

```
In [13]: # Preamble: minimal imports + local include
using Random
using Statistics
using Printf
using Plots
using Logging

include("formatting.jl")

if !isdefined(Main, :System1D)
    include("../src/System1D.jl")
end
using .System1D: Hamiltonian, TrialWF, Walker, DMCPParams, DMCSim, Importance
```

System: Coupled Two-Particle 1D Harmonic Oscillator

Potential

$$V(x_1, x_2) = \frac{1}{2}\omega^2(x_1^2 + x_2^2) + \frac{1}{2}\kappa(x_1 - x_2)^2$$

Define normal coordinates $S = x_1 + x_2$ and $D = x_1 - x_2$.

Trial wavefunction (normal modes)

$$\psi_T(x_1, x_2) = \exp\left[-\frac{\omega}{4}S^2 - \frac{\omega_{\text{rel}}}{4}D^2\right]$$

with $\omega_{\text{rel}} = \sqrt{\omega^2 + 2\kappa}$.

This cell initializes walkers and runs importance-sampled DMC.

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In [14]: # System: coupled 2-particle 1D harmonic oscillator
omega = 1.0
kappa = 0.7

V(R) = begin
    x1, x2 = R
    0.5 * omega^2 * (x1^2 + x2^2) + 0.5 * kappa * (x1 - x2)^2
end

H = Hamiltonian(2, 0.5, V)

omega_rel = sqrt(omega^2 + 2 * kappa)
E_ref = 0.5 * (omega + omega_rel)

# Ground-state trial wavefunction in normal-mode form
logpsi(R) = begin
    x1, x2 = R
    S = x1 + x2
    D = x1 - x2
    return -0.25 * omega * S^2 - 0.25 * omega_rel * D^2
end
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end

gradlogpsi(R) = begin
    x1, x2 = R
    S = x1 + x2
    D = x1 - x2
    return [-0.5 * (omega * S + omega_rel * D),
            -0.5 * (omega * S - omega_rel * D)]
end

lapllogpsi(R) = -(omega + omega_rel)

trial = TrialWF(logpsi, gradlogpsi, lapllogpsi)
guiding = ImportanceGuiding(trial, H)

# Walkers and params
targetN = 5000
rng_init = MersenneTwister(123)
walkers = [Walker(2 .* rand(rng_init, 2) .- 1) for _ in 1:targetN]

params = DMCPParams(0.005, 400, 50, targetN, E_ref, 0.1, 10, 50)

# Run
rng_sim = MersenneTwister(124)
sim = DMCSim(H, params, walkers, rng_sim; guiding=guiding, nodepolicy=NoNode)
run_simulation!(sim; snapshot_steps=[params.nsteps])

ET_history = sim.ET_history
population_history = sim.population_history
energy_mean_history = sim.energy_mean_history
energy_variance_history = sim.energy_variance_history

