```
## Load libraries
library(splines)
library(MASS)
library(FDRreg)
## Loading required package: fda
## Warning: package 'fda' was built under R version 3.3.3
## Loading required package: Matrix
##
## Attaching package: 'fda'
## The following object is masked from 'package:graphics':
##
      matplot
## Loading required package: BayesLogit
## Warning: package 'BayesLogit' was built under R version 3.3.2
## Loading required package: mutnorm
## Warning: package 'mvtnorm' was built under R version 3.3.2
library(curl)
library(doParallel) ##to make cluster (on Windows)
## Loading required package: foreach
## Loading required package: iterators
## Loading required package: parallel
library(foreach) ##to use foreach function that does the parallel processing
library(doRNG) ##for reproducible seeds when doing parallel processing
## Loading required package: rngtools
## Warning: package 'rngtools' was built under R version 3.3.2
## Loading required package: pkgmaker
## Warning: package 'pkgmaker' was built under R version 3.3.2
## Loading required package: registry
## Warning: package 'registry' was built under R version 3.3.2
##
## Attaching package: 'pkgmaker'
## The following object is masked from 'package:base':
##
##
      isNamespaceLoaded
##Source functions
source("../functions.R")
options(warn=1)
```

Define nulltype for Scott method:

```
nulltype <- "empirical"</pre>
```

Simulations are performed for a variety of alternative distributions:

1 Probability of being a false positive is flat

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_1.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
 piOhatScottMat_emp <- estimate_Scott_sims(zValuesSims, tme, nulltype)</pre>
 pi0hatScottMean_emp <- colMeans(pi0hatScottMat_emp[,1:ntest])</pre>
 pi0hatScottVar_emp <- apply(pi0hatScottMat_emp[,1:ntest],2,var)</pre>
 piOhat.ScottMat_emp <- piOhatScottMat_emp[,1:ntest]</pre>
 FDR.ScottMat_emp <- pi0hatScottMat_emp[,(ntest+1):(2*ntest)]</pre>
  ##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_1_full.RData", sep="/"),
       list=c("pi0hat.ScottMat_emp", "FDR.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_1.RData", sep="/"),
       list=c("tme", "pi0",
            "piOhatScottMean_emp","piOhatScottVar_emp"))
## [1] "alt_beta"
## [1] "alt_chisq_large_3_3"
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
```

```
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Error in apply(as.matrix(piOhatScottMat), 2, as.numeric): (list)
object cannot be coerced to type 'double'
```

2 Probability of being a false positive is smooth in one variable

```
for(alt in alts)
{
    print(alt)

load(paste(alt, "simResults_2.RData", sep="/"))
    ntest <- ncol(zValuesSims)

##------##
print("linear")
piOhatScottMat_empFitLin <- estimate_Scott_sims(zValuesSims, tme, nulltype)

piOhatLin.ScottMean_emp <- colMeans(piOhatScottMat_empFitLin[,1:ntest])
piOhatLin.ScottVar_emp <- apply(piOhatScottMat_empFitLin[,1:ntest], 2, var)

piOhat.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,1:ntest]
FDR.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,(ntest+1):(2*ntest)]

