

```
In [8]: # Preamble: minimal imports + local include
using Random
using Statistics
using Printf
using Plots
using Logging

include("formatting.jl")

if !isdefined(Main, :System1D)
    include("../src/System1D.jl")
end
using .System1D: Hamiltonian, TrialWF, Walker, DMCPParams, DMCSim, Importance
```

## System: Hydrogen Atom in 1D with Odd Parity Trial Wavefunction

### Potential

$$V(x) = -\frac{1}{|x|}$$

### Trial wavefunction (odd parity)

$$\psi_T(x) = xe^{-\alpha|x|}$$

This enforces a node at  $x = 0$  via the sign of  $x$ . The simulation uses fixed-node DMC with importance sampling.

This cell sets parameters, initializes walkers, and runs the simulation.

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In [9]: # System: 1D Coulomb-like potential
V(R) = -1 / abs(R[1])
H = Hamiltonian(1, 0.5, V)

# Trial wavefunction (odd parity): psi_T(x) = x * exp(-alpha*|x|)
alpha = 1.0
logpsi(R) = begin
    x = R[1]
    ax = abs(x)
    return ax == 0 ? -Inf : log(ax) - alpha * ax
end

gradlogpsi(R) = begin
    x = R[1]
    ax = abs(x)
    s = sign(x)
    return ax == 0 ? [0.0] : [(s / ax) - alpha * s]
end

lapllogpsi(R) = begin
```

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    x = R[1]
    ax = abs(x)
    return ax == 0 ? -Inf : -1.0 / ax^2
end

signpsi(R; tol=1e-12) = abs(R[1]) < tol ? 0.0 : sign(R[1])

trial = TrialWF(logpsi, gradlogpsi, lapllogpsi, signpsi)
guiding = ImportanceGuiding(trial, H)

# Walkers and params
targetN = 1000
walkers = [Walker([randn()]) for _ in 1:targetN]

params = DMCPParams(0.005, 200, 40, targetN, -0.5, 0.1, 10, 50)

# Run
rng_sim = MersenneTwister(42)
sim = DMCSim(H, params, walkers, rng_sim; guiding=guiding, nodepolicy=FixedN
run_simulation!(sim; snapshot_steps=[params.nsteps])

ET_history = sim.ET_history
population_history = sim.population_history
energy_mean_history = sim.energy_mean_history
energy_variance_history = sim.energy_variance_history

nothing

```

## Results

The 1D hydrogen atom has an analytic solution with ground state

$$E_0 \approx -\frac{1}{2} \text{ (a.u.)}$$

This cell reports the post-equilibration energy and plots the reference energy, population, mean local energy, and local-energy variance over time, plus the final walker density.

```

In [10]: # Results and plots
t = (0:params.nsteps) .* params.dt

nequil = params.nequil
start_idx = min(nequil + 1, length(energy_mean_history))
postE = energy_mean_history[start_idx:end]

Ebar = mean(postE)
SEM = (length(postE) > 1) ? std(postE) / sqrt(length(postE)) : NaN

Ebar_str, SEM_str = format_with_uncertainty(Ebar, SEM)
println("Hydrogen DMC energy (post-eq, nequil=$(nequil)): E = $(Ebar_str) +/-
E_final_str, var_str = format_pair_sigfig(energy_mean_history[end], energy_v
println("Final step: E = $(E_final_str), Var(E_L) = $(var_str)")

```

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Logging.with_logger(Logging.NullLogger()) do
  redirect_stderr(devnull) do
    p1 = plot(t, ET_history, xlabel="step", ylabel="E_T", title="Referer
    display(p1)

