pre>
                                                 nulltype = 'empirical',
                                                  control=list(lambda=1));
     piOhatScottMatFitSpl.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
```

```
dim(piOhatScottMatFitLin)
## [1] 8779 1000
dim(pi0hatScottMatFitSpl)
## [1] 8779 1000
piOhatLin.ScottMean <- colMeans(piOhatScottMatFitLin)</pre>
piOhatLin.ScottVar <- apply(piOhatScottMatFitLin,2,var)</pre>
pi0hatSpl.ScottMean <- colMeans(pi0hatScottMatFitSpl)</pre>
pi0hatSpl.ScottVar <- apply(pi0hatScottMatFitSpl,2,var)</pre>
length(pi0hatLin.ScottMean)
## [1] 1000
length(pi0hatSpl.ScottMean)
## [1] 1000
##save results
save(file="simResults_pi0x_Scott_2.RData",
     list=c("tme", "pi0",
            "piOhatLin.ScottMean", "piOhatLin.ScottVar",
            "piOhatSpl.ScottMean", "piOhatSpl.ScottVar"))
```

3 Probability of being a false positive as a sine + step function

Load simulations and (re)define some variables:

```
load("simResults_3.RData")

nSims <- length(pValuesSims)
ntest <- length(pValuesSims[[1]])

## Set up the time vector and the probability of being null
tme1 <- seq(-1*pi,2*pi,length=ntest)
tme2 <- rep(1:0, each=ntest/2)

pi0 <- 1/4*sin(tme1) + tme2/4 + 1/2
range(pi0)</pre>
```

```
## [1] 0.2500028 0.9999972

splineMat3 <- cbind(ns(tme1,df=3), tme2)
splineMat20 <- cbind(ns(tme1,df=20), tme2)</pre>
```

Perform estimation and save estimates:

```
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMat3 <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorhandling
  zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2)##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)##
  fdr <- FDRreg(zScores, splineMat3,</pre>
                 nulltype = 'empirical',
                 control=list(lambda=1));
  piOhatScottMat3.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
cl<-makeCluster(8) ##specify number of cores less than or equal to number of cores on your
registerDoParallel(cl)
set.seed(31084)
piOhatScottMat20 <- foreach(sim=1:nSims, .combine="rbind", .packages="FDRreg", .errorhandling")
  zScores \leftarrow qnorm(1-pValuesSims[[sim]]/2)##*sample(c(-1,1), replace=TRUE, size=length(pValuesSims[[sim]]/2)##
  fdr <- FDRreg(zScores, splineMat20,</pre>
                 nulltype = 'empirical',
                 control=list(lambda=1));
  piOhatScottMat20.sim <- 1-fdr$priorprob</pre>
##close the cluster
stopCluster(cl)
dim(pi0hatScottMat3)
## [1] 9045 1000
dim(pi0hatScottMat20)
## [1] 9045 1000
```

Session info:

```
devtools::session_info()
## Session info -----
## setting value
## version R version 3.3.1 (2016-06-21)
## system x86_64, mingw32
       RTerm
## ui
## language (EN)
## collate English_United States.1252
## tz
         America/New_York
## date
           2016-12-31
## Packages -----
## package * version date
## assertthat 0.1 2013-12-06
## BayesLogit * 0.5.1 2014-07-21
## codetools 0.2-14 2015-07-15
## colorspace 1.2-6 2015-03-11
## curl * 1.0 2016-07-24
            0.4-1 2016-05-08
## DBI
## devtools 1.12.0 2016-06-24
## digest 0.6.9 2016-01-08
## doParallel * 1.0.10 2015-10-14
```

```
##
   doRNG
               * 1.6
                         2014-03-07
##
   dplyr
                 0.5.0
                         2016-06-24
##
   evaluate
                 0.10
                         2016-10-11
##
               * 2.4.4
                         2014-12-16
   fda
               * 0.2-1
                         2016-08-30
##
   FDRreg
##
    foreach
               * 1.4.3
                         2015-10-13
##
    ggdendro
                 0.1-20
                         2016-04-27
##
    ggplot2
                 2.1.0
                         2016-03-01
##
   gridExtra
                 2.2.1
                         2016-02-29
                 0.2.0
##
    gtable
                         2016-02-26
##
   highr
                 0.6
                         2016-05-09
   iterators * 1.0.8
##
                         2015-10-13
##
   knitr
               * 1.15.1 2016-11-22
##
   lattice
                 0.20-33 2015-07-14
               0.2.0
                         2016-06-12
##
   lazyeval
##
   magrittr
                1.5
                         2014-11-22
##
   MASS
               * 7.3-45 2016-04-21
##
   Matrix
               * 1.2-6
                         2016-05-02
##
   memoise
                1.0.0
                         2016-01-29
   mosaic
                0.14.4 2016-07-29
##
   mosaicData 0.14.0
                         2016-06-17
##
               0.4.3
##
   munsell
                         2016-02-13
##
   mvtnorm
               * 1.0-5
                         2016-02-02
##
   pkgmaker * 0.22
                         2014-05-14
##
   plyr
                 1.8.4
                         2016-06-08
##
   R6
                 2.1.2
                         2016-01-26
##
   Rcpp
                 0.12.6 2016-07-19
##
   registry
               * 0.3
                         2015-07-08
## rngtools
                         2014-03-06
               * 1.2.4
##
   scales
                0.4.0
                         2016-02-26
##
   stringi
                 1.1.1
                         2016-05-27
##
   stringr
                 1.0.0
                         2015-04-30
##
   tibble
                 1.1
                         2016-07-04
##
   tidyr
                 0.5.1
                         2016-06-14
##
   withr
                 1.0.2
                         2016-06-20
                 1.8-2
##
   xtable
                         2016-02-05
##
   source
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.0)
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   CRAN (R 3.3.1)
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```
## CRAN (R 3.3.2)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.2)
##
   CRAN (R 3.3.1)
##
   Github (jgscott/FDRreg@8025d1a)
   CRAN (R 3.3.1)
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