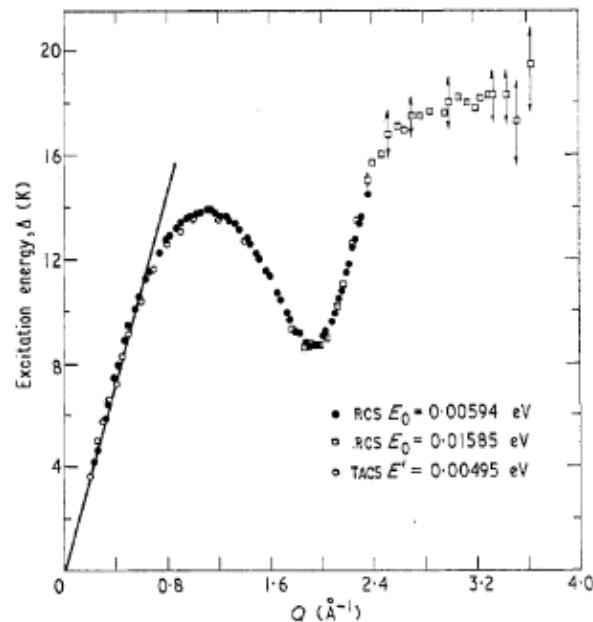


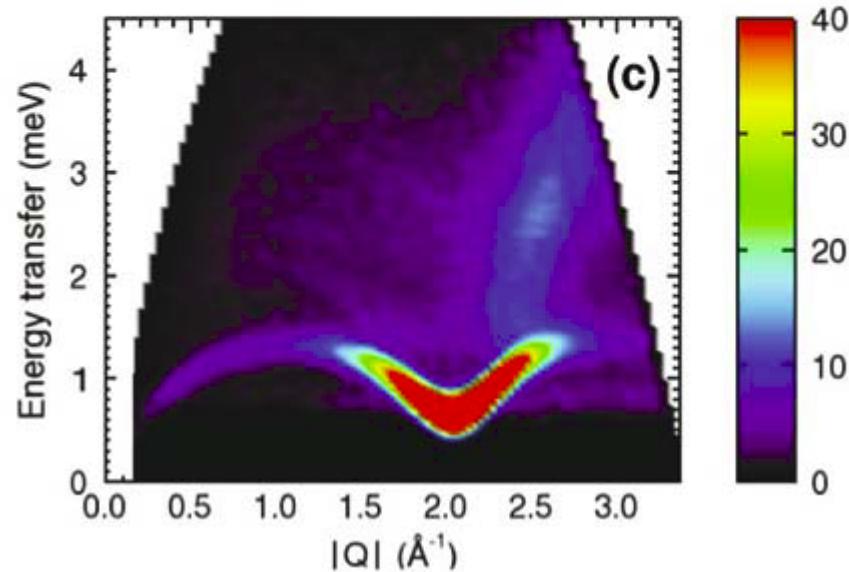
# Excitations

Elizabeth Blackburn

University of Birmingham



Cowley and Woods., Can. J. Phys. 49, 177 (1971)



Blackburn *et al.*, Pramana 71, 673 (2008)

14<sup>th</sup> Oxford School of Neutron Scattering

# Excitations

Elizabeth Blackburn

University of Birmingham

- What are excitations?
- What can we learn from them?
- How do we measure them?

# What are excitations?

The inelastic (or dynamical) response of the material to stimulus.

## Examples

Phonons (lattice vibrations)

[Magnon video](#)

Magnons (spin vibrations)

[Martin Boehm and Alain Filhol](#)

Crystal field excitations

Vibrations internal to a molecule

## For neutron scattering

The excitation has to couple to the neutron, either through the strong nuclear interaction or via the magnetic moment.

# Recap from Intro to Neutron Scattering

$$\frac{d^2\sigma}{d\Omega dE_f} = \frac{\text{No. particles scattered per sec. into solid angle } d\Omega \text{ with final energies between } E_f \text{ and } E_f + dE_f}{I_0 \times d\Omega \times dE_f}$$

$$\frac{d^2\sigma}{d\Omega dE_f} = \frac{k_f}{k_i} S(\mathbf{Q}, \omega)$$

$S(\mathbf{Q}, \omega)$  is the **scattering function** or **response function**

$S(\mathbf{Q}, \omega)$  is determined by the physics of the material.

You have already seen expressions for this for phonons and for spin waves.

# Recap from Intro to Neutron Scattering

$$\frac{d^2\sigma}{d\Omega dE_f} = \frac{\text{No. particles scattered per sec. into solid angle } d\Omega \text{ with final energies between } E_f \text{ and } E_f + dE_f}{I_0 \times d\Omega \times dE_f}$$

$$\frac{d^2\sigma}{d\Omega dE_f} = \frac{k_f}{k_i} S(\mathbf{Q}, \omega)$$

$S(\mathbf{Q}, \omega)$  is the scattering function or response function

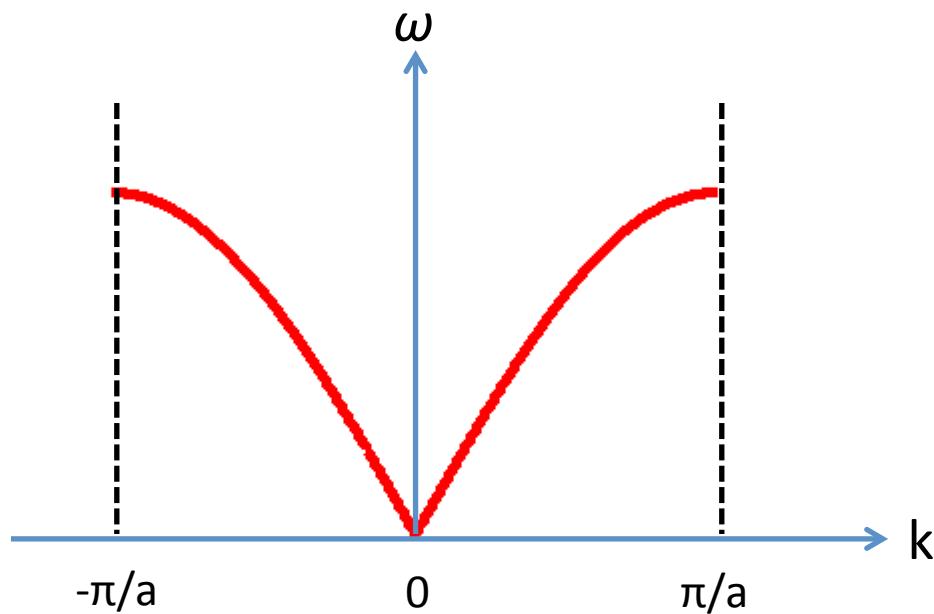
(i) Phonons

$$S(\mathbf{Q}, \omega) \propto \exp \{ -2W(Q, T) \} \times |\mathbf{G}(\mathbf{Q})|^2 \times [n(\omega_{ph}) + 1] \times \frac{1}{\omega_{ph}} \times Q^2$$

(ii) Spin waves

$$S(\mathbf{Q}, \omega) \propto \exp \{ -2W(Q, T) \} \times [n(\omega_{mag}) + 1] \times \frac{1}{\omega_{mag}} \times f^2(Q)$$

# Phonons on a 1-D chains



$$\omega_{ph} = 2\sqrt{\frac{K}{M}} \left| \sin \left( \frac{k_{ph} a}{2} \right) \right|$$

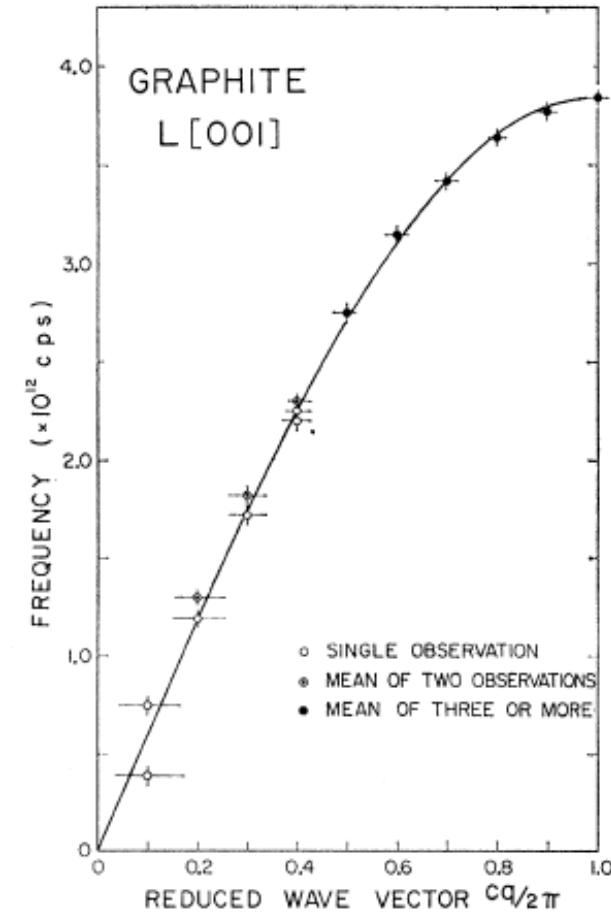


FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.

Dolling and Brockhouse., Phys. Rev. 128, 1120 (1962)

# What can we learn from them?

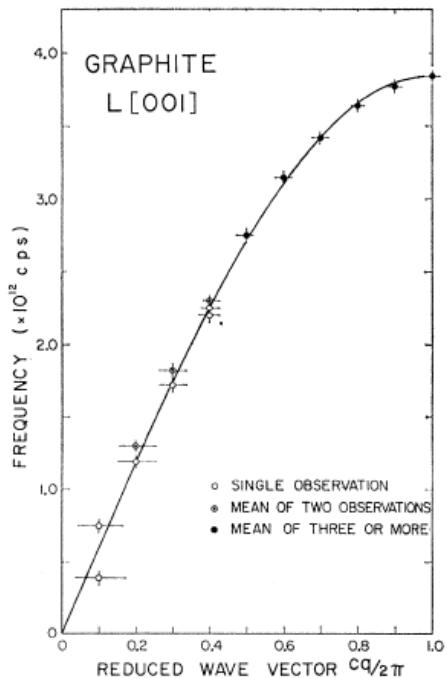
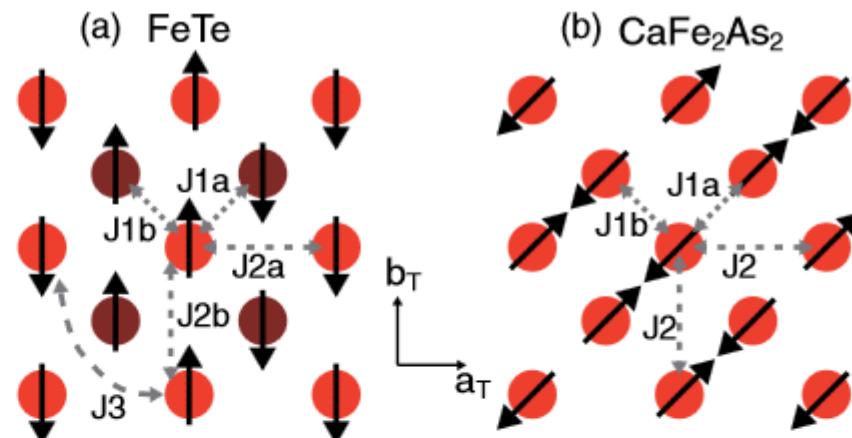


FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.

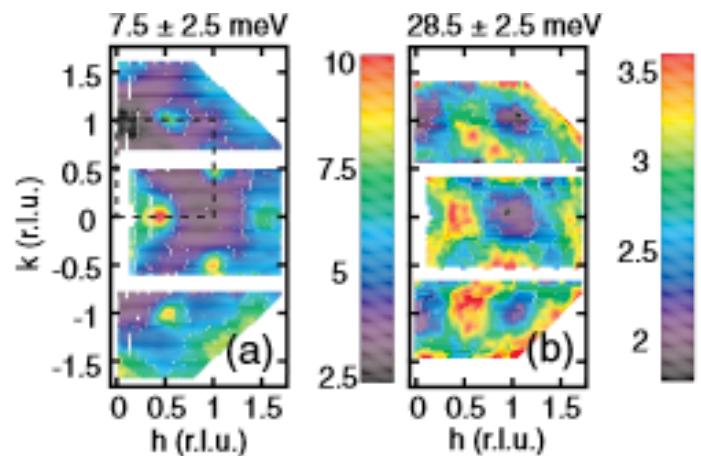
- Elastic constants

$$\omega_{ph} = 2\sqrt{\frac{K}{M}} \left| \sin\left(\frac{k_{ph} a}{2}\right) \right|$$

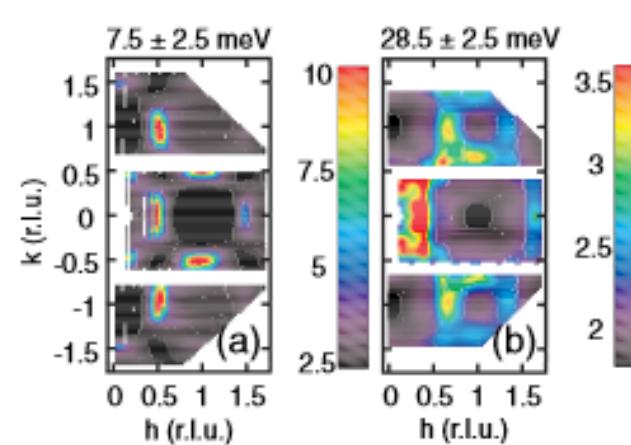
# What can we learn from them?



- Elastic constants
- Spin Hamiltonians

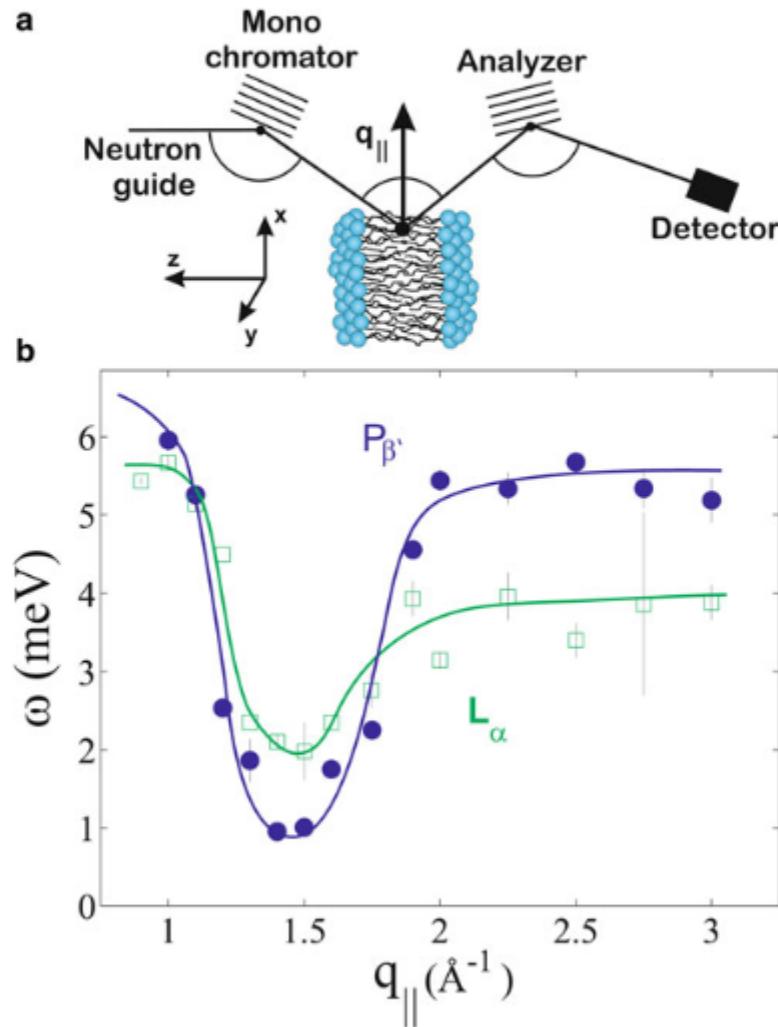


Data



Simulation

# What can we learn from them?



- Elastic constants
- Spin Hamiltonians
- Membrane dynamics

Fig. 10.5 (a) Schematic of a triple-axis spectrometer. (b) Short-wavelength dispersion relations in the gel ( $P_{\beta'}$ ) and fluid phase  $L_{\alpha}$  of the phospholipid (DMPC) bilayers [42]

# What can we learn from them?

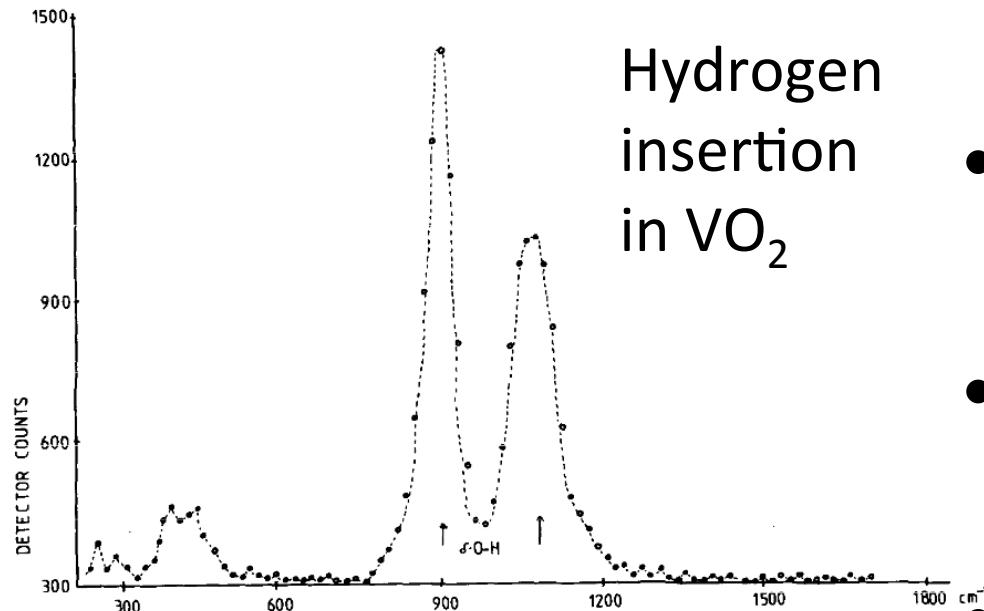


FIG. 2. Inelastic neutron scattering spectrum of  $\text{H}_{0.3}\text{VO}_2$  at 80 K.

