1. Evaluate the following determinants:

2. Given the matrix

$$A = \left(\begin{array}{ccccc} 1 & -2 & 1 & 3 & 4 \\ 1 & -1 & 0 & 2 & 4 \\ 2 & 1 & 3 & 1 & 2 \\ -1 & 0 & 1 & 1 & 3 \\ 0 & 1 & -1 & 1 & 3 \end{array}\right)$$

Use Gauss elimination to transform A in an upper triangular matrix  $\operatorname{Deduce}\,|A|$ 

3. Let

$$A = \left(\begin{array}{ccc} 1 & 2 & 0 \\ -1 & 3 & 0 \\ 0 & 1 & -1 \end{array}\right)$$

Evaluate |A| and deduce that A is invertible

Find the inverse of A by the cofactors method and then by the Gauss-Jordan method deduce from a) the determinant of  $A^{-1}$  and then calculate directly  $|A^{-1}|$ 

- 4. For what values of  $a \in IR$  the matrix  $A = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 2 & 4 \\ 1 & 3 & a \end{pmatrix} \in M_3(IR)$  is invertible? Find in this case, its inverse.
- 5. Show that a square matrix A is invertible if and only if  ${}^tA.A$  is invertible

Find the matrix A if 
$$(I + 2A)^{-1} = \begin{pmatrix} 2 & 5 & 5 \\ -1 & -1 & 0 \\ 2 & 4 & 3 \end{pmatrix}$$