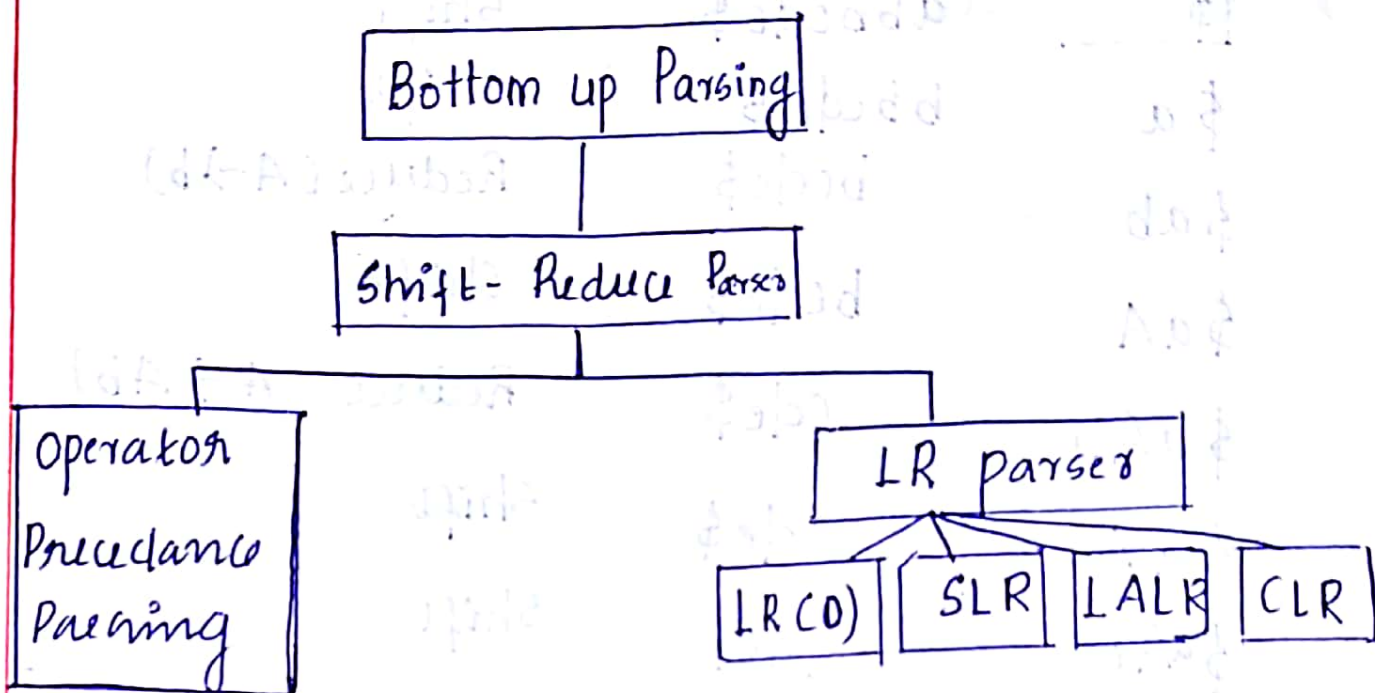


16/2/2018

Module - III



Shift Reduce Parsing:

eg:

Consider the following set of production:

$S \rightarrow aAcBe$

$A \rightarrow Ab / b$

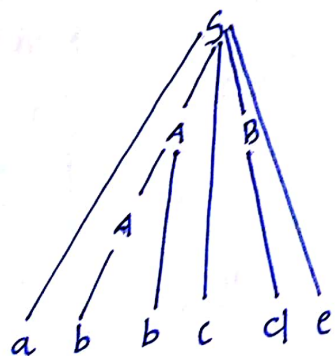
$B \rightarrow d$

Shift reduce parsing of input is done as follows:



Stack	Input buffer	Operation
\$	abbcd\$	Shift
\$a	bcbcd\$	Shift
\$ab	bcbcd\$	Reduce ($A \rightarrow b$)
\$aA	bcdcd\$	Shift
\$aAb	bcdcd\$	Reduce ($A \rightarrow Ab$)
\$aA	cde\$	Shift
\$aA	cde\$	Shift
\$aAc	de\$	Shift
\$aAc	e\$	Shift
\$aAc	e\$	reduce ($B \rightarrow d$)
\$aAcB	\$	reduce ($A \rightarrow aAcBe$)
\$aAcBe	\$	accept string
\$S		

Parse Tree:



Operator Precedence Parsing:
It is applied to ~~all~~ ^{some} class of grammars.

Operator grammar has two important characteristics:

- 1) There is no ϵ production in grammar.
- 2) Production should not have two adjacent variables.

eg: for operator grammar:

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow id$$

eg: for non-operator grammar:

$$E \rightarrow EPE$$

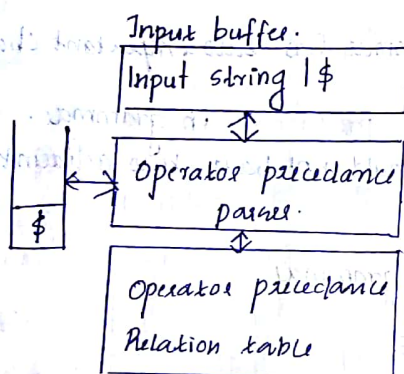
$$P \rightarrow * / +$$

$$E \rightarrow id$$

Components Operator

- 1) Input buffer.
- 2) Stack \rightarrow Top element is '\$'

- 3) Operator precedence Parser.
- 4) Operator precedence Relation table



Precedence relation between a and b is given below

Relation	meaning
$a > b$	a has higher precedence than b
$b > a$	a has lower precedence than b .
$a = b$	Equal precedence.

