

## QUESTIONS: LÉVY-KHINTCHINE FORMULA

- (1) Page 17: Remark 2. Give a formal argument that

$$t \mapsto \int_{\mathbb{R}^d} (\exp(i\langle t, x \rangle) - 1 - i\langle t, x \rangle I_D(x)) \nu(dx) \text{ is continuous}$$

- (2) Page 17: Remark 5: Why can we re-write the formula as claimed?
- (3) What can you say over an infinitely divisible distribution if the Lévy measure  $\nu$  is finite?
- (4) Page 18, line 6: Give a formal argument that the limit is indeed  $-\langle t, At \rangle/2$ .
- (5) Page 20, line 3: why can we apply the dominated convergence theorem?
- (6) Page 22, line -4: Show (without calculating the integral) that  $\int_{[-h, h]^d} \psi_n(t) dt \in \mathbb{R}$ .
- (7) Page 23, line 1: Why can we apply Fubini's theorem?
- (8) Page 23, line 15: Is this easy to see?
- (9) Page 23, line -4: why does  $h_\epsilon$  exist?
- (10) Formula (2.12). Check why we had to insert the extra term  $\langle t, x \rangle^2/2$ . (See also definition of  $I_{n, \epsilon}(t)$ .)
- (11) Page 25, line -9: Why do we have  $I_\epsilon(t) \rightarrow 0$ ?
- (12) Page 26, line -1: Prove that  $\int_A f d\nu_n \rightarrow \int_A f d\nu$  if  $\nu(\partial A) = 0$ .
- (13) Page 27, lines 6+7: Why is this the case?
- (14) Page 27, formula (2.15). Try to prove this formally. Hint: see questions 2 and 3.