TABLE V

FREQUENCIES AND ASSIGNMENTS OF GENERATED VIBRATIONAL MODES OF  $\text{H}_x\text{VO}_2$

Calculated frequency ( $\text{cm}^{-1}$ )	Observed frequency ( $\text{cm}^{-1}$ )	Assignment	Mode
3407 ( $\times 4$ )		$B_{1g} B_{3u} B_{2u} A_g$	$\nu(\text{O-H})$
1098 1095	1083	$B_{2u} B_{3u} B_{1g} A_g$	$\delta(\text{O-H})$ in $xy$ plane
1093 1092			
918 916 914	909	$B_{1u} A_u B_{3g} B_{2g}$	$\delta(\text{O-H})$ out of $xy$ plane
914			
587 583 553	476 431	$B_{3u} B_{2u} B_{1u} A_g$	
517 515 493		$B_{1g} A_u B_{3g} B_{2g}$	Lattice modes
414 414 342		$B_{2u} B_{1g} B_{3u}$	
342 341 322		$B_{3u} B_{2u} A_u A_g$	
292 267 212			
177			

- Elastic constants
- Spin Hamiltonians
- Membrane dynamics
- How to synthesise particular molecules

# How do we measure excitations?

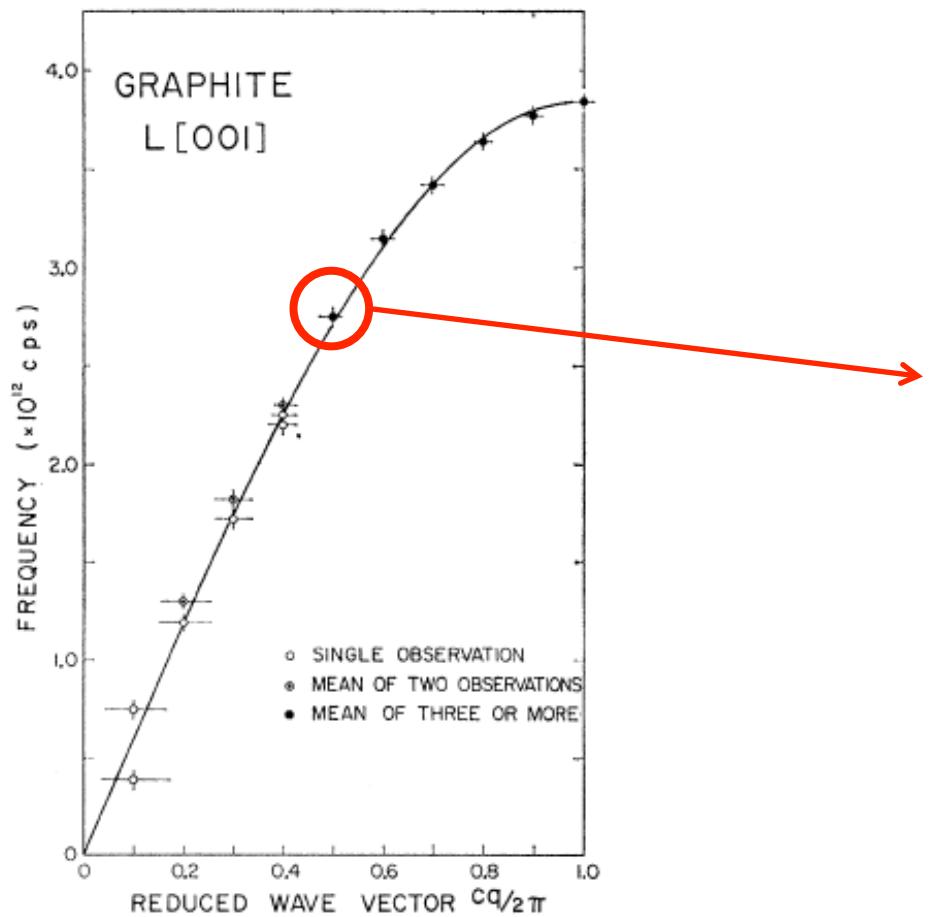


FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.

Dolling and Brockhouse., Phys. Rev. 128, 1120 (1962)

# Measuring a phonon spectrum

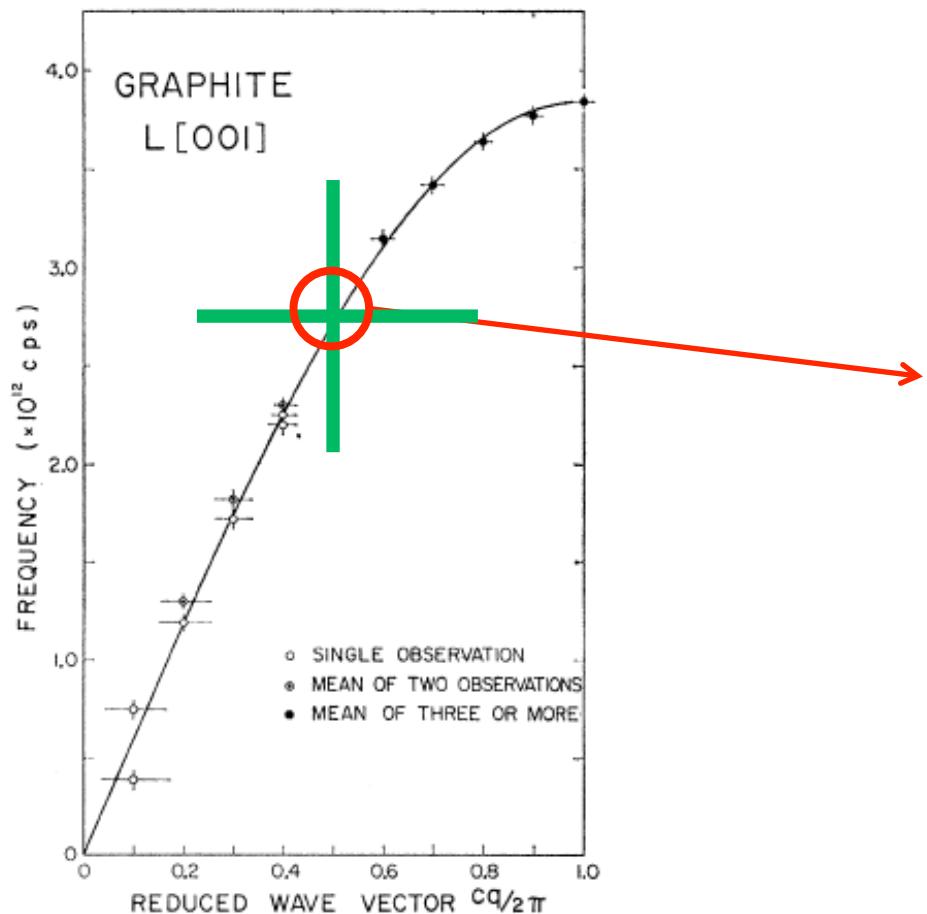


FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.

Dolling and Brockhouse., Phys. Rev. 128, 1120 (1962)

# Measuring a phonon spectrum

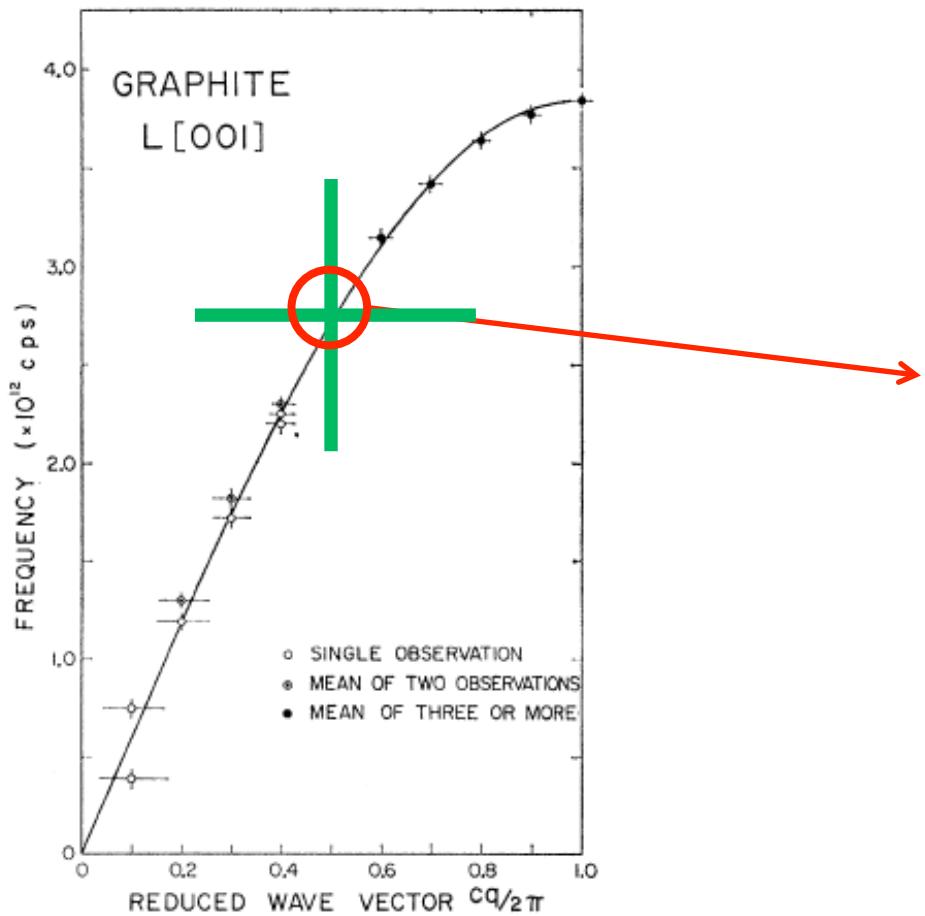


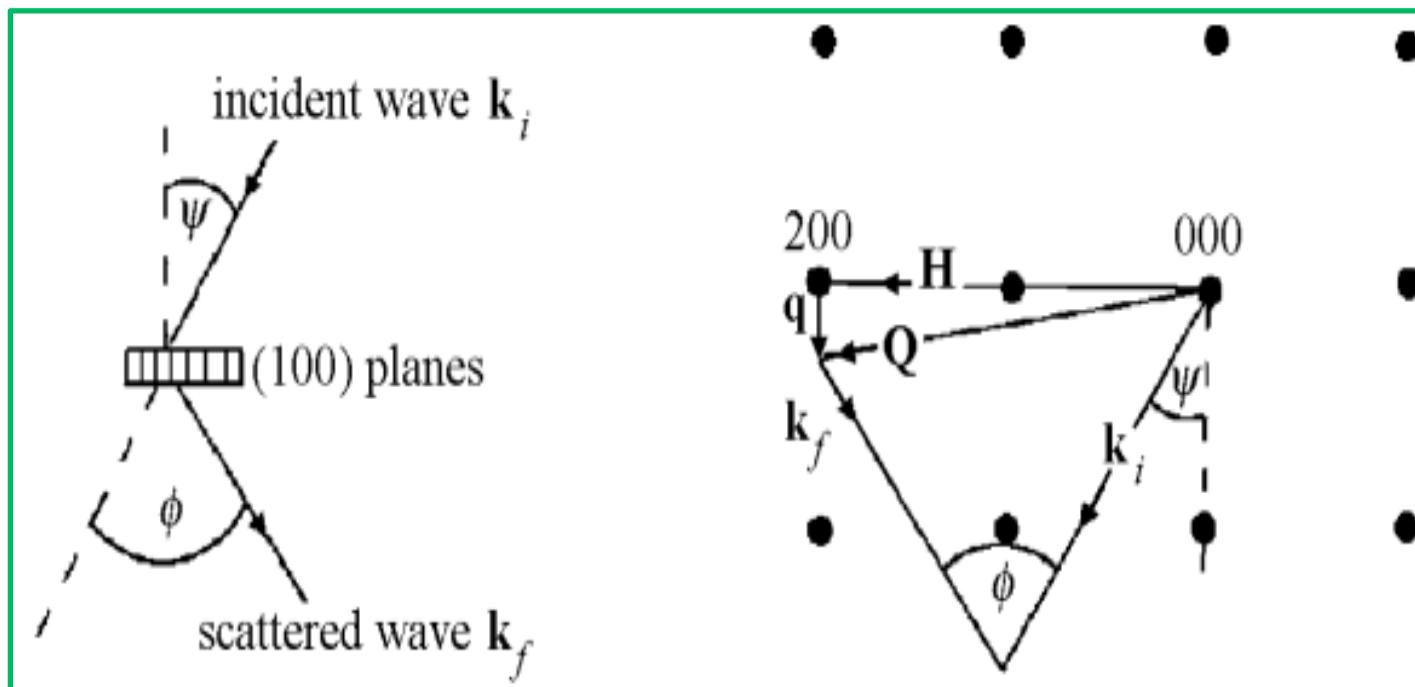
FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.

Things to consider:

- resolution
- spurious

# How do we measure these points?

- Momentum transfer       $\hbar\mathbf{Q} = \hbar(\mathbf{k}_i - \mathbf{k}_f)$
- Energy transfer       $\hbar\omega = E_i - E_f = \frac{\hbar^2}{2m} (k_i^2 - k_f^2)$



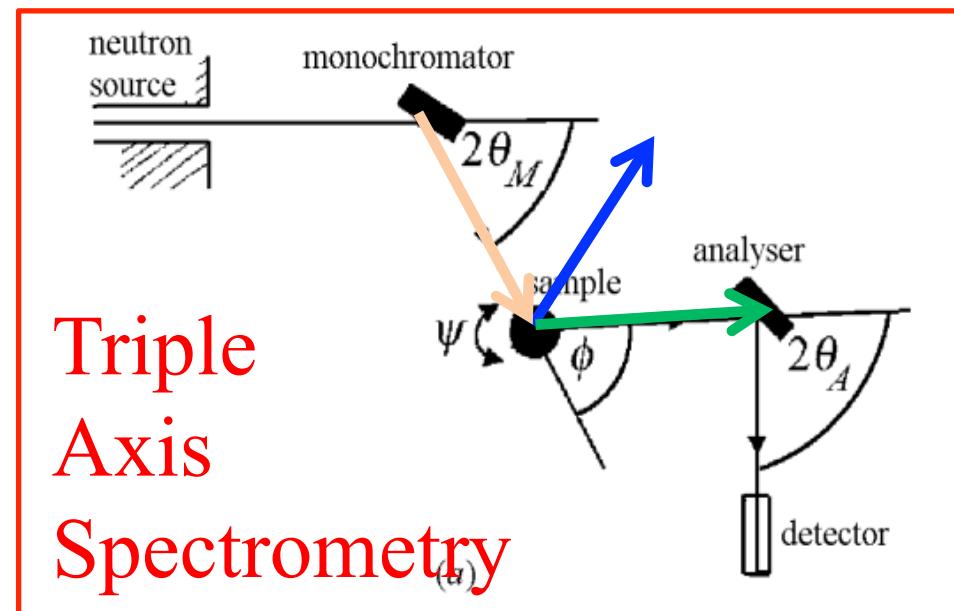
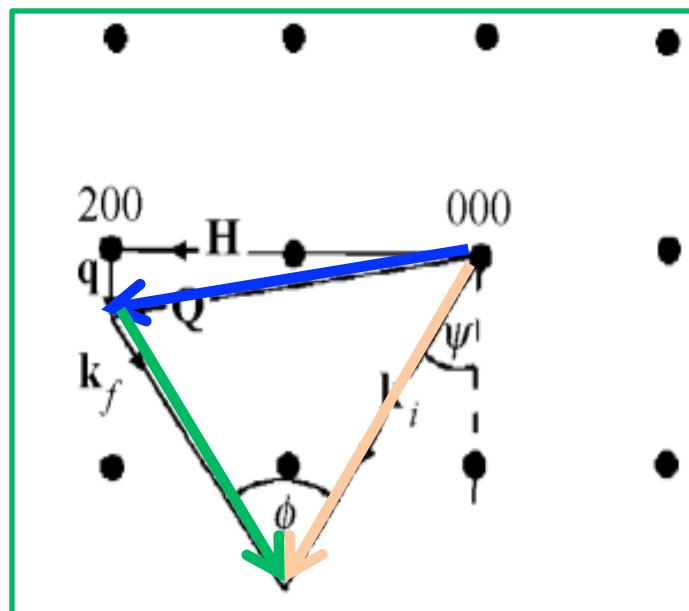
Real space