##------spline fit--------#
print("spline")
splineMat <- ns(tme,df=3)</pre>
```

```
pi0hatScottMat_empFitSpl <- estimate_Scott_sims(zValuesSims, splineMat, nulltype)</pre>
  piOhatSpl.ScottMean_emp <- colMeans(piOhatScottMat_empFitSpl[,1:ntest])</pre>
  pi0hatSpl.ScottVar_emp <- apply(pi0hatScottMat_empFitSpl[,1:ntest],2,var)</pre>
  piOhat.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,1:ntest]</pre>
  FDR.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,(ntest+1):(2*ntest)]</pre>
  ##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_2_full.RData", sep="/"),
       list=c("pi0hat.Lin.ScottMat_emp", "FDR.Lin.ScottMat_emp",
              "piOhat.Spl.ScottMat_emp", "FDR.Spl.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_2.RData", sep="/"),
       list=c("tme", "pi0",
              "piOhatLin.ScottMean_emp", "piOhatLin.ScottVar_emp",
              "piOhatSpl.ScottMean_emp", "piOhatSpl.ScottVar_emp"))
## [1] "alt_beta"
## [1] "linear"
## [1] "spline"
## [1] "alt_chisq_large_3_3"
## [1] "linear"
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Error in apply(as.matrix(piOhatScottMat), 2, as.numeric): (list)
object cannot be coerced to type 'double'
```

3 Probability of being a false positive is smooth in one variable within levels of second variable

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_3.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
 m <- model.matrix(~as.character(tme2))[,-1]</pre>
 linearMat <- cbind(tme1, m)</pre>
  splineMat <- cbind(ns(tme1,df=3), m)</pre>
  ##----##
  print("linear")
 pi0hatScottMat_empFitLin <- estimate_Scott_sims(zValuesSims, linearMat, nulltype)</pre>
 pi0hatLin.ScottMean_emp <- colMeans(pi0hatScottMat_empFitLin[,1:ntest])</pre>
 pi0hatLin.ScottVar_emp <- apply(pi0hatScottMat_empFitLin[,1:ntest],2,var)</pre>
  piOhat.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,1:ntest]</pre>
  FDR.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,(ntest+1):(2*ntest)]
  ##-----#
  print("spline")
  pi0hatScottMat_empFitSpl <- estimate_Scott_sims(zValuesSims, splineMat, nulltype)</pre>
  pi0hatSpl.ScottMean_emp <- colMeans(pi0hatScottMat_empFitSpl[,1:ntest])</pre>
 piOhatSpl.ScottVar_emp <- apply(piOhatScottMat_empFitSpl[,1:ntest],2,var)</pre>
  piOhat.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,1:ntest]</pre>
 FDR.Spl.ScottMat_emp <- pi0hatScottMat_empFitSpl[,(ntest+1):(2*ntest)]</pre>
  ##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_3_full.RData", sep="/"),
       list=c("piOhat.Lin.ScottMat_emp", "FDR.Lin.ScottMat_emp",
              "piOhat.Spl.ScottMat_emp", "FDR.Spl.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_3.RData", sep="/"),
       list=c("tme", "pi0",
```

```
"piOhatLin.ScottMean_emp", "piOhatLin.ScottVar_emp",
              "piOhatSpl.ScottMean_emp", "piOhatSpl.ScottVar_emp"))
## [1] "alt_beta"
## [1] "linear"
## [1] "spline"
## [1] "alt_chisq_large_3_3"
## [1] "linear"
## [1] "spline"
## [1] "alt_chisq_large"
## [1] "linear"
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Error in apply(as.matrix(pi0hatScottMat), 2, as.numeric): (list)
object cannot be coerced to type 'double'
```

4 Probability of being a false positive is smooth in one variable within levels of second variable - lower priors

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_4.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
 m <- model.matrix(~as.character(tme2))[,-1]</pre>
 linearMat <- cbind(tme1, m)</pre>
  splineMat <- cbind(ns(tme1,df=3), m)</pre>
  ##----##
  print("linear")
  pi0hatScottMat_empFitLin <- estimate_Scott_sims(zValuesSims, linearMat, nulltype)</pre>
  ##if only have 2 columns, make everything NULL (this means there was an error in every si
  if(ncol(pi0hatScottMat_empFitLin) > 2)
    piOhatLin.ScottMean_emp <- colMeans(piOhatScottMat_empFitLin[,1:ntest])</pre>
    pi0hatLin.ScottVar_emp <- apply(pi0hatScottMat_empFitLin[,1:ntest],2,var)</pre>
    piOhat.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,1:ntest]</pre>
    FDR.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,(ntest+1):(2*ntest)]</pre>
  } else {
    piOhatLin.ScottMean_emp <- piOhatLin.ScottVar_emp <-</pre>
      piOhat.Lin.ScottMat_emp <- FDR.Lin.ScottMat_emp <- NULL</pre>
  ##----#
 print("spline")
 pi0hatScottMat_empFitSpl <- estimate_Scott_sims(zValuesSims, splineMat, nulltype)</pre>
  ##if only have 2 columns, make everything NULL (this means there was an error in every si
  if(ncol(pi0hatScottMat_empFitLin) > 2)
    pi0hatSpl.ScottMean_emp <- colMeans(pi0hatScottMat_empFitSpl[,1:ntest])</pre>
    pi0hatSpl.ScottVar_emp <- apply(pi0hatScottMat_empFitSpl[,1:ntest],2,var)</pre>
    pi0hat.Spl.ScottMat_emp <- pi0hatScottMat_empFitSpl[,1:ntest]</pre>
    FDR.Spl.ScottMat_emp <- pi0hatScottMat_empFitSpl[,(ntest+1):(2*ntest)]</pre>
    pi0hatSpl.ScottMean_emp <- pi0hatSpl.ScottVar_emp <-</pre>
      piOhat.Spl.ScottMat_emp <- FDR.Spl.ScottMat_emp <- NULL</pre>
```

