# Financial Data Analysis Group Project

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#### Abstract

The change in the exchange rate reflects the economic situation of a country. The increase or decrease in national income, the development of agriculture, the domestic interest rate, and even the domestic employment are impacted deeply by the change of it. The accuracy of exchange rate forecast has great influence on foreign exchange holders, enterprises' import and export trade, foreign exchange trading of individuals and enterprises, foreign exchange holders and so on. With the continuous development of China's economy, in recent years, China's position in the international community has also been strengthened. At present, the Chinese Yuan(CNY) and the United States Dollar(USD) as the world's most influential two currencies, the exchange rate fluctuations on the global financial and economic development have played a decisive role in the global market.

This paper establishes the ARCH model and GARCH model of USD / CNY exchange rate fluctuation, using the daily exchange rate after China has established the exchange rate regime reformation since 2005. Besides, we do a model comparison among different estimated models to try to find a best fitted one. Using AIC and BIC methods of informative criteria and checking the likelihood of the model, we collude that GARCH(1,1) model is the appropriate one to estimate and forecast the USD / CNY exchange rate which can provide some reference for the central bank's control measures and the exchange rate reform policy.

Key Words: GARCH, ARCH, ARIMA, USD / CNY exchange rate, Comparison, Prediction

## Contents

1	Introduction	2				
2	Data Source and Data Description2.1 Data Source2.2 Data Description	<b>3</b> 3				
3	Model Specification3.1 Autoregressive Integrated Moving Average Model	4 4 6				
4	4 Estimation and Result Analysis					
5 Conclusions						

### 1 Introduction

An exchange rate between two currencies is the rate at which one currency will be exchanged for another. It is also regarded as the value of one countrys currency in relation to another currency. Exchange rates are determined in the foreign exchange market, which is open to a wide range of different types of buyers and sellers, and where currency trading is continuous. US Dollar(USD) is considered as the most influential currency in the world and many countries have anchored their foreign exchange rate to the dollar. While Chinese Yuan(CNY) shows an increasing power in the international environment. Thus, discussing the relationship between the two currencies is quite meaningful.

Each country determines the exchange rate regime that will apply to its currency. For example, the currency may be free-floating, pegged (fixed), or a hybrid. The Central Committee and the State Council promulgated the reform of the CNY exchange rate formation mechanism on July 21, 2005. The CNY exchange rate was no longer pegged to a single dollar, and fluctuated according to the market supply and demand. After August 11, 2015, the correlation between the CNY and the dollar index has declined. In 2016, the annual depreciation of CNY is about 6.67%, against a basket of currency depreciation rate is 5.13%. But the degree of marketization of the CNY in 2016 significantly increased, and gradually drops out of the "dollar anchor". CNY exchange rate changes as China's international financial relations and even the normal development of economic relations. It is an important link and plays an increasingly important role. Therefore, it has a vital significance to correct analysis and forecast the exchange rate and its volatility for the economic subject of financial policy and investment and financing decision-making undoubtedly. Thus, it is important to choose a satisfactory model to better analyse USD / CNY exchange rate.

Many domestic scholars have studied this based on time series measurement method. Which model of ARIMA model, ARCH model or GARCH model is more appropriate for the exchange rate fluctuations is controversial. Zhang(2005) suggested that the exchange rate change was fit into ARIMA(2,4,5) model. Hui(2005) argued that there was a GARCH effect in the time series of USD / CNY, and the GARCH(1,1) model was suitable for USD / CNY modeling. Xu and Li(2007) used the ARMA model to forecast the exchange rate of the euro and yen of a basket of currencies and calculated the future exchange rate of the yuan against the US dollar according to the CNY benchmark exchange rate formula. Liu(2008) selected data of the changes in the daily parity of CNY against the US dollar from Jul.25th, 2005 to Nov.1st, 2007 and stated that the GARCH(1,1)model and the ARMA(1,1) model are all suitable. Zhai(2009) showed that the CNY exchange rate volatility had certain leverage effect and the CNY exchange rate did not have the characteristics of floating exchange rate regime through the TGARCH model empirical study. Luo(2009) analysed the exchange rate volatility model established form the data after the reform of China's exchange rate system. The study shows that there existed ARCH effect in China's foreign exchange market and GARCH(1,1) was suitable for estimating.

From previous papers, many studies have been conducted using different techniques of estimation like ARIMA model, ARCH model and GARCH model. But we can also see that some of the papers are using data far from now and have little values of exchange rate after changing the exchange regime. So the past results may be out of date due to the lack of large data set. While right now we gain more data than before, we have the probability to update the model and find a more appropriate one to describe the mean and volatility equations which can provide some reference for further studies.

