



EUROPEAN
SPALLATION
SOURCE

Neutron Instrumentation

Oxford School on Neutron Scattering

5th September 2019

Ken Andersen

Summary

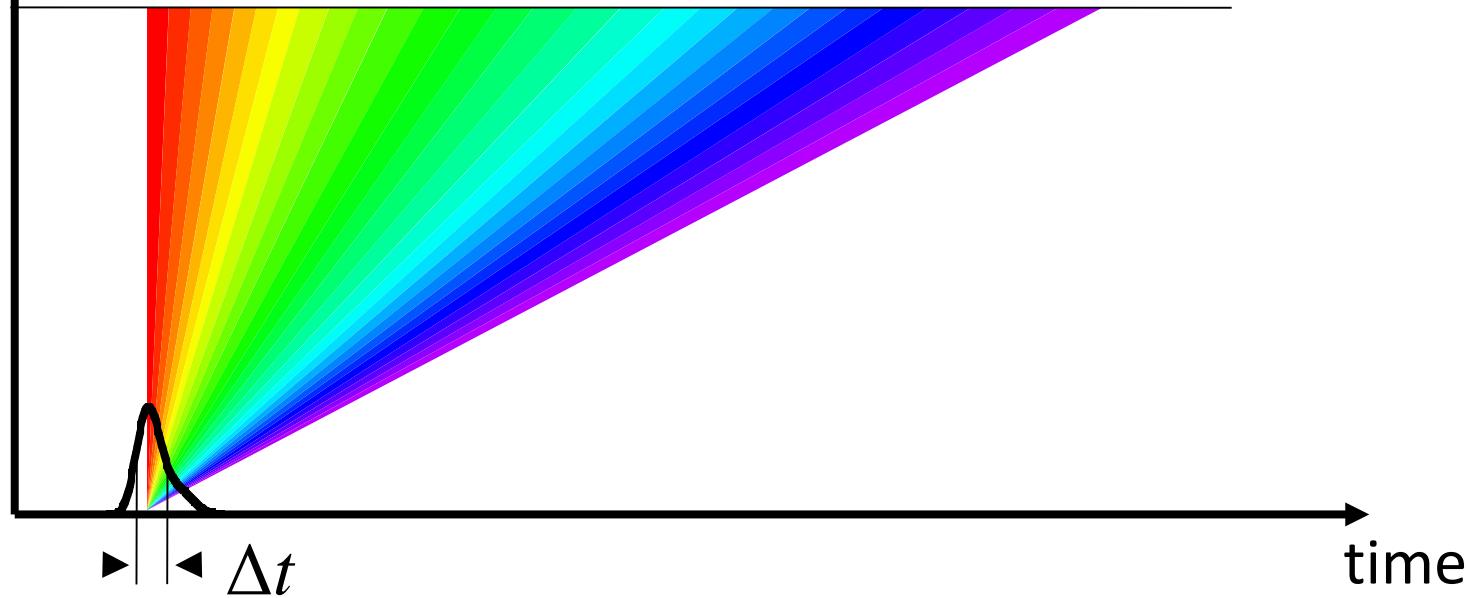
- Neutron instrument concepts
 - time-of-flight
 - Bragg's law
- Neutron Instrumentation
 - guides
 - monochromators
 - shielding
 - detectors
 - choppers
 - sample environment
 - collimation
- Neutron diffractometers
- Neutron spectrometers

The time-of-flight (TOF) method

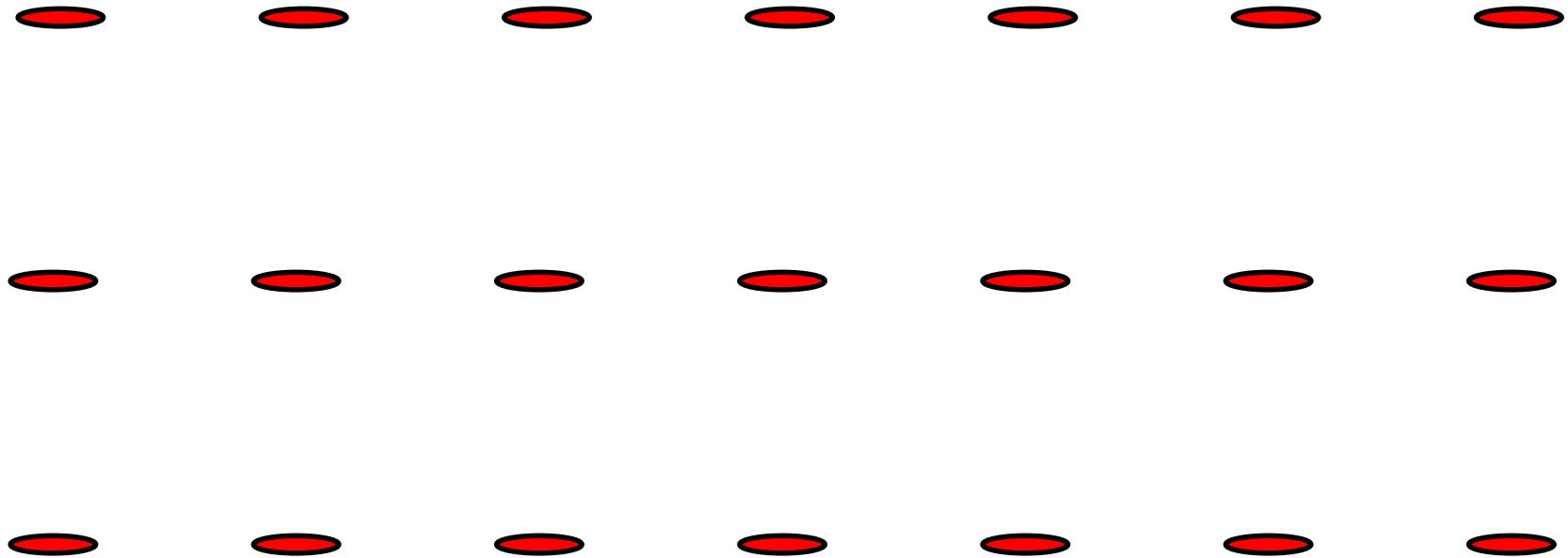
distance

$$t[\text{ms}] = L[\text{m}] \times \lambda[\text{\AA}] / 3.956$$

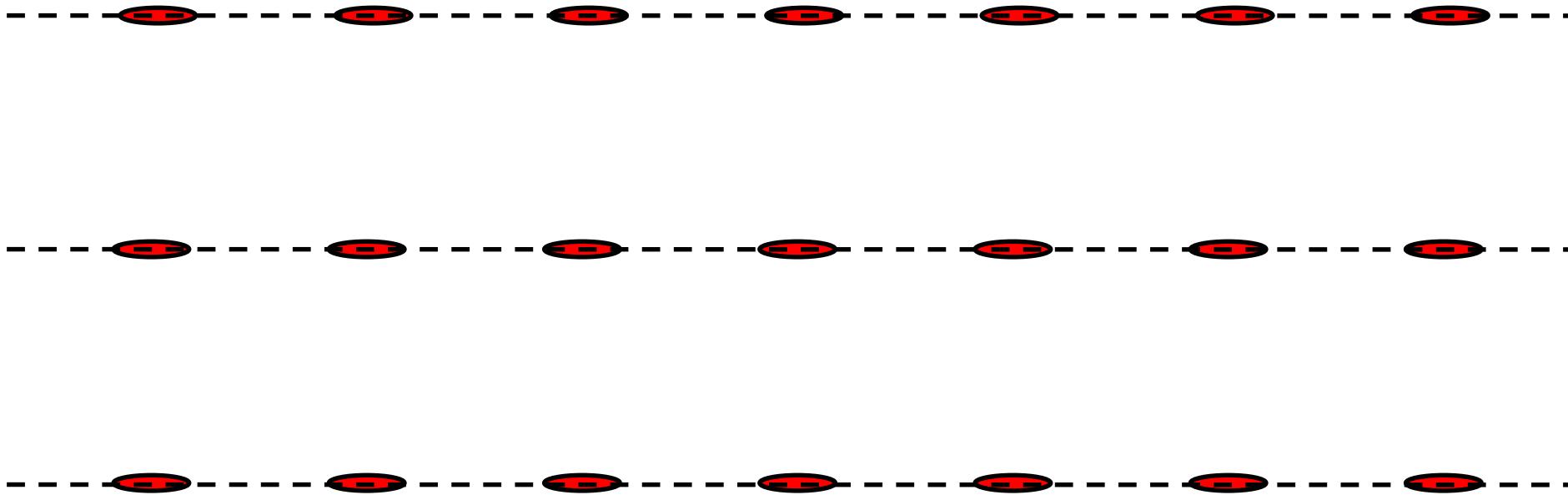
$$t[\mu\text{s}] = L[\text{m}] \times \lambda[\text{\AA}] \times 252.8$$



