

Самостоятельная работа №4
КНФ, ДНФ, СКНФ, СДНФ

Построить СКНФ, СДНФ и упростить их:

1. СКНФ

$$\bar{x} \vee y$$

СДНФ

$$\bar{x} \wedge \bar{y} \vee \bar{x} \wedge y \vee x \wedge y = \bar{x} \wedge \bar{y} \vee y = y \vee \bar{x}$$

2. СКНФ

$$(x \vee y) \wedge (x \vee \bar{y}) \wedge (\bar{x} \vee \bar{y}) = (x \vee x \wedge \bar{y} \vee x \wedge y) \wedge (\bar{x} \vee y) = x \wedge (\bar{x} \vee \bar{y}) = x \wedge \bar{y}$$

СДНФ

$$x \wedge \bar{y}$$

3. СКНФ

$$\begin{aligned} & (x \vee y \vee \bar{z}) \wedge (x \vee \bar{y} \vee z) \wedge (\bar{x} \vee y \vee \bar{z}) \wedge (\bar{x} \vee \bar{y} \vee \bar{z}) = \\ & (x \vee x \wedge \bar{y} \vee x \wedge z \vee x \wedge y \vee y \wedge z \vee x \wedge \bar{z} \vee \bar{y} \wedge \bar{z}) \wedge (\bar{x} \vee y \vee \bar{z}) \wedge (\bar{x} \vee \bar{y} \vee \bar{z}) = \\ & (x \vee y \wedge z \vee \bar{y} \wedge \bar{z}) \wedge (\bar{x} \vee y \vee \bar{z}) \wedge (\bar{x} \vee \bar{y} \vee \bar{z}) = \\ & (x \wedge y \vee x \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \vee y \wedge z \vee \bar{x} \wedge \bar{y} \wedge \bar{z} \vee \bar{y} \wedge \bar{z}) \wedge (\bar{x} \vee \bar{y} \vee \bar{z}) = \\ & (x \wedge y \vee x \wedge \bar{z} \vee y \wedge z \vee \bar{y} \wedge \bar{z}) \wedge (\bar{x} \vee \bar{y} \vee \bar{z}) = \\ & x \wedge y \wedge \bar{z} \vee x \wedge \bar{y} \wedge \bar{z} \vee x \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \vee \bar{x} \wedge \bar{y} \wedge \bar{z} \vee \bar{y} \wedge \bar{z} = \\ & x \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \vee \bar{y} \wedge \bar{z} \end{aligned}$$

СДНФ

$$\begin{aligned} & \bar{x} \wedge \bar{y} \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \vee x \wedge \bar{y} \wedge \bar{z} \vee x \wedge y \wedge \bar{z} = \\ & \bar{x} \wedge \bar{y} \wedge \bar{z} \vee x \wedge \bar{y} \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \vee x \wedge y \wedge \bar{z} = \\ & \bar{y} \wedge \bar{z} \wedge (\bar{x} \vee x) \vee \bar{x} \wedge y \wedge z \vee x \wedge y \wedge \bar{z} = \\ & \bar{y} \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \vee x \wedge y \wedge \bar{z} = \\ & \bar{y} \wedge \bar{z} \vee x \wedge y \wedge \bar{z} \vee \bar{x} \wedge y \wedge z = \\ & \bar{z} \wedge (\bar{y} \vee x \wedge y) \vee \bar{x} \wedge y \wedge z = \\ & \bar{y} \wedge \bar{z} \vee x \wedge \bar{z} \vee \bar{x} \wedge y \wedge z \end{aligned}$$