Reciprocal space

# How do we measure these points?

- Momentum transfer       $\hbar\mathbf{Q} = \hbar(\mathbf{k}_i - \mathbf{k}_f)$

- Energy transfer       $\hbar\omega = E_i - E_f = \frac{\hbar^2}{2m} (k_i^2 - k_f^2)$



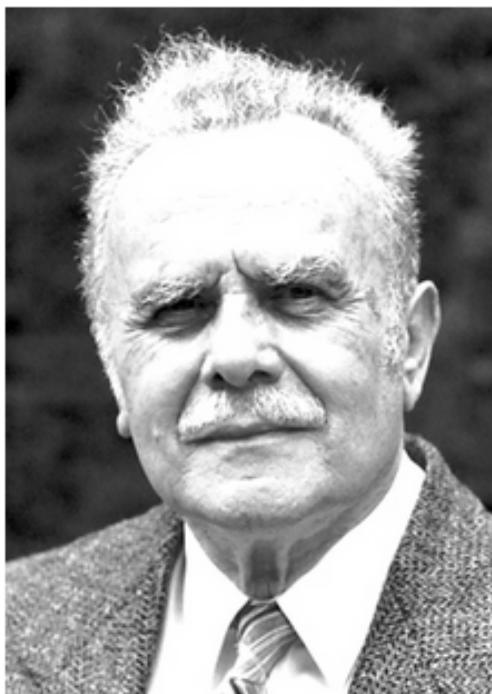
$$|\mathbf{Q}|^2 = |\mathbf{k}_i|^2 + |\mathbf{k}_f|^2 - 2 |\mathbf{k}_i||\mathbf{k}_f| \cos(2\theta)$$



The Nobel Prize in Physics 1994

Bertram N. Brockhouse, Clifford G. Shull

# Bertram N. Brockhouse - Facts



Bertram N. Brockhouse

**Born:** 15 July 1918, Lethbridge,  
Alberta, Canada

**Died:** 13 October 2003, Hamilton,  
Ontario, Canada

**Affiliation at the time of the award:**  
McMaster University, Hamilton,  
Ontario, Canada

**Prize motivation:** "for the  
development of neutron  
spectroscopy"

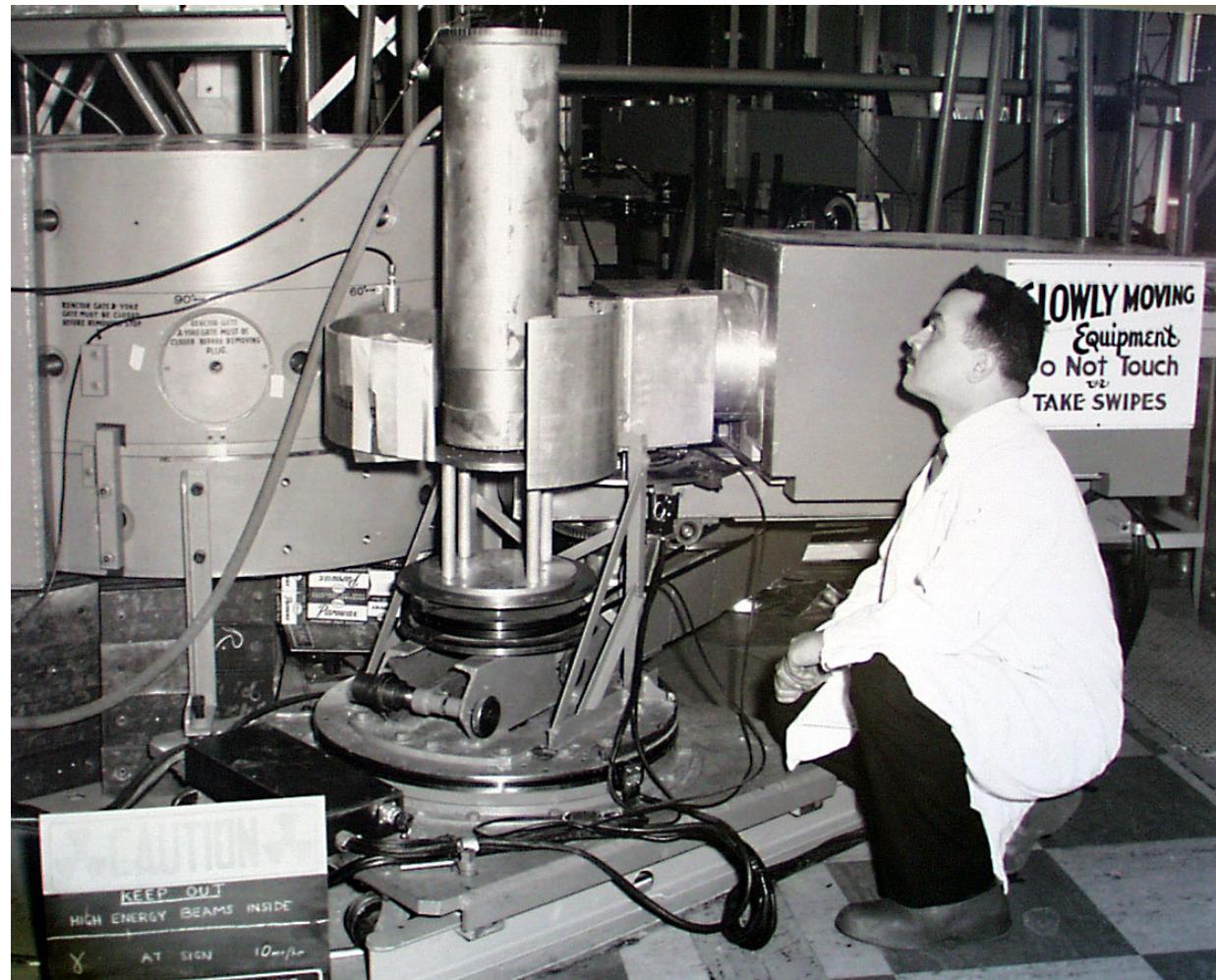
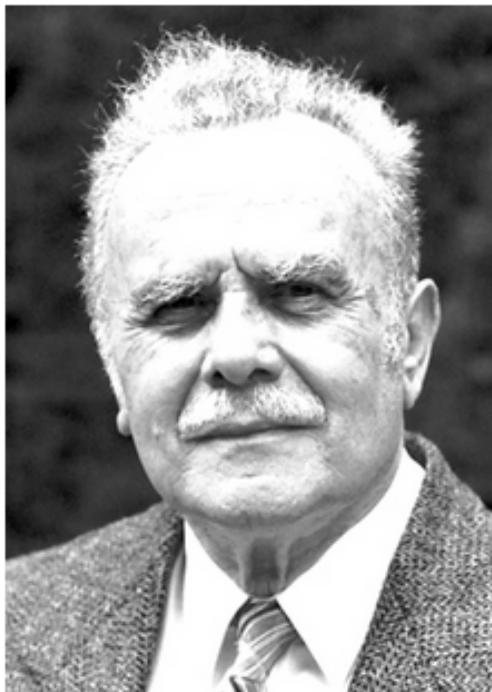
**Field:** Condensed matter physics,  
instrumentation



The Nobel Prize in Physics 1994

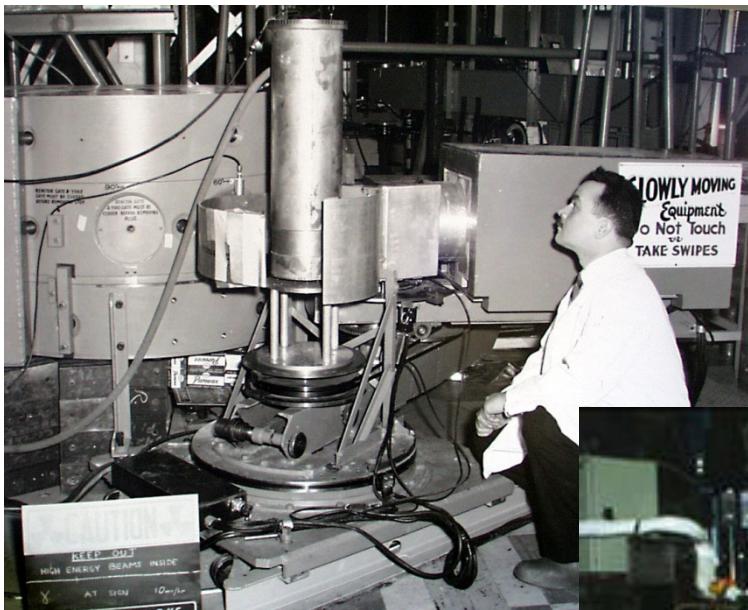
Bertram N. Brockhouse, Clifford G. Shull

# Bertram N. Brockhouse - Facts



Source: Atomic Energy of Canada Limited, Chalk River, Ontario (CC BY-NC-ND 2.0)

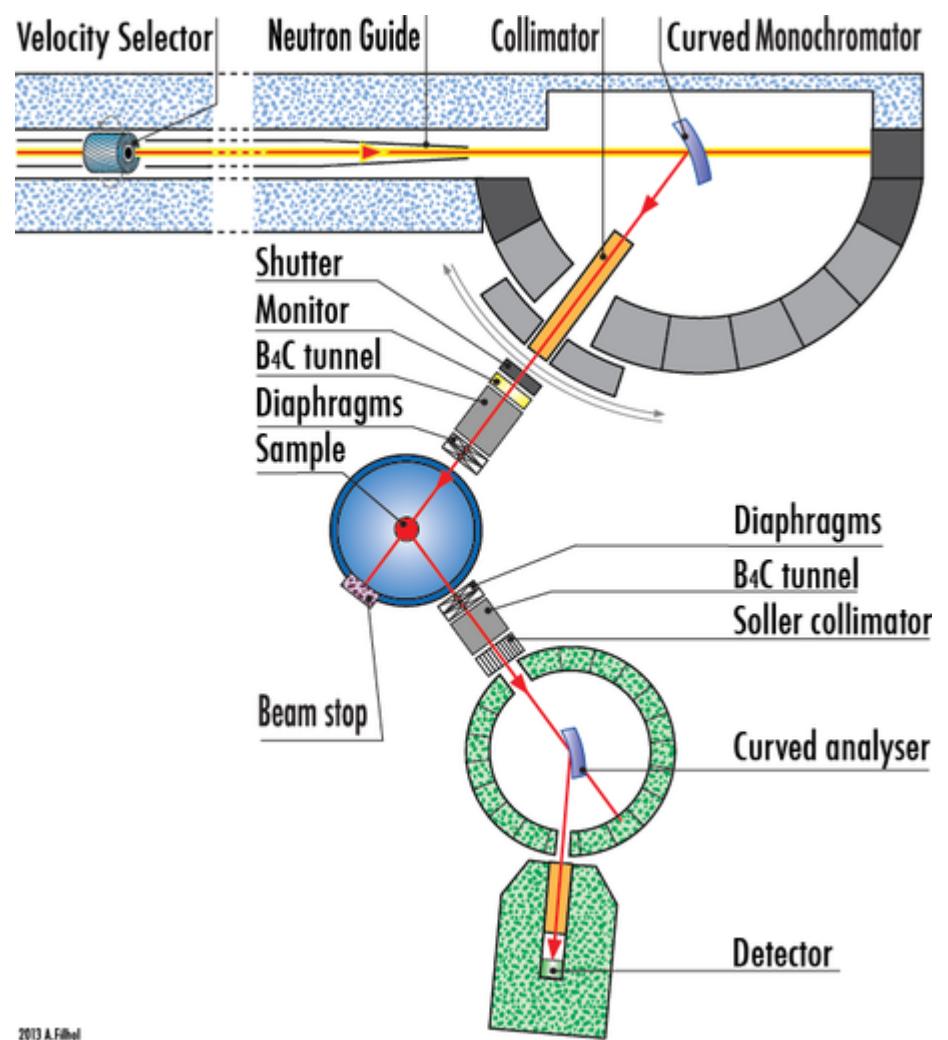
Bertram N. Brockhouse. [Nobelprize.org](https://www.nobelprize.org). Nobel Media AB 2013.



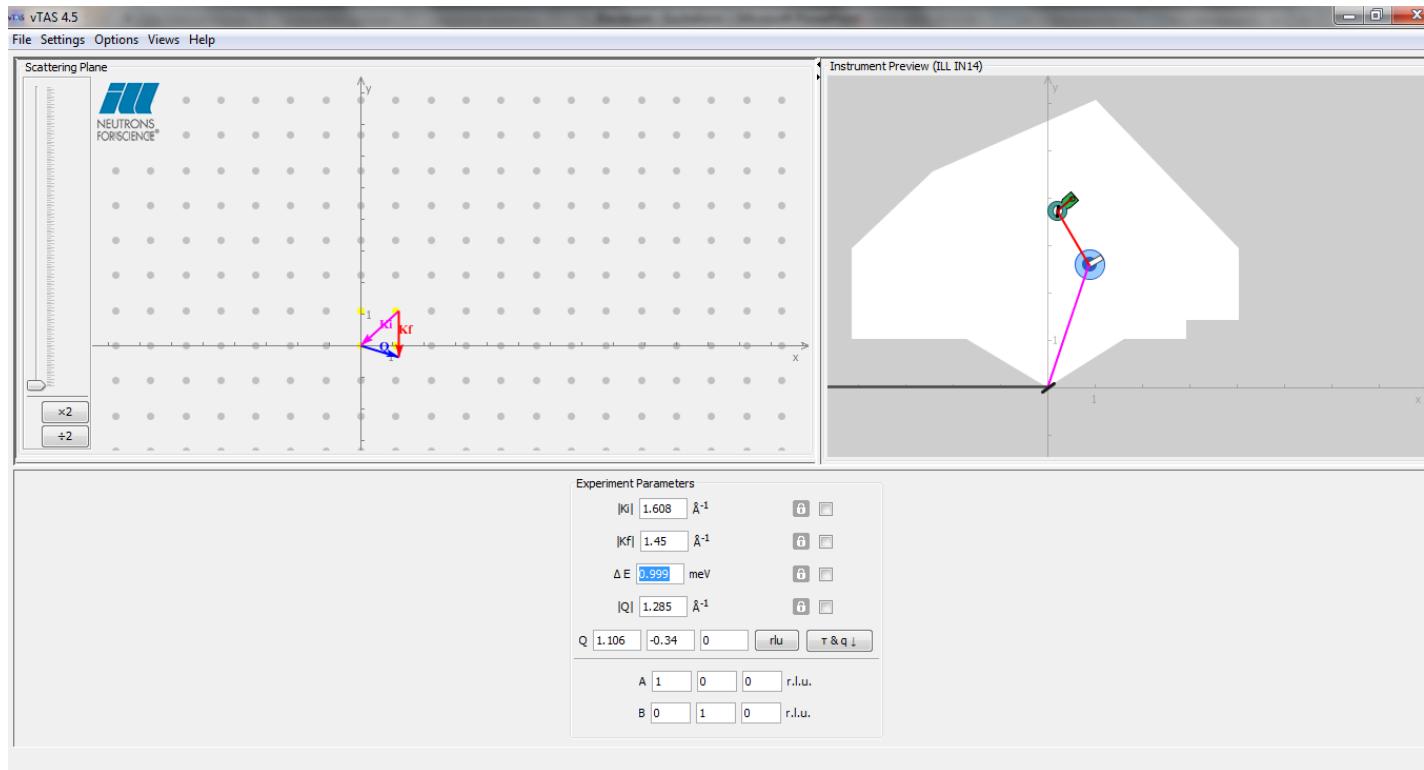
Source: Atomic Energy of Canada Limited, Chalk River, Ontario, Canada