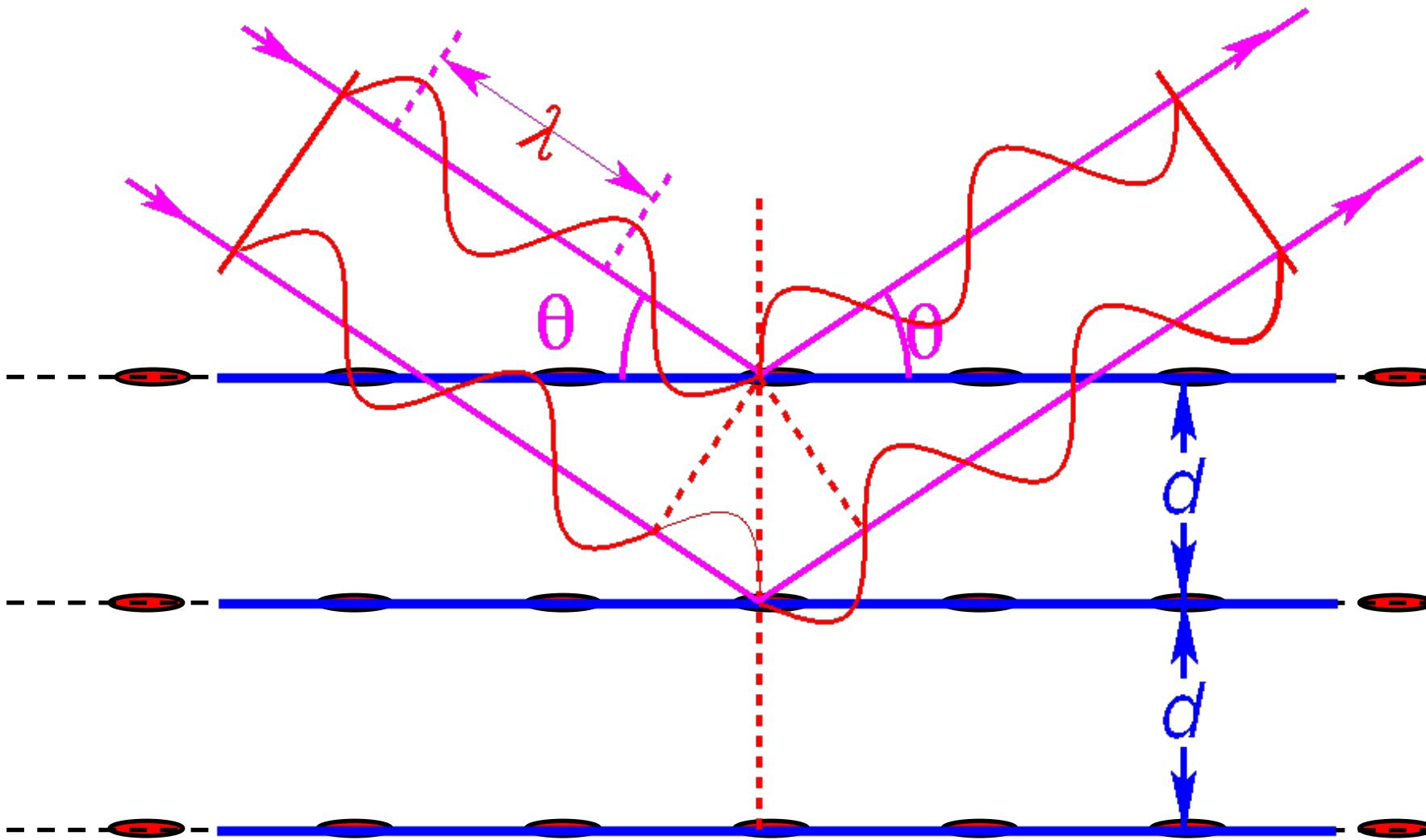
Diffraction: Bragg's Law



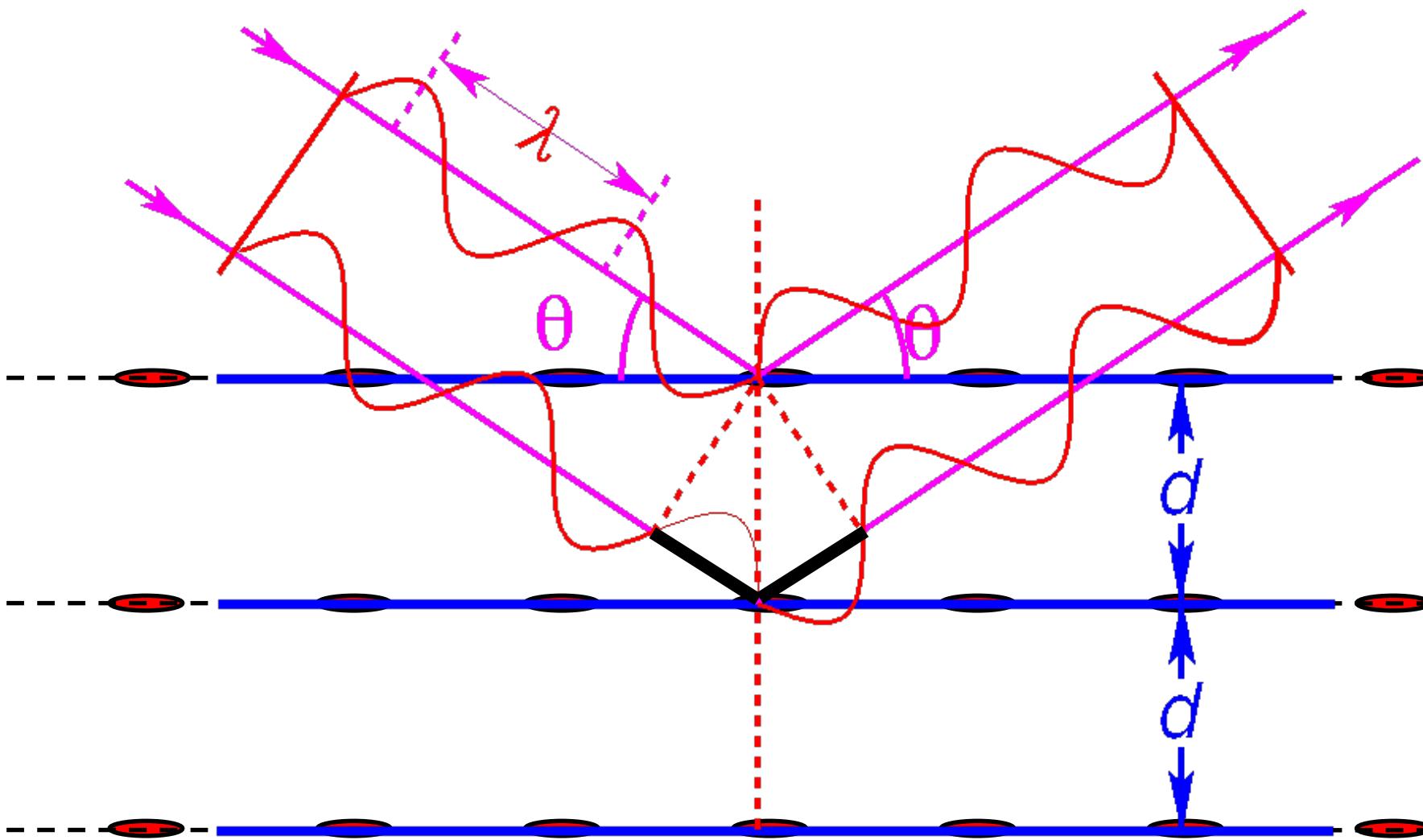
Diffraction: Bragg's Law



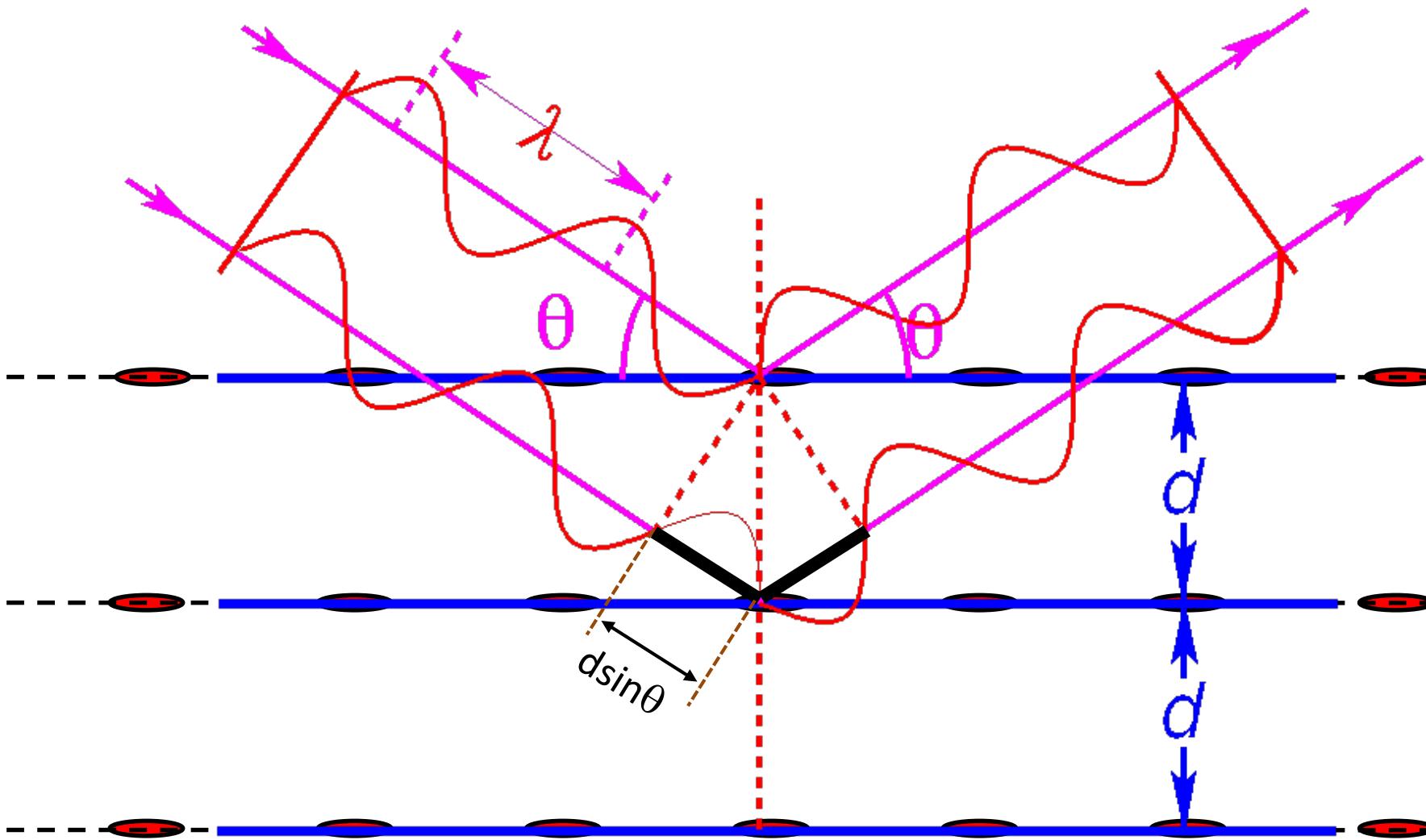
Diffraction: Bragg's Law



Diffraction: Bragg's Law

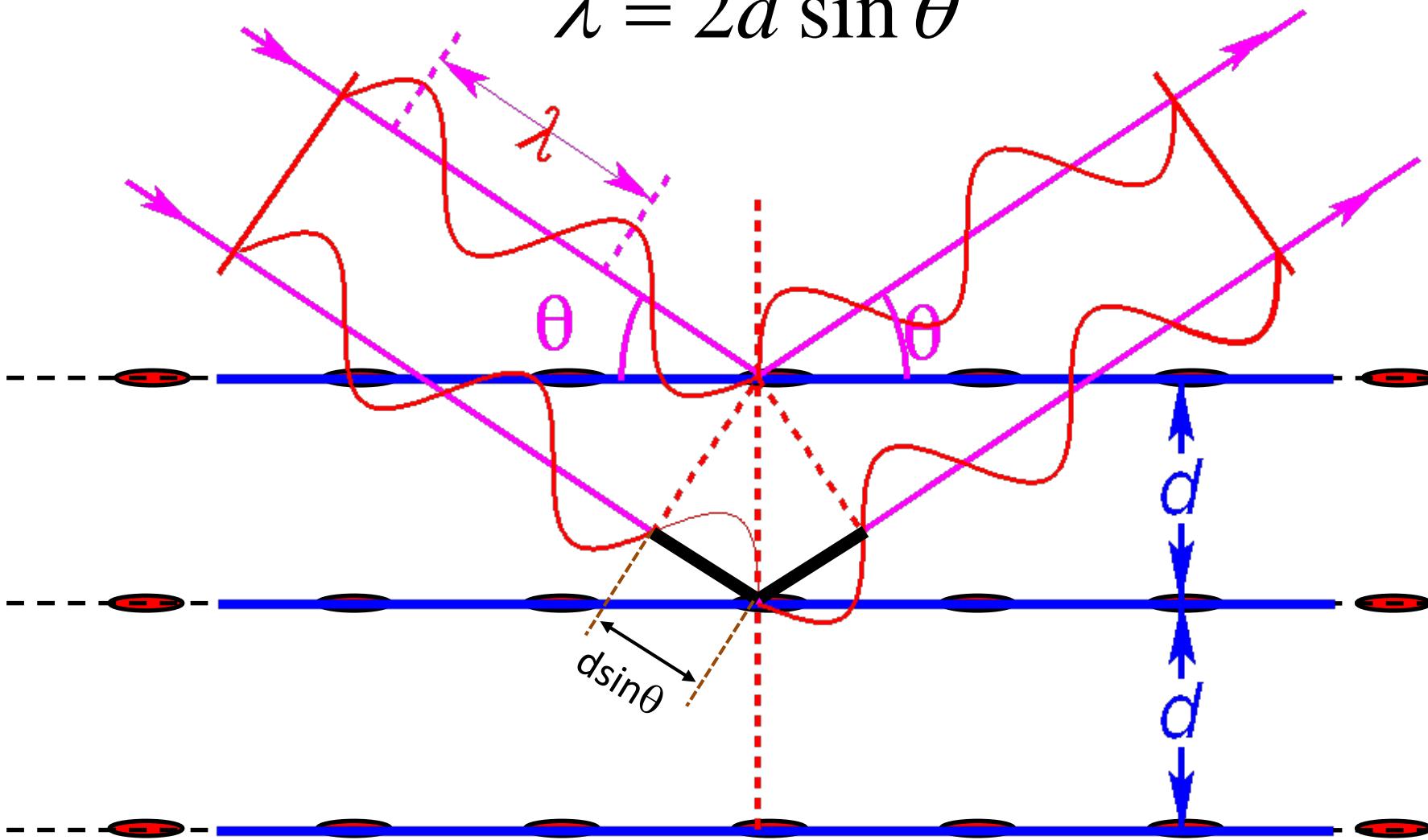


Diffraction: Bragg's Law



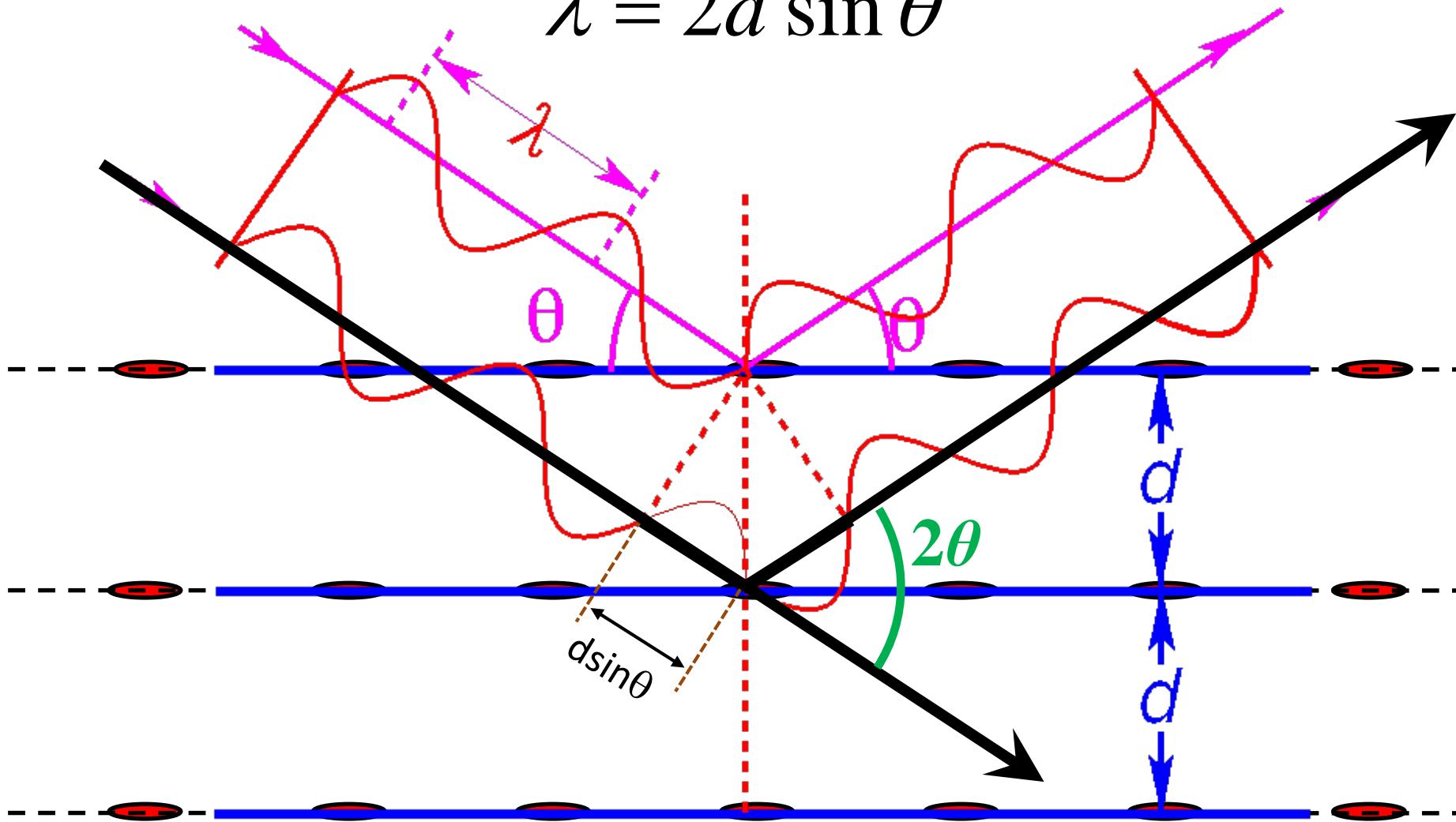
Diffraction: Bragg's Law

$$\lambda = 2d \sin \theta$$

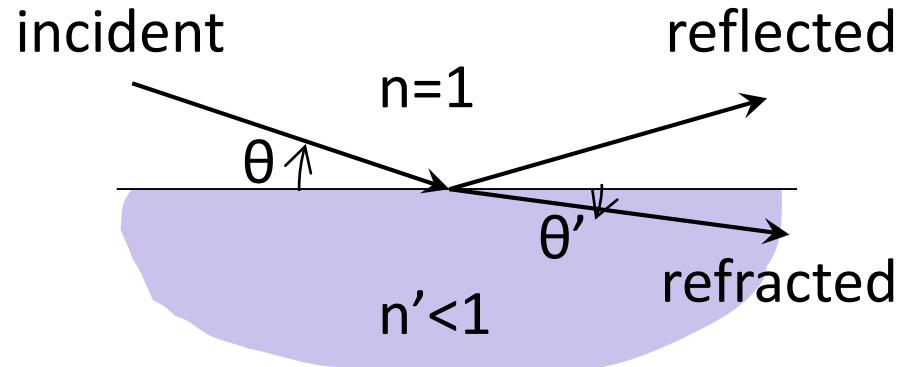


Diffraction: Bragg's Law

$$\lambda = 2d \sin \theta$$

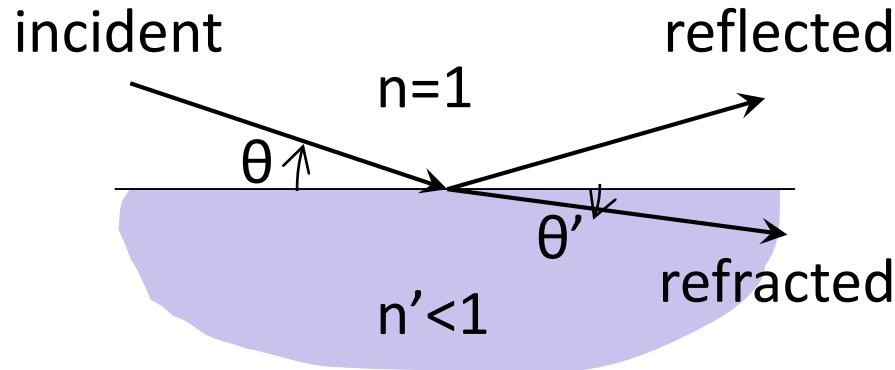


Reflection: Snell's Law



$$\frac{\cos \theta}{\cos \theta'} = \frac{v_1}{v_2} = \frac{n'}{n} = n'$$

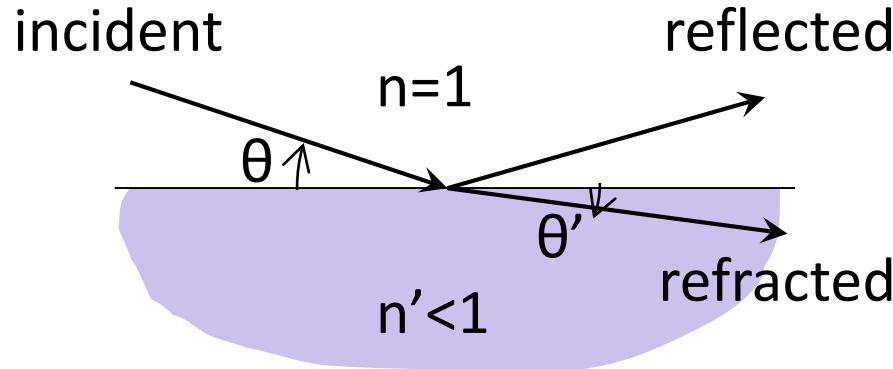
Reflection: Snell's Law



$$\frac{\cos \theta}{\cos \theta'} = \frac{v_1}{v_2} = \frac{n'}{n} = n'$$

$\theta' = 0$: critical angle of total reflection θ_c

Reflection: Snell's Law

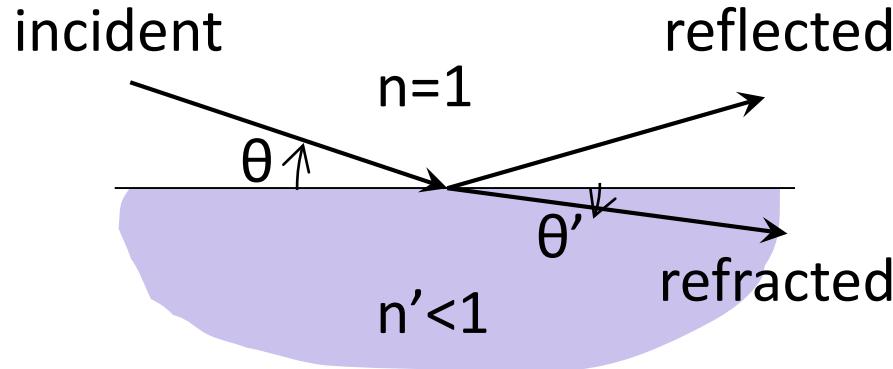


$$\frac{\cos \theta}{\cos \theta'} = \frac{v_1}{v_2} = \frac{n'}{n} = n'$$

$\theta' = 0$: critical angle of total reflection θ_c

$$\left. \begin{aligned} \cos \theta_c &= n'/n = n' \\ n' &= 1 - \frac{N\lambda^2 b}{2\pi} \\ \cos \theta_c &\approx 1 - \theta_c^2/2 \end{aligned} \right\} \Rightarrow \theta_c = \lambda \sqrt{Nb/\pi}$$

Reflection: Snell's Law



$$\frac{\cos \theta}{\cos \theta'} = \frac{v_1}{v_2} = \frac{n'}{n}$$

$\theta' = 0$: critical angle of total reflection θ_c

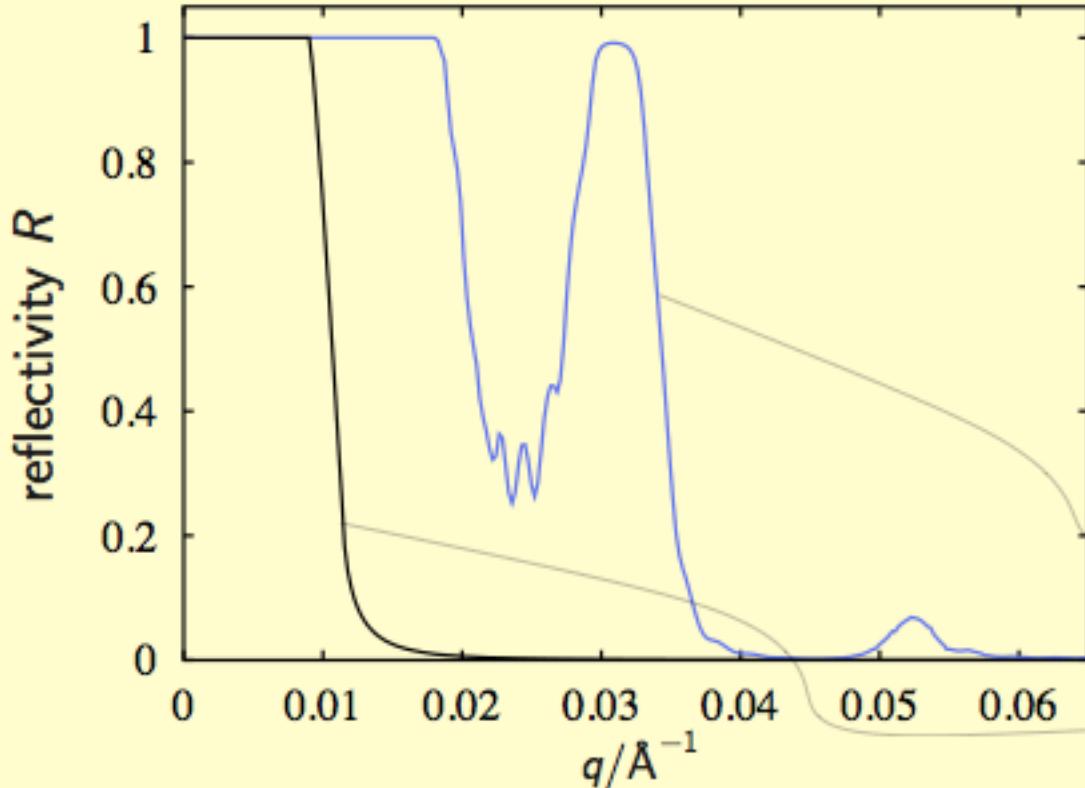
$$\left. \begin{aligned} \cos \theta_c &= n'/n = n' \\ n' &= 1 - \frac{N\lambda^2 b}{2\pi} \\ \cos \theta_c &\approx 1 - \theta_c^2/2 \end{aligned} \right\} \Rightarrow \theta_c = \lambda \sqrt{Nb/\pi}$$

for natural Ni,

$$\theta_c = \lambda [\text{\AA}] \times 0.1^\circ$$

$$Q_c = 0.0218 \text{ \AA}^{-1}$$

Neutron Supermirrors

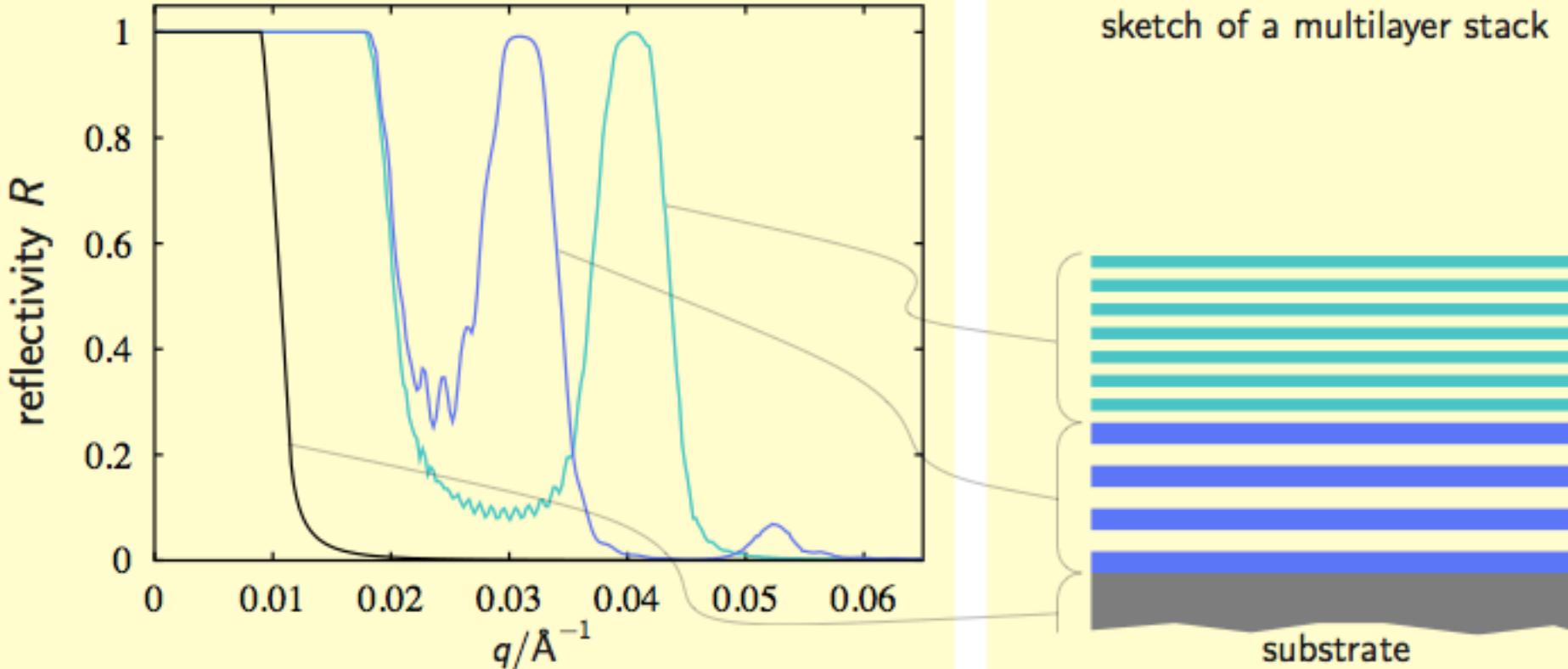


sketch of a multilayer



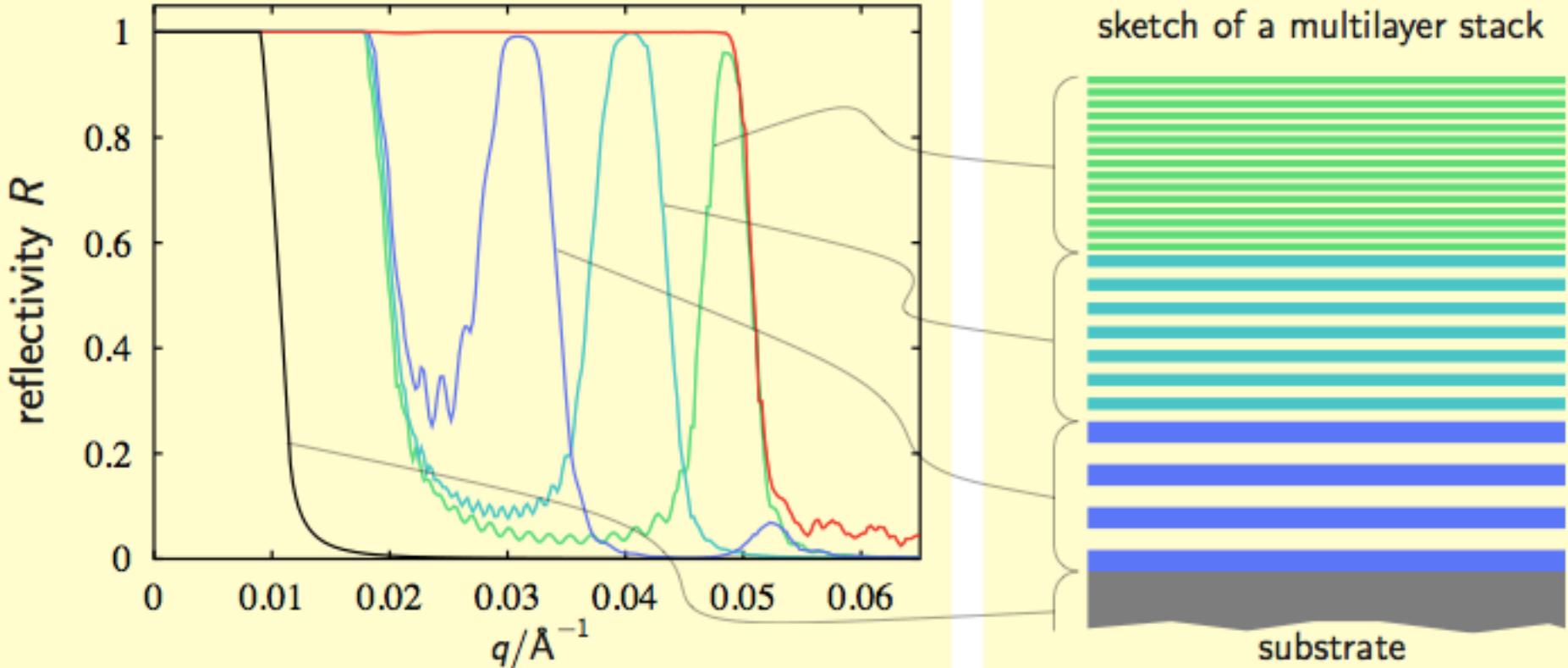
Courtesy of J. Stahn, PSI

Neutron Supermirrors



Courtesy of J. Stahn, PSI

Neutron Supermirrors

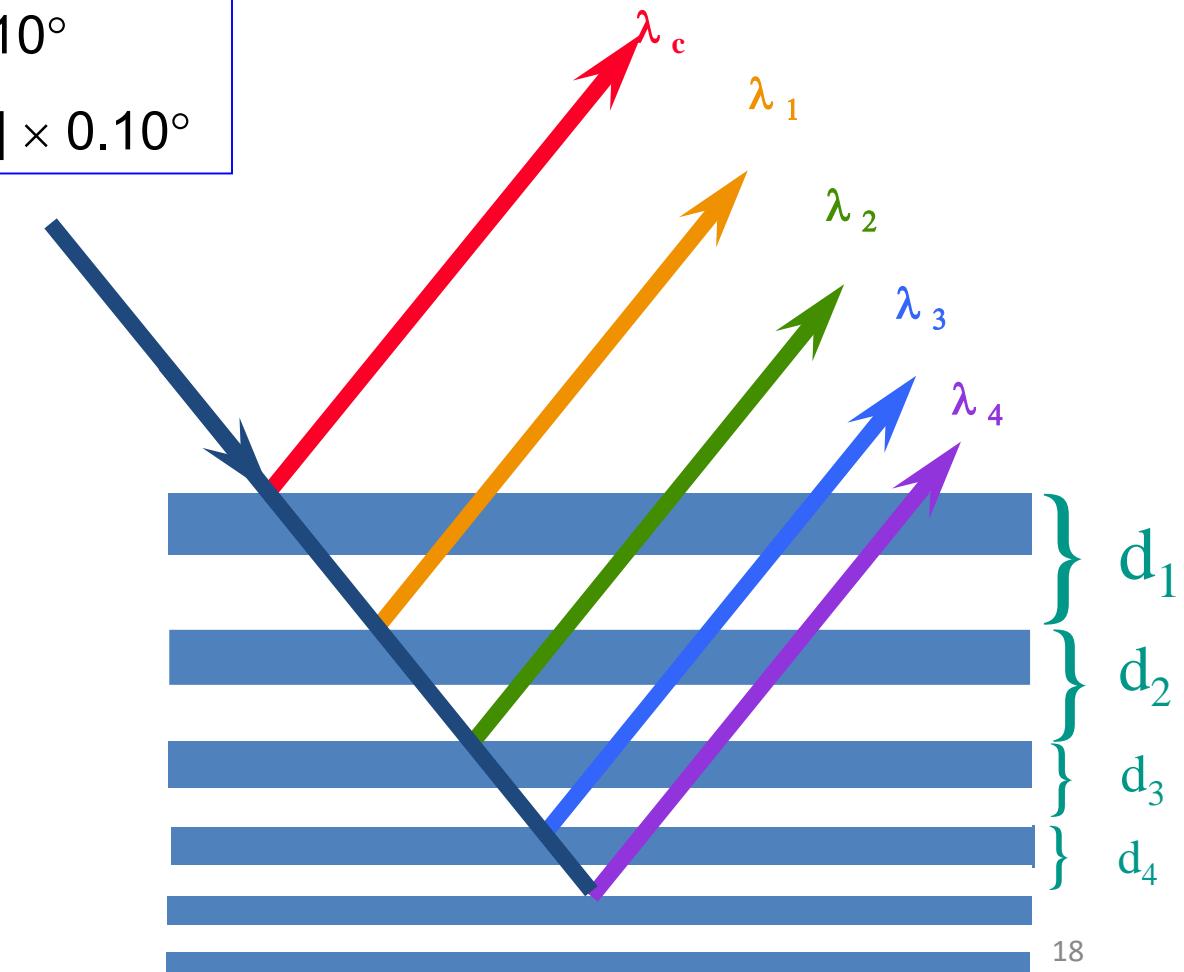


Courtesy of J. Stahn, PSI

Neutron Supermirrors

Reflection: $\theta_c(\text{Ni}) = \lambda[\text{\AA}] \times 0.10^\circ$

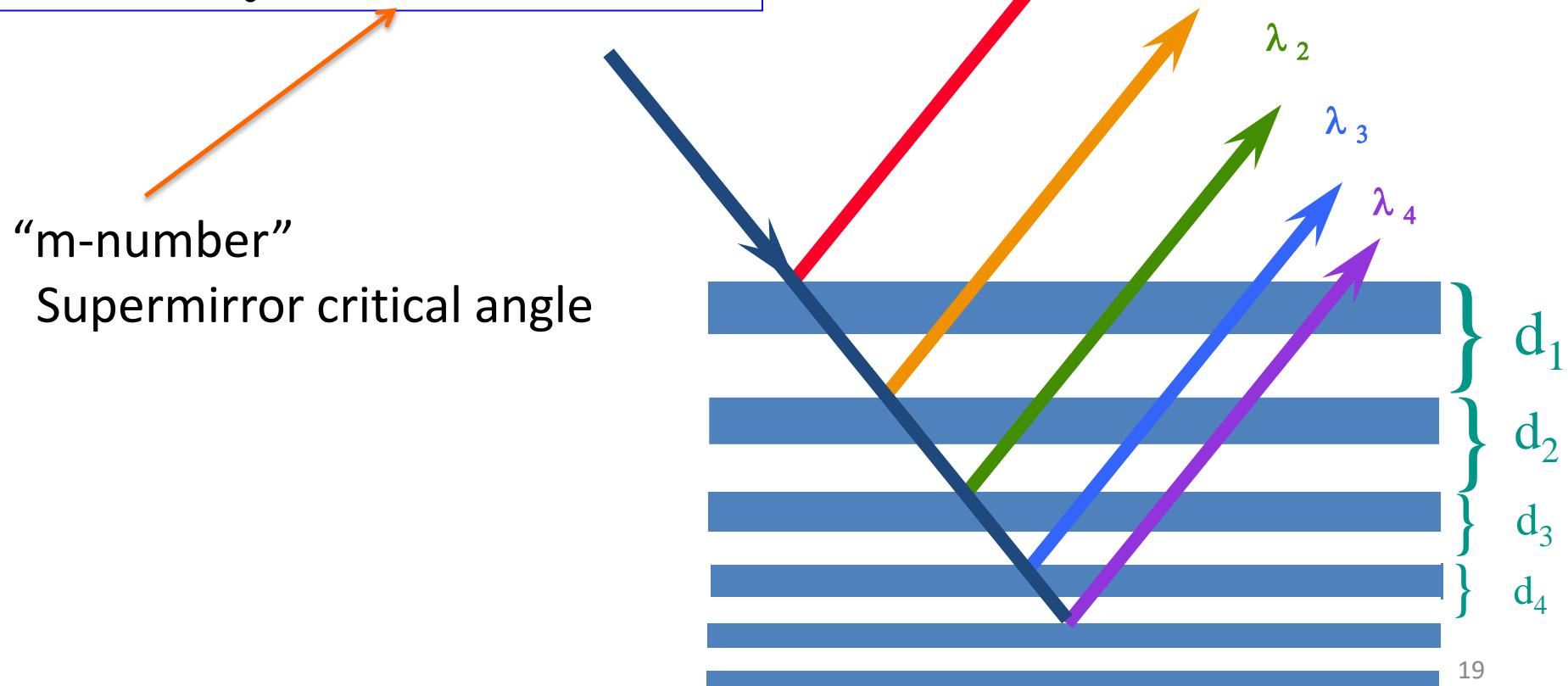
Multilayer: $\theta_c(\text{SM}) = m \times \lambda[\text{\AA}] \times 0.10^\circ$



