

Input Values	Expected Output	Actual = Expected?
10 random values in head	Random values ordered ascending (for fun)	Yes
Head and tail NULL, empty lists	Nothing	Yes
Head is 8 3 5 6, tail NULL	3 5 6 8 (baseline test)	Yes
Head is 2 1 0, tail NULL	0 1 2 (testing odd # input)	Yes
Head is 0 2 1 0, tail NULL	0 0 1 2 (testing repeats)	Yes
Head is values -1 through -10, in order	-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 (testing negative numbers)	Yes
Head is 1 2, tail is 30x the value 1	1 2 (ensuring that tail can be non-Null and the sort will function)	Yes
Head is 10 random numbers between -120 and 120	Random values ordered ascending (ensuring random and negative work together)	Yes
Head is random numbers with alternating sign	Random values ordered ascending (testing random and non-random values next to each other of unknowns size)	Yes
Head is the letter a	Some sort of code death (checking for alpha responses)	Yes

Analysis of regMergeSort:

Test Case #1:

We begin with the list head containing 6 5 3 8.

recMergeSort begins by allocating memory for a pointer to *otherHead, then checks if *head or (*head)->next are null, which they are not. Then recMergeSort calls divideList, passing head as 6 5 3 8 and otherHead as empty.

divideList begins by allocating memory for a middle and current list, then checks if the argument first1—in this case head—is NULL; if so it sets first2—otherHead—to be NULL as well. Even if the condition is not met the same thing happens if first1->next is NULL. As neither are true, first2 is not set to be NULL.

Otherwise, middle is set to be first1, containing 6 5 3 8. current is then set to 5 3 8, or first1->next.

As current is not NULL, current is again set to current->next, or 3 8.

Then, while current is not NULL, middle is set to middle->next, which is 5 3 8. current is then set to current->next to give 8. As this is not NULL, current is then set to NULL.

current is iterating through head twice as fast as middle, making middle the second half of head. This process continues, until current becomes NULL and the while loop exits.

After the while loop, `*first2` is set to be `middle->next`; this sets `otherHead` to be the second half of the list. `middle->next` is then set to `NULL`, after which `head` has been set to 6 5, and `otherHead` to be 3 8.

We then return to the first call of `recMergeSort`. At this point, `recMergeSort` is called with `head` as an argument.

At this second level of recursion, another `otherHead` is created, then `head` and `head->next` are checked to not be `NULL` (which they are not as `head` is 6 5 3 8). After this point, `divideList` is called again with `*head` and `&otherHead` as arguments.

`divideList`, through a similar process detailed above, sets `head` to be 6 5 and `otherHead` to contain 3 8. We then return to the second level recursion of `recMergeSort` with 6 5 3 8 as the argument, and call `recMergeSort` with `head` (6 5) as the argument.

At a third level of recursion, an `otherHead` is created, `head` and `head->next` are checked to not be `NULL` and `divideList` is called with `head` (6 5) and `otherHead` (empty) as arguments.

After `divideList` is called, `head` contains 6 and `otherHead` contains 5. At this point, `recMergeSort` is called with `head` (6) as an argument.

In this fourth level of recursion, as `head->next == NULL`, `recMergeSort` exits immediately, and the same occurs when it is next called by the third level of recursion with the argument `otherHead` (5).

In the third level of recursion, `*head` is then set to be the return value of `mergeList` with arguments `*head` and `otherHead`.

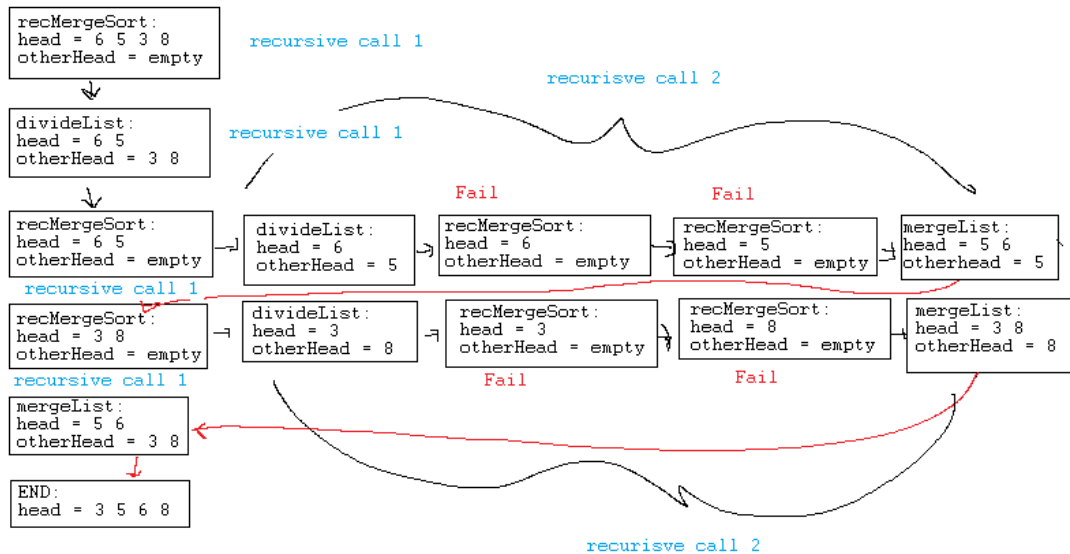
`mergeList` creates a pointer `*lastSmall` and `*newHead`, then checks if either of its arguments are `NULL`; if they are, the other list is returned immediately. As this is not the case, the flow proceeds.