IN12, ILL



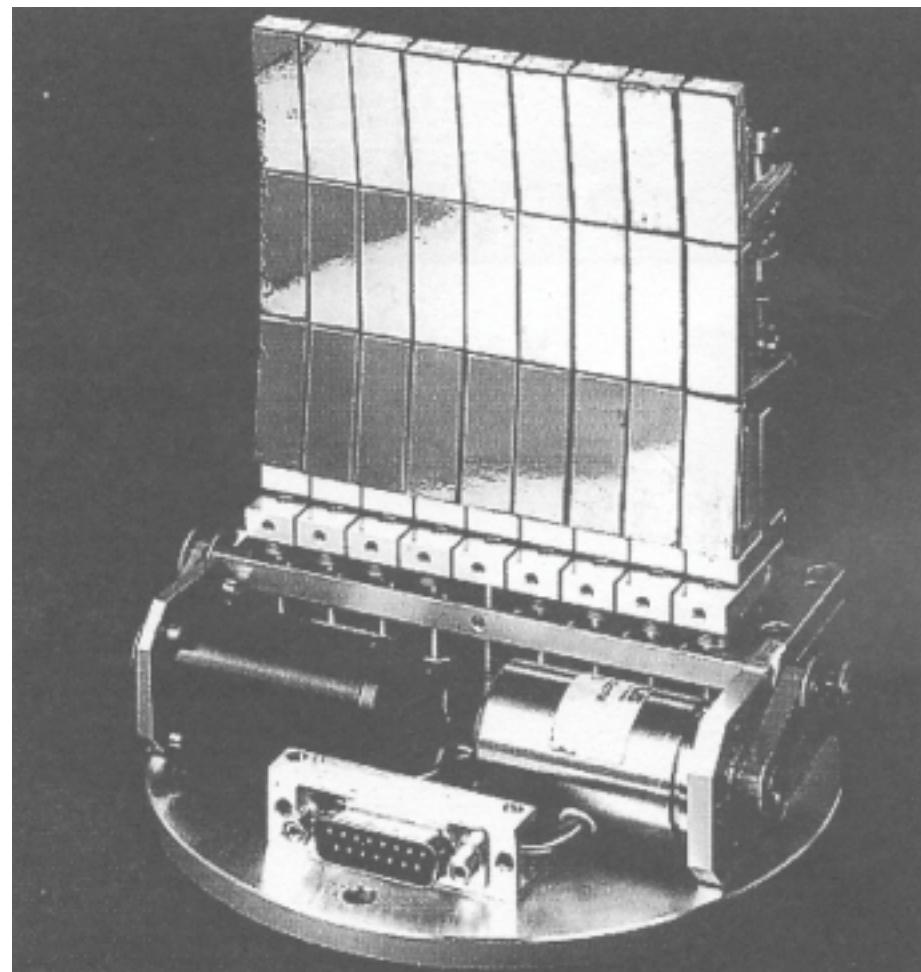
# vTAS – a virtual TAS



<http://www.ill.eu/instruments-support/computing-for-science/cs-software/all-software/vtas/>

The vTAS suite: a simulator for classical and multiplexed three-axis neutron spectrometers  
M. Boehm, A. Filhol, Y. Raoul, J. Kulda, W. Schmidt, K. Schmalzl,  
[Nuclear Inst. and Methods in Physics Research, A \(2013\) 697, 40-44.](https://doi.org/10.1016/j.nima.2013.04.044)

# Experimental Choices: Monochromator and Analyser



# Experimental Choices: Monochromator and Analyser

Material	reflection	d-spacing [Å]	E-range [meV]	comments
PG	(002)	3.3539	42-3.6	high reflectivity
PG	(004)	1.6770	168-14.5	"
Cu	(200)	1.8075	145-12.5	used for high energies
Cu	(220)	1.27813	290-25	"
Si	(111)	3.13543	48-4.2	absence of second order
Si	(220)	1.92005	128-11.1	"
Si	(311)	1.63742	176-15.3	"
Si	(511)	1.04514	433-37.4	"
Ge	(111)	3.26651	44-3.8	absence of second order
Ge	(311)	1.70588	163-14.1	"
Be	(002)	1.79035	148-12.8	

# Experimental Choices: Collimation

## Why collimate?

- cut down beam divergence
- make sure you're looking at sample



 **euro**  
**collimators**   
Ltd  
Bespoke collimator design and manufacture since 1970

## Soller collimators

A set of parallel (neutron absorbing) plates  
(divergence distribution is triangular)

For TAS, about 10' to 80'  
FWHM

# Experimental Choices: Filters

**Why filter?**

cut out higher order wavelengths

**Which filter?**

Be filters for cold neutrons (need  
to be kept at liquid nitrogen  
temperatures)

PG filters for thermal neutrons  
(might need rotating!)

**Where?**

Constant  $k_f$   
after the sample  
Constant  $k_i$   
before the sample



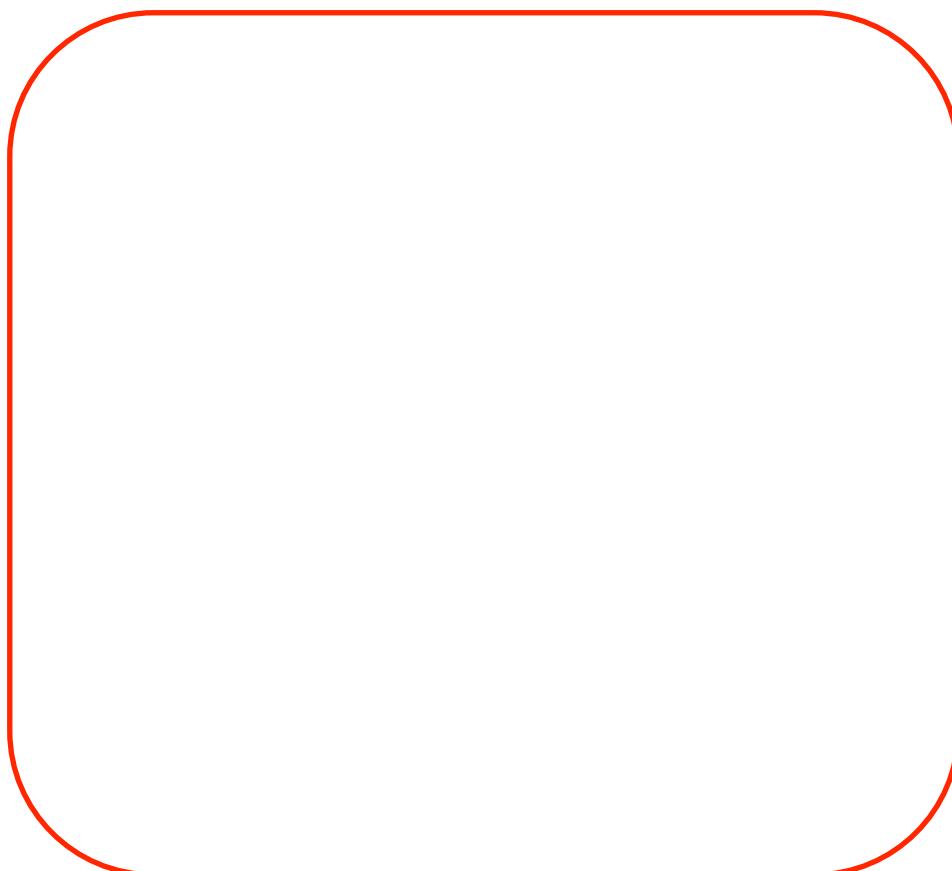
# Experimental Choices: Resolution

$\mathbf{Q}$  and  $\omega$  only defined to a certain level of precision

Bragg's law makes uncertainties  
lead to a better resolution

**BUT**  
 $k_i$  and  $k_f$  have their own  
resolution volumes, with  
distinct orientations in  $\mathbf{Q}$ -  $\omega$   
space.

→ resolution ellipsoid.



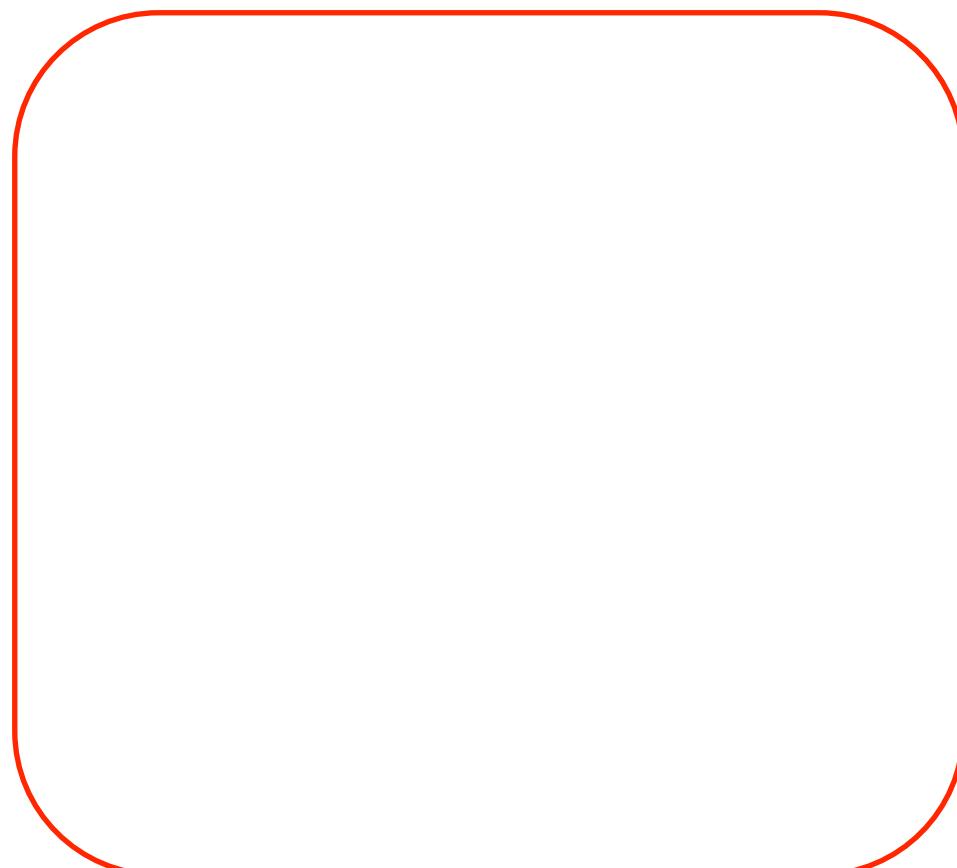
# Experimental Choices: Resolution

**Q** and  $\omega$  only defined to a certain level of precision

Bragg's Law,  $n\lambda = 2d \sin\theta$   
→  $\theta$  and  $\lambda$  are coupled.

**$k_i$**  and  **$k_f$**  have their own  
resolution volumes, with  
distinct orientations in **Q**-  $\omega$   
space.

→ resolution ellipsoid.



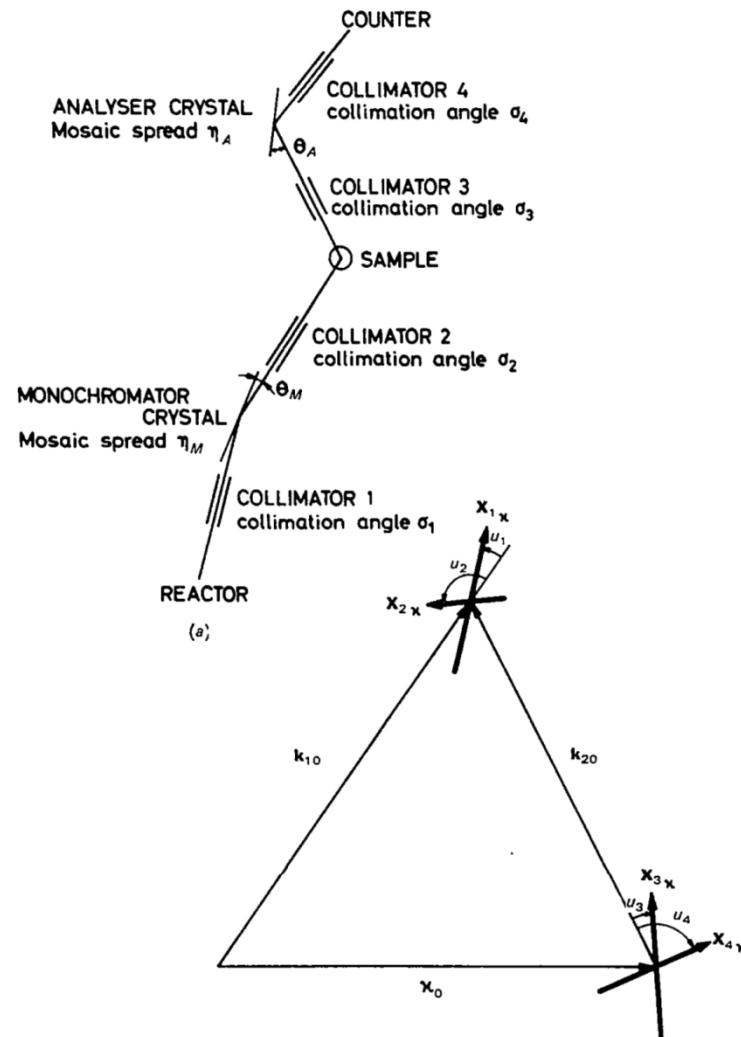
# Experimental Choices: The resolution ellipsoid

**Shape** and **size** depend upon:  
Collimation and crystal mosaic of  
monochromator and analyzer

**Orientation** depends upon:  
Sense of scattering at the  
monochromator, sample and  
analyzer

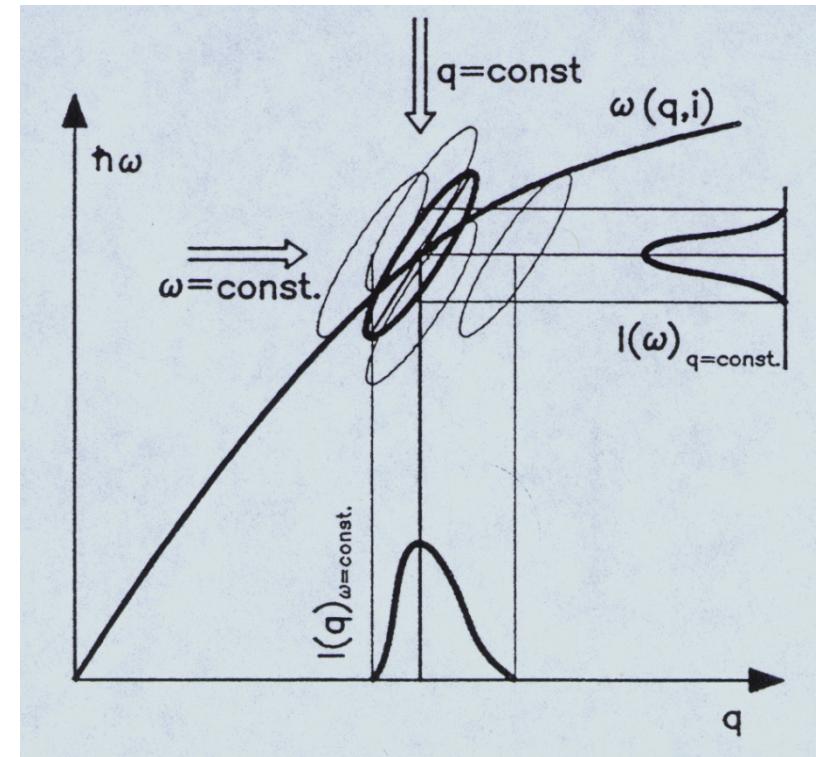
**Focussing** can also have an effect

**Tune your experiment to give you  
what you want**



# Experimental Choices: The resolution ellipsoid

Tune your experiment to give you  
what you want

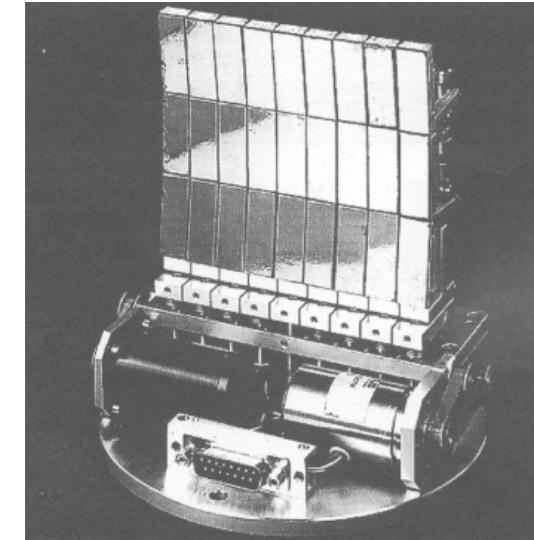


## References:

- RESTRAX – Saroun and Kulda, <http://neutron.ujf.cas.cz/restrax/doc/index.html>
- ResLib – Zheludev, <http://www.neutron.ethz.ch/research/resources/reslib>
- Cooper and Nathans, Acta Cryst 23, 357 (1967)
- Popovici *et al.*, J. Appl. Cryst. 20, 90 (1987).