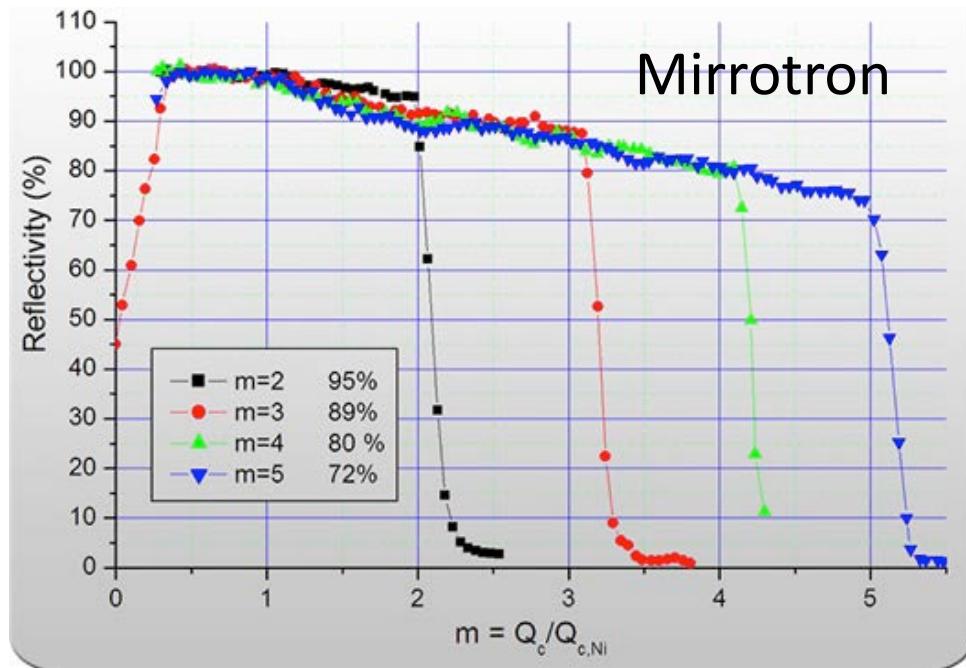
Neutron Supermirrors

Reflection: $\theta_c(\text{Ni}) = \lambda[\text{\AA}] \times 0.10^\circ$

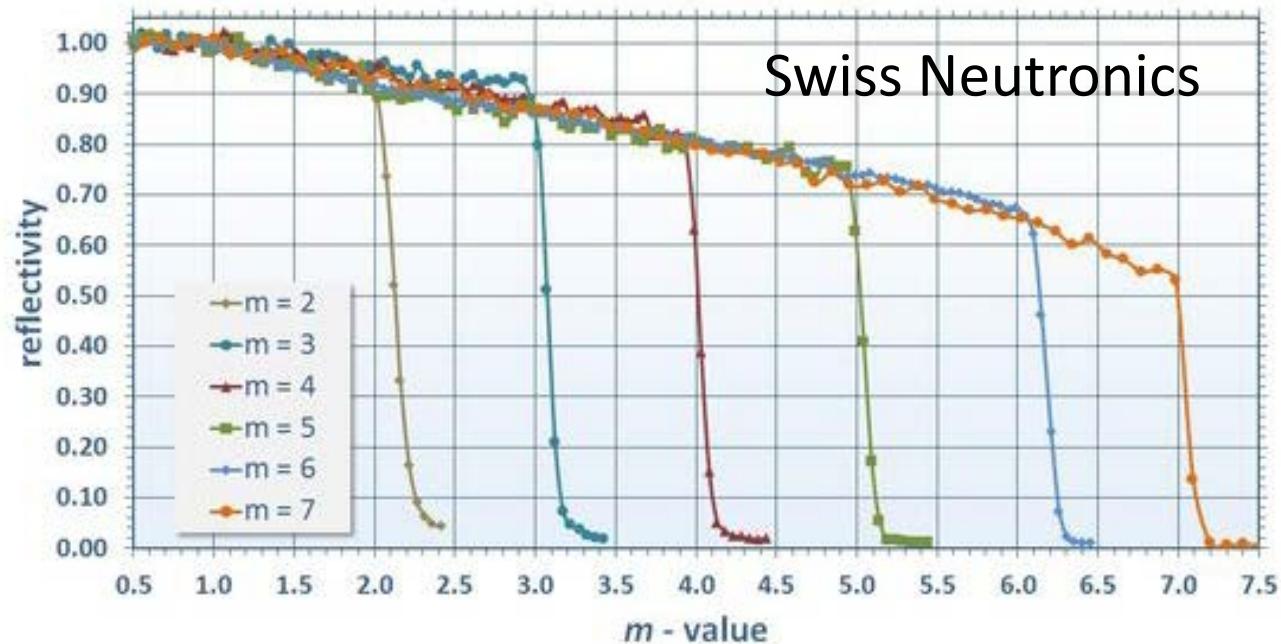
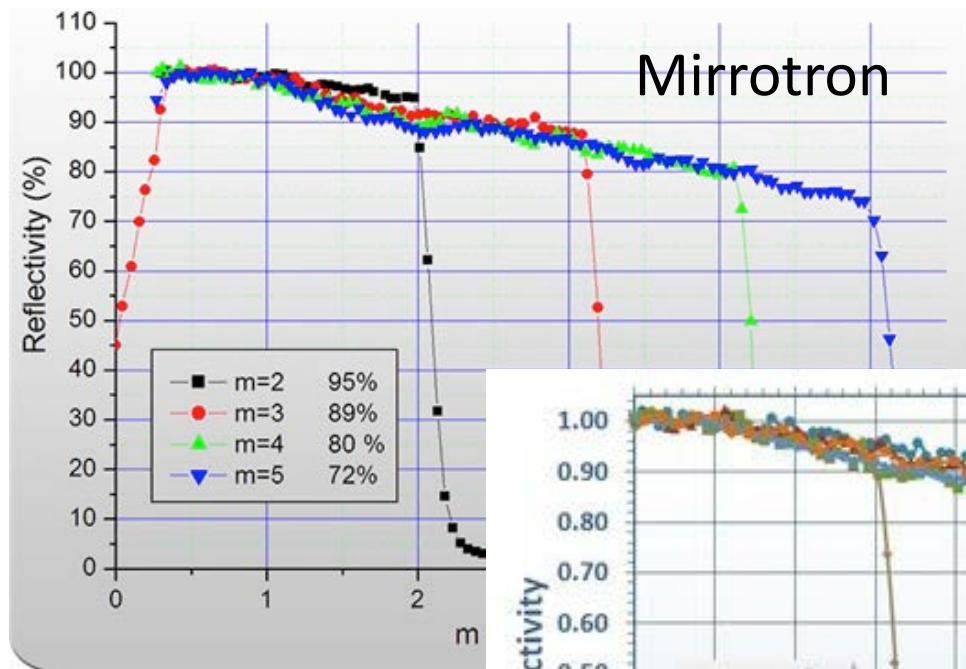
Multilayer: $\theta_c(\text{SM}) = m \times \lambda[\text{\AA}] \times 0.10^\circ$



State-of-the-art Supermirrors



State-of-the-art Supermirrors



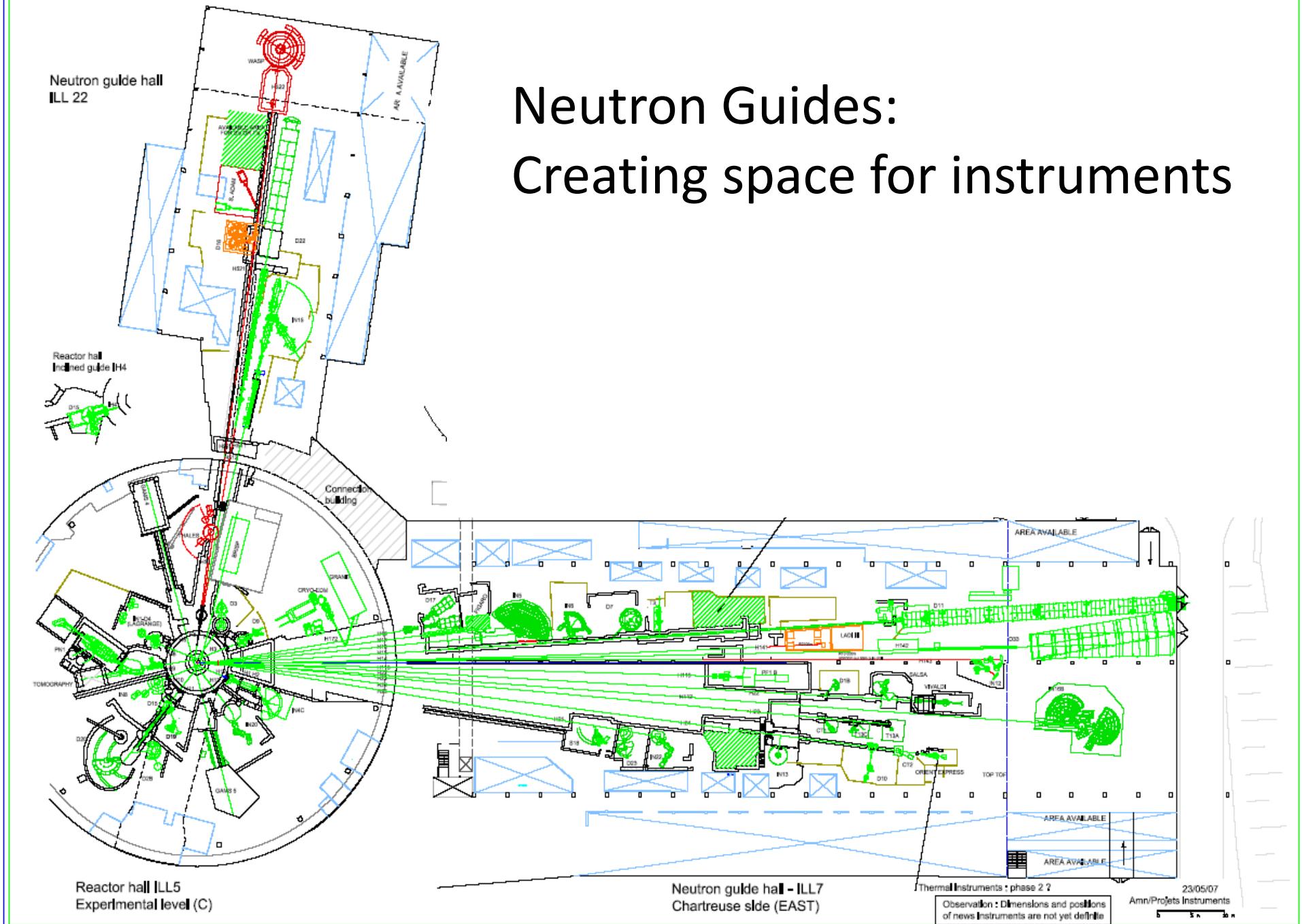
Neutron guides



Swiss Neutronics guides for NIST



Neutron Guides: Creating space for instruments



Background Reduction

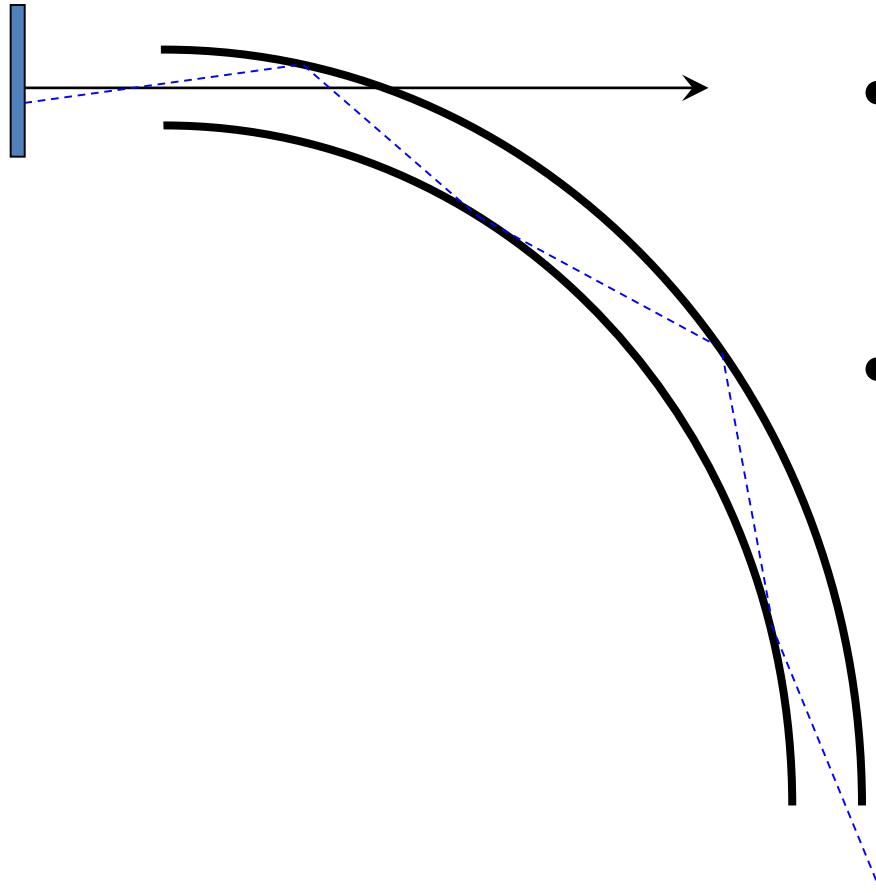


Guides can be used to reduce background

- Distance:
 - move away from fast-neutron source $\sim 1/R^2$

Background Reduction

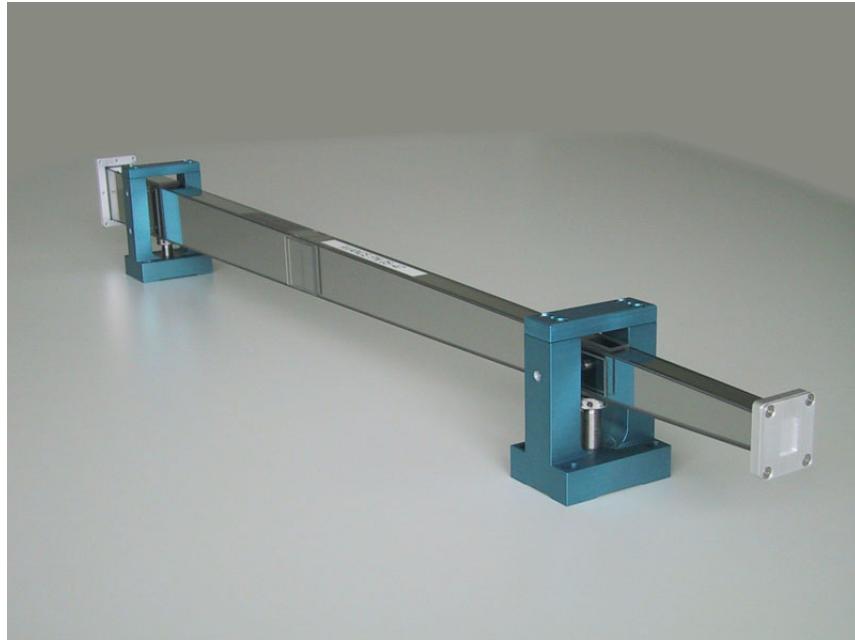
Guides can be used to reduce background



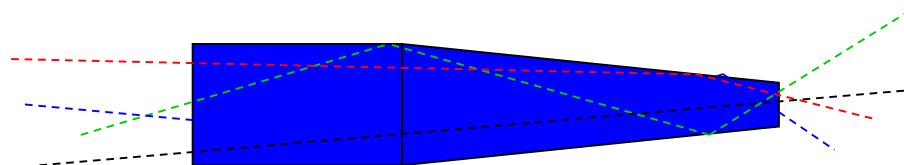
- Distance:
 - move away from fast-neutron source $\sim 1/R^2$
- Curved Guides:
 - avoid direct line-of-sight
 - avoid gammas
 - avoid fast neutrons

Focusing

Guides can also be used to increase flux



Converging guide increases flux,
but increases divergence



Shielding

- Shielding functions:
 - allow safe operation
 - keep background down
 - reduce activation
- Radiation components:
 - Slow neutrons
 - Fast neutrons
 - Gammas

Shielding: radiation units and numbers

Unit	Description
Curies	Decay rate: 3.7×10^{10} Bq (decays/s)
Gray	Energy dose: J/kg
Sievert	Biological effect of radiation
Roentgen, rad, rem – legacy units	

Examples	Dose
Dental x-ray	10 μ Sv
Abdominal CAT scan	10 mSv
Airline flight crew members	10 mSv/year
50% probability of death	5 Sv
Neutron experimental halls	< 3 μ Sv/hour \times 2000 hours: < 6 mSv/year

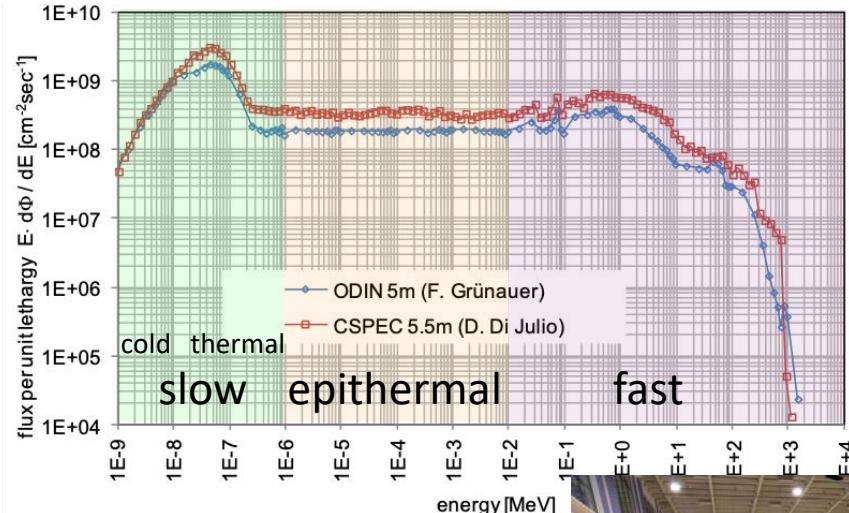
Average Person	Dose
Radon	2 mSv/year
Cosmic	0.28 mSv/year
Terrestrial	0.28 mSv/year
Internal	0.4 mSv/year
Medical x-rays	0.39 mSv/year
Nuclear medical	0.14 mSv/year
Consumer products	0.1 mSv/year
Other	0.03 mSv/year
Total	3.62 mSv/year



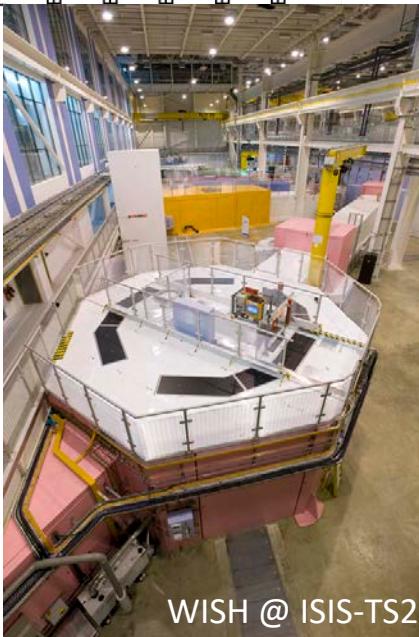
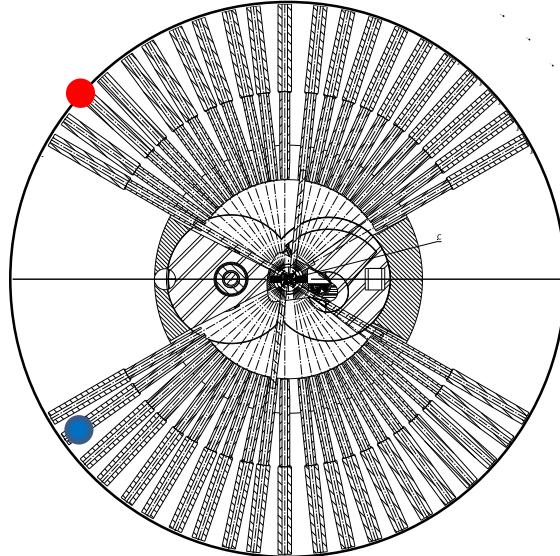
Source: Günter Muhrer, Los Alamos, New Mexico