nothing

```

Results

Exact ground-state energy

$$E_0 = \frac{1}{2}(\omega + \omega_{\text{rel}})$$

This cell reports the post-equilibration energy and plots the reference energy, population, mean local energy, and local-energy variance over time, plus the final walker distribution.

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In [16]: # Results and plots
t = (0:params.nsteps) .* params.dt

nequil = params.nequil
start_idx = min(nequil + 1, length(energy_mean_history))
postE = energy_mean_history[start_idx:end]

Ebar = mean(postE)

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SEM = (length(postE) > 1) ? std(postE) / sqrt(length(postE)) : NaN

Ebar_str, SEM_str = format_with_uncertainty(Ebar, SEM)
println("Coupled H0 DMC energy (post-eq, nequil=$(nequil)): E = $(Ebar_str)
E_final_str, var_str = format_pair_sigfig(energy_mean_history[end], energy_v
println("Final step: E = $(E_final_str), Var(E_L) = $(var_str)")
println("Reference energy: $(format_sigfig(E_ref; sigfigs=5))")

Logging.with_logger(Logging.NullLogger()) do
    redirect_stderr(devnull) do
        p1 = plot(t, ET_history, xlabel="step", ylabel="E_T", title="Referer
        display(p1)

        p2 = plot(t, population_history, xlabel="step", ylabel="N_w", title=
        display(p2)

        p3 = plot(t, energy_mean_history, xlabel="step", ylabel="<E_L>", tit
        plot!(p3, [t[1], t[end]], [E_ref, E_ref], ls=:dash, label="ref")
        display(p3)

        p4 = plot(t, energy_variance_history, xlabel="step", ylabel="Var(E_L
        display(p4)

        if !isempty(sim.walker_positions_history)
            snap = sim.walker_positions_history[end]
            x1 = [R[1] for R in snap]
            x2 = [R[2] for R in snap]
            p5 = scatter(x1, x2, xlabel="x1", ylabel="x2", title="Final walk
            display(p5)
        end
    end
end
end

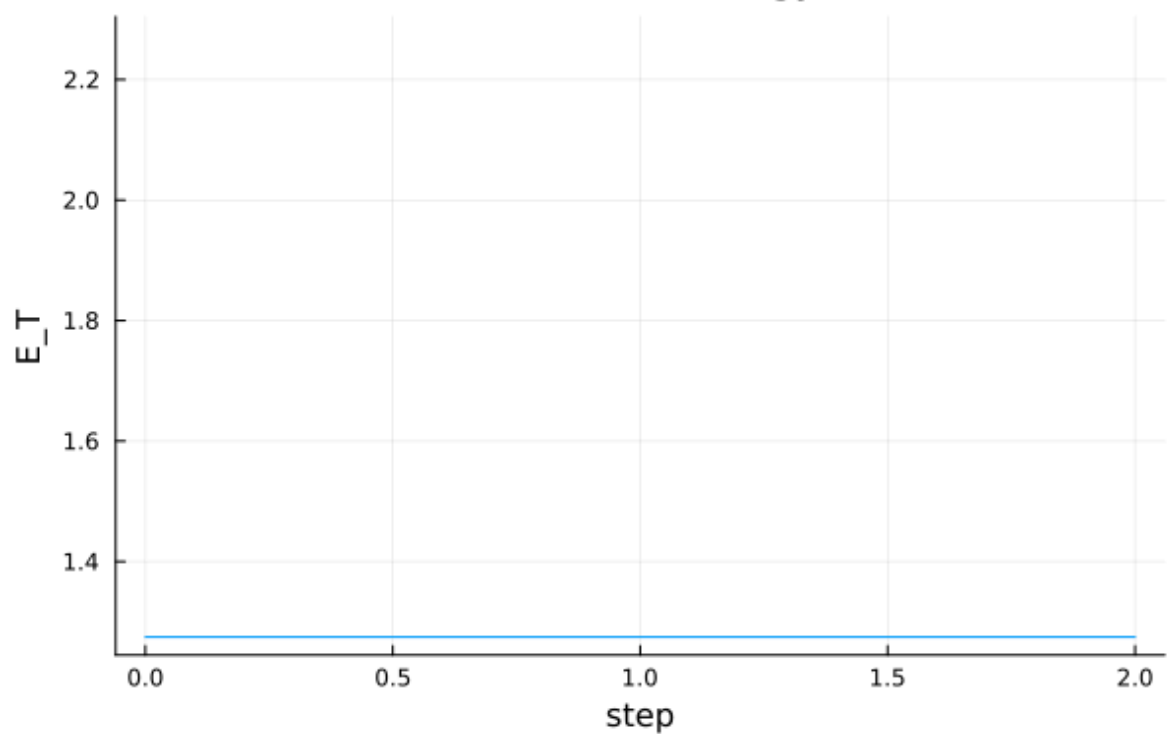
```