# Experimental Choices: Focussing

**Vertical focussing**  
opens up **Q** resolution in  
the vertical direction (out  
of the scattering plane)

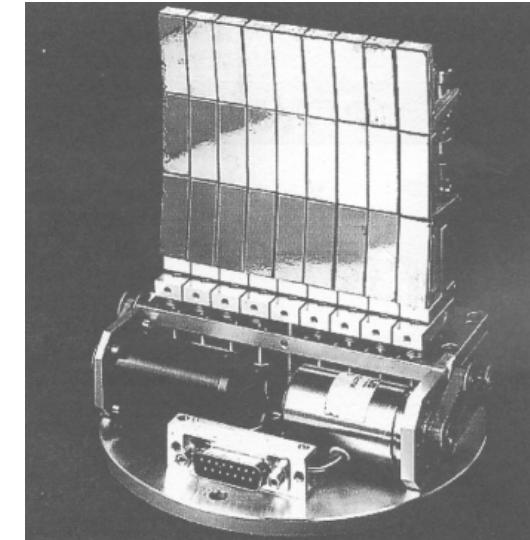


Focussing distance depends upon Bragg angle so the radius,  $R$ , of the mono/analyzer crystal needs to be variable.

$$L_0 = \text{source to mono} \quad L_1 = \text{mono to sample} \quad \frac{1}{L_0} + \frac{1}{L_1} = \frac{2 \sin \theta_{Bragg}}{R} \quad ; \quad h_{image} = h_{source} \frac{L_1}{L_0}$$

# Experimental Choices: Focussing

**Horizontal focussing**  
messes up Bragg conditions at  
the monochromator and  
analyzer, but increases intensity



Affects **Q** resolution in the scattering plane, and the  
energy resolution

# Beware: Spurions



ELSEVIER

Available online at [www.sciencedirect.com](http://www.sciencedirect.com)

SCIENCE @ DIRECT®

Physica B 350 (2004) 11–16

PHYSICA B

[www.elsevier.com/locate/physb](http://www.elsevier.com/locate/physb)

## Chasing ghosts in reciprocal space—a novel inelastic neutron multiple scattering process

H.M. Rønnow<sup>a,b,\*</sup>, L.-P. Regnault<sup>b</sup>, J.E. Lorenzo<sup>c</sup>

<sup>a</sup>NEC Laboratories, Princeton and University of Chicago, USA

<sup>b</sup>MDN/SPSMS/DRFMC, CEA-Grenoble, 38054 Grenoble, France

<sup>c</sup>Laboratoire de Cristallographie, CNRS, 38042 Grenoble, France

---

### Abstract

We have discovered that a recently reported weak excitation branch in the spin-Peierls material CuGeO<sub>3</sub> is in fact a ghost image of the primary magnetic excitation shifted in reciprocal space by a novel multiple scattering process. A model is developed that predicts the occurrence of such multiple scattering and accounts for the observations in CuGeO<sub>3</sub>. New ‘ghostons’ can occur when the magnetic unit cell is smaller than the structural, while mixing of intensities from different reciprocal space zones jeopardize accurate polarisation analysis and the study of weak modes in general.  
© 2004 Elsevier B.V. All rights reserved.

PACS: 25.40.Fq; 75.40.Gb; 78.70.Nx

Keywords: Inelastic neutron scattering; Copper germanate CuGeO<sub>3</sub>; Neutron polarisation analysis

---

# Beware: Spurious

- Bragg peaks from the sample holder/cryostat
- Incoherent scattering from the mono/analyzer
- Beam on to detector
- Phonons from mono/analyzer

Check temperature dependence  
Sample angle scans

# Measuring a phonon spectrum

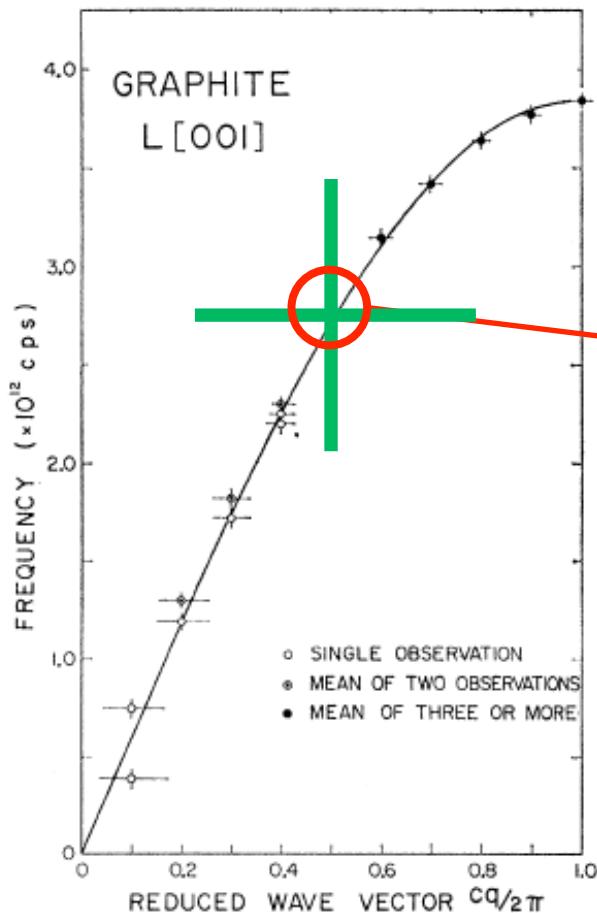


FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.

Dolling and Brockhouse., Phys. Rev. 128, 1120 (1962)

$$\frac{d^2\sigma}{d\Omega dE_f} = \frac{k_f}{k_i} S(Q, \omega)$$

Constant- $\mathbf{Q}$   
or  
Constant- $E$  ??

Fixed  $k_i$  or fixed  $k_f$ ?

We normalised to the number of incident neutrons using a low efficiency monitor whose efficiency depends on the neutron velocity. In fixed  $k_i$  mode, this efficiency is fixed and we therefore measure signal per monitor

# Measuring a phonon spectrum

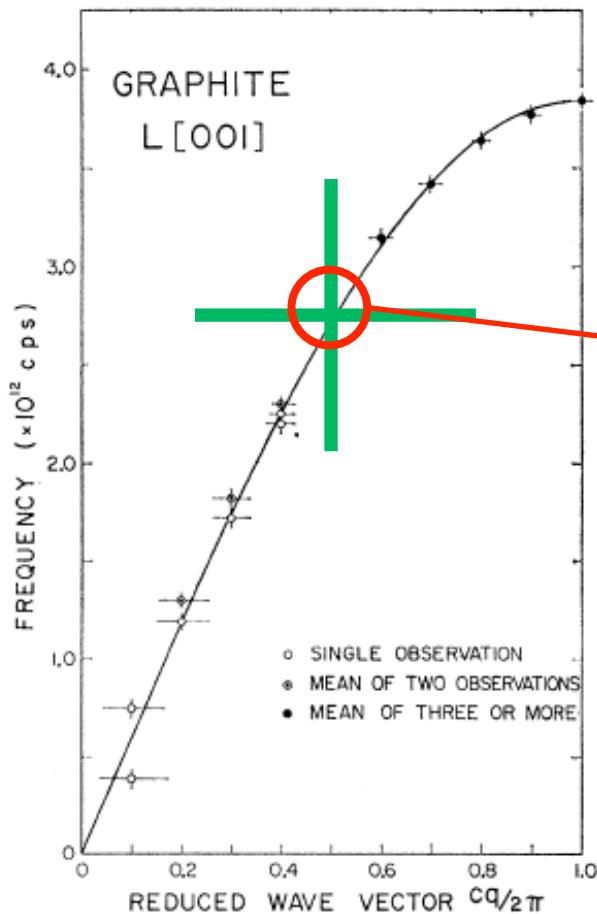
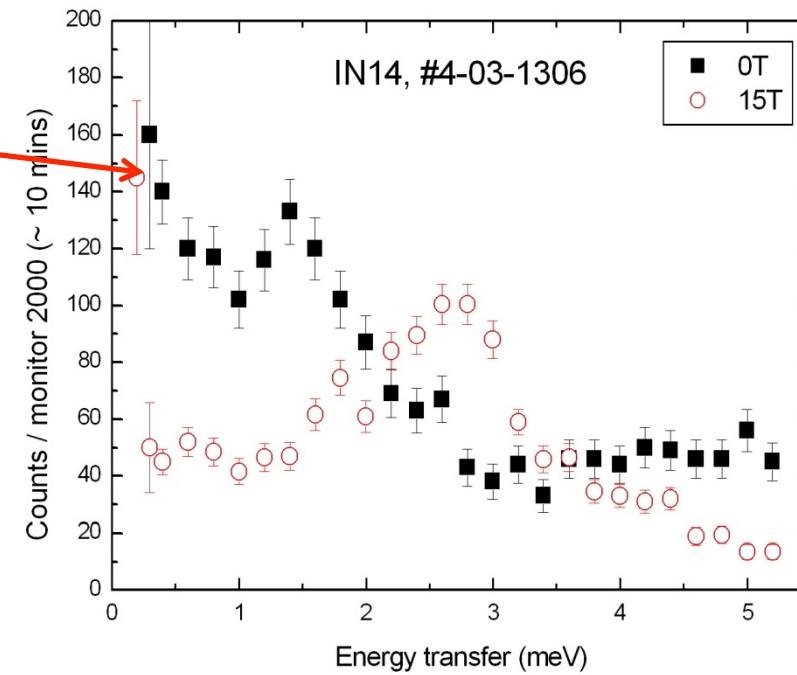
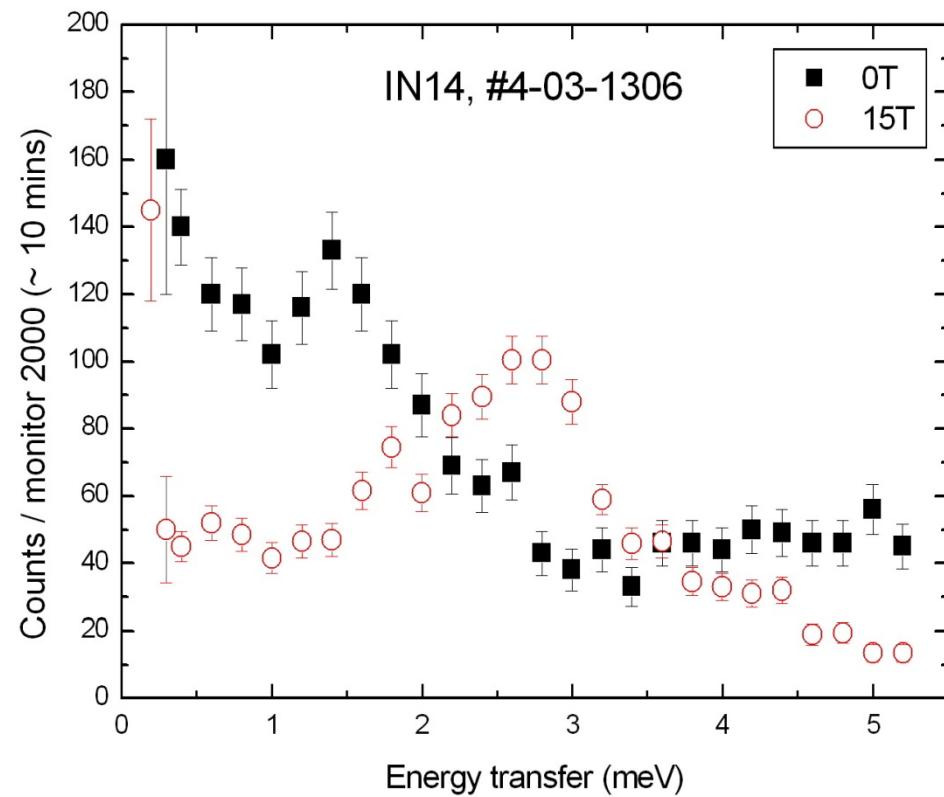


FIG. 3. Dispersion curve for the  $L[001]$  modes in which the planes move as rigid units. The solid line is the best fitting (simple) sine wave to the experimental points. The assignment of errors is discussed in the text.



Dolling and Brockhouse., Phys. Rev. 128, 1120 (1962)



# Advantages and disadvantages of the triple-axis method

## Advantages

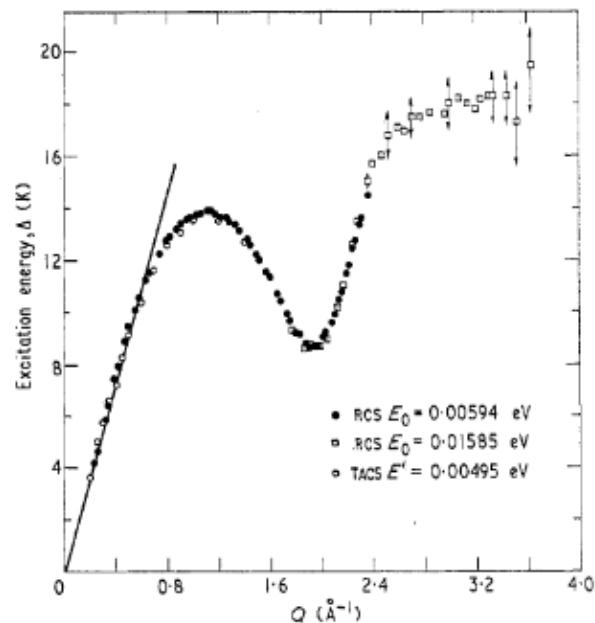
1. Can focus all intensity on point in reciprocal space that is important
2. Can make measurements along high-symmetry directions
3. Can use either constant- $Q$  or constant-E, depending on type of excitation being examined.
4. Can use focusing and other ‘tricks’ to improve the signal/noise
5. Can use polarisation analysis to separate electronic and phonon signals

## Disadvantages

1. Technique is slow and requires some expert attention
2. Use of monochromators and analysers gives rise to possible higher-order effects that give rise to “spurious”
3. With measurements restricted to high-symmetry directions it is eminently possible that something important might be missed

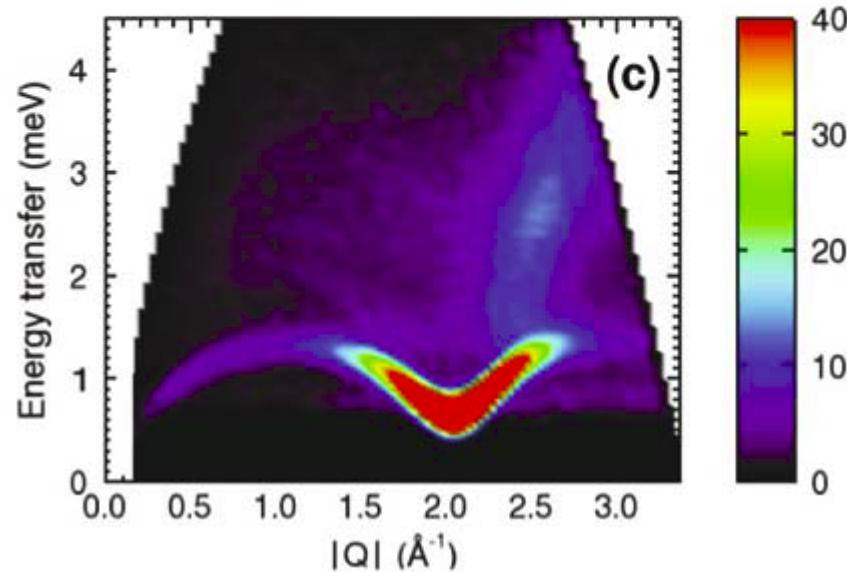
# Superfluid helium

TAS



Cowley and Woods., Can. J. Phys. 49, 177 (1971)

TOF



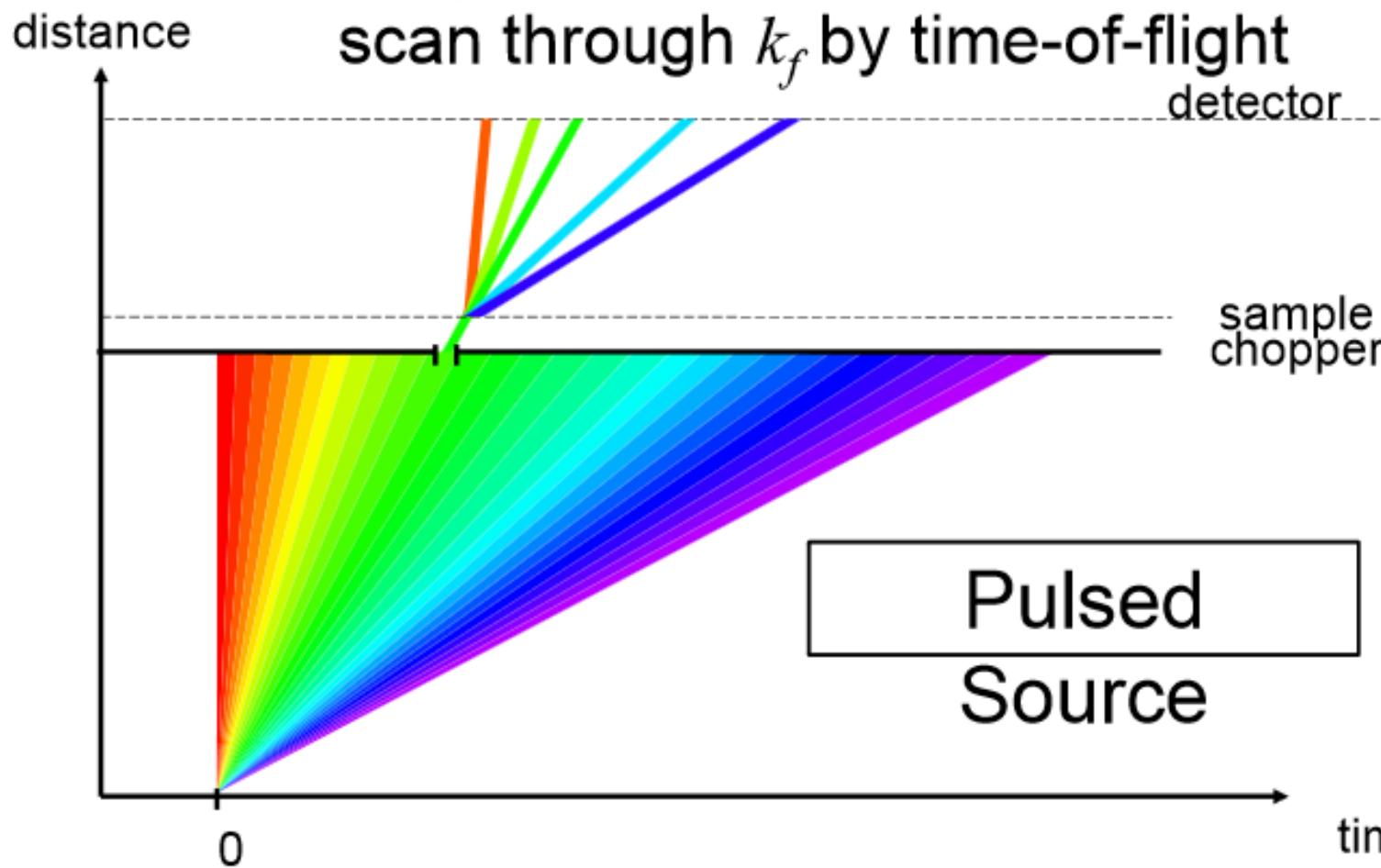
Blackburn *et al.*, Pramana 71, 673 (2008)

