```
## Load libraries
library(splines)
library(MASS)
library(FDRreg)
## Loading required package: fda
## Warning: package 'fda' was built under R version 3.3.3
## Loading required package: Matrix
##
## Attaching package: 'fda'
## The following object is masked from 'package:graphics':
##
      matplot
## Loading required package: BayesLogit
## Warning: package 'BayesLogit' was built under R version 3.3.2
## Loading required package: mutnorm
## Warning: package 'mvtnorm' was built under R version 3.3.2
library(curl)
library(doParallel) ##to make cluster (on Windows)
## Loading required package: foreach
## Loading required package: iterators
## Loading required package: parallel
library(foreach) ##to use foreach function that does the parallel processing
library(doRNG) ##for reproducible seeds when doing parallel processing
## Loading required package: rngtools
## Warning: package 'rngtools' was built under R version 3.3.2
## Loading required package: pkgmaker
## Warning: package 'pkgmaker' was built under R version 3.3.2
## Loading required package: registry
## Warning: package 'registry' was built under R version 3.3.2
##
## Attaching package: 'pkgmaker'
## The following object is masked from 'package:base':
##
##
      isNamespaceLoaded
##Source functions
source("../functions.R")
options(warn=1)
```

Define nulltype for Scott method:

```
nulltype <- "empirical"</pre>
```

Simulations are performed for a variety of alternative distributions:

```
altsGrid <- as.matrix(expand.grid(dist=c("z","t"),nrBlocks=c(10,20),corr=c(0.2,0.5,0.9)))
alts <- apply(altsGrid, 1, function(x){paste("alt",x[1],"large",x[2],x[3],sep="_")})
alts

## [1] "alt_z_large_10_0.2" "alt_t_large_10_0.2"
## [3] "alt_z_large_20_0.2" "alt_t_large_20_0.2"
## [5] "alt_z_large_10_0.5" "alt_t_large_10_0.5"
## [7] "alt_z_large_20_0.5" "alt_t_large_20_0.5"
## [9] "alt_z_large_10_0.9" "alt_t_large_10_0.9"
## [11] "alt_z_large_20_0.9" "alt_t_large_20_0.9"</pre>
```

### 1 Probability of being a false positive is flat

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_1.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
 piOhatScottMat_emp <- estimate_Scott_sims(zValuesSims, tme, nulltype)
 pi0hatScottMean_emp <- colMeans(pi0hatScottMat_emp[,1:ntest])</pre>
 pi0hatScottVar_emp <- apply(pi0hatScottMat_emp[,1:ntest],2,var)</pre>
  piOhat.ScottMat_emp <- piOhatScottMat_emp[,1:ntest]</pre>
  FDR.ScottMat_emp <- pi0hatScottMat_emp[,(ntest+1):(2*ntest)]
  ##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_1_full.RData", sep="/"),
       list=c("pi0hat.ScottMat_emp", "FDR.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_1.RData", sep="/"),
       list=c("tme", "pi0",
            "pi0hatScottMean_emp","pi0hatScottVar_emp"))
```