ISIS-TS2

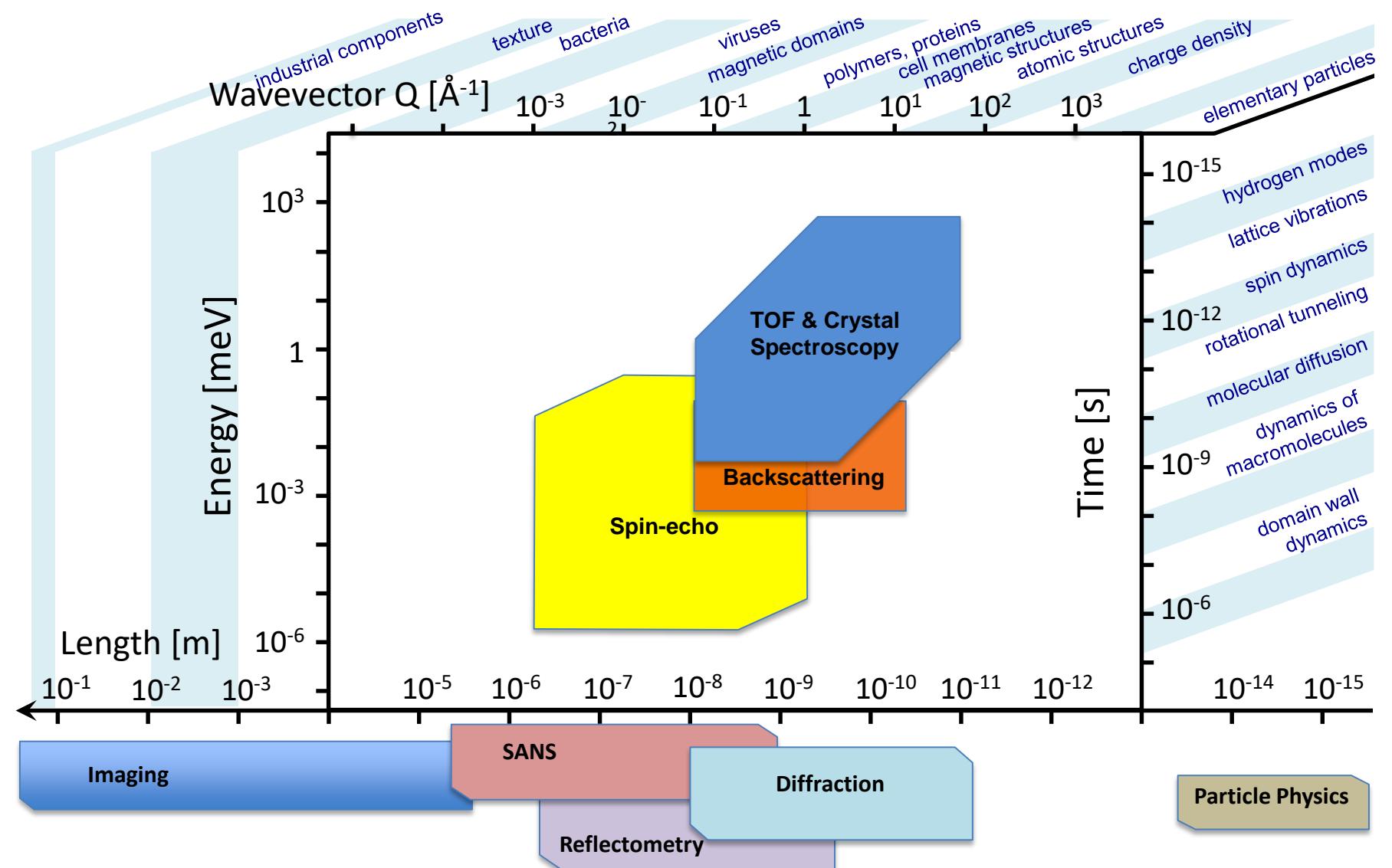
Shielding: slow & fast neutrons

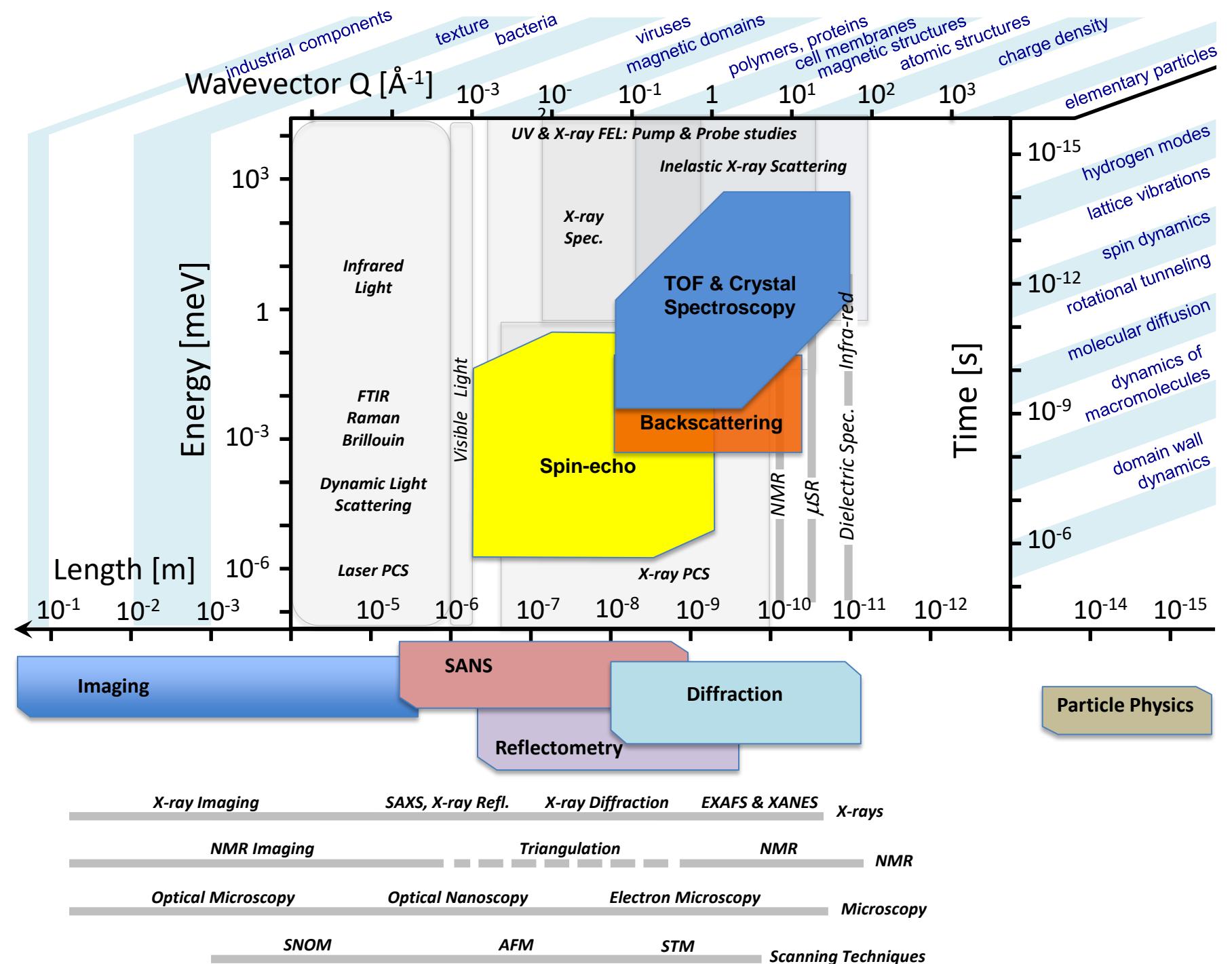


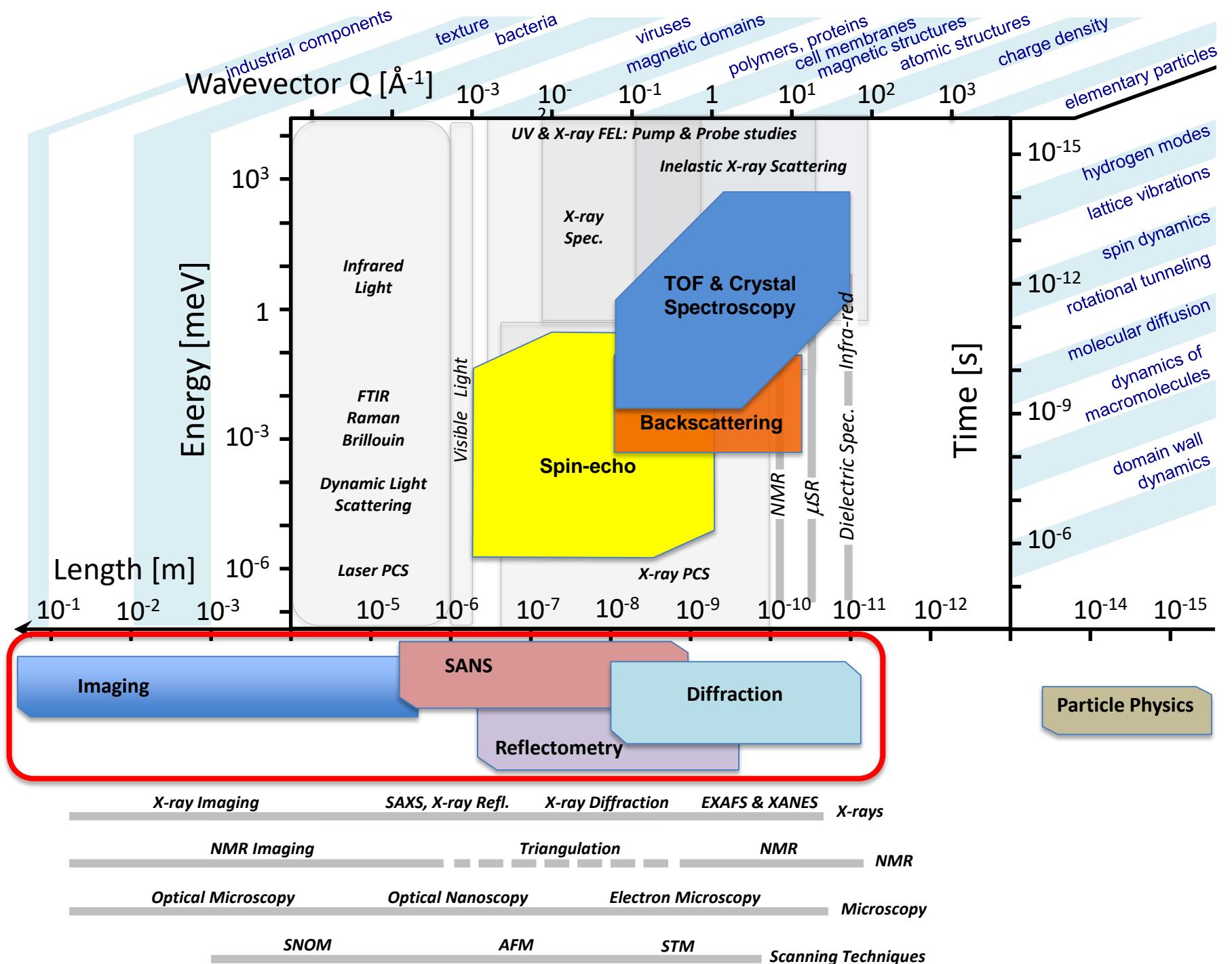
ESS Target Monolith: 11m diameter



- Slow neutrons
 - easy to absorb (few mm B, Cd, Gd, ..)
 - emit gammas when absorbed
 - easily detected
- Fast neutrons
 - can require several m of material for absorption
 - alternatively, thermalise using hydrogenous material (e.g. wax or polyethylene) then absorb
 - both require multiple (10s) of collisions
 - visualise as a gas, filling both solids and air
 - difficult to detect
- Gammas
 - high-energy photons
 - absorbed by any material
 - absorption length scales inversely with density: Pb 11.3 kg/m³, steel 7.9 kg/m³, concrete 2.4 kg/m³

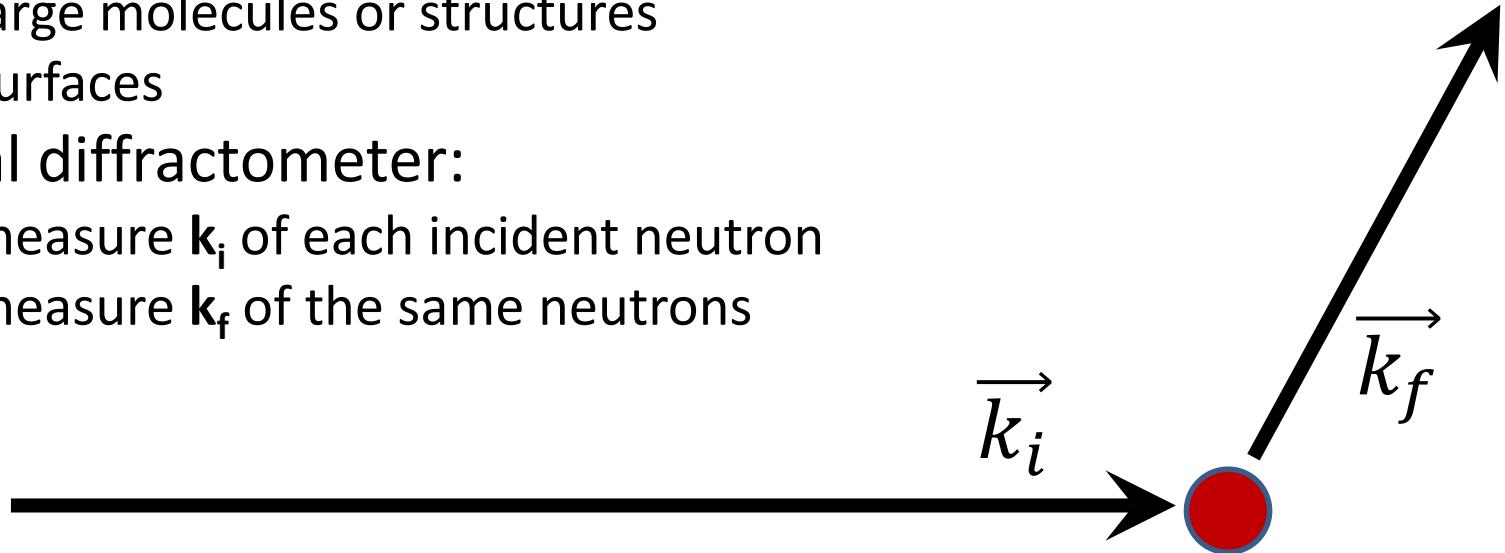






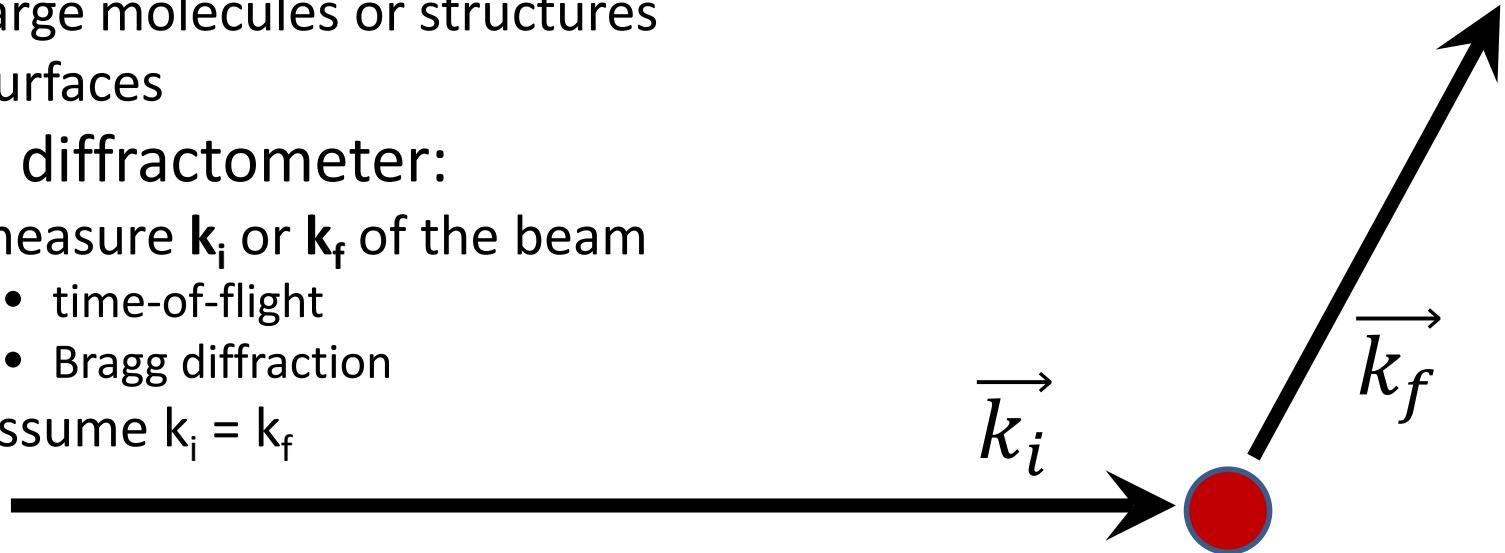
Diffractometers

- Measure structures (d-spacings)
- Very general method:
 - crystals
 - powders
 - polycrystalline materials
 - liquids
 - large molecules or structures
 - surfaces
- Ideal diffractometer:
 - measure \vec{k}_i of each incident neutron
 - measure \vec{k}_f of the same neutrons



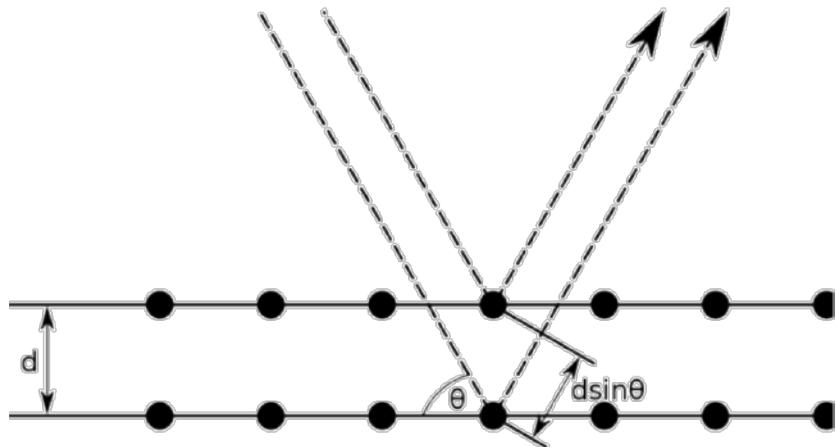
Diffractometers

- Measure structures (d-spacings)
- Very general method:
 - crystals
 - powders
 - polycrystalline materials
 - liquids
 - large molecules or structures
 - surfaces
- Real diffractometer:
 - measure \vec{k}_i or \vec{k}_f of the beam
 - time-of-flight
 - Bragg diffraction
 - assume $\vec{k}_i = \vec{k}_f$

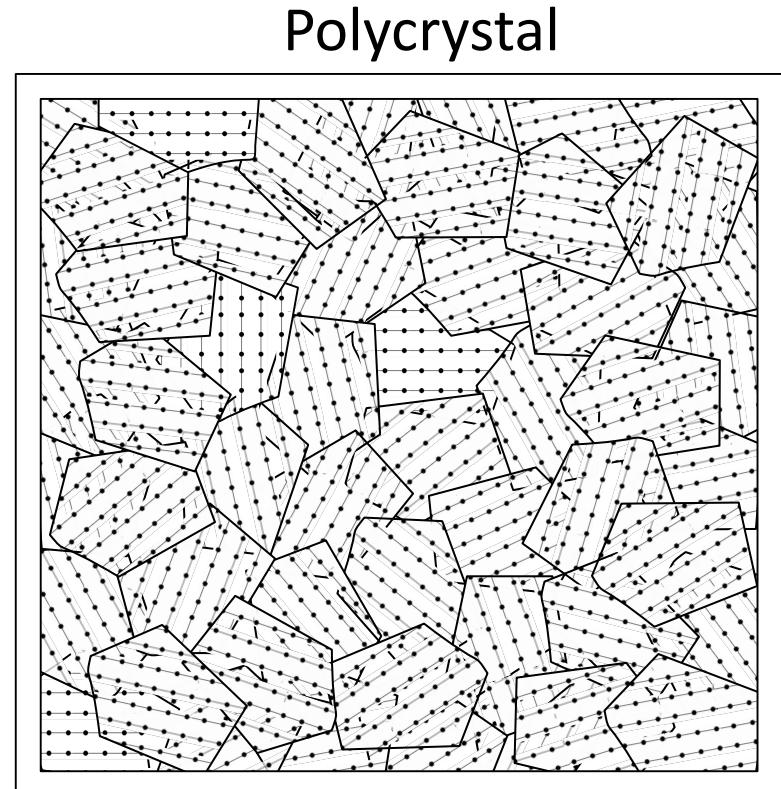


Powder diffractometers

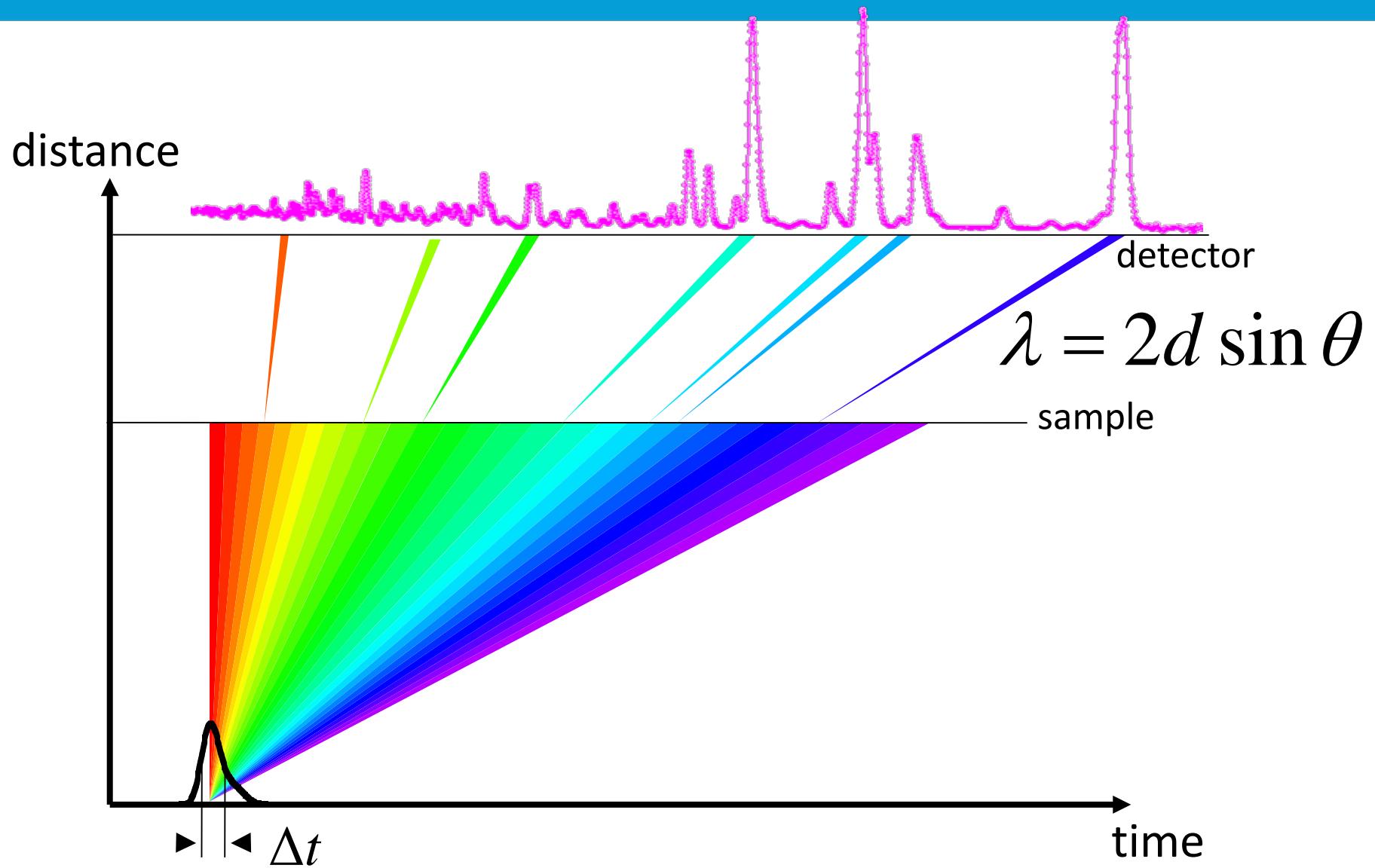
- Measure crystal structure using Bragg's law
 - Rietveld refinement
- Large single crystals are rarely available



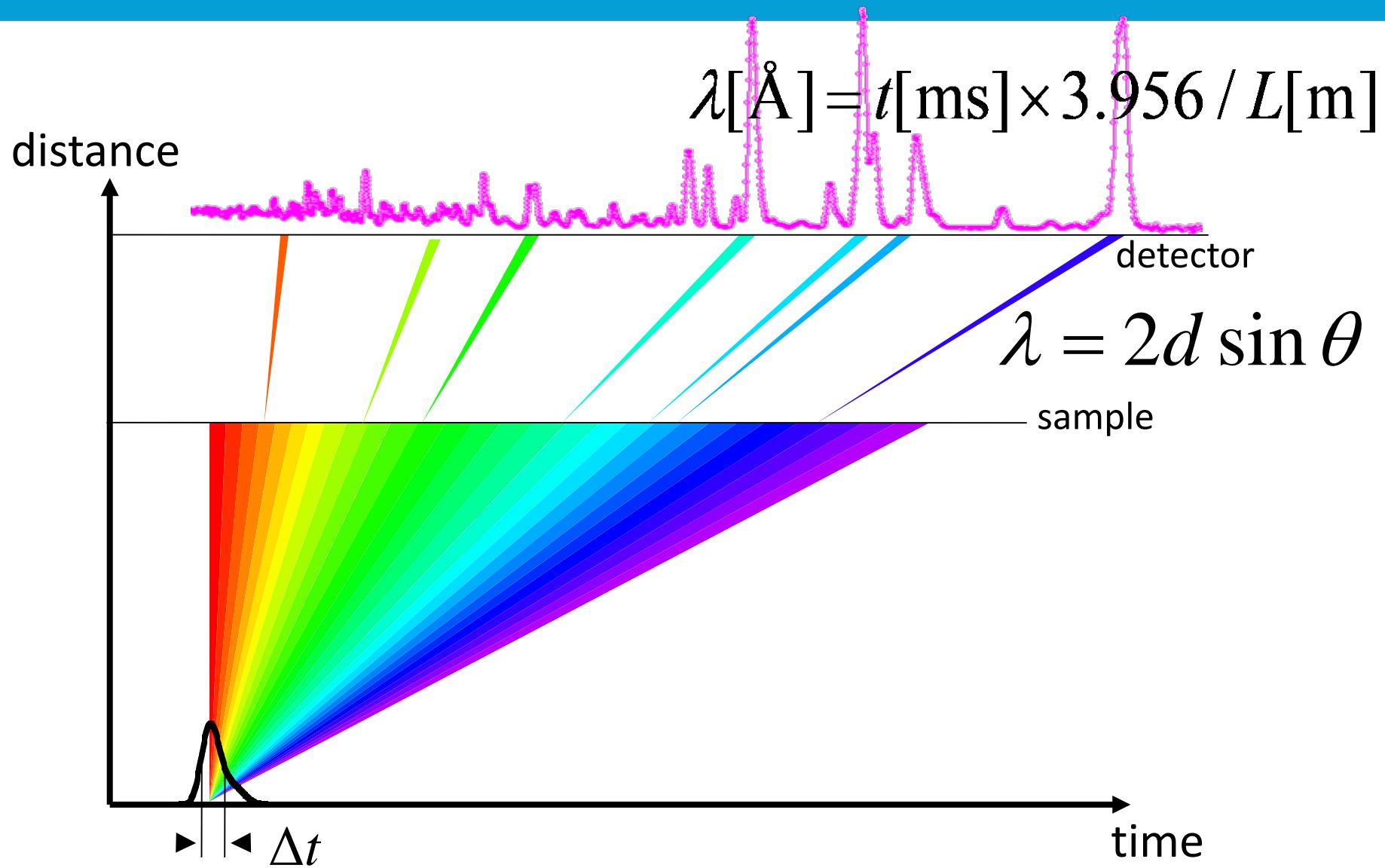
$$Q = \frac{2\pi}{d} \quad \lambda = 2d \sin \theta$$