# Time-of-flight spectroscopy

Direct geometry:

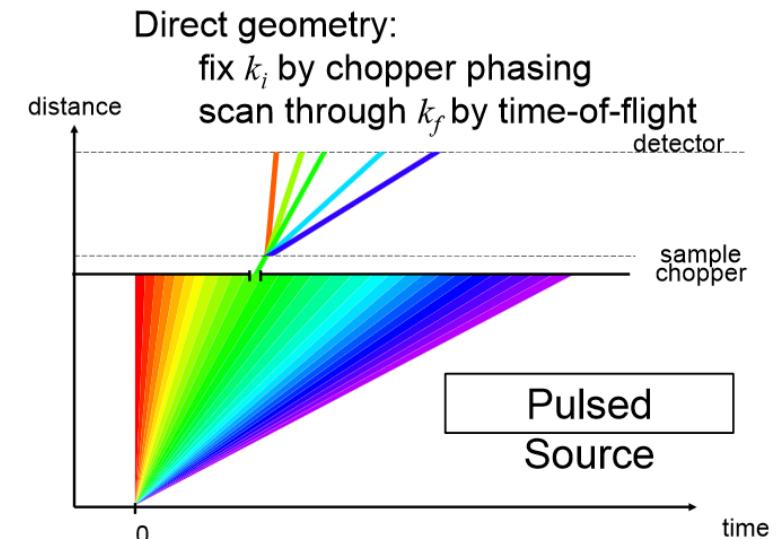
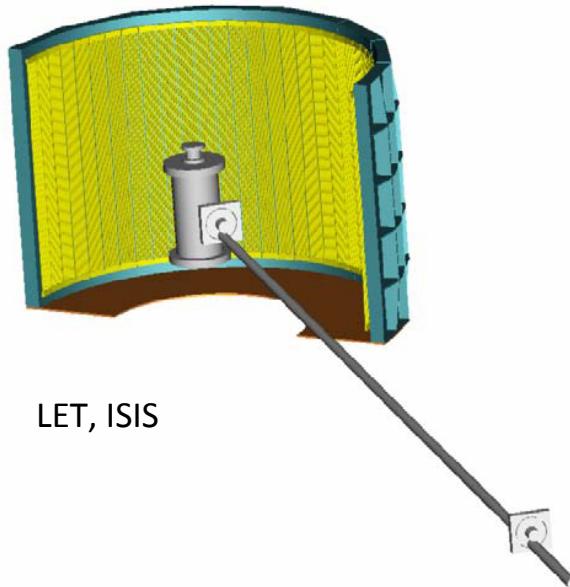
fix  $k_i$  by chopper phasing

scan through  $k_f$  by time-of-flight



from Ken Andersen

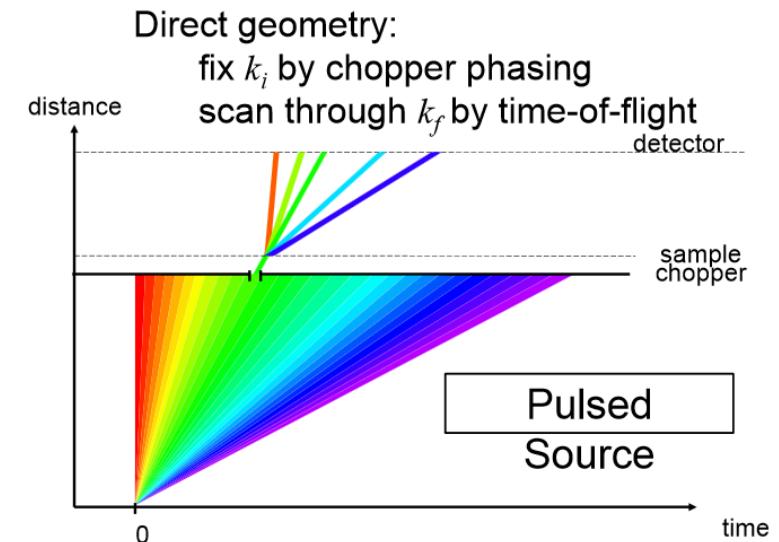
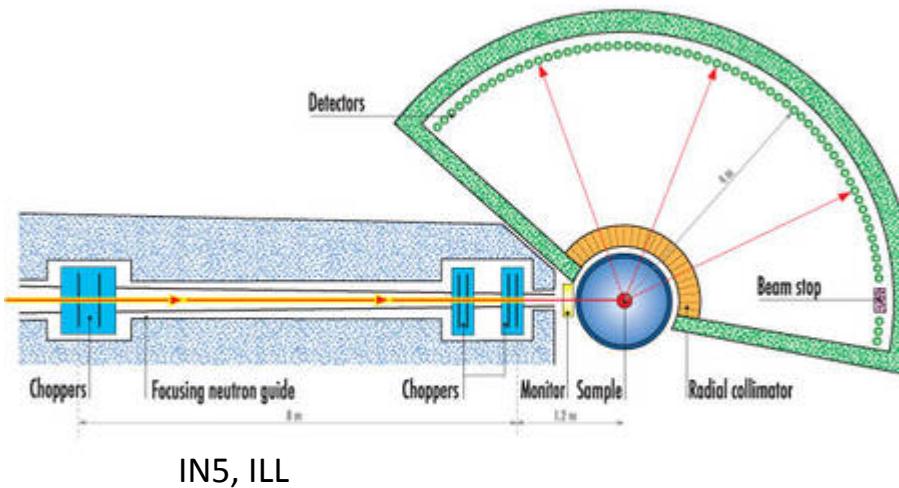
# Time-of-flight spectroscopy



sample-detector distance

$$\text{final velocity} = \frac{\text{sample-detector distance}}{\text{time to detector} - \text{time to sample}}$$

# Time-of-flight spectroscopy



$$\text{final velocity} = \frac{\text{sample-detector distance}}{\text{time to detector} - \text{time to sample}}$$

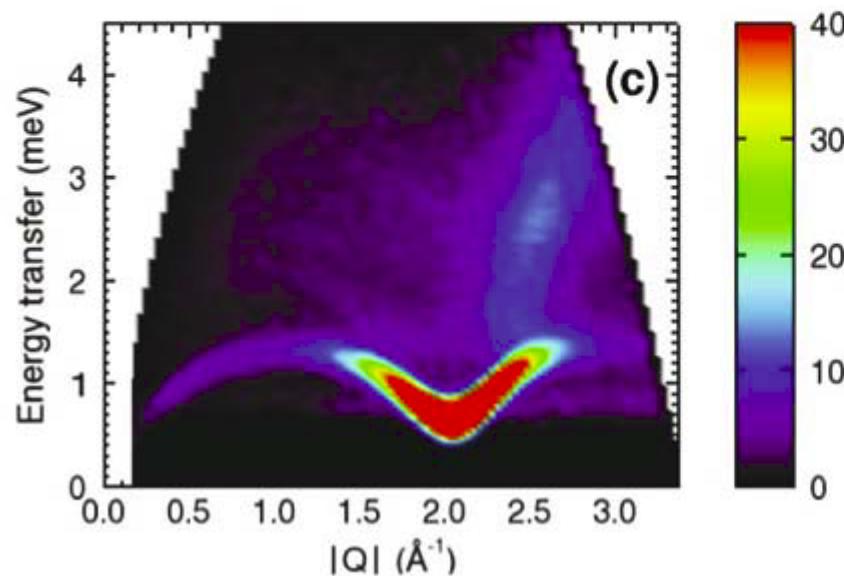
This gives us the neutron's final energy

# Time-of-flight spectroscopy

Measured quantity:

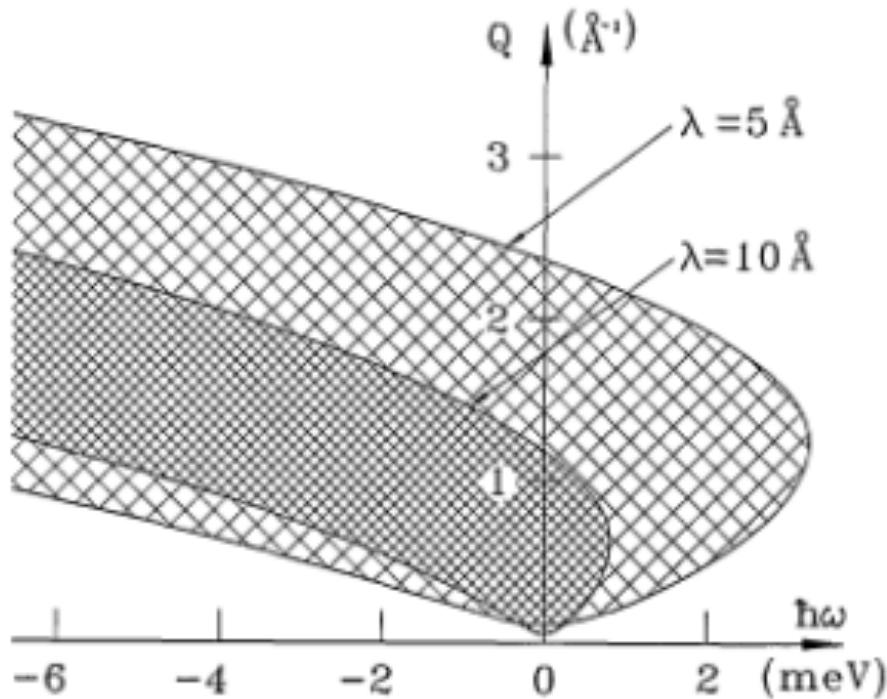
$$I(2\theta, t_D) \rightarrow S(\mathbf{Q}, \omega)$$

Remember the bin sizes:



# Time-of-flight spectroscopy

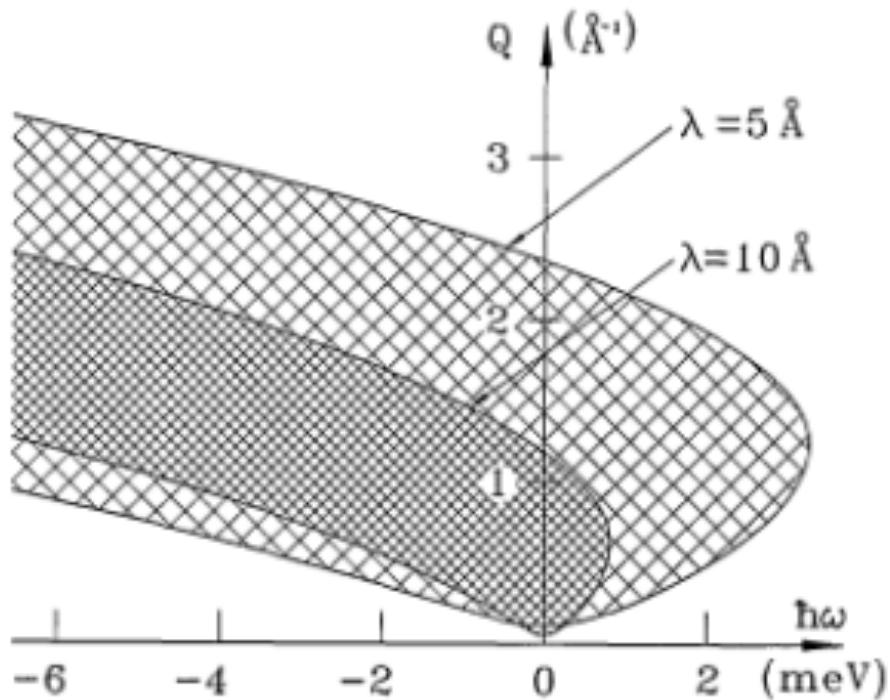
$$|\mathbf{Q}|^2 = |\mathbf{k}_i|^2 + |\mathbf{k}_f|^2 - 2 |\mathbf{k}_i||\mathbf{k}_f| \cos(2\theta)$$



**Fig. 17.** Plots of the accessible region in  $(Q, \omega)$  space for neutrons of wavelength 5 and 10 Å (energy 3.272 and 0.818 meV, respectively). The minimum and maximum scattering angles are 5° and 140°. There is no (theoretical) limit to the energy transfer in neutron energy gain.

# Time-of-flight spectroscopy

$$\frac{\hbar^2 Q^2}{2m} = 2E_0 - \hbar\omega - 2\sqrt{E_0(E_0 - \hbar\omega)} \cos(2\theta)$$

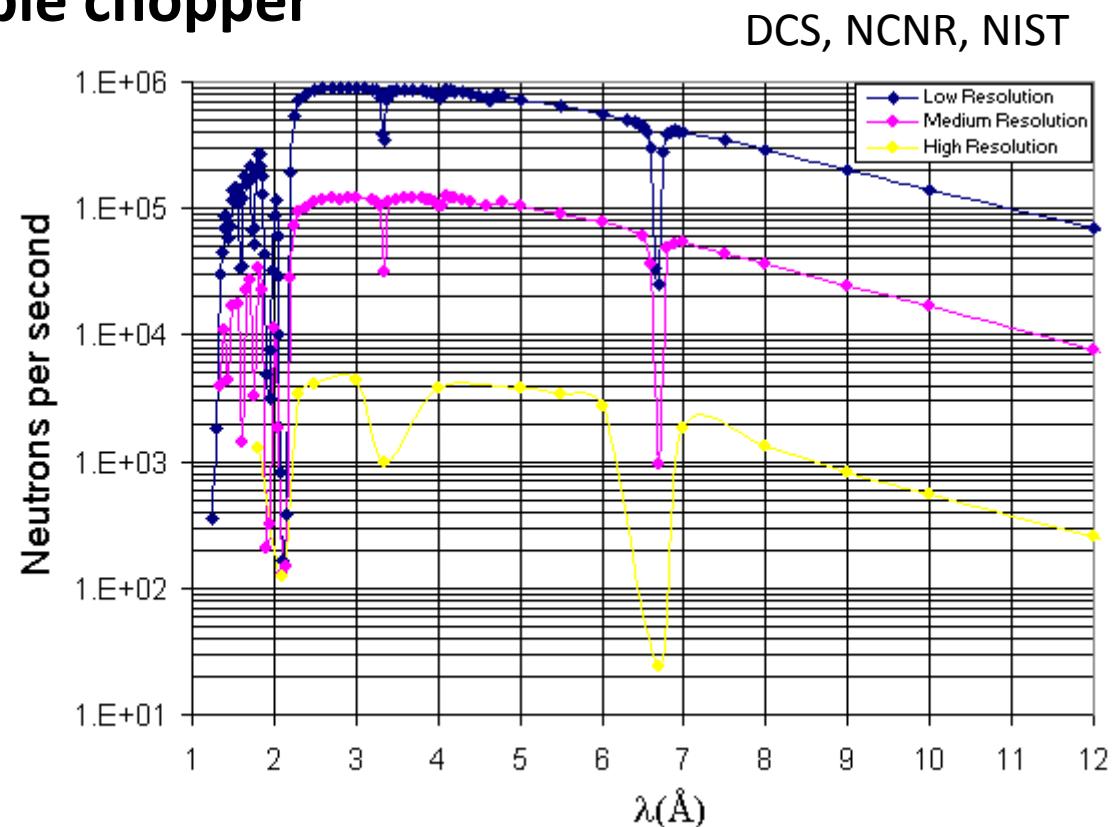


**Fig. 17.** Plots of the accessible region in  $(Q, \omega)$  space for neutrons of wavelength 5 and 10  $\text{\AA}$  (energy 3.272 and 0.818 meV, respectively). The minimum and maximum scattering angles are 5° and 140°. There is no (theoretical) limit to the energy transfer in neutron energy gain.