```
## [1] "alt_z_large_10_0.2"
## [1] "alt_t_large_20_0.2"
## [1] "alt_t_large_20_0.2"
## [1] "alt_t_large_10_0.5"
## [1] "alt_t_large_10_0.5"
## [1] "alt_t_large_20_0.5"
## [1] "alt_t_large_20_0.5"
## [1] "alt_t_large_20_0.9"
## [1] "alt_t_large_10_0.9"
## [1] "alt_t_large_20_0.9"
## [1] "alt_t_large_20_0.9"
```

## 2 Probability of being a false positive is smooth in one variable

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_2.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
  ##----##
 print("linear")
 piOhatScottMat_empFitLin <- estimate_Scott_sims(zValuesSims, tme, nulltype)
  pi0hatLin.ScottMean_emp <- colMeans(pi0hatScottMat_empFitLin[,1:ntest])</pre>
 pi0hatLin.ScottVar_emp <- apply(pi0hatScottMat_empFitLin[,1:ntest],2,var)</pre>
  piOhat.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,1:ntest]</pre>
  FDR.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,(ntest+1):(2*ntest)]
  ##----#
  print("spline")
  splineMat <- ns(tme,df=3)</pre>
  piOhatScottMat_empFitSpl <- estimate_Scott_sims(zValuesSims, splineMat, nulltype)</pre>
  pi0hatSpl.ScottMean_emp <- colMeans(pi0hatScottMat_empFitSpl[,1:ntest])</pre>
 pi0hatSpl.ScottVar_emp <- apply(pi0hatScottMat_empFitSpl[,1:ntest],2,var)</pre>
```

```
piOhat.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,1:ntest]</pre>
  FDR.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,(ntest+1):(2*ntest)]</pre>
  ##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_2_full.RData", sep="/"),
       list=c("piOhat.Lin.ScottMat_emp", "FDR.Lin.ScottMat_emp",
              "piOhat.Spl.ScottMat_emp", "FDR.Spl.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_2.RData", sep="/"),
       list=c("tme", "pi0",
              "piOhatLin.ScottMean_emp", "piOhatLin.ScottVar_emp",
              "pi0hatSpl.ScottMean_emp", "pi0hatSpl.ScottVar_emp"))
## [1] "alt_z_large_10_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_20_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_10_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_20_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_10_0.9"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.9"
## [1] "linear"
## [1] "spline"
```

```
## [1] "alt_z_large_20_0.9"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_20_0.9"
## [1] "linear"
## [1] "spline"
```

#### 3 Probability of being a false positive is smooth in one variable within levels of second variable

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_3.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
 m <- model.matrix(~as.character(tme2))[,-1]</pre>
 linearMat <- cbind(tme1, m)</pre>
  splineMat <- cbind(ns(tme1,df=3), m)</pre>
  ##----##
  print("linear")
 pi0hatScottMat_empFitLin <- estimate_Scott_sims(zValuesSims, linearMat, nulltype)</pre>
 piOhatLin.ScottMean_emp <- colMeans(piOhatScottMat_empFitLin[,1:ntest])</pre>
  pi0hatLin.ScottVar_emp <- apply(pi0hatScottMat_empFitLin[,1:ntest],2,var)</pre>
  piOhat.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,1:ntest]</pre>
  FDR.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,(ntest+1):(2*ntest)]
  ##----#
  print("spline")
  pi0hatScottMat_empFitSpl <- estimate_Scott_sims(zValuesSims, splineMat, nulltype)</pre>
  piOhatSpl.ScottMean_emp <- colMeans(piOhatScottMat_empFitSpl[,1:ntest])</pre>
  pi0hatSpl.ScottVar_emp <- apply(pi0hatScottMat_empFitSpl[,1:ntest],2,var)</pre>
  piOhat.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,1:ntest]</pre>
  FDR.Spl.ScottMat_emp <- pi0hatScottMat_empFitSpl[,(ntest+1):(2*ntest)]</pre>
```

```
##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_3_full.RData", sep="/"),
       list=c("pi0hat.Lin.ScottMat_emp", "FDR.Lin.ScottMat_emp",
              "piOhat.Spl.ScottMat_emp", "FDR.Spl.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_3.RData", sep="/"),
       list=c("tme", "pi0",
              "pi0hatLin.ScottMean_emp", "pi0hatLin.ScottVar_emp",
              "pi0hatSpl.ScottMean_emp", "pi0hatSpl.ScottVar_emp"))
## [1] "alt_z_large_10_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_20_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_10_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_20_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_10_0.9"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.9"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.9"
## [1] "linear"
## [1] "spline"
```

```
## [1] "alt_t_large_20_0.9"
## [1] "linear"
## [1] "spline"
```

# 4 Probability of being a false positive is smooth in one variable within levels of second variable - lower priors