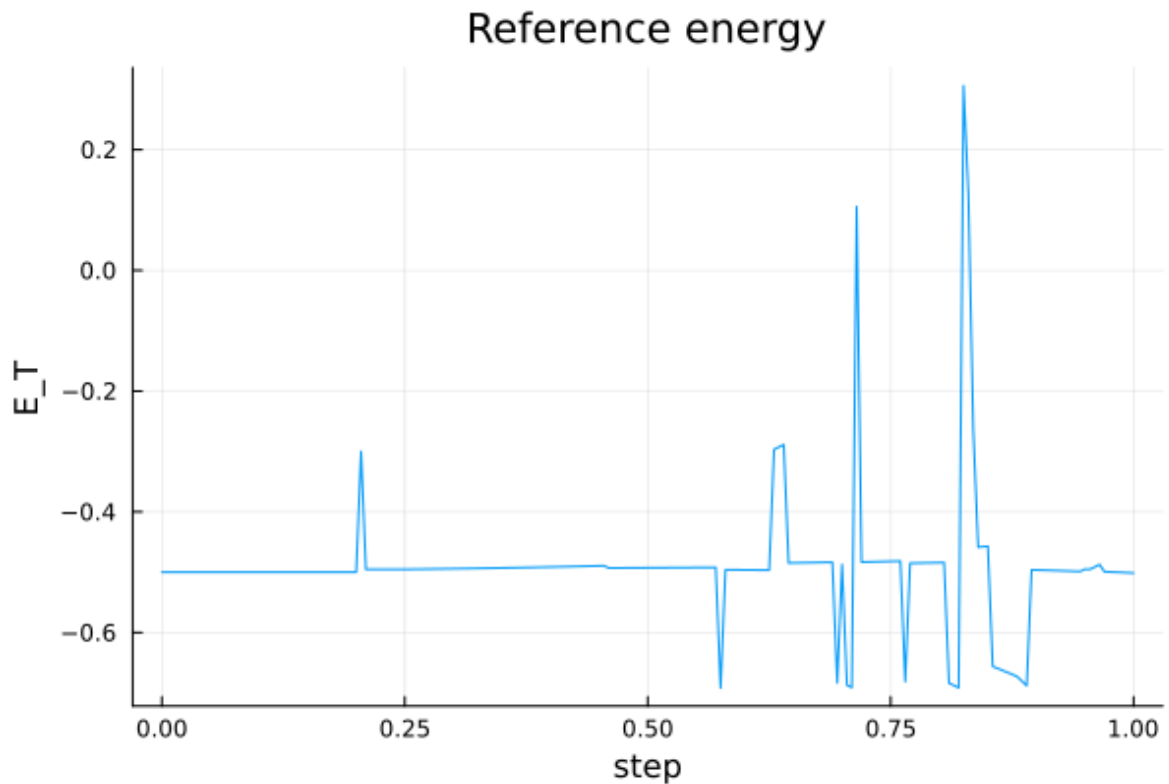
    p2 = plot(t, population_history, xlabel="step", ylabel="N_w", title=
    display(p2)

    p3 = plot(t, energy_mean_history, xlabel="step", ylabel="<E_L>", tit
    display(p3)

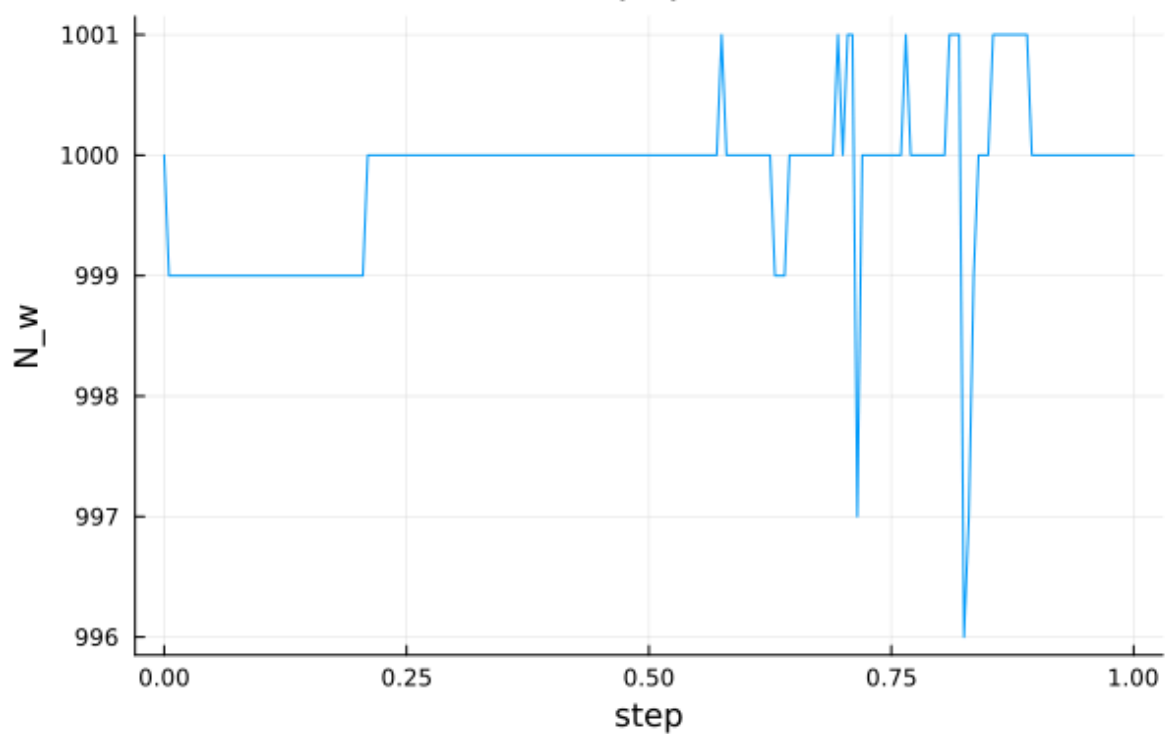
    p4 = plot(t, energy_variance_history, xlabel="step", ylabel="Var(E_L
    display(p4)

    if !isempty(sim.walker_positions_history)
      snap = sim.walker_positions_history[end]
      p5 = plot_snapshot_1d_density(snap; nbins=120, title="Final walk
      display(p5)
    end
  end
end