The first node in `head` is then compared with the first node in `otherHead`; as $6 > 5$, the `if` statement is not executed and instead the `else` statement is.

This statement sets `newHead` to `otherHead`, sets `first2` equal to `first2->next` (which is `NULL`), and then sets `lastSmall` to be `newHead`.

As `first2` is now `NULL`, the `while` statement does not execute. The next `if` statement does not execute as `first1` is not `NULL`. `lastSmall` then has `head` appended to it, giving it the value 5 6. `newHead` is then returned, giving the third level recursion's head list the contents 5 6.

We then regress to the second level of recursion, where `recMergeSort` is called with the second level `otherHead` list 3 8.



`divideList` fills this third level recursion's `head` value with 3 and its `otherHead` value with 8. `recMergeSort` is called with both `head` and `otherHead` as arguments, failing both times as the next value in both arguments is NULL.

`mergeList` is then called; in the same process as above it fills `head` with 3 8, meaning the second level `otherHead` is set to 3 8 as well.

As both of the second recursion level's `recMergeSort` functions have executed, `head` is then set to the return value of `mergeList` is then called with the arguments `head` and `otherHead`, containing 5 6 and 3 8 respectively.

`mergeList` creates pointers for `lastSmall` and `newHead`, then as `first1` and `first2` are not null moves into its first else statement.

`first1->info` is the value 6 and `first2->info` is the value 3, and as $5 > 3$ the else statement is executed instead of the if statement.

This else fills `newHead` with `otherHead`, the values 3 8, then sets `first2=first2->next`, meaning `first2` now has the value 8.

The flow then moves into a while loop; the while loop's conditions are not met, so its first if statement is checked. This time $5 < 8$, so it executes instead of the else statement.

It sets `lastSmall->next` to be `first1`, so `lastSmall` contains 3 5 6. `lastSmall` is then set to be `lastSmall->next`, so `lastSmall` contains 5 6. Finally, `first1` is set to be `first1->next`, so `first1` contains 6.

The while loop is checked, and its conditions are not met, so `first1->info` is compared with `first2->info`. As $6 < 8$, the if statement is executed.

It sets lastSmall->next to be first1, so lastSmall contains 5 6. lastSmall is then set to be lastSmall->next, so lastSmall contains 6. Finally, first1 is set to be first1->next, so first1 contains NULL.

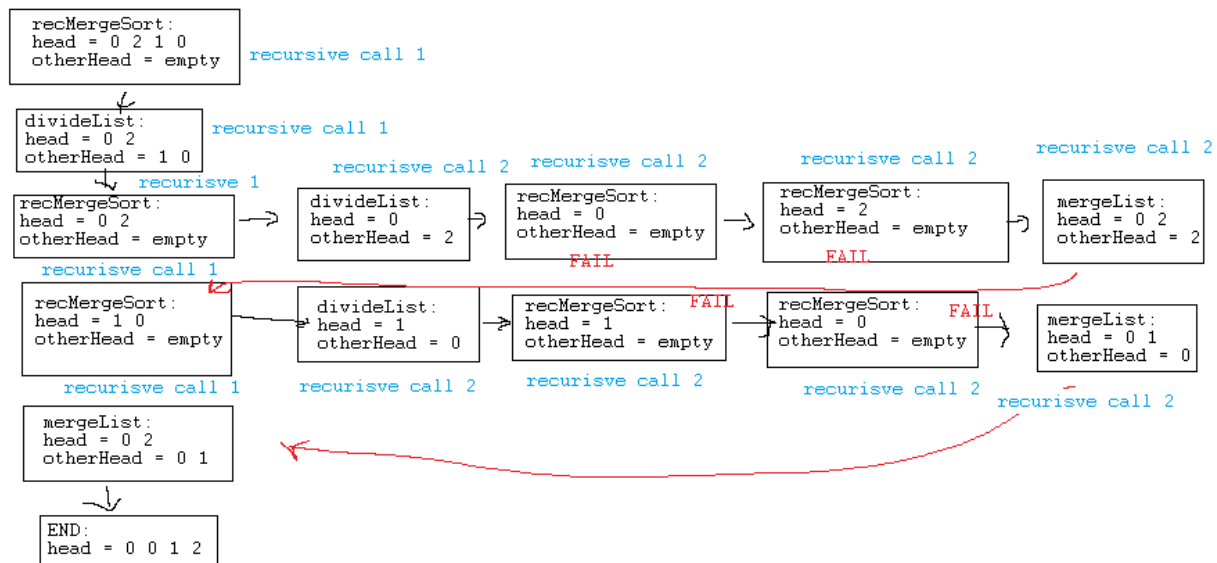
The while loop's conditions are met, so the next if statement is checked; first1 is indeed null so lastSmall->next is set to 8.