```
for(alt in alts)
 print(alt)
 load(paste(alt, "simResults_4.RData", sep="/"))
 ntest <- ncol(zValuesSims)</pre>
 m <- model.matrix(~as.character(tme2))[,-1]</pre>
 linearMat <- cbind(tme1, m)</pre>
  splineMat <- cbind(ns(tme1,df=3), m)</pre>
  ##----##
  print("linear")
 pi0hatScottMat_empFitLin <- estimate_Scott_sims(zValuesSims, linearMat, nulltype)</pre>
  ##if only have 2 columns, make everything NULL (this means there was an error in every si
  if(ncol(pi0hatScottMat_empFitLin) > 2)
    pi0hatLin.ScottMean_emp <- colMeans(pi0hatScottMat_empFitLin[,1:ntest])</pre>
    pi0hatLin.ScottVar_emp <- apply(pi0hatScottMat_empFitLin[,1:ntest],2,var)</pre>
    piOhat.Lin.ScottMat_emp <- piOhatScottMat_empFitLin[,1:ntest]</pre>
    FDR.Lin.ScottMat_emp <- pi0hatScottMat_empFitLin[,(ntest+1):(2*ntest)]
  } else {
    piOhatLin.ScottMean_emp <- piOhatLin.ScottVar_emp <-</pre>
      piOhat.Lin.ScottMat_emp <- FDR.Lin.ScottMat_emp <- NULL</pre>
  ##----#
  print("spline")
  pi0hatScottMat_empFitSpl <- estimate_Scott_sims(zValuesSims, splineMat, nulltype)</pre>
```

```
##if only have 2 columns, make everything NULL (this means there was an error in every si
  if(ncol(pi0hatScottMat_empFitLin) > 2)
    piOhatSpl.ScottMean_emp <- colMeans(piOhatScottMat_empFitSpl[,1:ntest])</pre>
    piOhatSpl.ScottVar_emp <- apply(piOhatScottMat_empFitSpl[,1:ntest],2,var)</pre>
    pi0hat.Spl.ScottMat_emp <- pi0hatScottMat_empFitSpl[,1:ntest]</pre>
    FDR.Spl.ScottMat_emp <- piOhatScottMat_empFitSpl[,(ntest+1):(2*ntest)]</pre>
  } else {
    pi0hatSpl.ScottMean_emp <- pi0hatSpl.ScottVar_emp <-</pre>
      piOhat.Spl.ScottMat_emp <- FDR.Spl.ScottMat_emp <- NULL</pre>
  ##save full results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_4_full.RData", sep="/"),
       list=c("pi0hat.Lin.ScottMat_emp", "FDR.Lin.ScottMat_emp",
              "pi0hat.Spl.ScottMat_emp", "FDR.Spl.ScottMat_emp"))
  ##save summary results
  save(file=paste(alt, "simResults_pi0x_Scott_emp_4.RData", sep="/"),
       list=c("tme", "pi0",
              "piOhatLin.ScottMean_emp", "piOhatLin.ScottVar_emp",
              "pi0hatSpl.ScottMean_emp", "pi0hatSpl.ScottVar_emp"))
## [1] "alt_z_large_10_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_20_0.2"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_10_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_t_large_10_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_20_0.5"
## [1] "linear"
## [1] "spline"
```

```
## [1] "alt_t_large_20_0.5"
## [1] "linear"
## [1] "spline"
## [1] "alt_z_large_10_0.9"
## [1] "spline"
## [1] "alt_t_large_10_0.9"
## [1] "linear"
## [1] "spline"
## [1] "spline"
## [1] "alt_z_large_20_0.9"
## [1] "linear"
## [1] "spline"
```

#### Session info:

```
devtools::session_info()
## Session info -----
## setting value
## version R version 3.3.1 (2016-06-21)
## system x86_64, mingw32
## ui
         RTerm
## language (EN)
## collate English_United States.1252
##
  tz
       America/New_York
          2017-06-01
## date
## Packages ------
##
   package
          * version date
## assertthat 0.1 2013-12-06
## BayesLogit * 0.6
                  2016-10-20
## codetools 0.2-14 2015-07-15
## colorspace 1.2-6 2015-03-11
## curl * 0.9.7 2016-04-10
## DBI
            0.4-1 2016-05-08
            1.12.0 2016-06-24
## devtools
## digest 0.6.9
                    2016-01-08
## doParallel * 1.0.10 2015-10-14
## doRNG * 1.6 2014-03-07
            0.4.3 2015-09-01
## dplyr
## evaluate 0.10
                    2016-10-11
## fda * 2.4.4 2014-12-16
```

```
## FDRreg * 0.2-1
                       2017-05-03
## foreach
              * 1.4.3
                       2015-10-13
##
   ggdendro
                0.1-20 2016-04-27
##
   ggplot2
                2.2.1
                       2016-12-30
                2.2.1
##
   gridExtra
                       2016-02-29
##
   gtable
                0.2.0
                       2016-02-26
##
   highr
               0.6
                       2016-05-09
##
   iterators * 1.0.8
                       2015-10-13
## knitr
             * 1.15.1 2016-11-22
               0.20-33 2015-07-14
##
   lattice
              0.2.0
##
   lazyeval
                       2016-06-12
##
   magrittr
              1.5
                       2014-11-22
##
   MASS
              * 7.3-45 2016-04-21
##
   Matrix
              * 1.2-6
                       2016-05-02
##
              1.0.0
                       2016-01-29
   memoise
##
   mosaic
              0.14.4 2016-07-29
   mosaicData 0.14.0 2016-06-17
##
              0.4.3
##
                       2016-02-13
   munsell
            * 1.0-6
##
   mvtnorm
                       2017-03-02
   pkgmaker * 0.22
                       2014-05-14
##
               1.8.4
                       2016-06-08
##
   plyr
##
   R6
                2.1.2
                       2016-01-26
## Rcpp
              0.12.10 2017-03-19
## registry
            * 0.3
                       2015-07-08
## rngtools
             * 1.2.4
                       2014-03-06
## scales
               0.4.1
                       2016-11-09
##
   stringi
               1.1.1
                       2016-05-27
## stringr
               1.0.0
                       2015-04-30
   tibble
               1.2
                       2016-08-26
##
## tidyr
               0.5.1
                       2016-06-14
## withr
               1.0.2
                       2016-06-20
               1.8-2
## xtable
                       2016-02-05
##
   source
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.2)
##
   CRAN (R 3.3.1)
##
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.3)
##
   CRAN (R 3.3.1)
##
##
   CRAN (R 3.3.1)
   CRAN (R 3.3.1)
##
##
   CRAN (R 3.3.1)
  CRAN (R 3.3.1)
```

```
## CRAN (R 3.3.3)
## Github (jgscott/FDRreg@8025d1a)
## CRAN (R 3.3.1)
## CRAN (R 3.3.3)
   CRAN (R 3.3.3)
##
##
   CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.0)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
##
   CRAN (R 3.3.3)
## CRAN (R 3.3.3)
## CRAN (R 3.3.1)
## CRAN (R 3.3.2)
##
   CRAN (R 3.3.2)
## CRAN (R 3.3.1)
## CRAN (R 3.3.1)
## CRAN (R 3.3.3)
##
   CRAN (R 3.3.2)
## CRAN (R 3.3.2)
##
   CRAN (R 3.3.3)
   CRAN (R 3.3.0)
##
##
   CRAN (R 3.3.1)
## CRAN (R 3.3.2)
## CRAN (R 3.3.1)
##
   CRAN (R 3.3.1)
## CRAN (R 3.3.1)
```