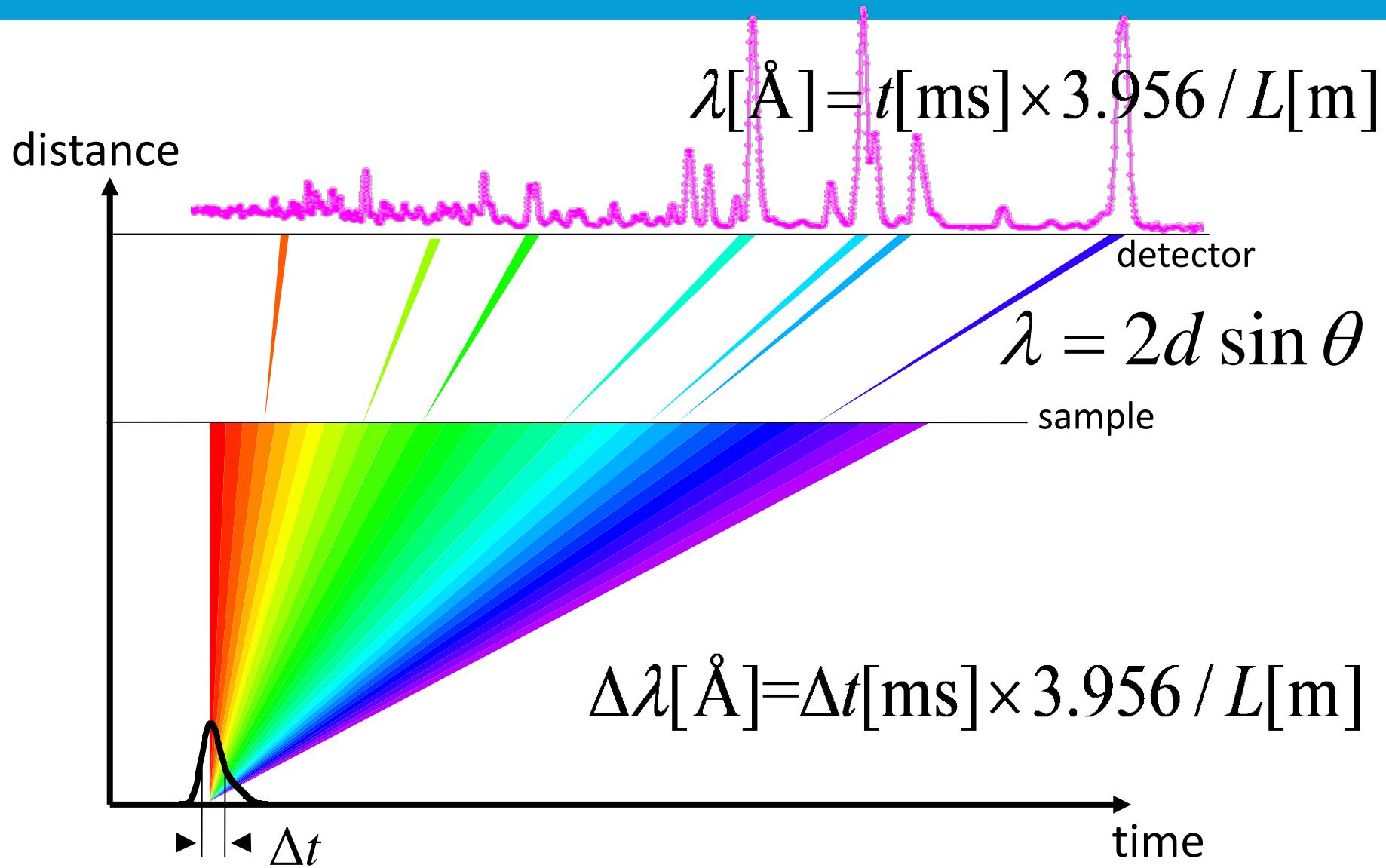
Time-of-flight (TOF) Method



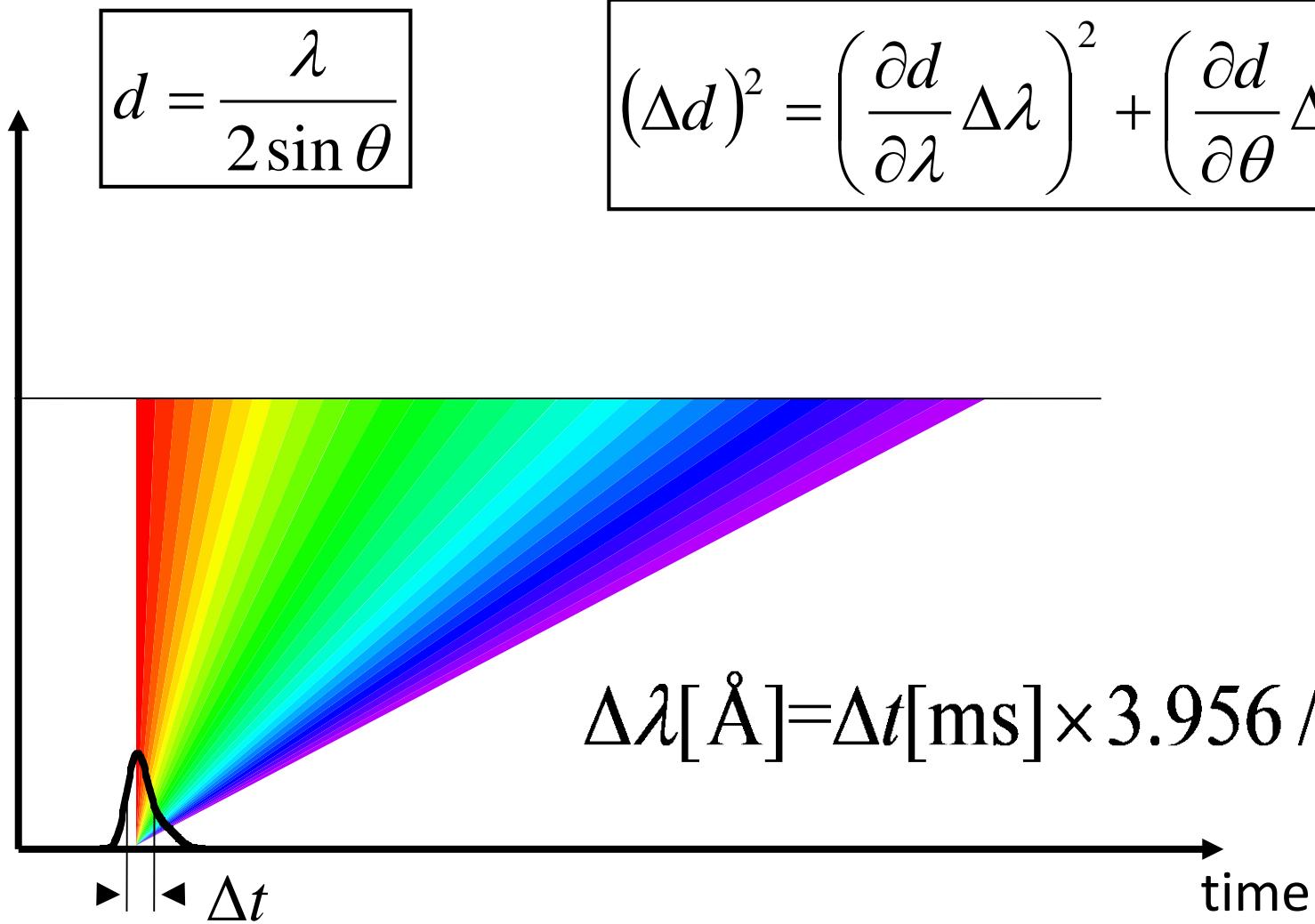
Time-of-flight (TOF) Method



Time-of-flight (TOF) Method



Time-of-flight Resolution



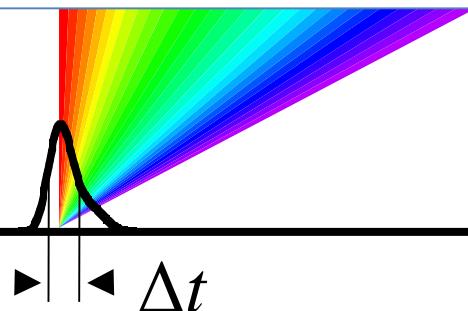
Time-of-flight Resolution

$$d = \frac{\lambda}{2 \sin \theta}$$

$$(\Delta d)^2 = \left(\frac{\partial d}{\partial \lambda} \Delta \lambda \right)^2 + \left(\frac{\partial d}{\partial \theta} \Delta \theta \right)^2$$

To improve the resolution:

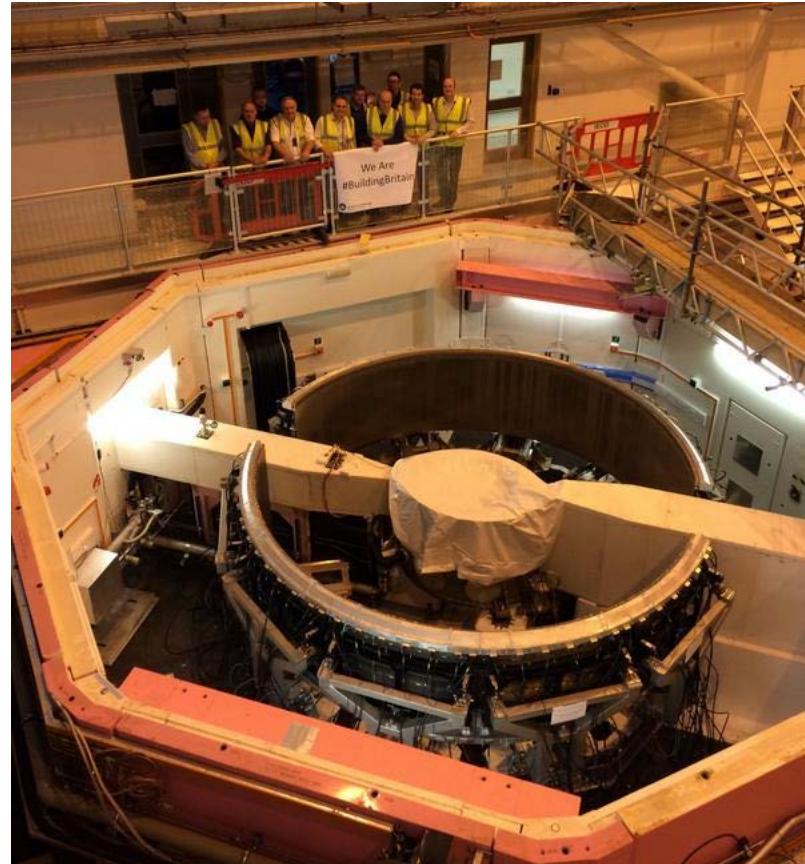
- increase the length: long guide
- move to a sharper moderator
- reduce the beam divergence



$$\Delta \lambda [\text{\AA}] = \Delta t [\text{ms}] \times 3.956 / L [\text{m}]$$

time

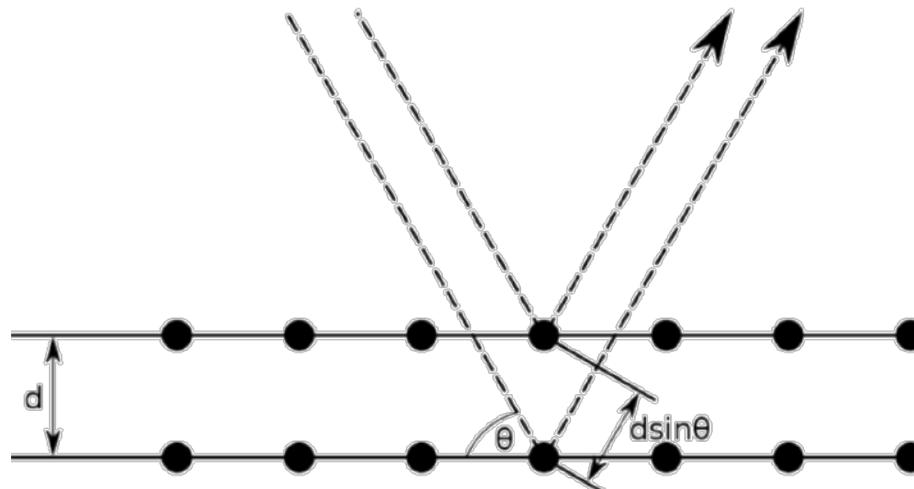
Time-of-flight (TOF) Method



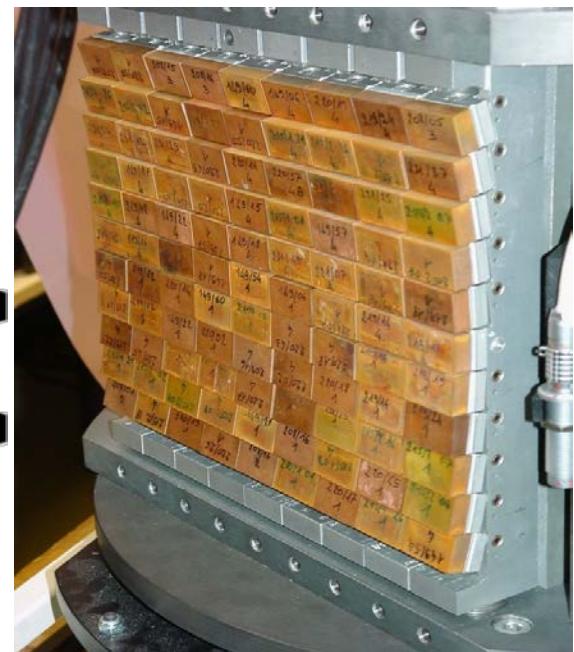
WISH @ ISIS TS2

Crystal Monochromators

Graphite 002

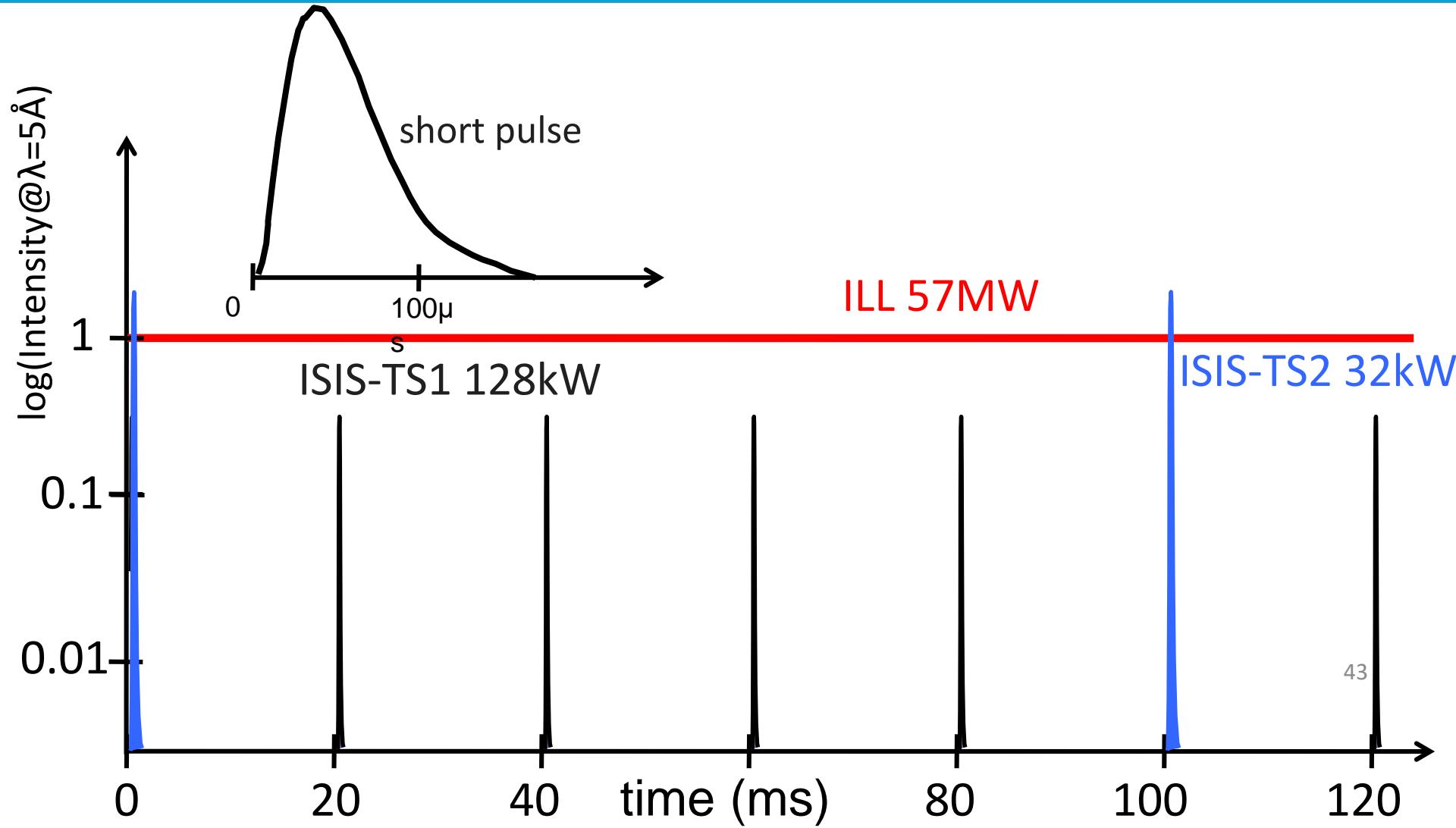


Copper 200

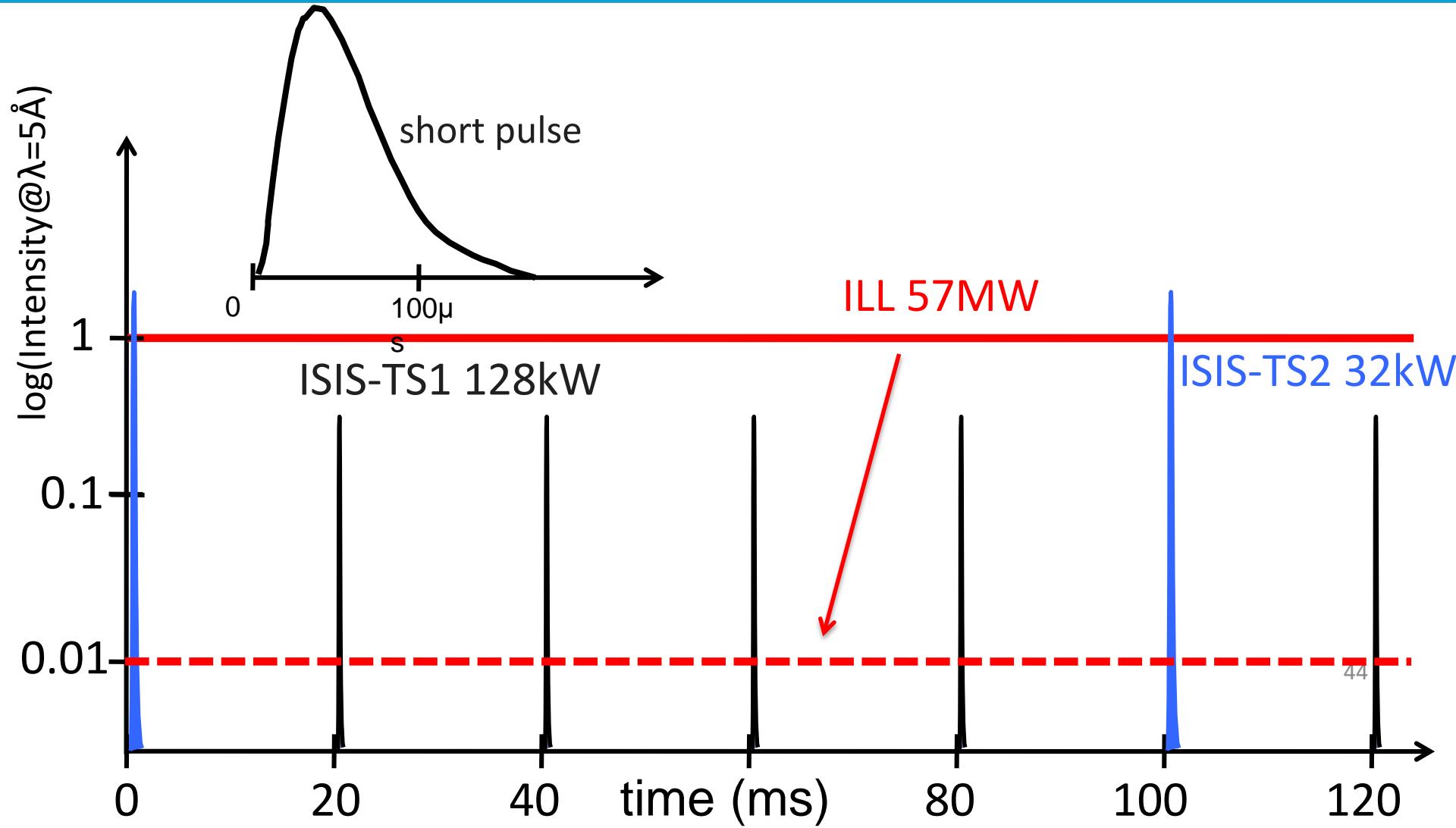


	d-spacing
Germanium 333	1.089 Å
Copper 200	1.807 Å
Silicon 111	3.135 Å
Graphite 002	3.355 Å

Pulsed source time structures ($\lambda=5\text{\AA}$)

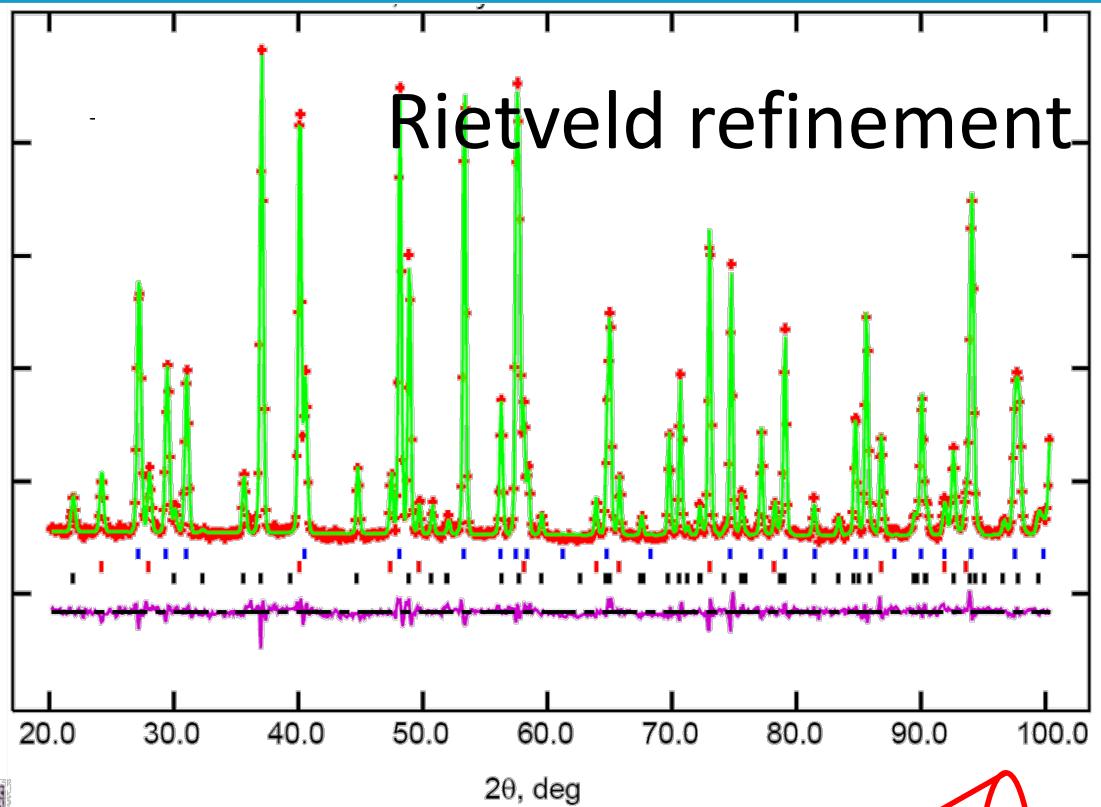
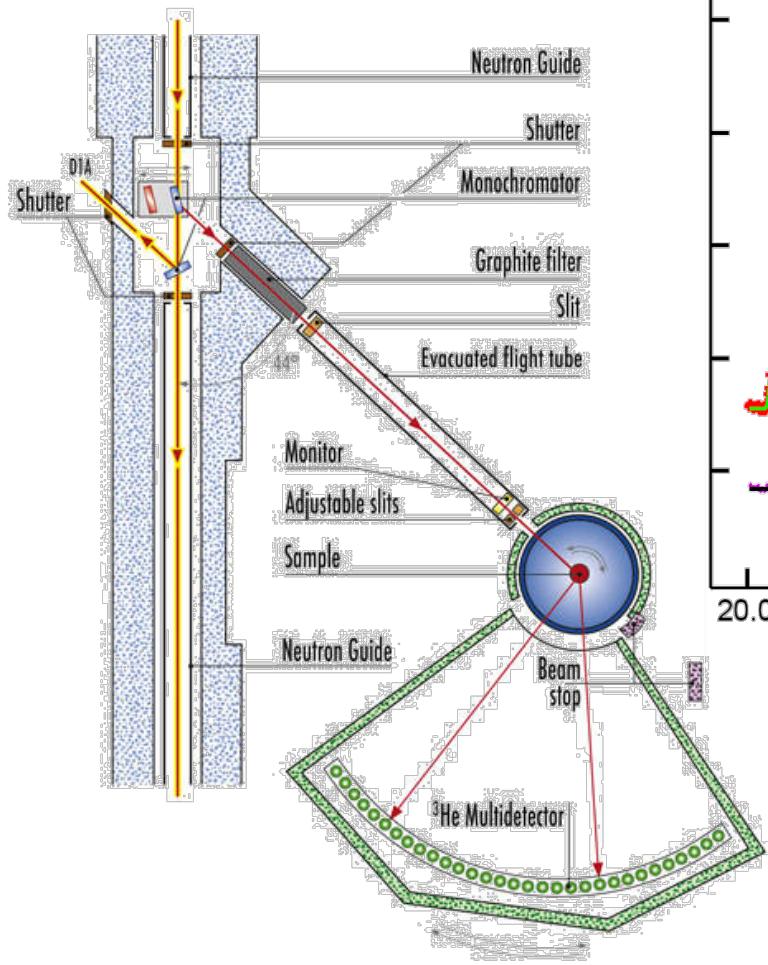