# Experimental choices: Intensity vs Resolution

**What can we change?**

- incident wavelength
- pulse width at sample chopper
- frame overlap ratio

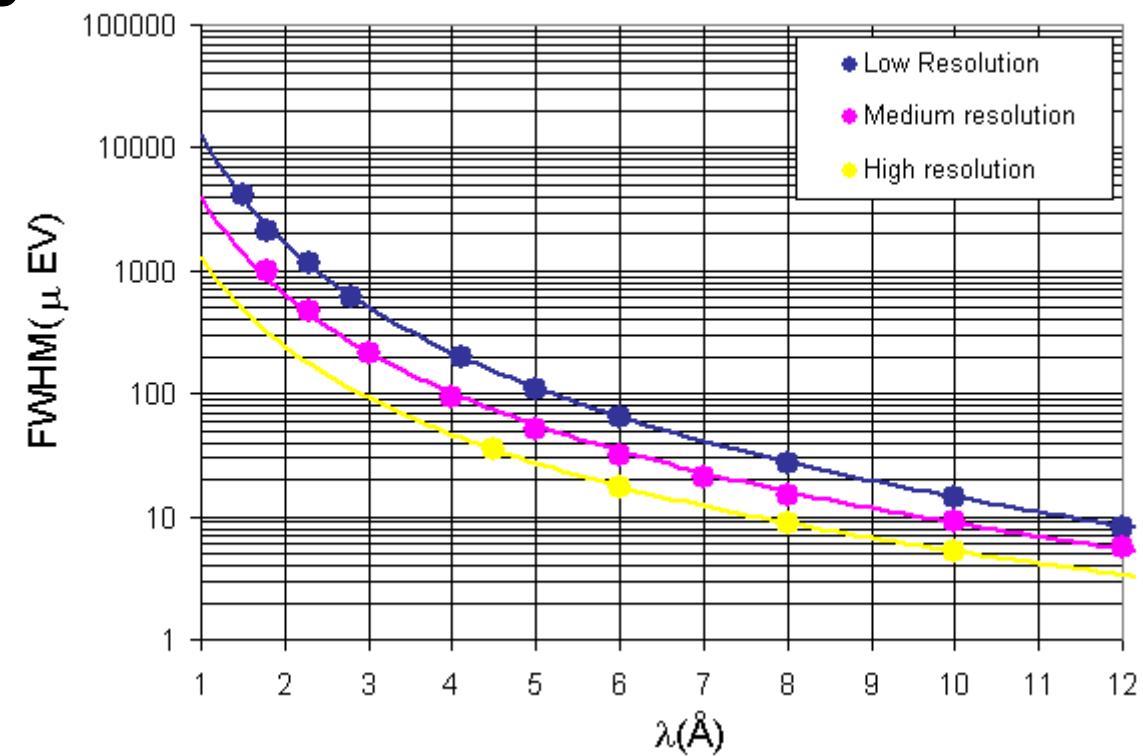


# Experimental choices: Intensity vs Resolution

**What can we change?**

- incident wavelength
- pulse width at sample chopper
- frame overlap ratio

DCS, NCNR, NIST



# Experimental choices: Intensity vs Resolution

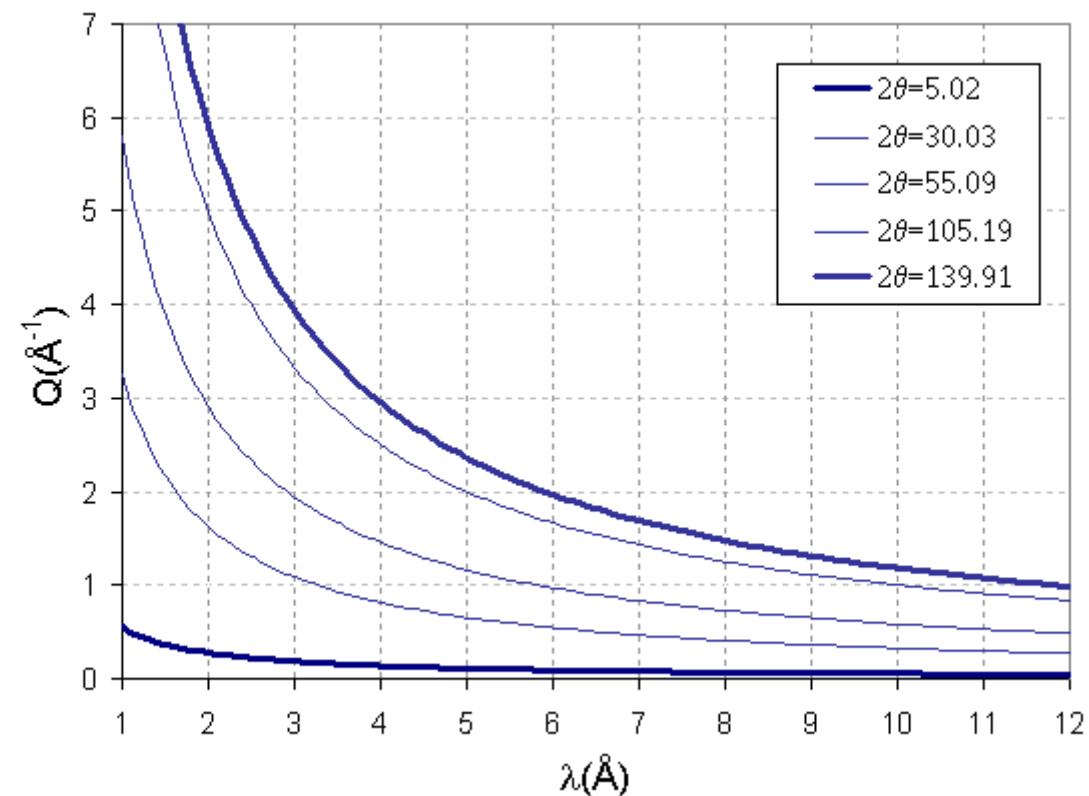
**What can we change?**

incident wavelength

pulse width at sample chopper

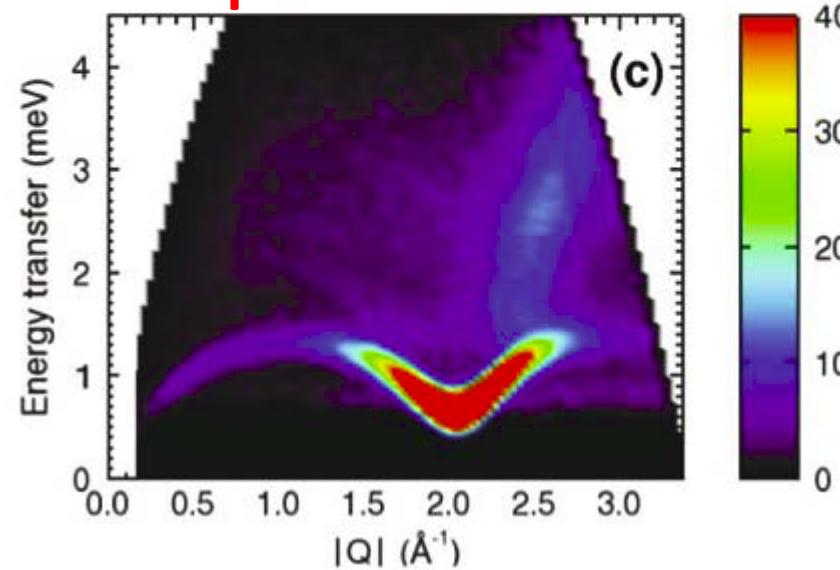
frame overlap ratio

DCS, NCNR, NIST

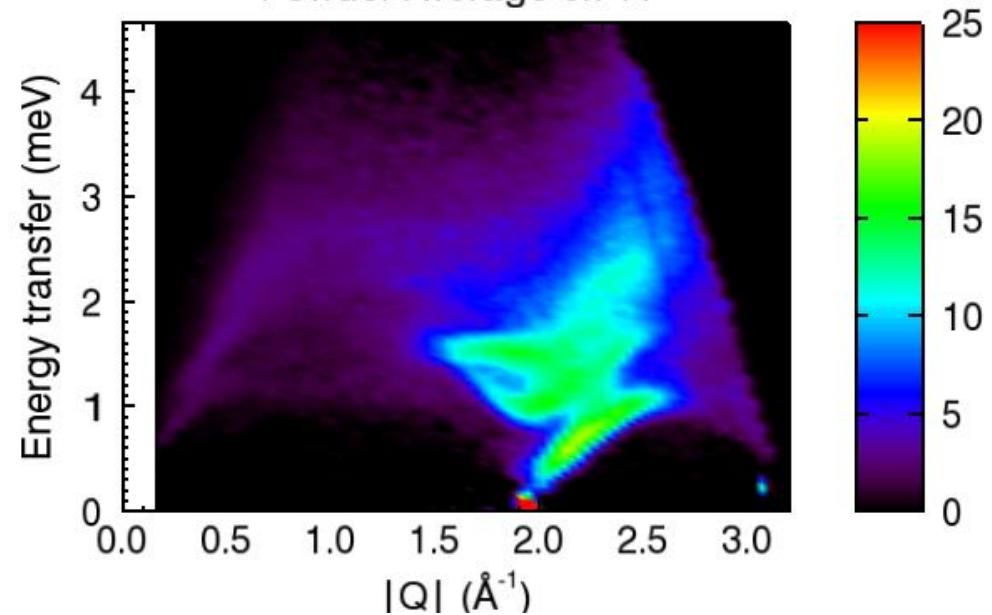


# TOF on single crystals

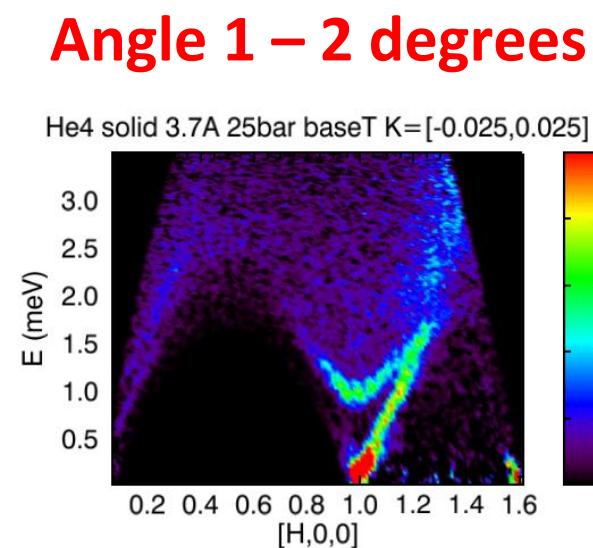
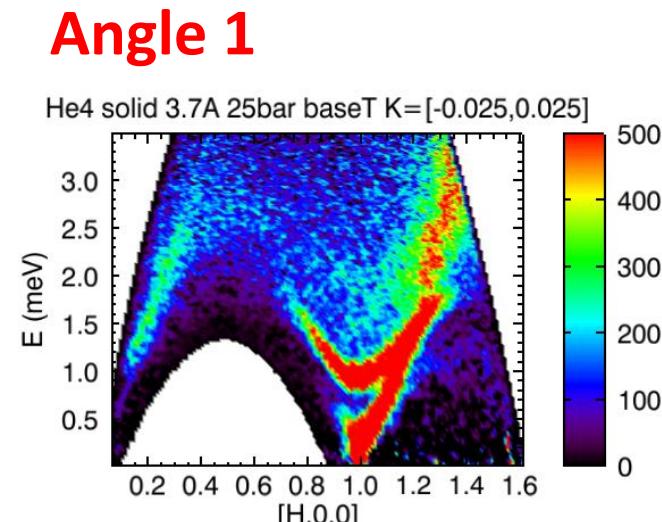
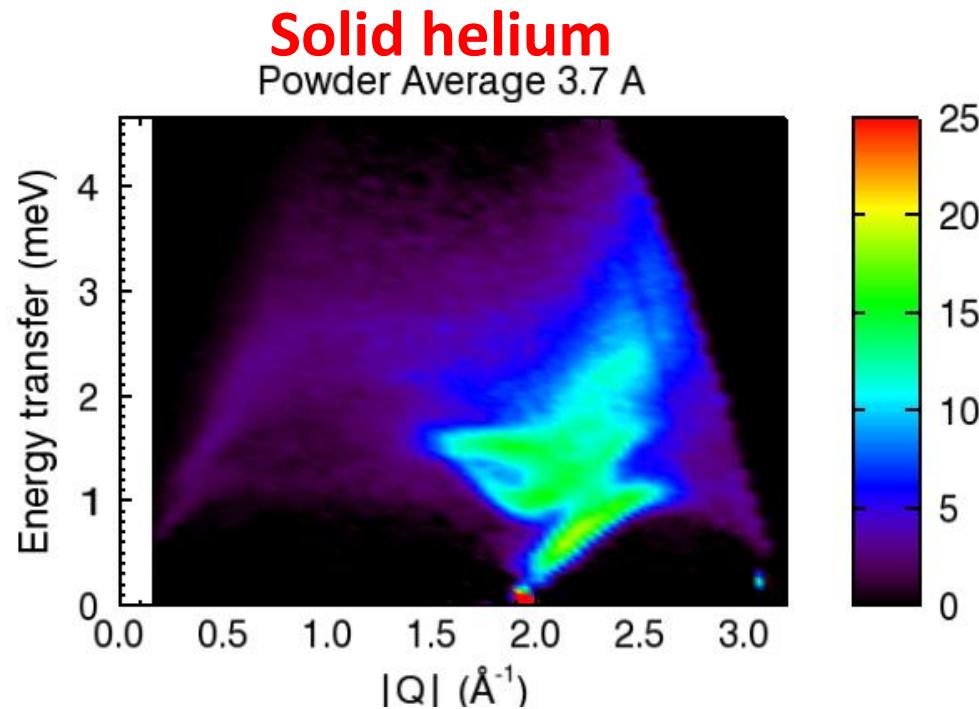
Superfluid helium



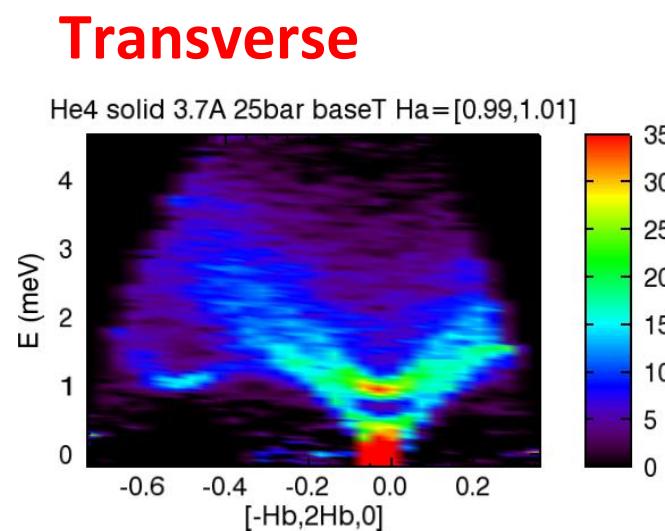
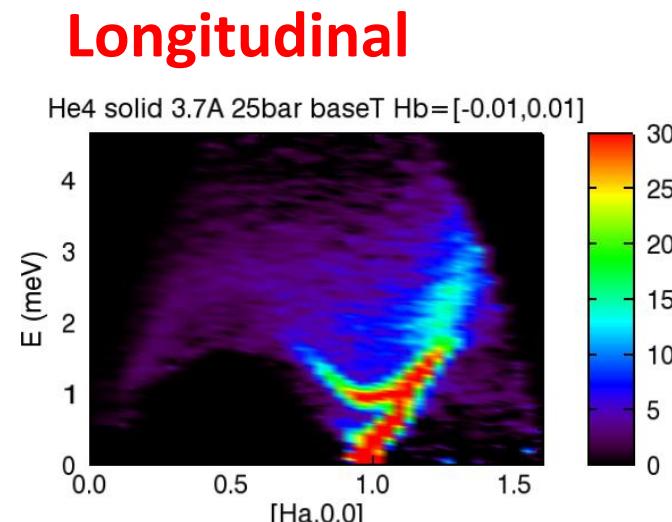
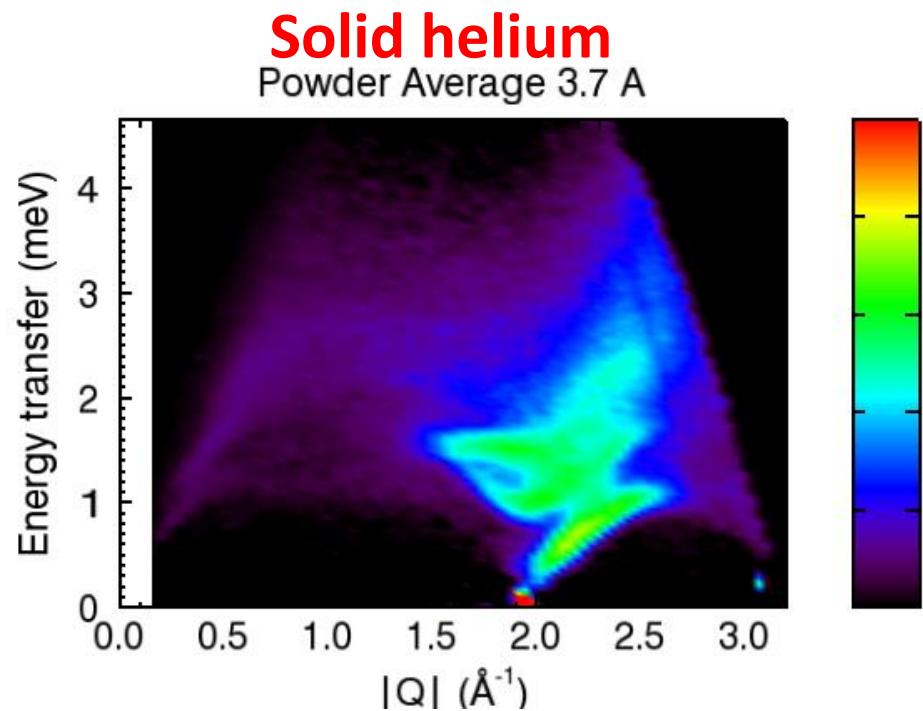
Solid helium  
Powder Average 3.7  $\text{\AA}$