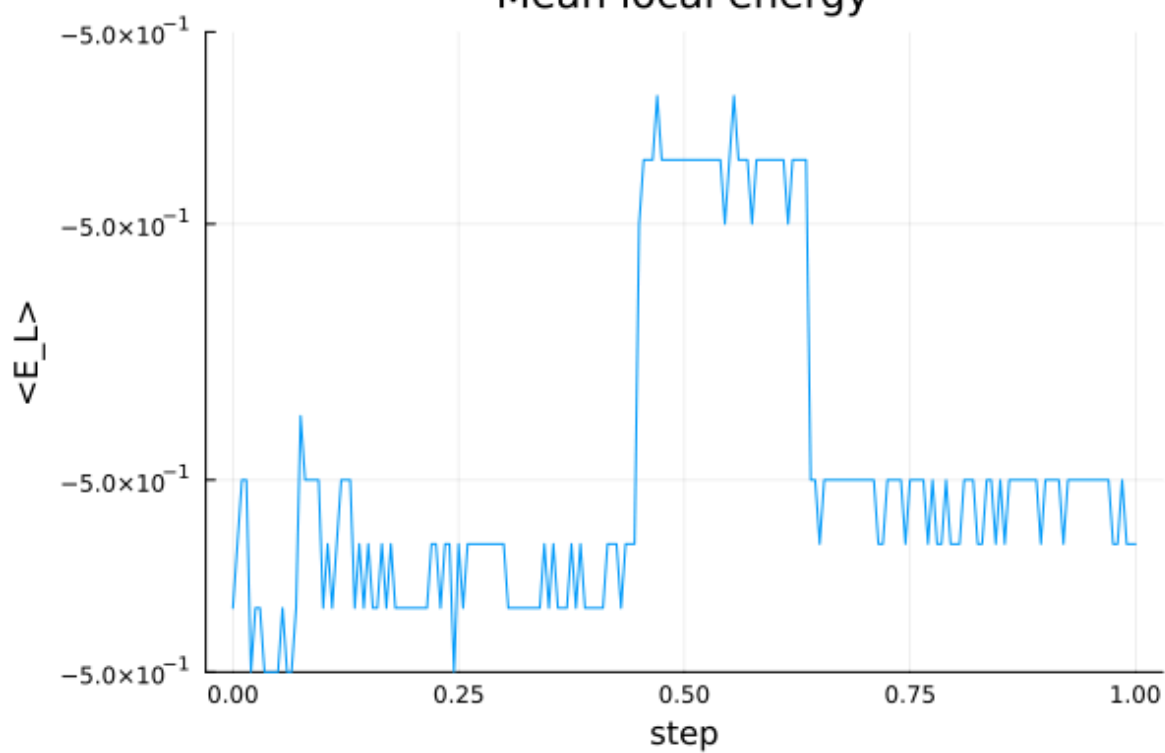
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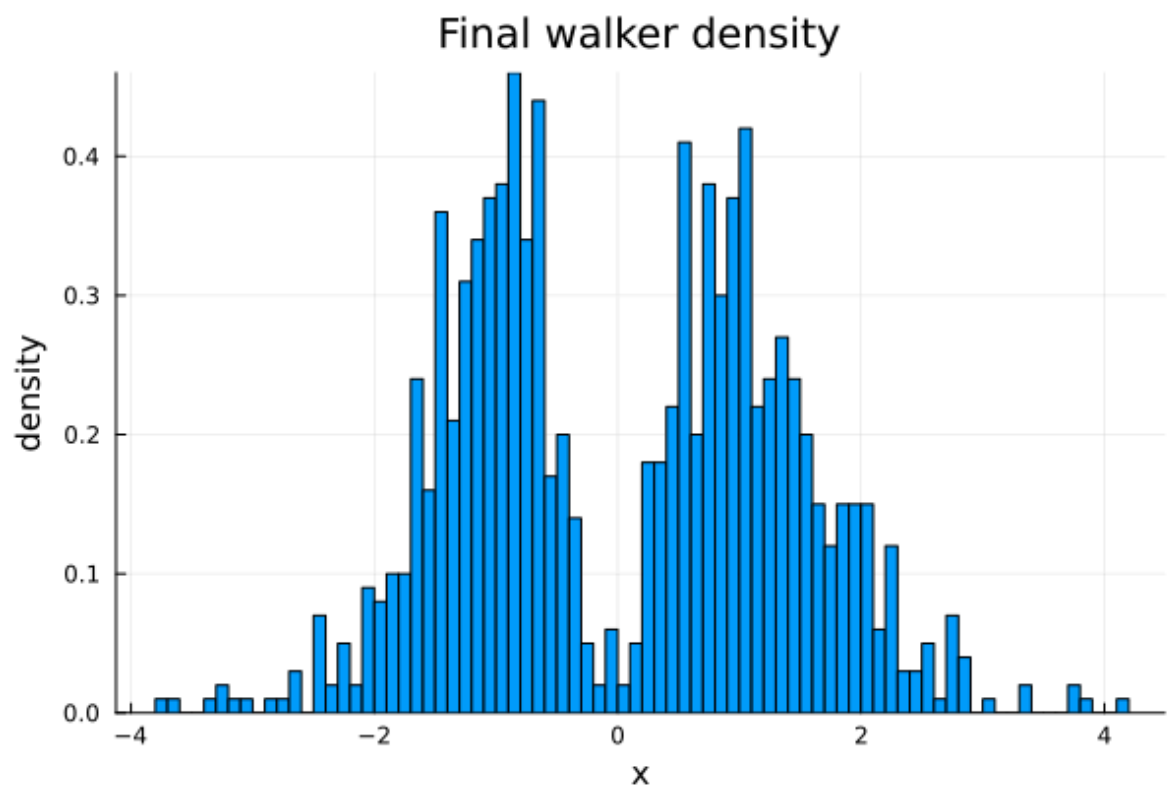
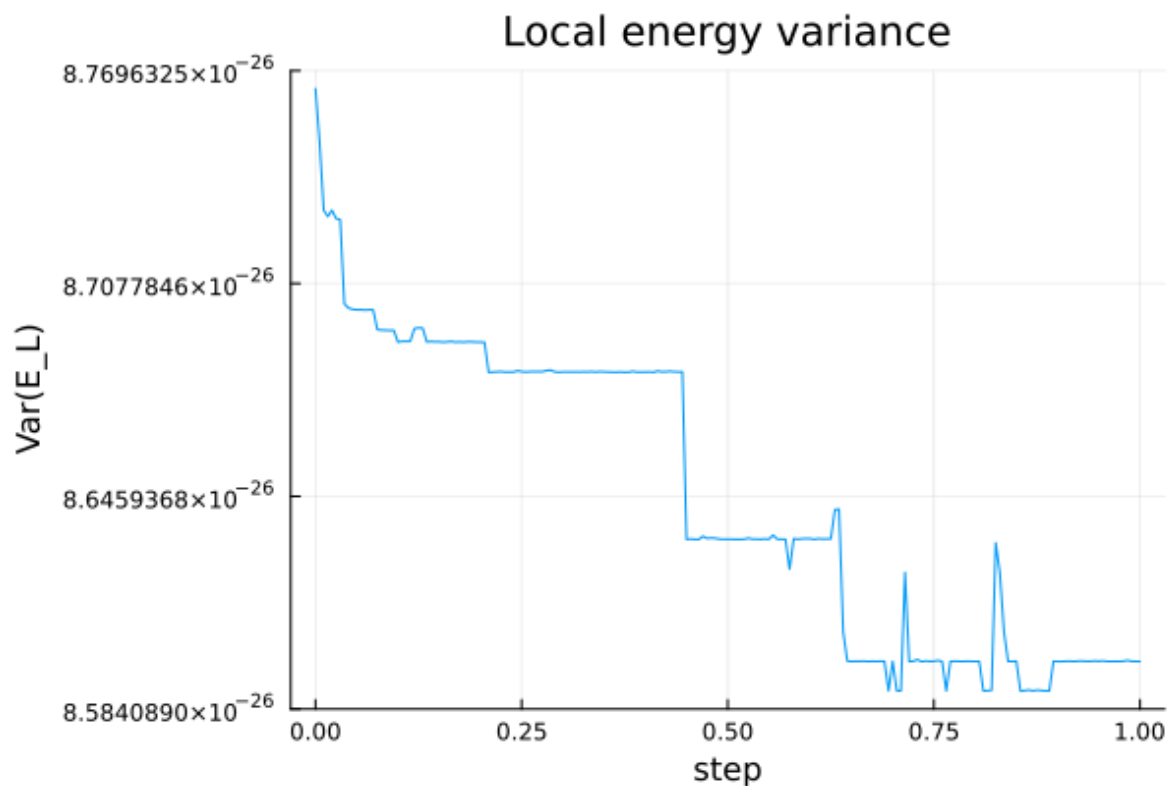


Walker population



Mean local energy





Hydrogen DMC energy (post-eq, nequil=40):  $E = -0.50000000000013545 \pm 0.0000000000000023$   
Final step:  $E = -0.50000000000013655743202889$ ,  $\text{Var}(E_L) = 0.000000000000000000000000000086$