### 2 Data Source and Data Description

#### 2.1 Data Source

We collected monthly USD / CNY exchange rate from 1981-01-01 to 2017-06-01, and daily exchange rate data from 2005-07-21 til 2017-06-09 from Federal Reserve System. According to the system, the data are already wiped out the seasonal effect.

#### 2.2 Data Description

We first use monthly USD / CNY exchange rate data to plot a trend figure shown as figure 1. According with the news, China used to set fixed exchange rate mechanism before 2015-07-21, the volatility of exchange rate was small. After that date, China started exchange rate regime reforming: announced a move away from the US dollar peg and used a floating exchange rate. Thus in this paper we will mainly focus on analysing exchange rate after the reform.

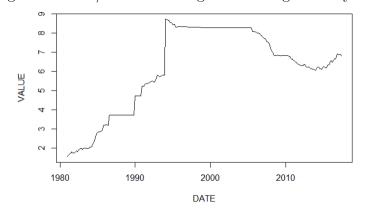


Figure 1: CNY/ USD Exchange Rate using monthly data

We collected the daily USD / CNY exchange rate as our data set. The data we found are already wiped out the seasonal effect so we use them directly in examining the model

and further doing forecast. We divided the data into two parts one until July 21st,2016 for examine the model and the data after that date until June 9th,2017 for checking the evaluation of the models. The trend figure is shown in figure 2.

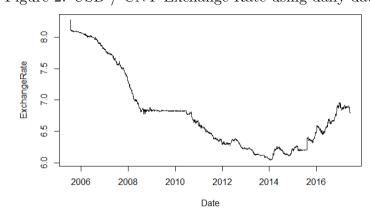


Figure 2: USD / CNY Exchange Rate using daily data

## 3 Model Specification

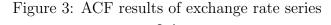
There are usually two ways in analysing the exchange rate in time series: ARIMA model and GARCH model since they are the more general form of an ARMA model and an ARCH model.

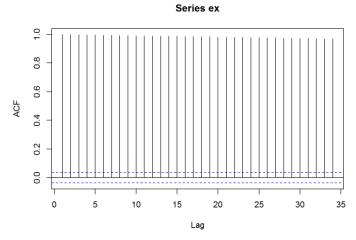
### 3.1 Autoregressive Integrated Moving Average Model

An Autoregressive Integrated Moving Average(ARIMA) model is a generalization of an Autoregressive Moving Average(ARMA) model with unit roots. Basically an ARMA model combines the ideas of Autocorrelation(AR) model and Moving Average(MA) model but it models with less number of parameters, achieving parsimony in the model. The general ARMA(p,q) form is like  $r_t = \phi_0 + \sum_{i=1}^p \phi_i r_{t-i} + a_t - \sum_{i=1}^q \theta_i a_{t-i}$  where  $a_t$  is a white noise series. An AR model forms a multiple linear regression model with lagged values serving as the explanatory variables. A MA model is an infinite-order AR model with some parameter constraints. And the "I" of Integrated indicates data values have been replaced with the difference between their values and the previous values.

To begin with, we want to check if the daily exchange rate series exists an unit root in the serial. As mentioned before, we first use the first 2766 data (from 2005-07-21 to 2016-07-21) to check the ACF of series. From figure 3, we can say that ACF shows a strong autocorrelation which almost does not decay indicates the existence of unit root. We also run an ADF-test double-check the unit-root result. The ADF-test statistic is -3.1048 with p-value 0.0274, which is larger than 0.01, so the unit-root hypothesis cannot

be rejected under 1% significant level.





```
origin=da$ExchangeRate
ex=origin[1:2766] # 2005-07-21 To 2016-07-21
acf(ex)
pacf(ex)
# ADF Test
adfTest(ex,lags=m1$order,type=c("c"))
##
##
   Title:
    Augmented Dickey-Fuller Test
##
##
##
   Test Results:
##
     PARAMETER:
##
       Lag Order: 12
     STATISTIC:
##
       Dickey-Fuller: -3.1048
##
##
     P VALUE:
       0.0274
##
```

However, when we want to further estimate a ARIMA model, the autocorrelation between the 8th difference exchange rate are still significant at lag 13th. Unlike Zhang(2005) who successfully estimated am ARIMA(2,4,5) model using monthly data from Jan. 1989 to Dec.2003, our estimation using daily data, an ARIMA(6,4,12) model, failed to adequate estimate the results. Thus, we focus on ARCH and GARCH model in the following research.

