

Symmetry, etc. Tutorial

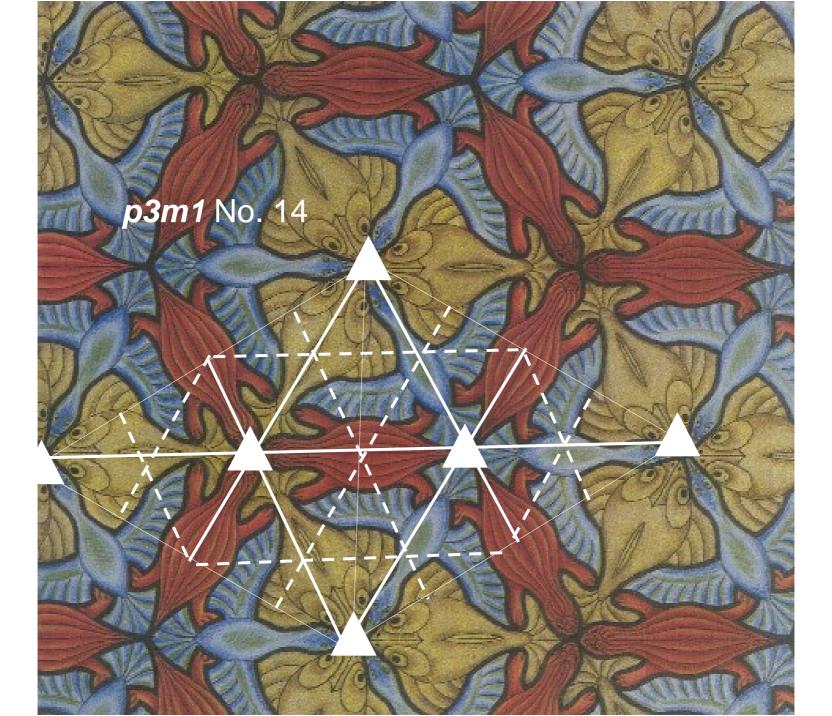
P.G. Radaelli ISIS Facility - RAL

ftp://ftp.nd.rl.ac.uk/scratch/UCL_Teaching_2007/



A phase transition in 2D

- 1. Examine the symmetry of the Escher drawing, and compare it with the IT entry.
- 2. Identify special positions and symmetry elements
- 3. Look at the modified drawing, with the colour pattern altered. Identify the lost symmetry elements.
- 4. Can you determine the low-symmetry space group?



Hexagonal

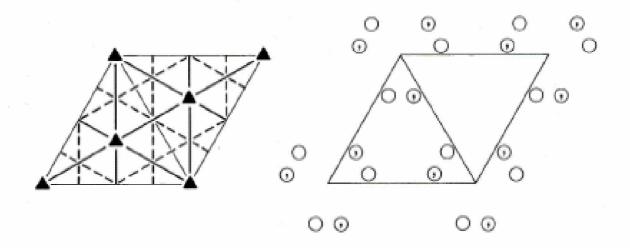
3m

p3m1

Patterson symmetry p6mm

p3m1

No. 14



Origin at 3m1

Asymmetric unit

 $0 \le x \le \frac{2}{5}$; $0 \le y \le \frac{1}{7}$; $x \le 2y$; $y \le \min(1 - x, 2x)$

Vertices

0,0 $\frac{2}{3},\frac{1}{1}$ $\frac{1}{8},\frac{2}{3}$

Symmetry operations

(1) 1

- (2) 3⁺ 0,0
- $(3) 3^- 0.0$

- (4) $m = x, \bar{x}$
- (5) m = x, 2x
- (6) m = 2x, x

Generators selected (1); t(1,0); t(0,1); (2); (4)

Positions

Multiplicity, Wyckoff letter, Site symmetry Coordinates

(2)
$$y, x - y$$

(3)
$$x + y, x$$

(4)
$$\vec{y}, \vec{x}$$

(5)
$$\bar{x} + y, y$$

(6)
$$x, x - y$$

$$3 \quad d \quad , m$$
.

$$x, \bar{x}$$

 $2\pi, \pi$

$$1 c 3m$$
.

$$1 \ b \ 3m$$
.

$$\frac{1}{3}, \frac{2}{3}$$

$$1 \quad a \quad 3 \quad m$$
.

Maximal non-isomorphic subgroups

Ha none

IIb [3]
$$h3m1$$
 ($a' = 3a, b' = 3b$) ($p31m, 15$)

Maximal isomorphic subgroups of lowest index

He [4]
$$p 3m1$$
 (a' = 2a, b' = 2b) (14)

Minimal non-isomorphic supergroups

I [2]
$$p6mm(17)$$

II [3]
$$h3m1(p31m, 15)$$

Reflection conditions

General:

no conditions

Special: no extra conditions