Pulsed source time structures ($\lambda=5\text{\AA}$)

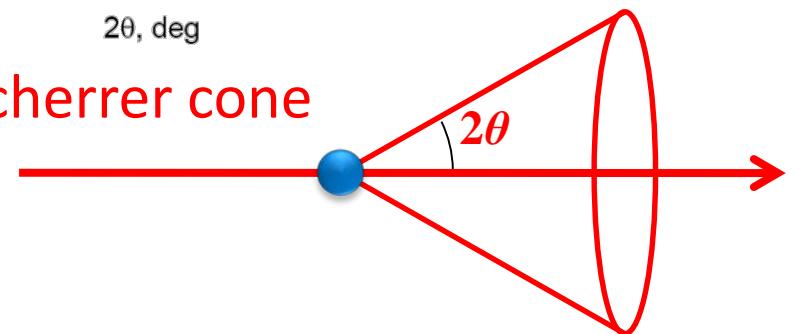


Constant-Wavelength Diffraction

D1B @ ILL



Debye-Scherrer cone



The Diffractometer Family

- Powder diffraction
 - chemical crystallography
 - disordered materials
 - engineering: strain scanning
- Single-crystal diffraction
 - magnetic ordering
 - diffuse scattering
 - large unit cells – protein crystallography
- Small Angle Neutron Scattering (SANS)
 - soft matter – macromolecules in solution
 - nanomaterials
- Reflectometry
 - surfaces and interfaces
 - both planar and in-plane structures

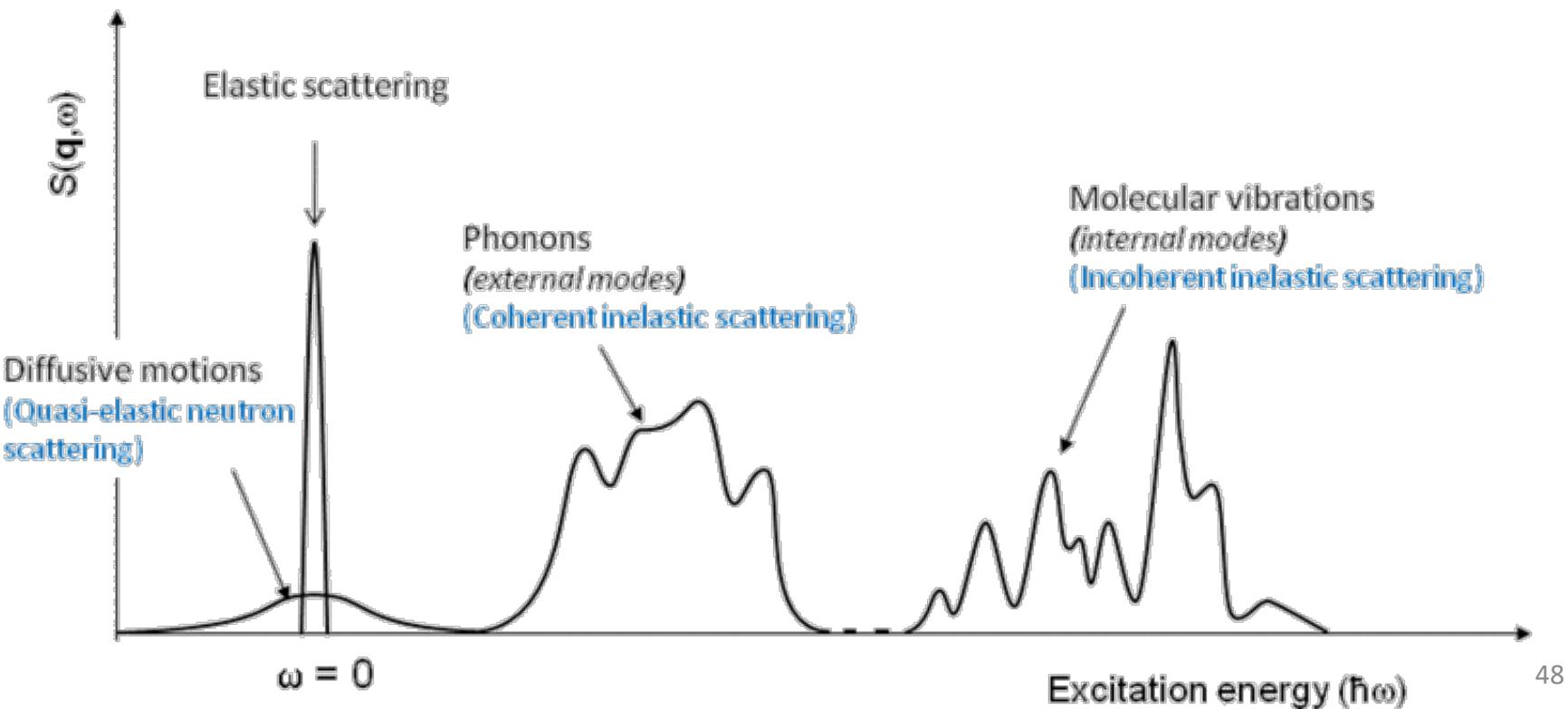
Sample environment

- neutron penetration: good
- sample volume: bad
- range as varied as the science
 - magnetic fields
 - low temperatures
 - high temperatures
 - pressure cells (TiZr)
 - sample changers
 - stress rigs
 - in-situ chemistry
 - flow cells
 - Langmuir troughs
 - ...



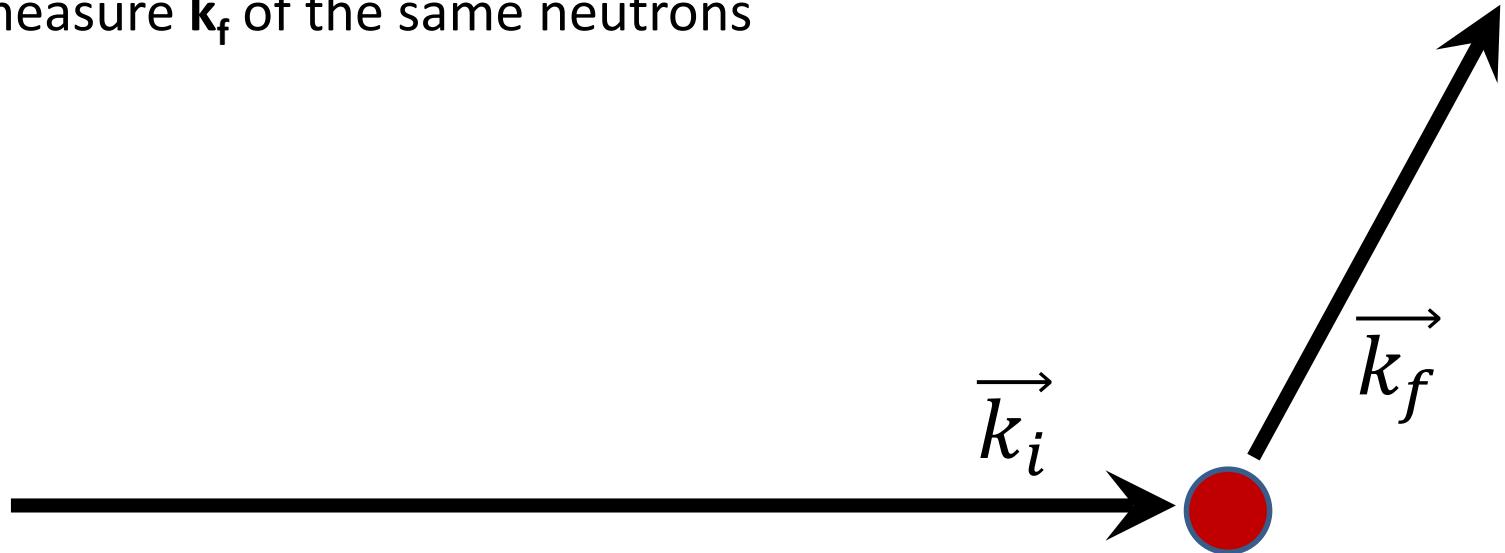
Neutron Spectroscopy

- Excitations: vibrations and other motions
 - lattice vibrations
 - magnetic excitations
 - quasi-elastic scattering: diffusion & relaxation



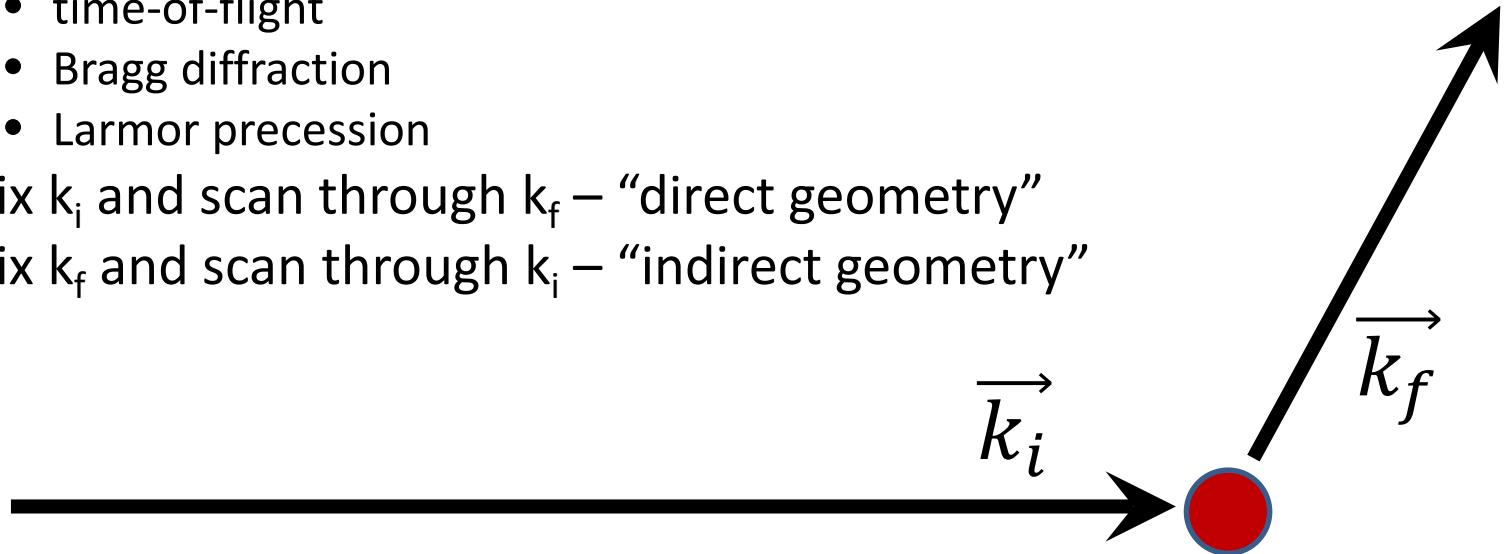
Neutron Spectroscopy

- Excitations: vibrations and other motions
 - lattice vibrations
 - magnetic excitations
 - quasi-elastic scattering: diffusion & relaxation
- Ideal spectrometer:
 - measure \mathbf{k}_i of each incident neutron
 - measure \mathbf{k}_f of the same neutrons



Neutron Spectroscopy

- Excitations: vibrations and other motions
 - lattice vibrations
 - magnetic excitations
 - quasi-elastic scattering: diffusion & relaxation
- Real spectrometer:
 - measure \mathbf{k}_i and \mathbf{k}_f of the beam
 - time-of-flight
 - Bragg diffraction
 - Larmor precession
 - Fix \mathbf{k}_i and scan through \mathbf{k}_f – “direct geometry”
 - Fix \mathbf{k}_f and scan through \mathbf{k}_i – “indirect geometry”

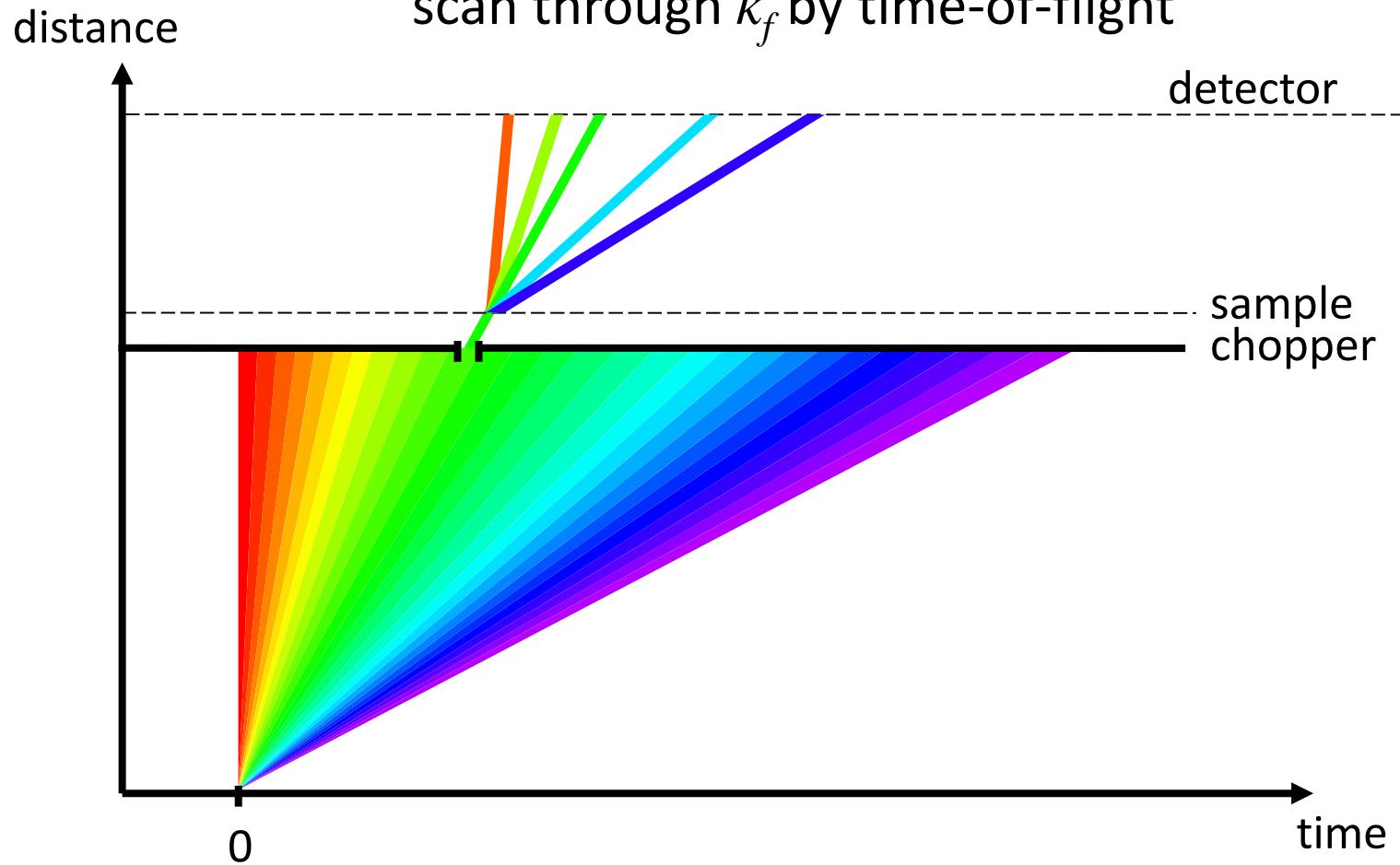


Chopper Spectrometers

Direct geometry:

fix k_i by chopper phasing

scan through k_f by time-of-flight

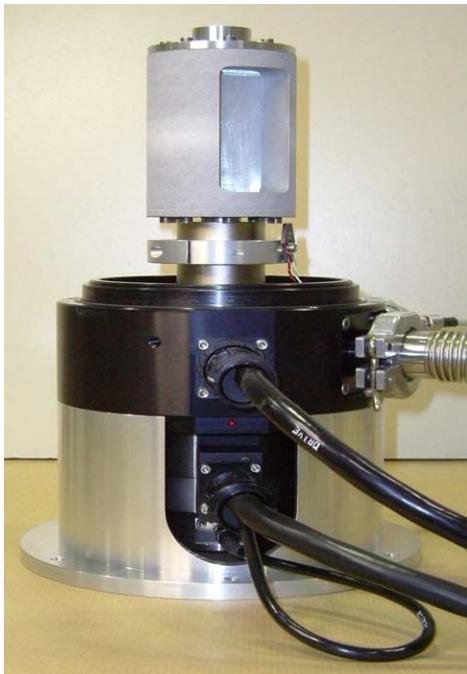
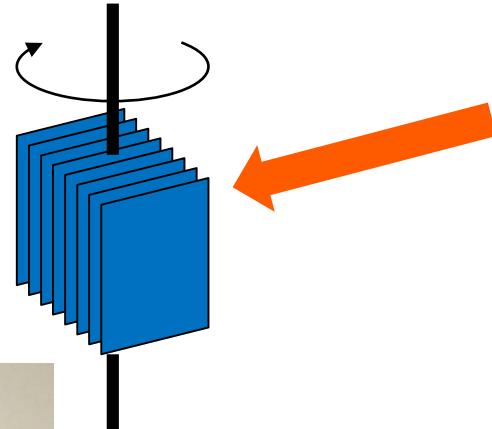


Neutron Choppers

Fermi choppers

$f < 600 \text{ Hz}$

$\Delta t > 1\mu\text{s}$



Disk choppers

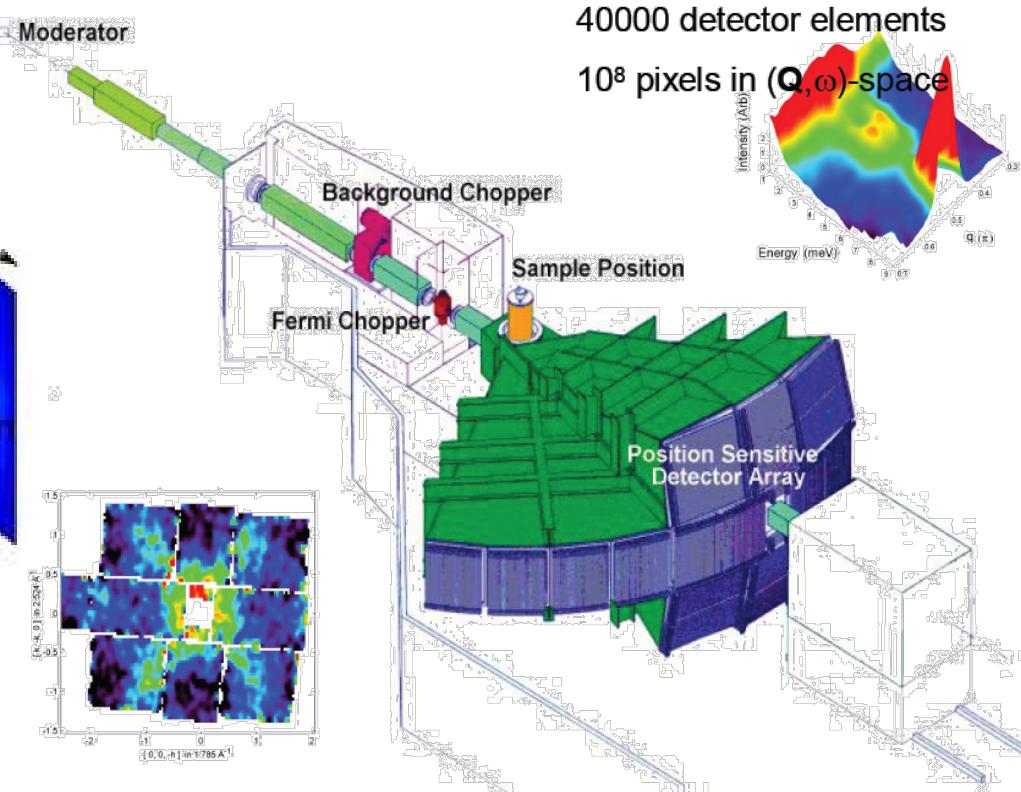
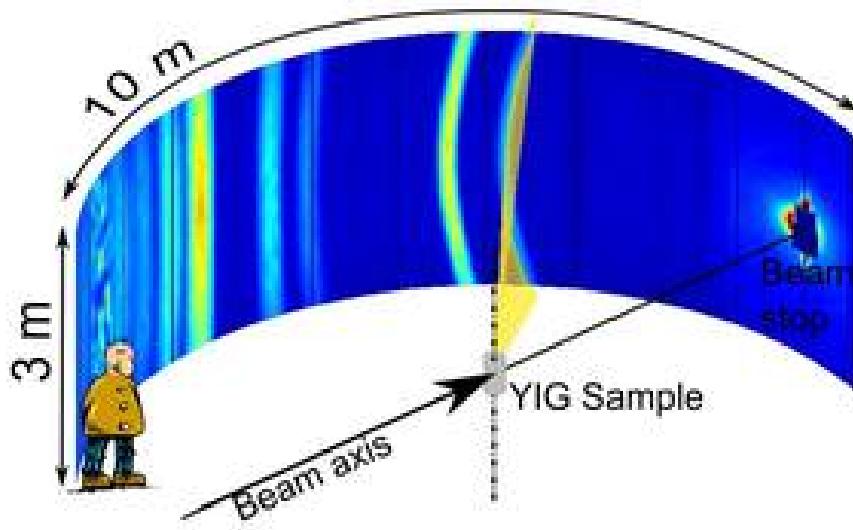
$f < 300 \text{ Hz}$

$\Delta t > 10\mu\text{s}$



Chopper Spectrometers

- General-Purpose Spectrometers
 - Incident energy ranges from 1meV to 1eV
- Huge position-sensitive detector arrays
 - Single-crystal samples



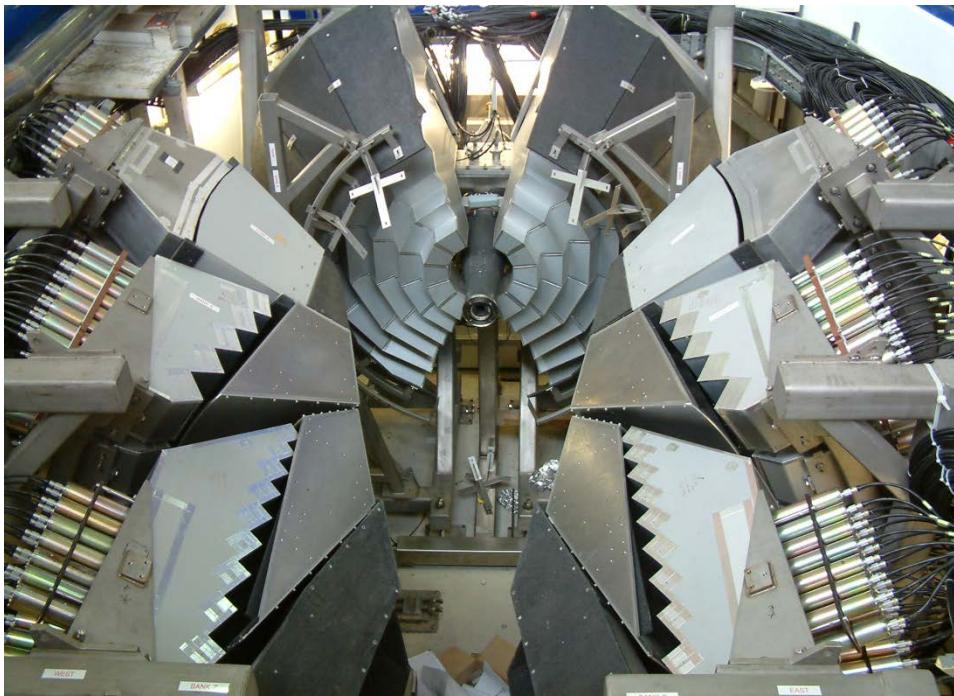
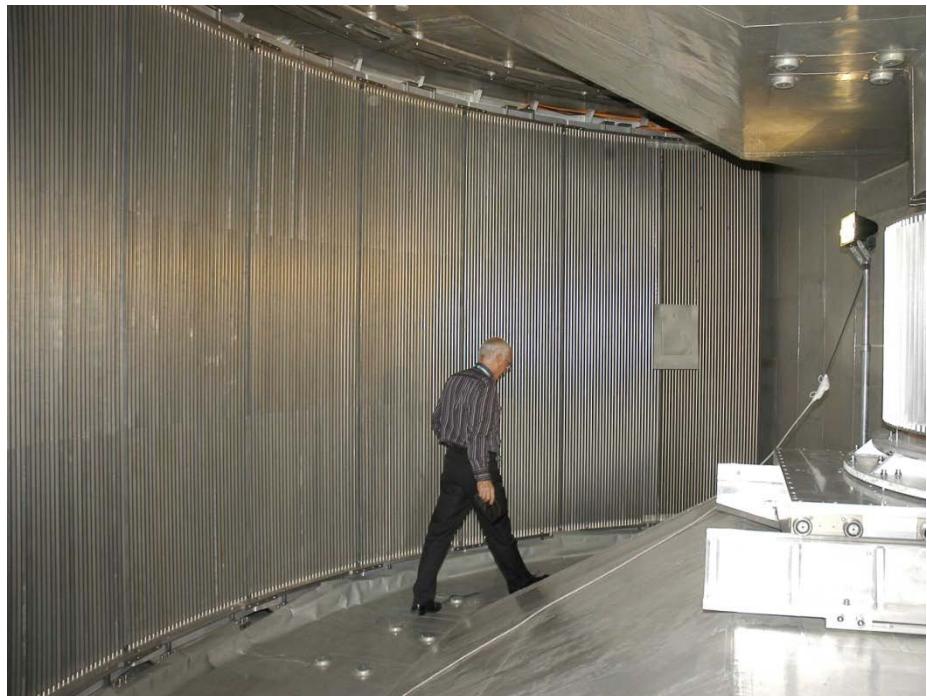
Detectors