Finally, newHead with the values 3 5 6 8 is returned.

Test Case #2:

head is the values 0 2 1 0. otherHead is created empty, then passed to divideList with head. divideList creates middle = 0 2 1 0, and current = 2 1 0. As current is not null, current = 1 0. While current is not null, first middle = 2 1 0, and then current = 0; if current is not null, it is then = current->next = NULL.

The while loop is then checked; as its conditions are met, it ends, and otherHead is set to be 1 0, while head is set to be 0 2.



The program behaves very similarly to test case one; next the list otherHead, containing 1 0, is divided into 1 and 0, then recMergeSort is attempted upon these one node lists and fails. mergeList is called with arguments 1 and 0, and results in 0 1.

The same happens to head, where its values of 0 2 are put into recMergeSort and then divideList, where its otherHead is set to 2 and head is set to 0. recMergeSort is attempted on these and fails, when mergeList is called with arguments 0 and 2, returning 0 2.

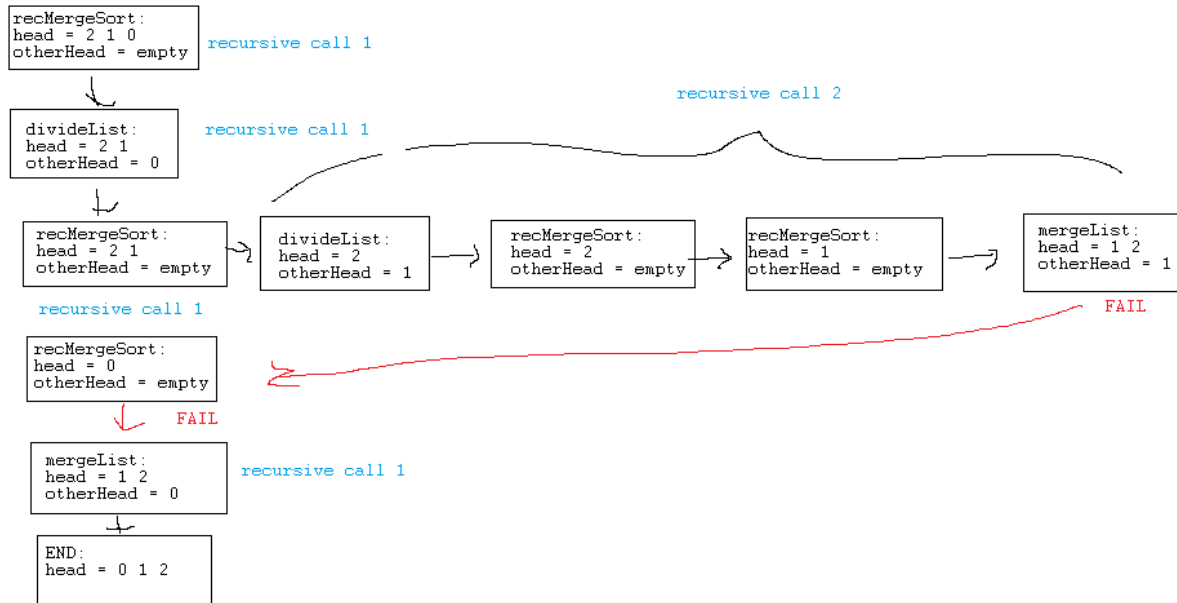
However, the crux of this test case comes at this point, when recMergeSort has been carried out on the original, first-recursion head and otherHead. mergeList is called with head=0 2 and otherHead = 0 1.

At first, `first1->info` is not less than `first2->info` as they are equal, so the else loop is executed, with `newHead` being set to 0 1. `first2` is then set to 1, and `lastSmall` is set to the `newHead` value of 0 1.

Then, as neither `first1` nor `first2` are NULL, and `first1->info` is not less than `first2->info`, this process repeats until we are left with head equal to 0 0 1 2.

Test Case #3:

With three nodes, things become slightly more complicated. Head = 2 1 0. The first recursive call behaves normally, however, when asked to split the three node list in half we get an



interesting result.

Passed to the function `divideList`, `first1 = 2 1 0` and `first2` is empty. `Middle = 2 1 0`, and `current = 1 0`. As `1 0` is not `NULL`, `current` then becomes `0` and we move into the while loop. However, when we are in the while loop, `middle` becomes `1 0` and `current` becomes `NULL` before the if statement, and `first2` becomes `middle->next` which is `0`. We then have two sublists of differing size; one fails immediately as it is only one element, and the other is parsed, sorted and returned as normal. When both these tasks are done, `mergeList` merges them to get the result `0 1 2`.

Test Case #4:

We begin with head = NULL.
otherHead is created, but the first if
statement is not satisfied, so the
function ends without performing
any other actions.