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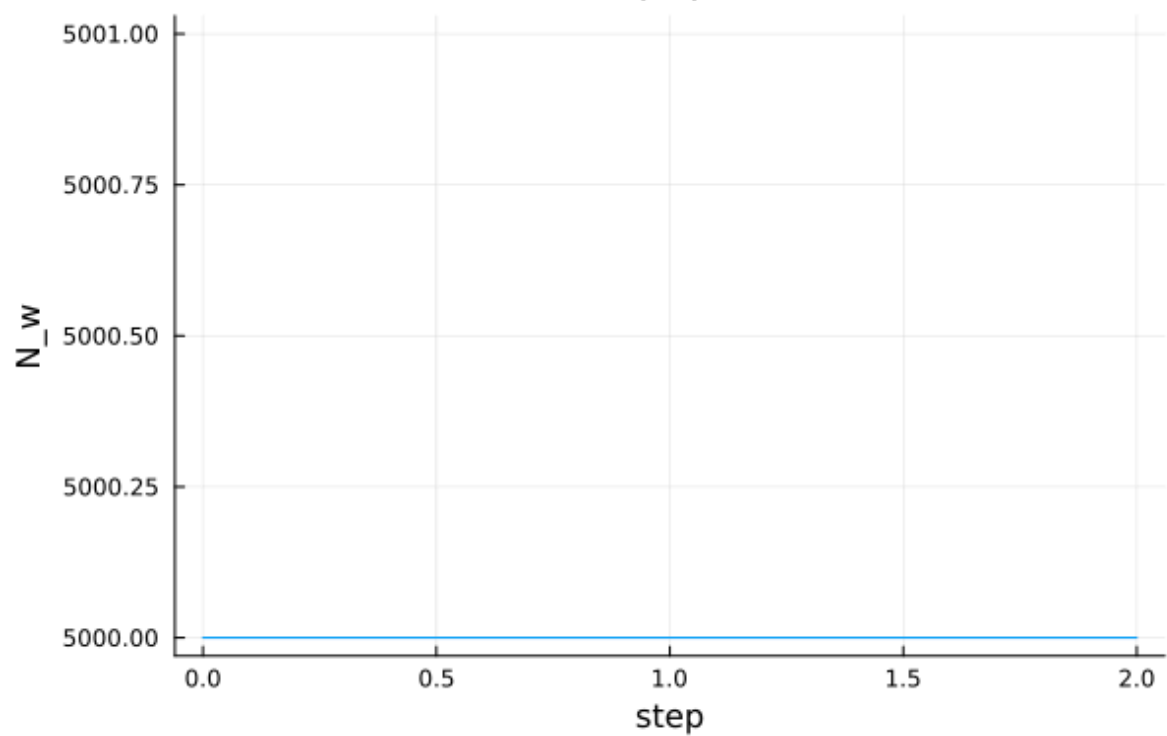
Coupled H0 DMC energy (post-eq, nequil=50): E = 1.27459666924148451 +/- 0.00
0000000000000005
Final step: E = 1.2745966692414854026793591401656, Var(E_L) = 0.000000000000
00000000000000041
Reference energy: 1.2746