${}^3\text{He}$ gas tubes

$\text{n} + {}^3\text{He} \rightarrow {}^3\text{H} + {}^1\text{H} + 0.764 \text{ MeV}$
 >1mm resolution
 High efficiency
 Low gamma-sensitivity
 ${}^3\text{He}$ supply problem

Scintillators

$\text{n} + {}^6\text{Li} \rightarrow {}^4\text{He} + {}^3\text{H} + 4.79 \text{ MeV}$
 <1mm resolution
 Medium efficiency
 Some gamma-sensitivity
 Magnetic-field sensitivity

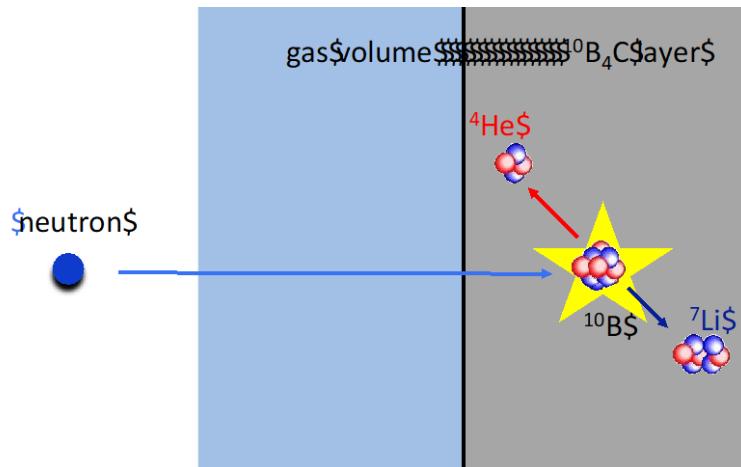


Detectors

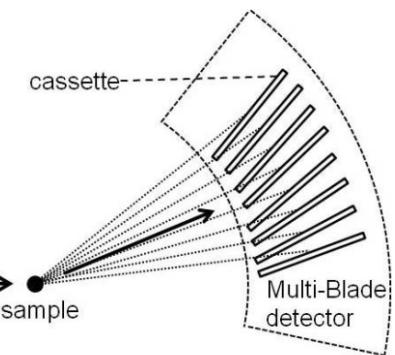
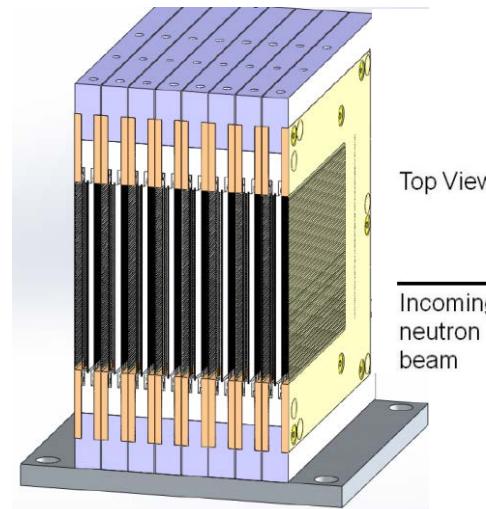
^{10}B detectors

$$\text{n} + ^{10}\text{B} \rightarrow ^7\text{Li} + ^4\text{He} + 0.48 \text{ MeV}$$

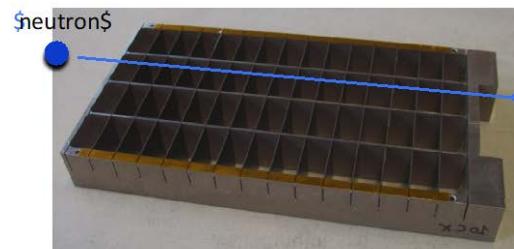
massive development programme
none yet in operation
many different types



boron layer thickness limited to $\sim 1 \mu\text{m}$
 $\Rightarrow \sim 5\%$ efficiency



inclined blades

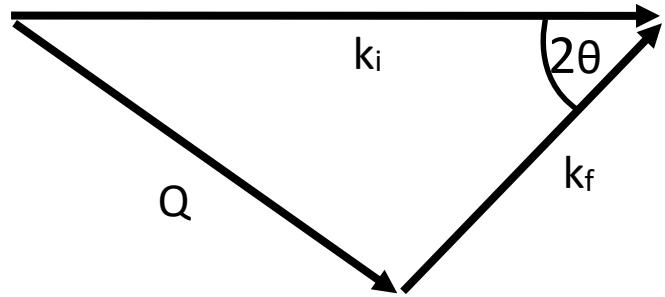


perpendicular blades



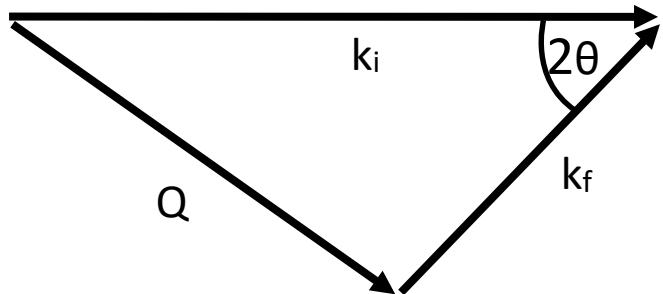
Multi-Grid detector

Direct-Geometry Kinematics



$$\vec{Q} = \vec{k}_i - \vec{k}_f$$

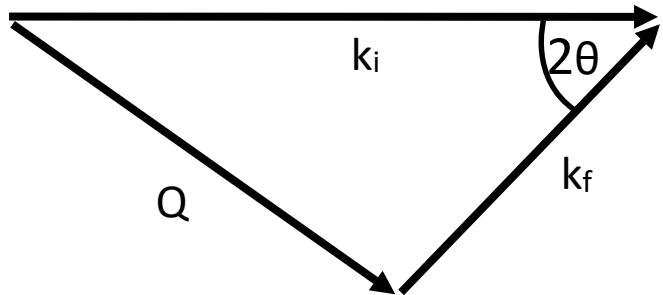
Direct-Geometry Kinematics



$$\vec{Q} = \vec{k}_i - \vec{k}_f$$

$$E = \frac{p^2}{2m} = \frac{\hbar^2 k^2}{2m}$$

Direct-Geometry Kinematics

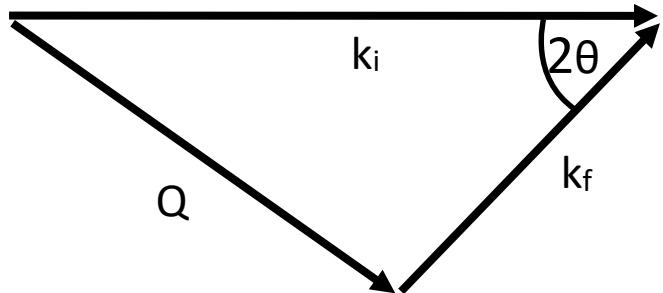


$$\vec{Q} = \vec{k}_i - \vec{k}_f$$

$$E = \frac{p^2}{2m} = \frac{\hbar^2 k^2}{2m}$$

$$\frac{\hbar Q^2}{2m_n} = E_i + E_f - 2\sqrt{E_i E_f} \cos 2\theta$$

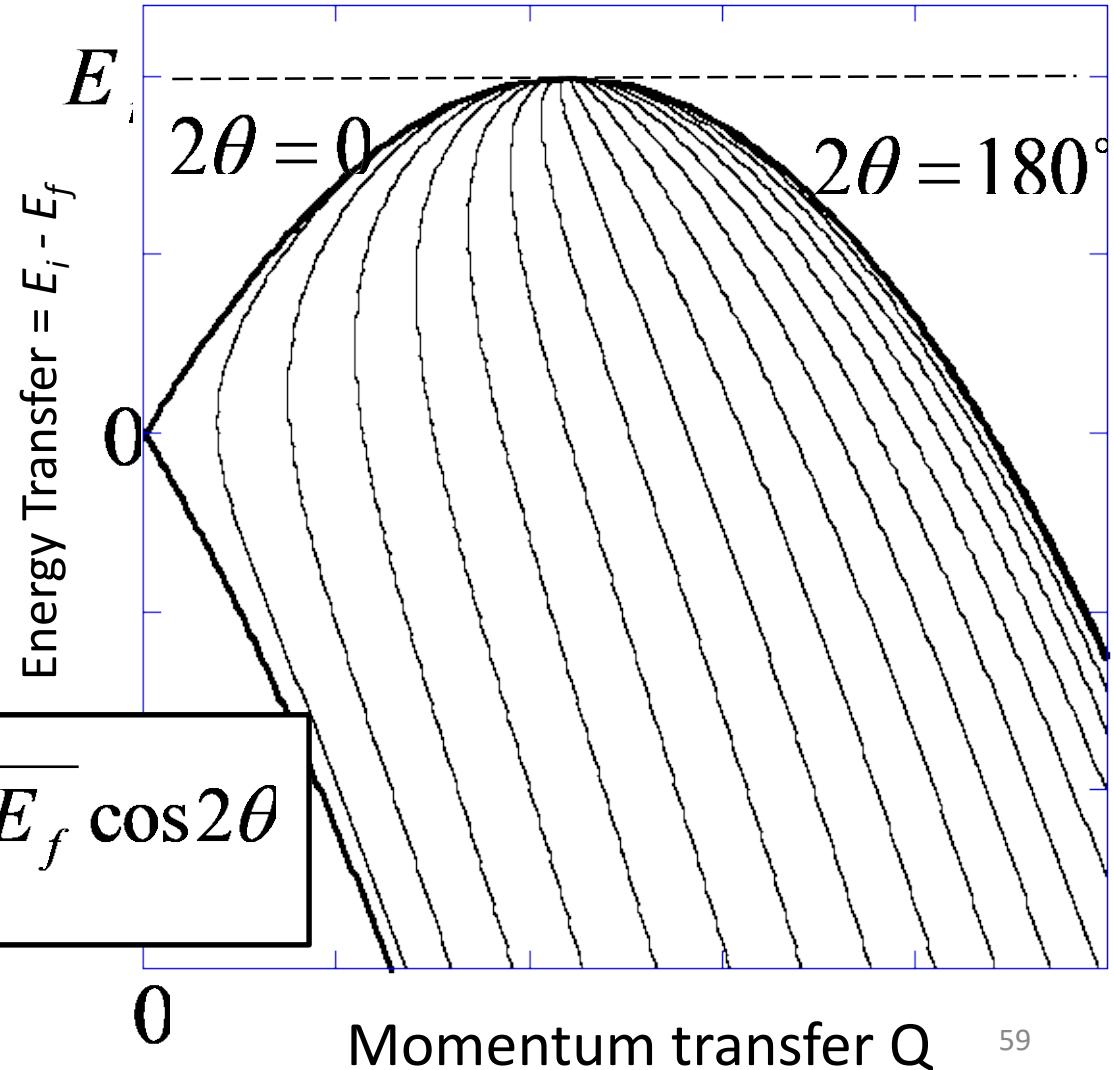
Direct-Geometry Kinematics



$$\vec{Q} = \vec{k}_i - \vec{k}_f$$

$$E = \frac{p^2}{2m} = \frac{\hbar^2 k^2}{2m}$$

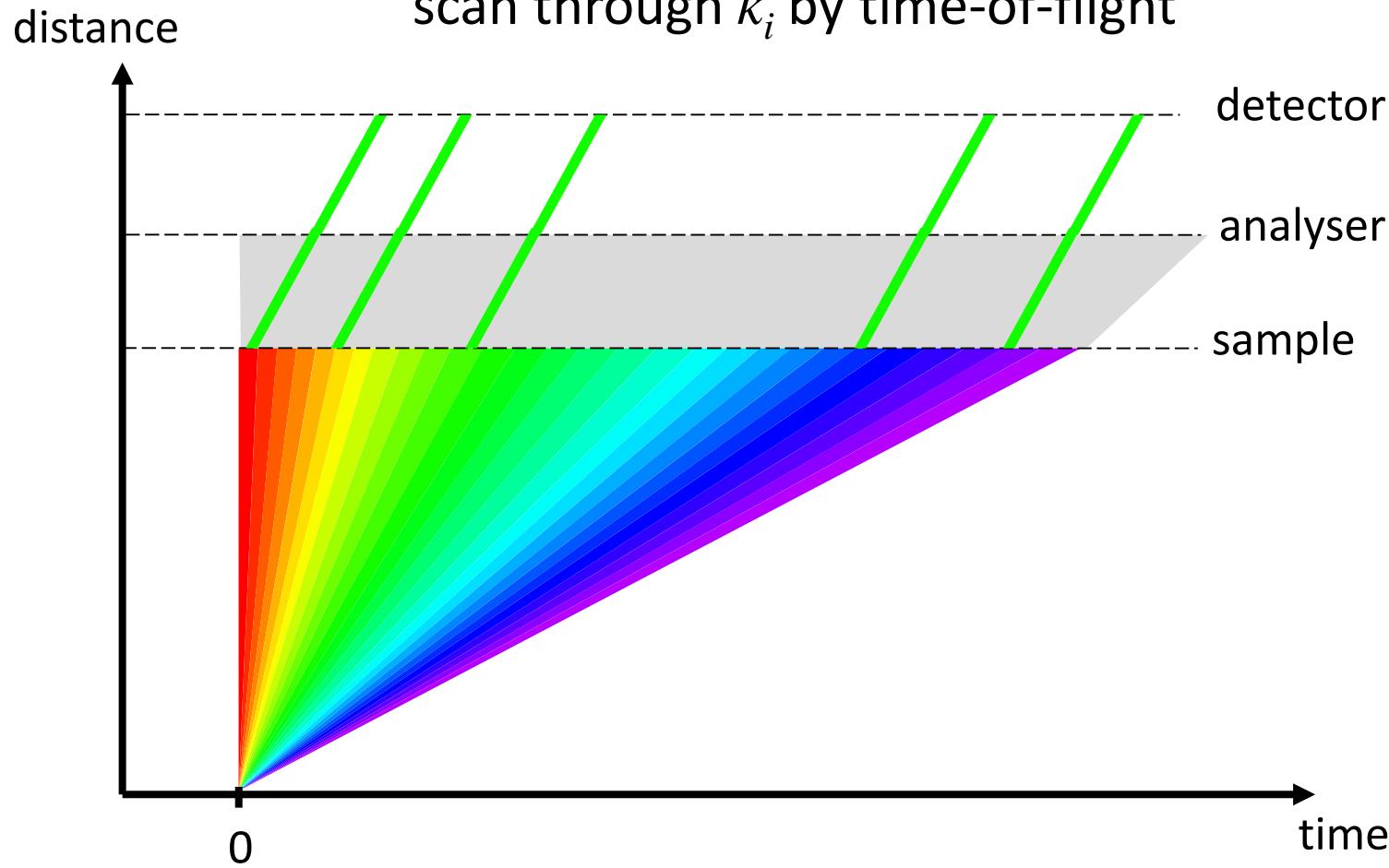
$$\frac{\hbar Q^2}{2m_n} = E_i + E_f - 2\sqrt{E_i E_f} \cos 2\theta$$



Alternative to Direct Geometry

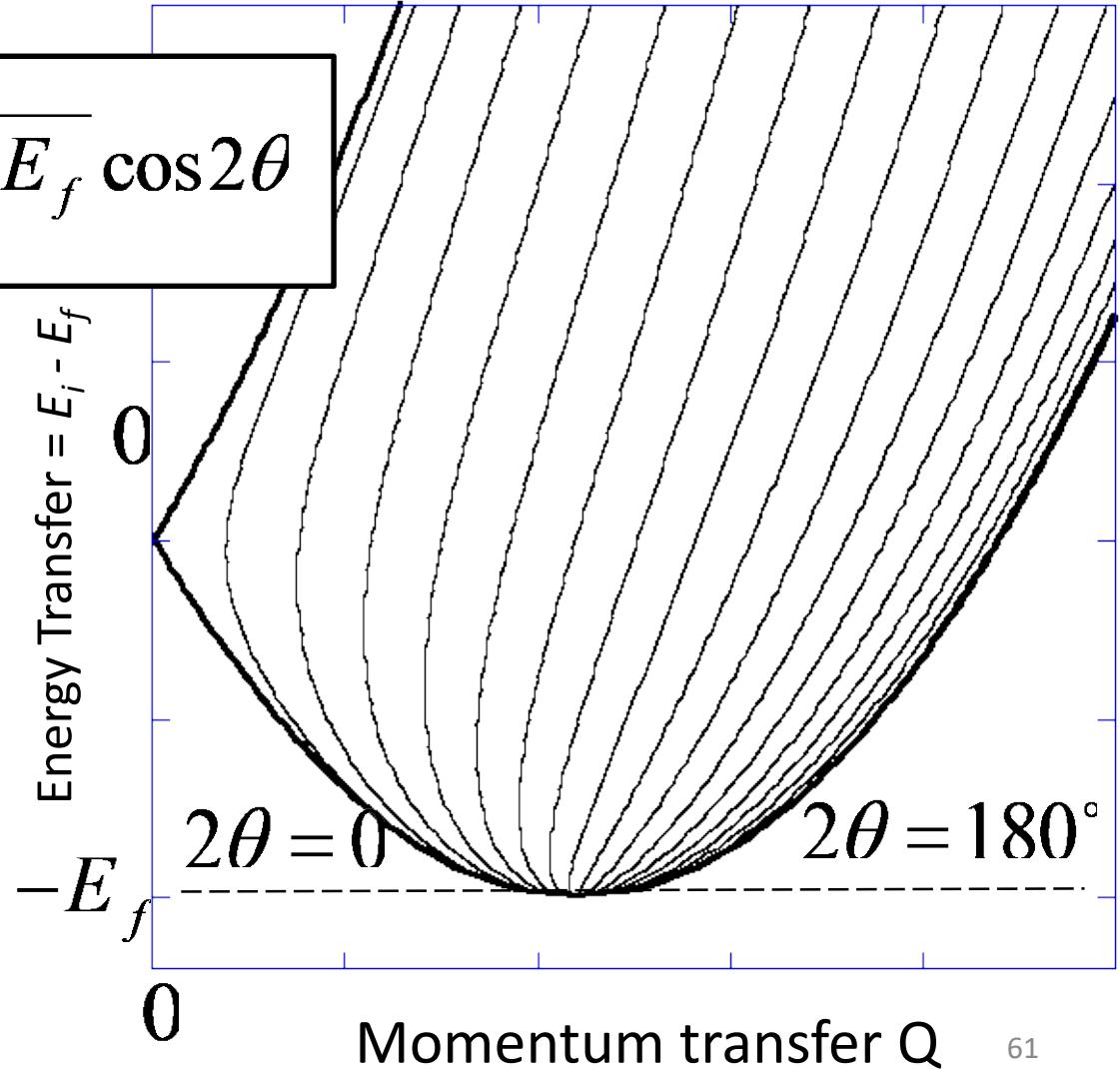
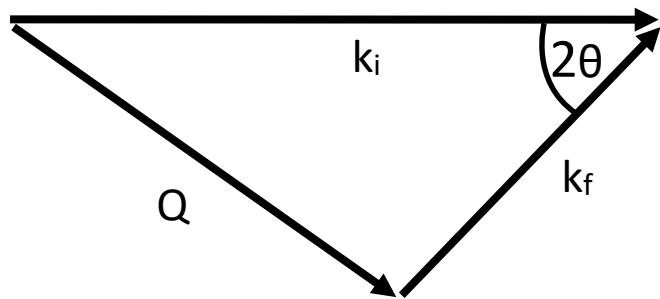
Indirect geometry:

fix k_f – usually by analyser crystals
 scan through k_i by time-of-flight



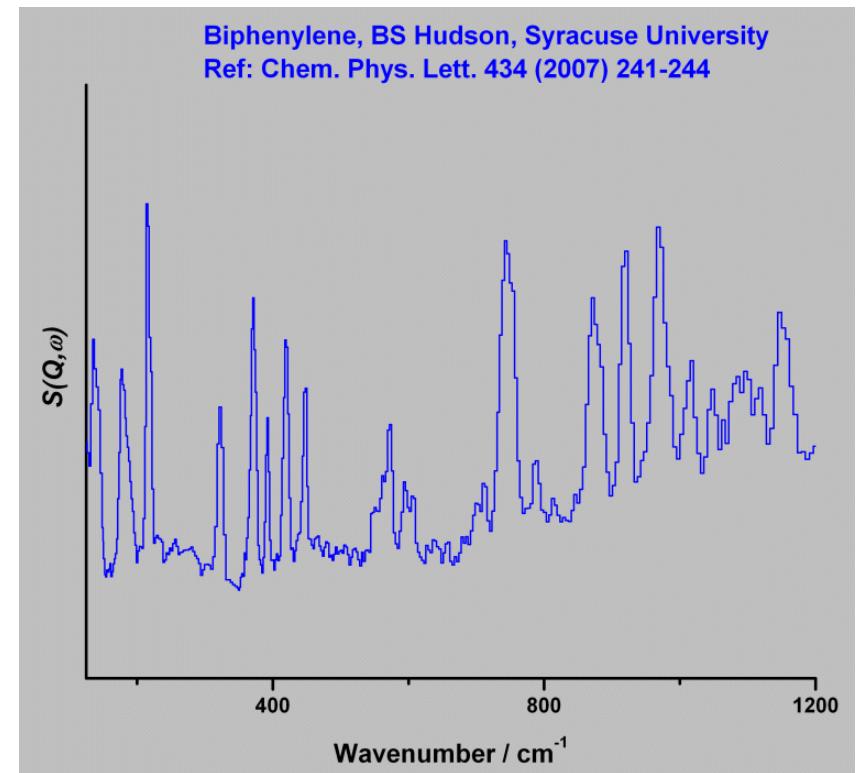
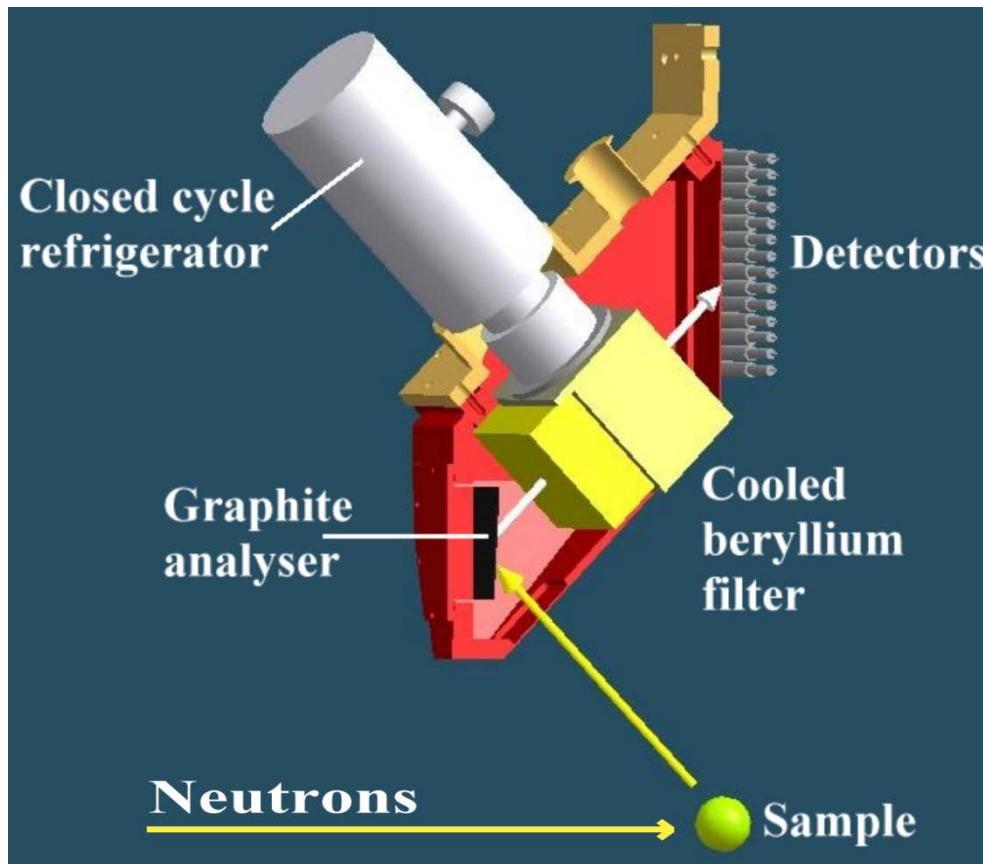
Indirect-Geometry Kinematics