#### 3.2 Autoregressive Conditional Heteroscedastic Model

The basic idea of Autoregressive Conditional Heteroscedastic(ARCH) model is that  $a_t$  is a serially uncorrelated but dependent, and the dependence of  $a_t$  can be described by a simple quadratic function of the lagged value. An ARCH(m) model is like

$$a_t = \sigma_t \epsilon_t$$
  
$$\sigma_t^2 = \alpha_0 + \alpha_1 a_{t-1}^2 + \dots + \alpha_m a_{t-m}^2$$

We first estimate an ARCH(1) model, results are like

$$r_t = 1.9966 + a_t$$
  
 $\sigma_t^2 = 6.055 * 10^{-07} + 1.000a_{t-1}^2$ 

Figure 4: ARCH(1)

```
Standardised Residuals Tests:
                                   Statistic p-Value
 Jarque-Bera Test
                           Chi^2
                                   407.1392
                                   0.6780088
Shapiro-Wilk Test R
                           Q(10)
                                   24517.65
Liuna-Box Test
                     R
Ljung-Box Test
                           Q(15)
                     R
                           Q(20)
                                   46652.09
Ljung-Box Test
                     R
                                              3.109177e-05
Ljung-Box Test
                     R∧2
                           Q(10)
                                   38.49667
                                   53.9964
                                              2.630455e-06
Ljung-Box Test
                     R<sub>1</sub>2
                           Q(15)
                                             1.369756e-05
Ljung-Box Test
                     R∧2
                           Q(20)
                                   58.15351
LM Arch Test
                           TR∧2
                                   43.46774
Information Criterion Statistics:
AIC BIC SIC HQIC
-3.765512 -3.759086 -3.765515 -3.763191
```

And an ARCH(3) model,

```
r_t = 1.9966 + a_t

\sigma_t^2 = 5.675 * 10^{-7} + 0.9953a_{t-1}^2 + 1.000 * 10^{-8}a_{t-2}^2 + 0.01381a_{t-3}^2
```

### 3.3 General Autoregressive Conditional Heteroscedastic Model

A General Autoregressive Conditional Heteroscedastic(GARCH) model is an extension of Autoregressive Conditional Heteroscedastic(ARCH) model. It shows the parsimonious of the parameters to adequately describe the volatility process of a series. The most commonly used GARCH model is GARCH(1,1), and its form is like  $a_t = \sigma_t \epsilon_t$ ,  $\sigma^2 = \alpha_0 + \alpha_1 a_{t-1}^2 + \beta_1 \sigma_{t-1}^2$  where  $0 \le \alpha_1, \beta_1 \le 1, (\alpha_1 + \beta_1) < 1$ .

Figure 5: ARCH(3)

```
Standardised Residuals Tests:
                                    Statistic p-Value
 Jarque-Bera Test
                           Chi∧2
                                   401.1047
                                   0.6802692 0
Shapiro-Wilk Test
                           W
                           Q(10)
Ljung-Box Test
                                   24436.1
                                   35600.29
Ljung-Box Test
                           Q(15)
Ljung-Box Test
                      R
                           Q(20)
                                   46469.15
                                               0
                                              2.268141e-05
2.957023e-06
                      RA2
                                   39.27942
Ljung-Box Test
                           Q(10)
                                   53.69209
Ljung-Box Test
                      R\Lambda 2
                           Q(15)
                                               2.024238e-05
                           Q(20)
                      R<sub>1</sub>2
                                   57.03984
Ljung-Box Test
                                   39.57381
                                              8.4608e-05
LM Arch Test
                            TR<sub>1</sub>2
Information Criterion Statistics:
                                       HQIC
      AIC
                 BIC
                            SIC
-3.762501 -3.751790 -3.762508
```

Also an GARCH(1,1) model,

```
r_t = 2.0576 + a_t

\sigma_t^2 = 6.144 * 10^{-9} + 0.1619a_{t-1}^2 + 0.8440\sigma_{t-3}^2
```

Figure 6: GARCH(1,1)

```
Standardised Residuals Tests:
                                Statistic p-Value
                         Chi∧2
 Jarque-Bera Test
                                8835.812
Shapiro-Wilk Test
                        W
                                0.7412733 0
                         Q(10)
Ljung-Box Test
                    R
                                20267.05
Ljung-Box Test
                         Q(15)
                                29406.02
Ljung-Box Test
                         Q(20)
                                38281.3
                                6.427786
                    R∧2
Ljung-Box Test
                         Q(10)
                                7.322057
                                          0.948089
Ljung-Box Test
                    R∧2
                         Q(15)
                                7.703267
Ljung-Box Test
                         Q(20)
                                          0.993656
                    R∧2
LM Arch Test
                         TR∧2
                                6.251706
                                          0.9028656
Information Criterion Statistics:
                                   HOTO
     ATC
               BTC
                        SIC
-4.166226 -4.157658 -4.166231 -4.163131
```

## 4 Estimation and Result Analysis

As the results above, we can find the GARCH(1,1) model have the highest likelihood with the lowest AIC and BIC, while the considering the alpha, ARCH1 model is also appropriate. Further, Ljung box test is needed to decide which model is better. If p value is less than 0.05, we can reject the null hypothesis, seeing the model is appropriate. As we can see from the results, GARCH(1,1) model is suitable for the volatility and mean equation.