```
##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_4_full.RData", sep="/"),
       list=c("pi0hat.Lin.ScottMat_emp", "FDR.Lin.ScottMat_emp",
              "piOhat.Spl.ScottMat_emp", "FDR.Spl.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_4.RData", sep="/"),
       list=c("tme", "pi0",
              "pi0hatLin.ScottMean_emp", "pi0hatLin.ScottVar_emp",
              "pi0hatSpl.ScottMean_emp", "pi0hatSpl.ScottVar_emp"))
## [1] "alt_beta"
## [1] "linear"
## [1] "spline"
## [1] "alt_chisq_large_3_3"
## [1] "linear"
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
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introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
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introduced by coercion
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introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(piOhatScottMat), 2, as.numeric): NAs
introduced by coercion
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
```

```
## Warning in apply(as.matrix(pi0hatScottMat), 2, as.numeric): NAs
introduced by coercion
## Error in apply(as.matrix(pi0hatScottMat), 2, as.numeric): (list)
object cannot be coerced to type 'double'
```

Session info:

```
devtools::session_info()
## Session info -----
## setting value
## version R version 3.3.1 (2016-06-21)
## system x86_64, mingw32
## ui
          RTerm
## language (EN)
## collate English_United States.1252
## tz America/New_York
         2017-06-13
## date
## Packages -----
## package * version date
## assertthat 0.1 2013-12-06
## BayesLogit * 0.6
                     2016-10-20
## codetools 0.2-14 2015-07-15
## colorspace 1.2-6 2015-03-11
        * 0.9.7 2016-04-10
## curl
            0.4-1
## DBI
                     2016-05-08
## devtools 1.12.0 2016-06-24
## digest 0.6.9 2016-01-08
## doParallel * 1.0.10 2015-10-14
## doRNG * 1.6
                    2014-03-07
## dplyr 0.4.3 2015-09-01
## evaluate 0.10 2016-10-11
           * 2.4.4 2014-12-16
## fda
## FDRreg
           * 0.2-1 2017-05-03
## foreach * 1.4.3 2015-10-13
            0.1-20 2016-04-27
## ggdendro
   ggplot2
            2.2.1 2016-12-30
## gridExtra 2.2.1 2016-02-29
## gtable
            0.2.0 2016-02-26
## highr
            0.6
                    2016-05-09
## iterators * 1.0.8
                     2015-10-13
## knitr * 1.15.1 2016-11-22
            0.20-33 2015-07-14
## lattice
## lazyeval 0.2.0 2016-06-12
```

```
magrittr 1.5 2014-11-22
##
##
   MASS
              * 7.3-45 2016-04-21
   Matrix
##
              * 1.2-6
                        2016-05-02
               1.0.0
                        2016-01-29
##
   {\tt memoise}
              0.14.4 2016-07-29
##
   mosaic
   mosaicData 0.14.0
                        2016-06-17
##
              0.4.3
##
   munsell
                        2016-02-13
##
   mvtnorm
              * 1.0-6
                        2017-03-02
##
   pkgmaker * 0.22
                        2014-05-14
##
   plyr
                1.8.4
                        2016-06-08
##
   R6
               2.1.2
                        2016-01-26
##
              0.12.10 2017-03-19
   Rcpp
## registry * 0.3
                        2015-07-08
## rngtools
             * 1.2.4
                        2014-03-06
## scales
              0.4.1
                        2016-11-09
## stringi
               1.1.1
                        2016-05-27
               1.0.0
                        2015-04-30
## stringr
##
   tibble
                1.2
                        2016-08-26
##
   tidyr
                0.5.1
                        2016-06-14
##
   withr
                1.0.2
                        2016-06-20
   xtable
                1.8-2
                        2016-02-05
##
##
   source
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.2)
##
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.3)
##
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.1)
##
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.3)
##
   Github (jgscott/FDRreg@8025d1a)
##
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.3)
##
   CRAN (R 3.3.3)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.1)
##
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.0)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.1)
```

```
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.3)
##
## CRAN (R 3.3.3)
## CRAN (R 3.3.1)
##
   CRAN (R 3.3.2)
##
   CRAN (R 3.3.2)
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.3)
##
##
   CRAN (R 3.3.2)
## CRAN (R 3.3.2)
## CRAN (R 3.3.3)
##
   CRAN (R 3.3.0)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.2)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
```