$$\frac{\hbar Q^2}{2m_n} = E_i + E_f - 2\sqrt{E_i E_f} \cos 2\theta$$



Vibrational Spectroscopy

TOSCA@ISIS



Density-of-states measurements

High Resolution 1: Backscattering

$$\lambda = 2d \sin \theta$$

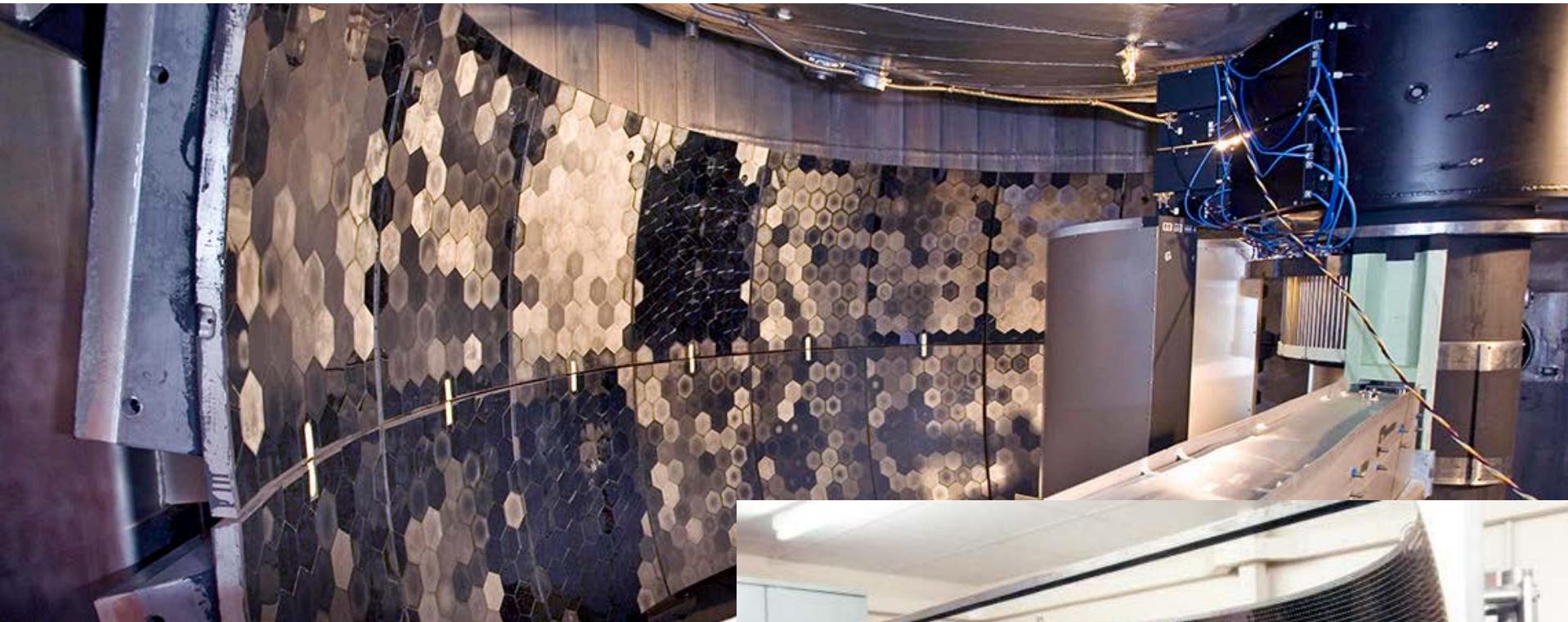
$$\Rightarrow \frac{\Delta\lambda}{\lambda} = \frac{\Delta d}{d} + \cot \theta \Delta \theta$$

$$\theta \rightarrow \frac{\pi}{2}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta} \rightarrow 0$$

Use single crystals in as close to backscattering as possible to define k_f .
 Scan through k_i with as good energy resolution.

Backscattering



BASIS@SNS Si111 3 μ eV

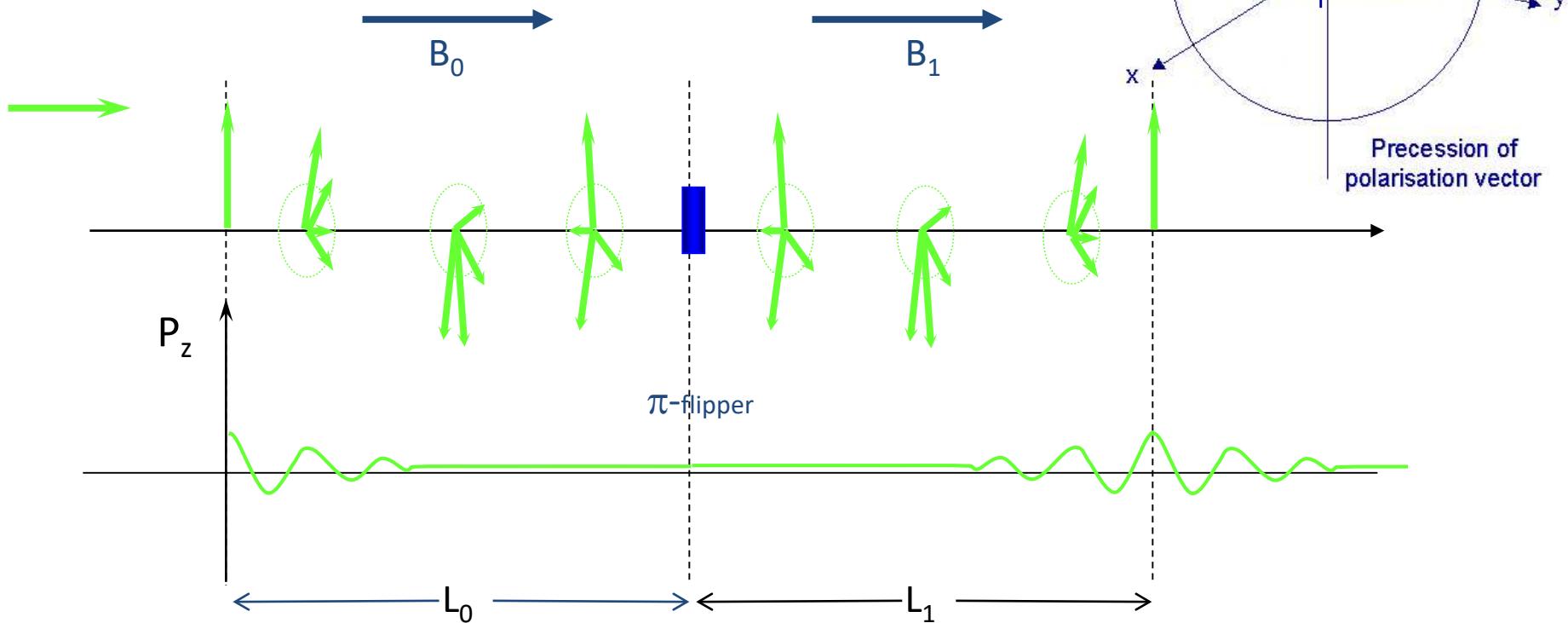


OSIRIS@ISIS PG002 25 μ eV

High Resolution 2: Neutron Spin Echo

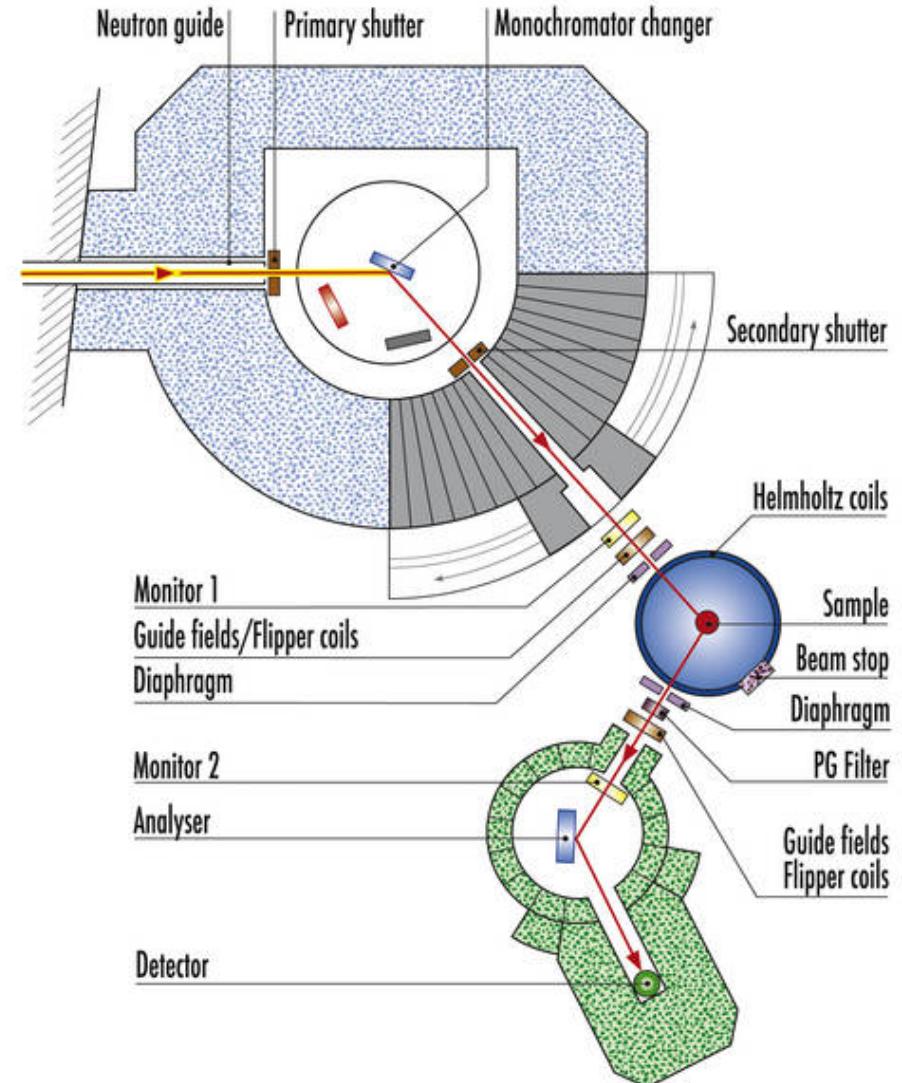
High energy resolution $< 1 \mu\text{eV}$

Larmor precessions encode energy transfer



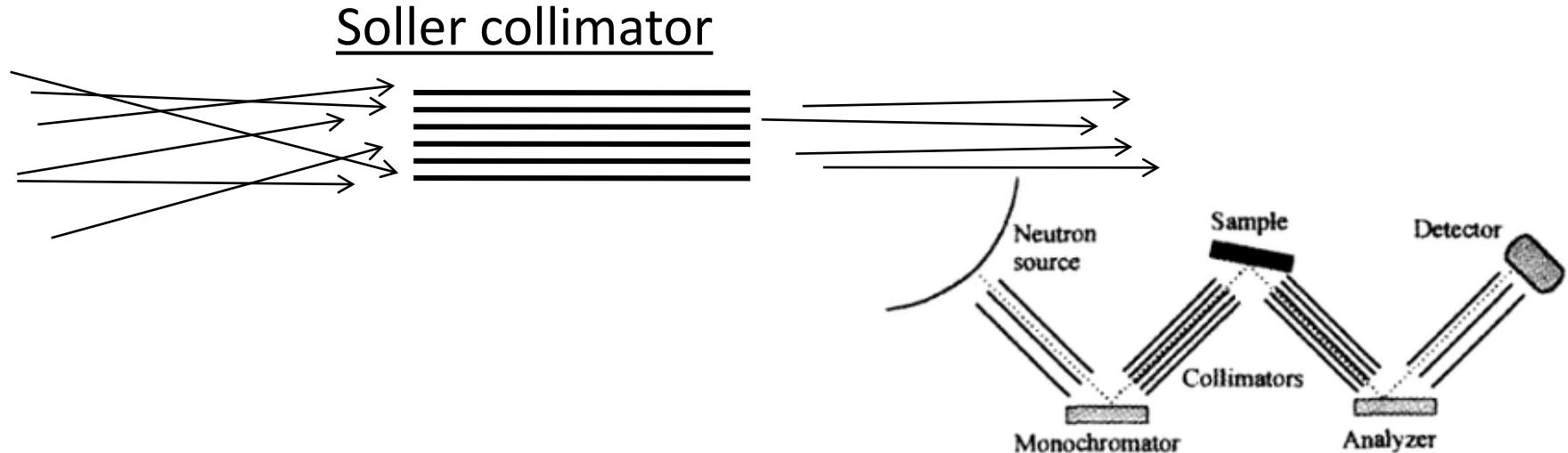
Triple-Axis Spectrometers

- Single-crystal excitations
- Very flexible
- Measures a single point in \vec{Q} -E space at a time
- Scans:
 - Constant \vec{Q} : Scan E at constant \mathbf{k}_i or \mathbf{k}_f
 - Constant E: Scan \vec{Q} in any direction



Collimation

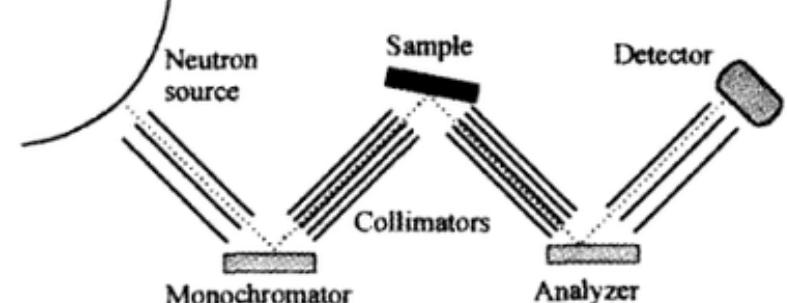
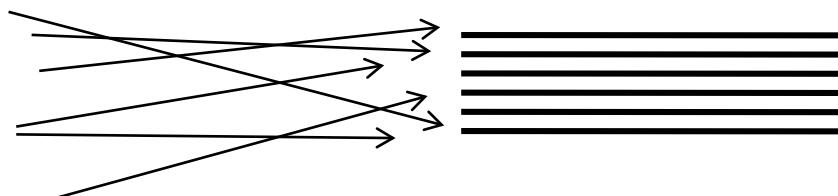
- TAS E and Q resolution adjusted by collimation



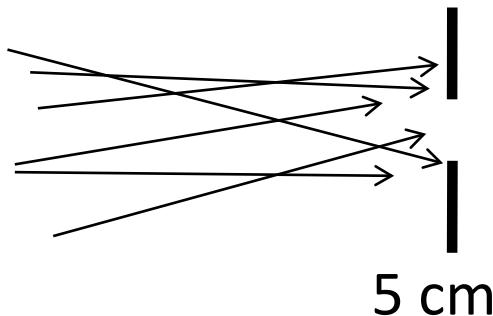
Collimation

- TAS E and Q resolution adjusted by collimation
- SANS resolution also adjusted by collimation

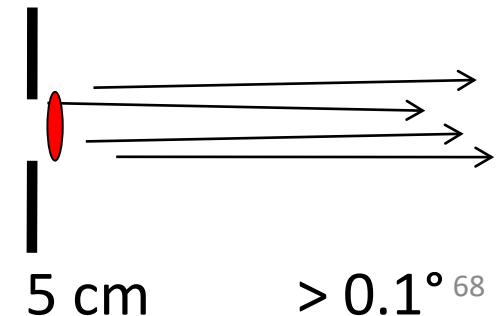
Soller collimator



Pin-holes separated by distance

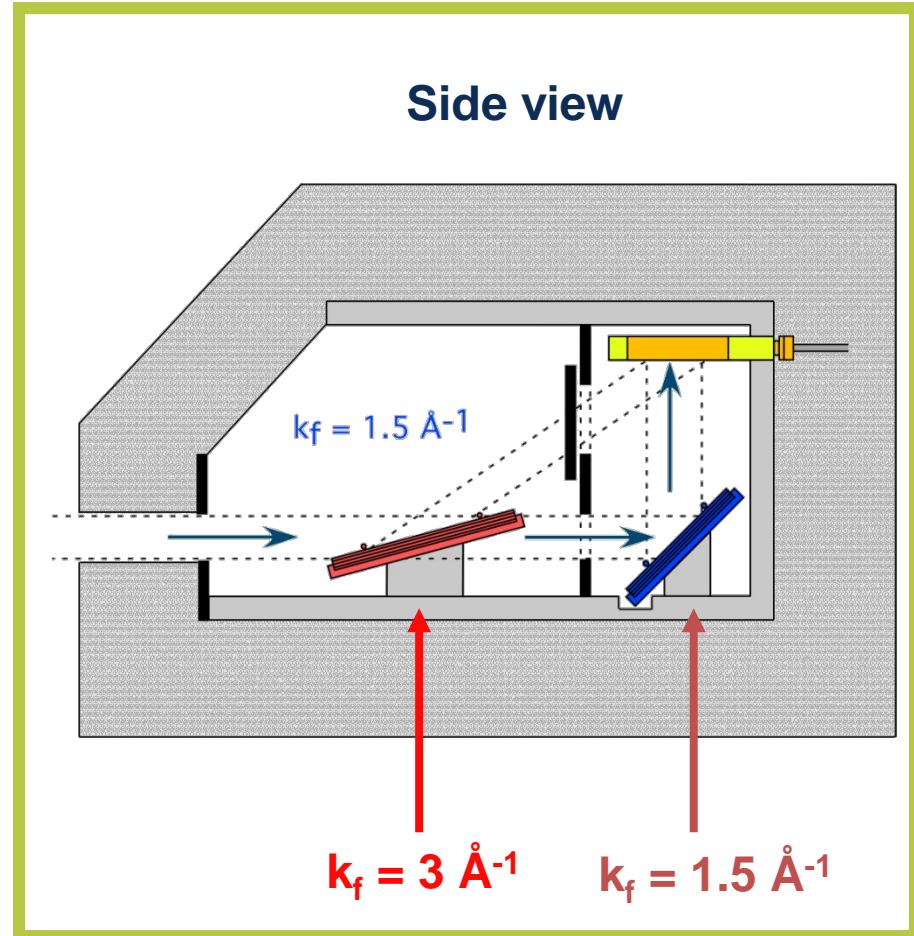
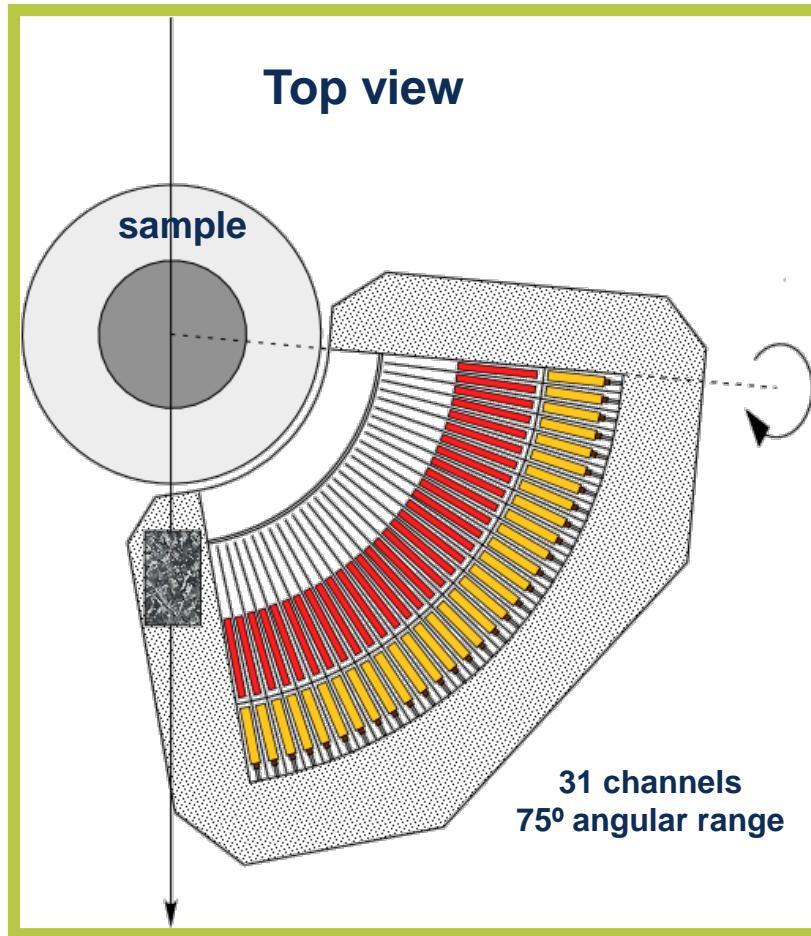


< 30 m

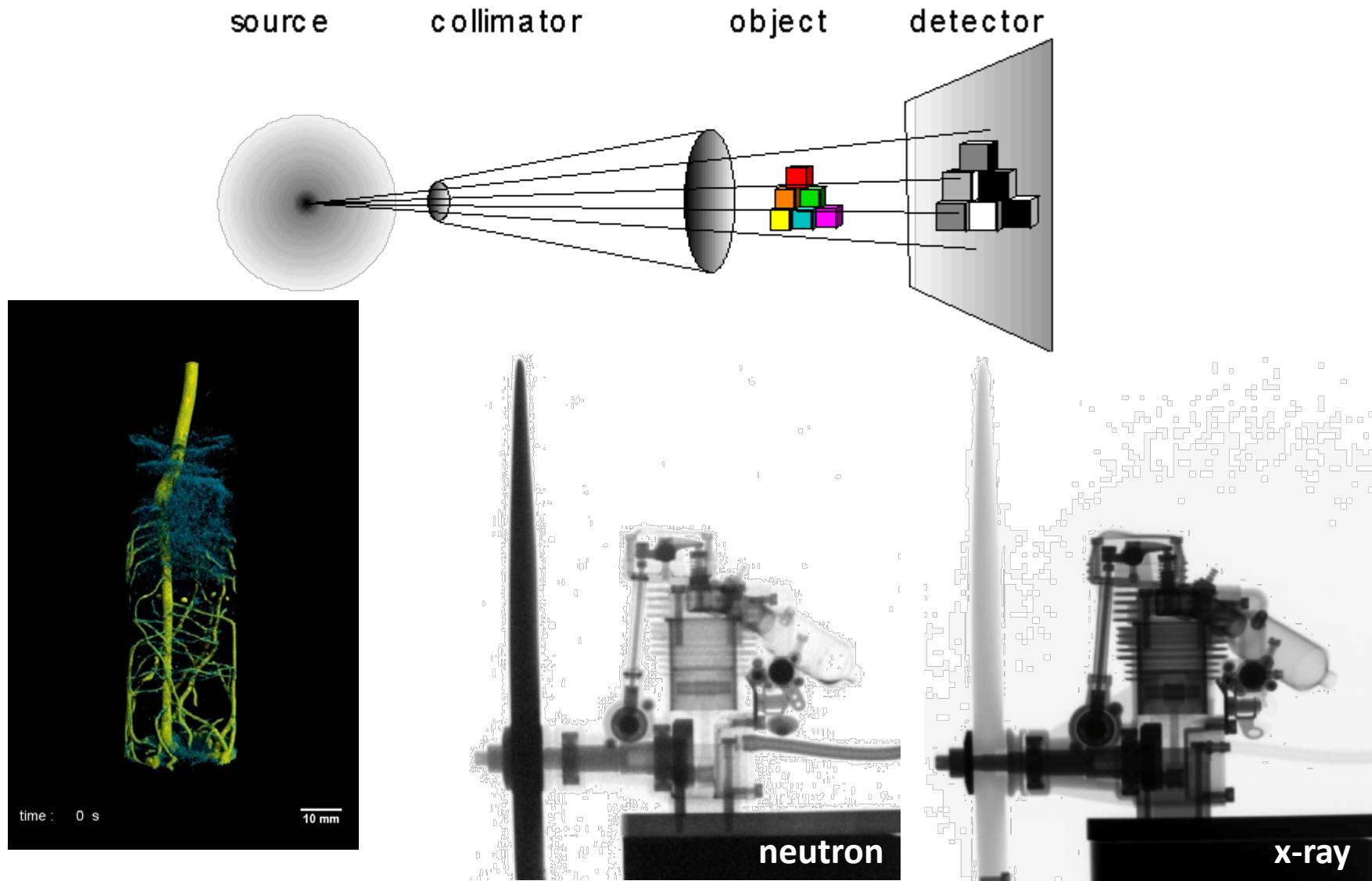


TAS with multiplexing

IN20 flat-cone multi-analyser



Neutron Imaging



Summary

- Neutron instrument concepts
 - time-of-flight
 - Bragg's law
- Neutron Instrumentation
 - guides
 - monochromators
 - shielding
 - detectors
 - choppers
 - sample environment
 - collimation
- Neutron diffractometers
 - powder diffraction
- Neutron spectrometers
 - direct and indirect geometry time-of-flight
 - backscattering
 - triple-axis
 - spin-echo
- Imaging

Thank you!