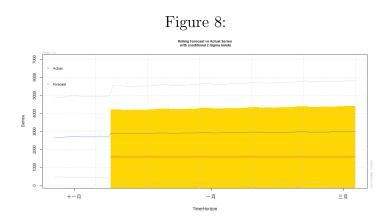
Here is the prediction we made

Figure 7: point forecast

	Point	Forecast	Lo 80	ні 80	Lo 95	ні 95
2767		2.037749	2.036294	2.039205	2.035523	2.039976
2768		2.037716	2.035652	2.039781	2.034559	2.040874
2769		2.037690	2.035143	2.040237	2.033795	2.041585
2770		2.037669	2.034707	2.040631	2.033139	2.042199
2771		2.037652	2.034318	2.040986	2.032554	2.042750
2772		2.037638	2.033965	2.041312	2.032020	2.043256
2773		2.037628	2.033639	2.041616	2.031528	2.043728
2774		2.037619	2.033335	2.041903	2.031067	2.044170
2775		2.037612	2.033050	2.042174	2.030634	2.044590
2776		2.037606	2.032780	2.042433	2.030225	2.044988

#### 5 Conclusions

While what really disappoint us is that the forecast is not consistent with the actual value, shown as figure 8. Having seen from the result, the test results showed the detection model did not possesses preferable practicability. The exchange rate volatility shows the forecast result is not consistent with the actual series in GARCH model.



This method have error, which might be the factor that make the estimate result is not pretty ideal. According to the analysis, we can see the exchange rate fluctuated remarkably, which is not normal distribution. According to the results, it seems infeasible to use this model to predict the exchange rate revealing the upward tendency for the CNY. Along with the SDR(Special Drawing Right), CNY gradually move in the line with the trend of the international financial market, while the non-stationary means it still needs to take measures to prevent the risk of the sharp appreciation and depreciation.

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### **Appendix**

#### Additional R code

```
library(readx1)
library(timeDate)
library(timeSeries)
library(TSA)
library(fUnitRoots)
library(forecast)
```

```
data <- read_excel("D:/Junior/GitHub/FDA_project_LYF/Data/MonthlyData.xls")</pre>
head(data)
dim(data)
plot(data,type="1")
da <- read_excel("D:/Junior/GitHub/FDA_project_LYF/Data/DailyData.xx")</pre>
head(da)
dim(da)
plot(da,type="1")
# Take difference
dex2=diff(dex)
dex3=diff(dex2)
dex4 = diff(dex3)
dex5=diff(dex4)
dex6=diff(dex5)
dex7=diff(dex6)
dex8=diff(dex7)
acf(dex8)
pacf (dex8)
#ARIMA
m2 = arima(ex, c(6, 4, 12))
Box.test(m2$residuals,lag=30,type = "Ljung")
pv2=1-pchisq(776.93,12)
pv2
Call:
arima(x = ex, order = c(6, 4, 12))
Coefficients:
                      ar2
                               ar3
                                         ar4
                                                  ar5
                                                            ar6
           ar1
                                                                       ma1
ma2
       -0.8638
                 -0.1001
                           0.0419
                                    -0.0185
                                               0.0187
                                                        -0.0084
                                                                  -1.6103
0.3084
s.e.
           {\tt NaN}
                      {\tt NaN}
                               {\tt NaN}
                                         {\tt NaN}
                                                  {\tt NaN}
                                                         0.0004
                                                                       {\tt NaN}
0.0003
          ma3
                                                ma7
                    ma4
                             ma5
                                       ma6
                                                          ma8
                                                                   ma9
          ma11
ma10
                                                                         -0.095
       0.2579
                          0.1486
                                   -0.033
                                           0.0986
                                                      -0.0976
                -0.0777
                                                               0.1079
-0.1169
```

```
s.e. NaN NaN 0.0001 NaN 0.0002 NaN NaN
NaN 0.0004
    ma12
    0.1103
s.e. 0.0003
sigma^2 estimated as 0.0001398: log likelihood = 8328.14, aic = -16620.28
    Box-Ljung test
data: m2$residuals
X-squared = 776.93, df = 30, p-value < 2.2e-16</pre>
```