## Empirical Exercise 7.1

Zheng Tian

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This file include answers and R codes for completing Empirical Exercise 7.1 in Introduction to Econometrics (3rd edition) by Stock and Watson.

## 1 Answers

The estimation results for two regression models are reported in Table 1.

Table 1: Regression Results

	Dependent variable:  ahe	
	(1)	(2)
age	0.605***	0.585***
	(0.040)	(0.037)
female		-3.664***
		(0.208)
bachelor		8.083***
		(0.213)
Constant	1.082	-0.636
	(1.167)	(1.083)
Observations	7,711	7,711
$\mathbb{R}^2$	0.029	0.200
Adjusted R <sup>2</sup>	0.029	0.199
Residual Std. Error	9.992	9.072
F Statistic	230.432***	641.492***
Note:	*p<0.1; **p<0.05; ***p<0.0	

a The estimated coefficient on Age is 0.605, which is significant at the 1% level. The estimated intercept is 1.082, which is insignificant at the 10% level.

**b** The estimated marginal effect of Age on AHE is 0.585 dollars per year, which is significant at the 1% level. The confidence interval is (0.514, 0.657).

- **c** The results are quite similar. Evidently the regression in (a) does not suffer from important omitted variable bias.
- d Bob's predicted average hourly earnings is 14.58 dollars. Alexis's predicted average hourly earnings is 21.34 dollars.
- e The regression in (b) fits the data much better. Gender and education are important predictors of earnings. The  $R^2$  and  $\bar{R}^2$  are similar because the sample size is very large relative to the number of regressors.
- f Gender and education are important. The t-statistic for Female is -17.643, the t-statistic for Bachelor is 37.993, and the F-statistic for both Female and Bachelor is 822.467, which are all significant at the 1% level.
- g The omitted variables must have non-zero coefficients and must correlated with the included regressor. From (f) Female and Bachelor have non-zero coefficients; yet there does not seem to be important omitted variable bias, suggesting that the correlation of Age and Female and Age and Bachelor is small.

## 2 R codes

```
# This file contains the answer for the empirical exercise 7.1 in Chapter 8
# Introduction to Econometrics by Stock and Watson
library(AER)
library(foreign)
cpsdata <- read.dta("./data/cps08.dta")</pre>
summary(cpsdata)
# a -----
fm.a <- ahe ~ age
ols.a <- lm(fm.a, data = cpsdata)
b0.a <- coef(ols.a)[1]
b1.a <- coef(ols.a)[2]
summ.a <- summary(ols.a)</pre>
rsq.a <- summ.a$r.squared
adrsq.a <- summ.a$adj.r.squared
se.a <- sqrt(diag(vcovHC(ols.a, type = "HC1")))</pre>
# b -----
fm.b <- ahe ~ age + female + bachelor
ols.b <- lm(fm.b, data = cpsdata)</pre>
b1.b <- coef(ols.b)[2]
ci.b <- confint(ols.b, "age")</pre>
summ.b <- summary(ols.b)</pre>
rsq.b <- summ.b$r.squared
adrsq.b <- summ.b$adj.r.squared
# with heteroskedasticity-robust se
se.b <- sqrt(diag(vcovHC(ols.b, type = "HC1")))</pre>
```

```
ci.b.rob <- matrix(</pre>
 c(b1.b - qnorm(0.975) * se.b[2], b1.b + qnorm(0.975) * se.b[2]),
 nrow = 1
colnames(ci.b.rob) <- c("2.5%", "97.5%")
rownames(ci.b.rob) <- "age"</pre>
library(stargazer)
stargazer(ols.a, ols.b, se = list(se.a, se.b),
         title = "Regression Results", style = "aer",
         no.space = TRUE)
# d -----
bob <- data.frame(age = 26, female = 0, bachelor = 0)
bob.hat <- predict(ols.b, bob)</pre>
alexis <- data.frame(age = 30, female = 1, bachelor = 1)</pre>
alexis.hat <- predict(ols.b, alexis)</pre>
# e -----
cmp.rsq <- rbind(c(rsq.a, adrsq.a),</pre>
               c(rsq.b, adrsq.b))
rownames(cmp.rsq) <- c("a", "b")</pre>
colnames(cmp.rsq) <- c("R sqd", "Adj. R sqd")</pre>
# f -----
# test female
tstat.b <- coeftest(ols.b, vcovHC, df = Inf)</pre>
b.female <- tstat.b[3, 1]
t.female <- tstat.b[3, 3]</pre>
p.female <- tstat.b[3, 4]</pre>
b.bach <- tstat.b[4, 1]
t.bach <- tstat.b[4, 3]
p.bach <- tstat.b[4, 4]</pre>
fstat.b <- linearHypothesis(ols.b,</pre>
                         hypothesis.matrix = rbind(c(0, 0, 1, 0),
                                                 c(0, 0, 0, 1)),
                         rhs = c(0, 0), test = "F")
F <- fstat.b[2, "F"]
F.p <- fstat.b[2, 6]
```