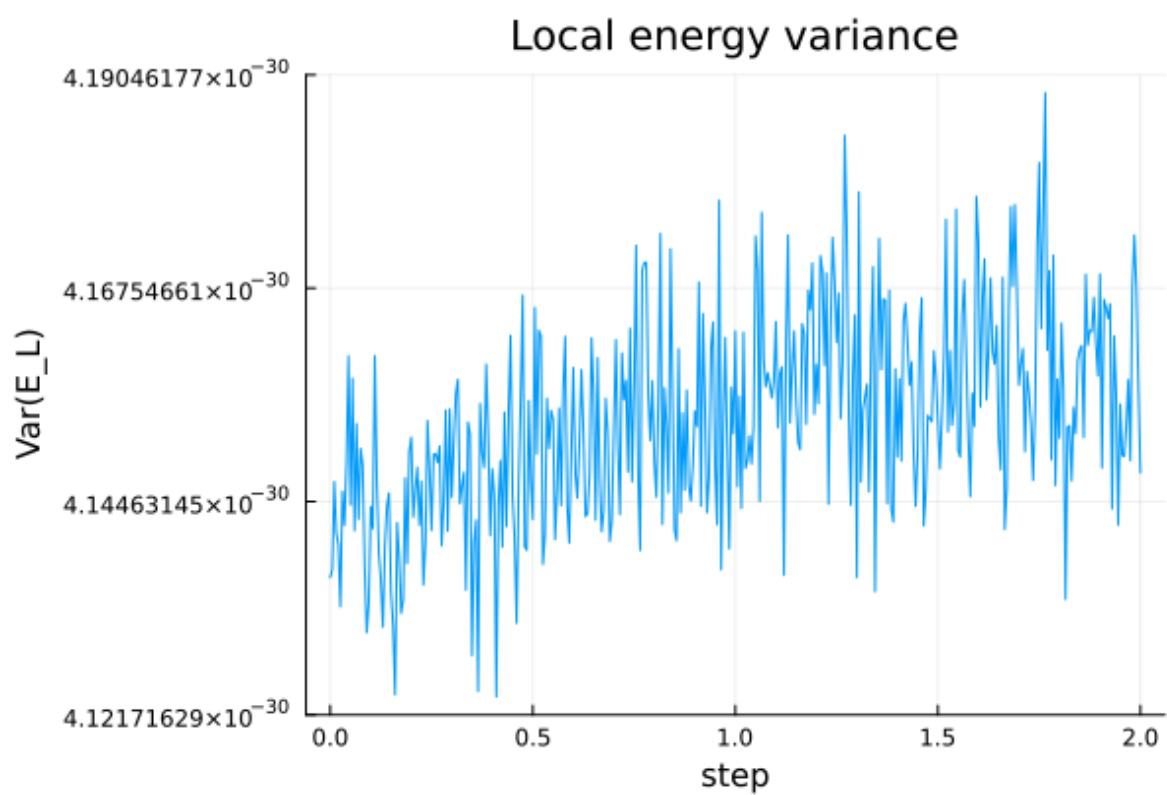
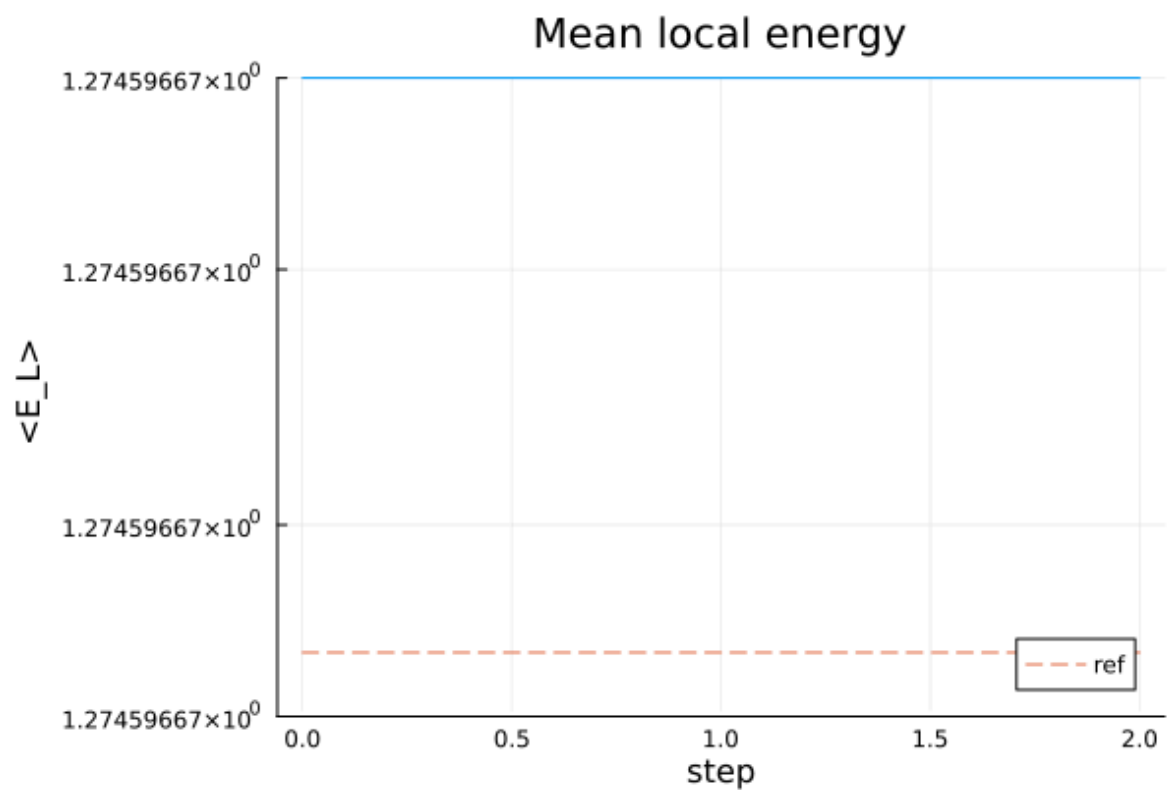
```

Reference energy



Walker population





Final walker distribution