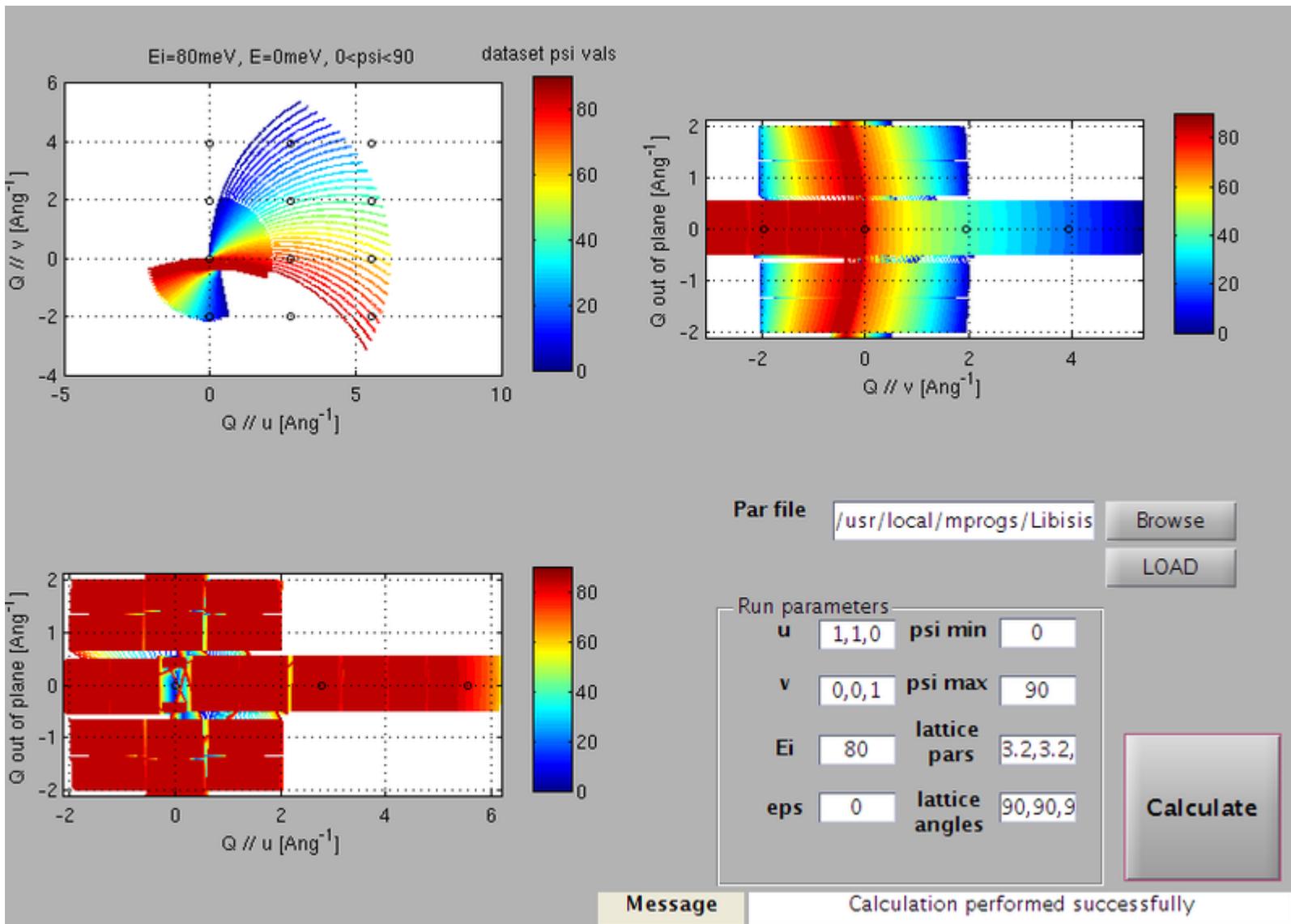
# TOF on single crystals



# TOF on single crystals



# TOF on single crystals



HORACE screenshot – horace.isis.rl.ac.uk

# Complete dataset in $\mathbf{Q}$ and $\omega$ space

Headings *et al.*,

PRL 105, 247001 (2010)

PHYSICAL REVIEW LETTERS

week ending  
10 DECEMBER 2010

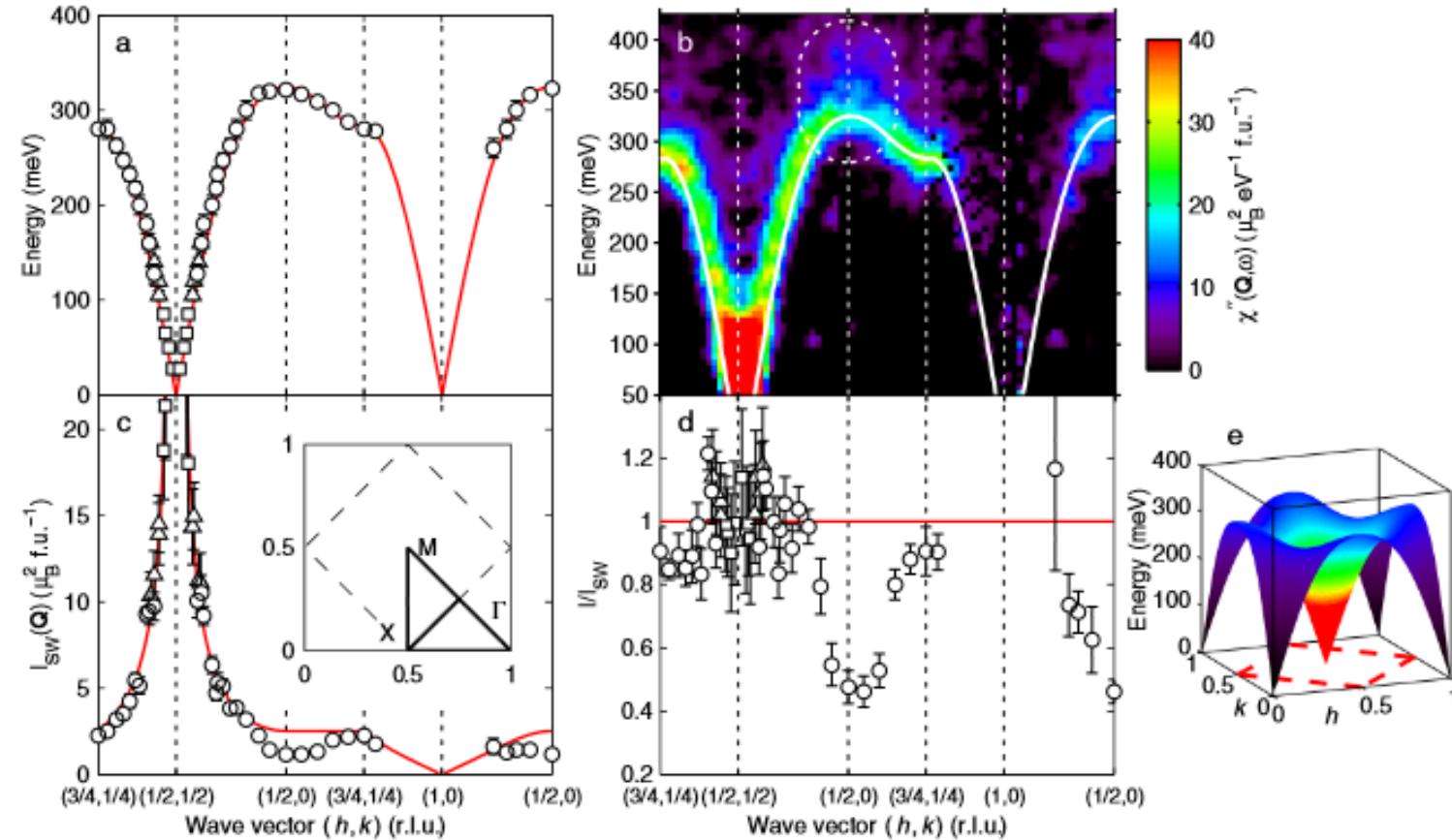
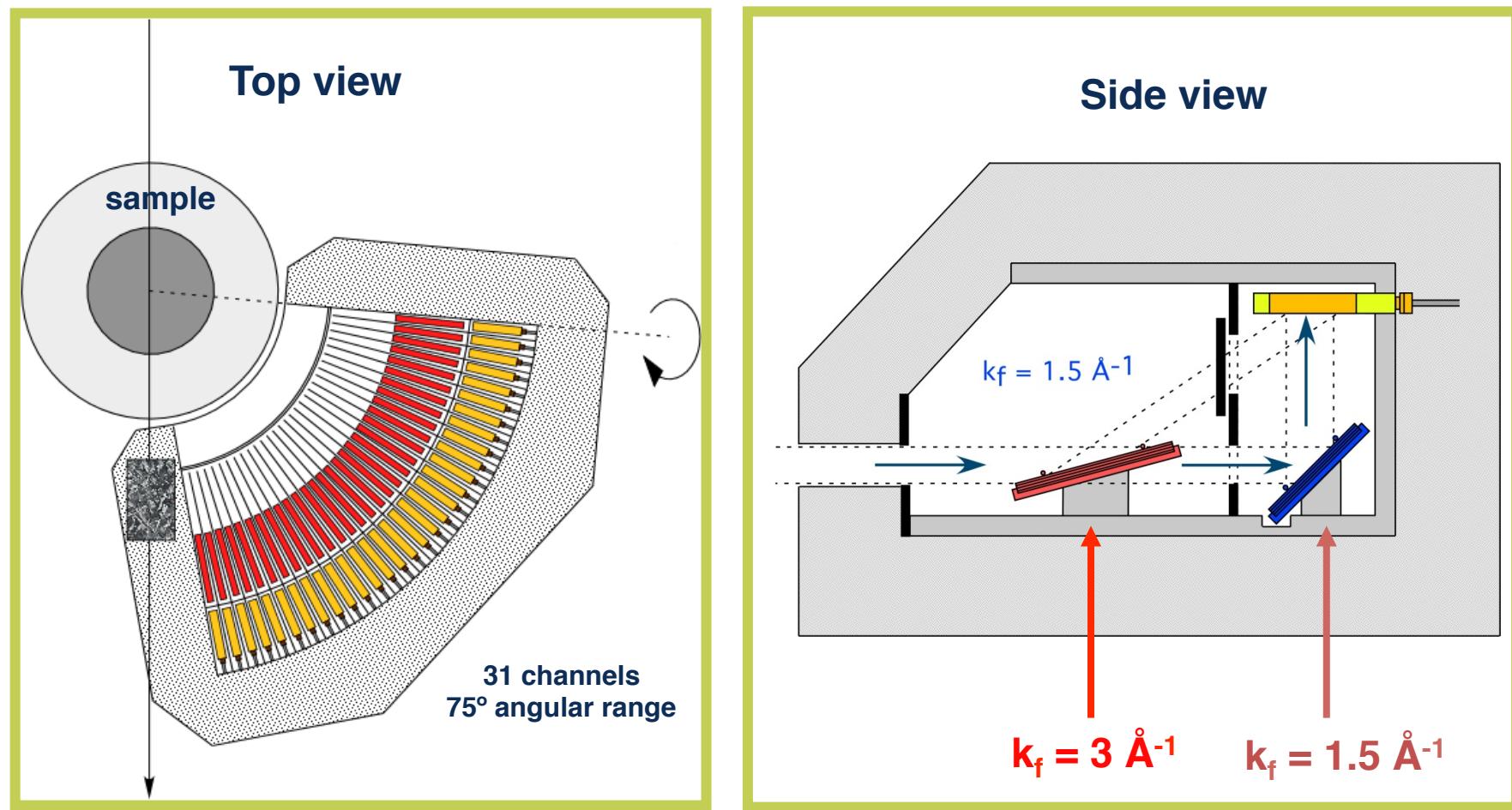


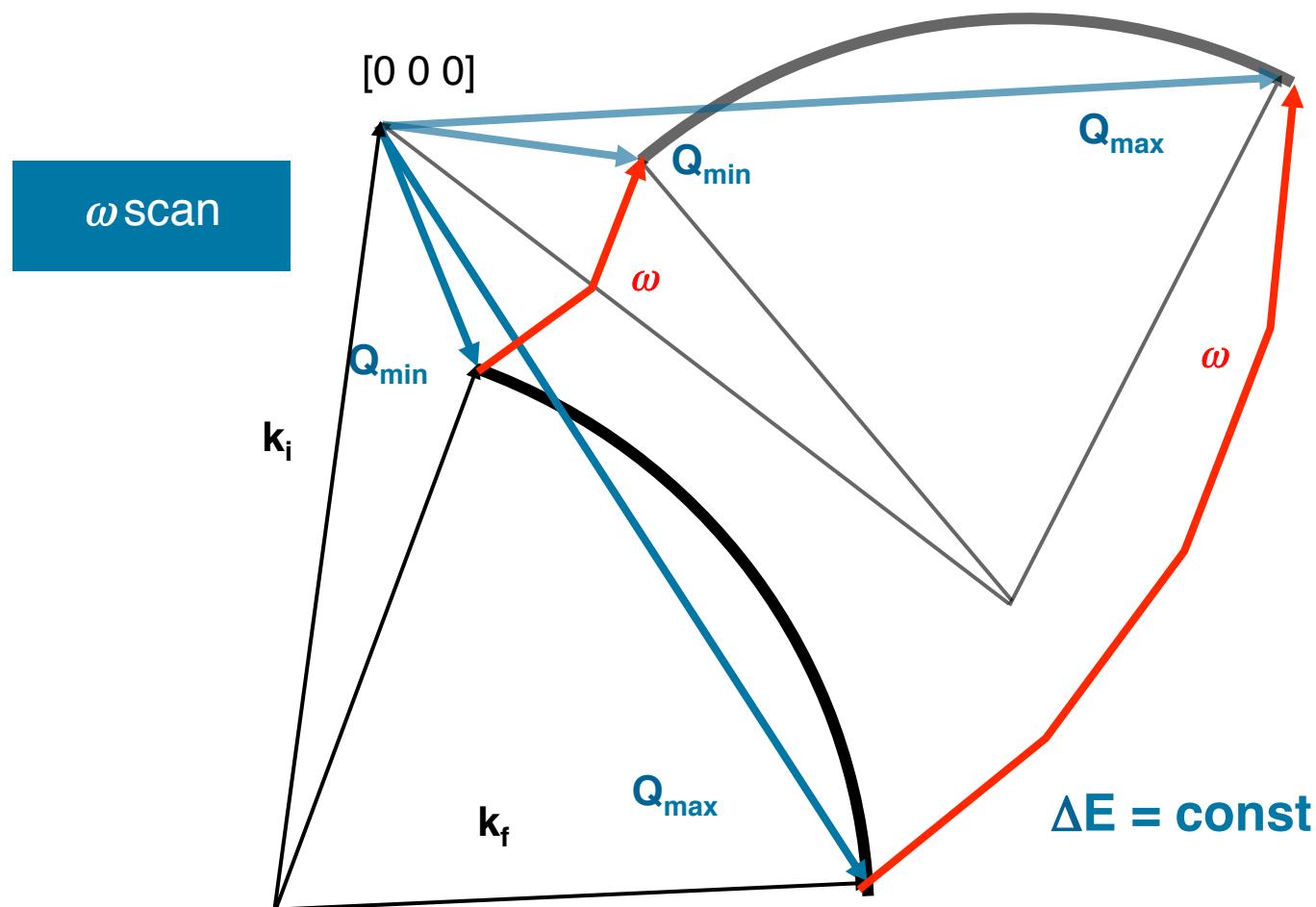
FIG. 2 (color online).  $\mathbf{q}$  dependence of the magnetic excitations in  $\text{La}_2\text{CuO}_4$ . (a) One-magnon dispersion ( $T = 10$  K) along lines in (c, inset). Symbols indicate  $E_i$ : 160 meV ( $\square$ ), 240 meV ( $\triangle$ ), and 450 meV ( $\circ$ ). The solid line is a SWT fit based on Eq. (1). (b) Measured  $\chi''(\mathbf{q}, \omega)$ . Dashed circle highlights the anomalous scattering near  $(1/2, 0)$ . An  $\hbar\omega$ -dependent background determined near  $(1, 0)$  has been subtracted. (c) One-magnon intensity. Line is a fit to SWT with renormalization factor  $Z_d = 0.4 \pm 0.04$ . (d) One-magnon intensity divided by SWT prediction. (e) SWT dispersion (color indicates SW intensity).

# Appendix

# FLAT CONE



# FC scan modes



- essential for mapping  $\mathbf{Q}, E$  space:  
*sweeps a plane in reciprocal space at  $\Delta E = \text{const}$*