Q: Operator precedence ~~table~~ for below grammar.

$E \rightarrow E + E$

$E \rightarrow E * E$

$E \rightarrow id$

terminals - $+, *, id, \$$

	id	$+$	$*$	$\$$
id	$-$	$>$	$>$	$>$
$+$	$<$	$>$	$<$	$>$
$*$	$<$	$>$	$>$	$>$
$\$$	$<$	$<$	$>$	$-$

Parsing Algorithm:

if ($\$$ is on Tos and $\$$ is in input)
 then accept
 else
 { if (a is on Tos and b is an input)
 if ($a < b$ or $a = b$)
 then shift b onto Tos
 else if ($a > b$)
 then reduce.

```

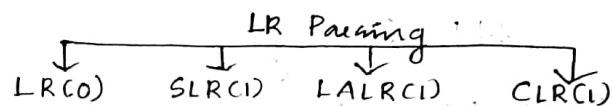
else
    print(error);
}

```

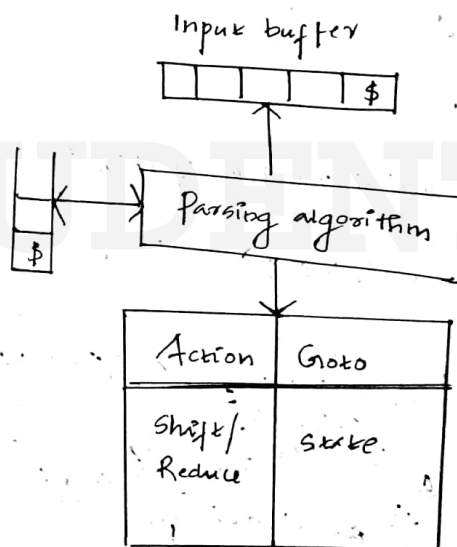
Parse the input string "id + id"

Stack	Input	Operation
\$	id + id \$	\$ \rightarrow id, shift
\$id	+ id \$	id \rightarrow +, reduce
\$E	+ id \$	\$ \rightarrow +, shift
\$E +	id \$	+ \rightarrow id, shift
\$E + id	\$	id \rightarrow \$, reduce $E \rightarrow id$
\$E + E	\$	+ \rightarrow \$, reduce $E \rightarrow E + E$
\$E	\$	Accept

$E \rightarrow E + E$
 $E \rightarrow E * E$
 $E \rightarrow id$



LR -
 SLR - Simple
 LALR - Look ahead
 CLR - Canonical



SLR Parsing

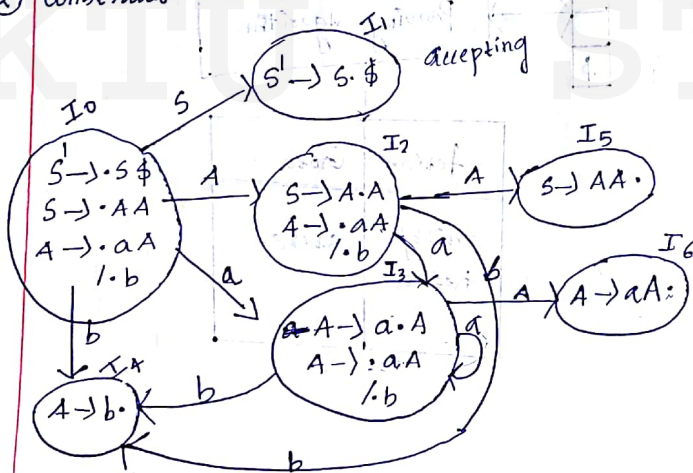
- Simple LR parsing
- Bottom up parsing technique

eg. $S \rightarrow AA$
 $A \rightarrow aA$
 $A \rightarrow b$

① Construct augmented grammar.

$S' \rightarrow S\$$
 $S \rightarrow AA$
 $A \rightarrow aA$
 $A \rightarrow b$

② Construct canonical collection of LR(0) items.



Number the productions

$S \rightarrow AA$ — (1)

$A \rightarrow aA$ — (2)

$A \rightarrow b$ — (3)

Follow(S) = $\{\$ \}$

Follow(A) = $\{a, b\}$

Now construct parsing table:

State	Action			Goto	
	a	b	\$	S	A
0	S ₃	S ₄		1	2
1			Accept		
2	S ₃	S ₄			5
3	S ₃	S ₄			6
4	r ₃	r ₃			
5			r ₁		
6	r ₂	r ₂			

Q Construct SLR parsing table for below grammar.

$S \rightarrow dA$ — ①

$/aB$ — ②

$A \rightarrow bA$ — ③

$/c$ — ④

$B \rightarrow bB$ — ⑤

$/c$ — ⑥

A augmented grammar

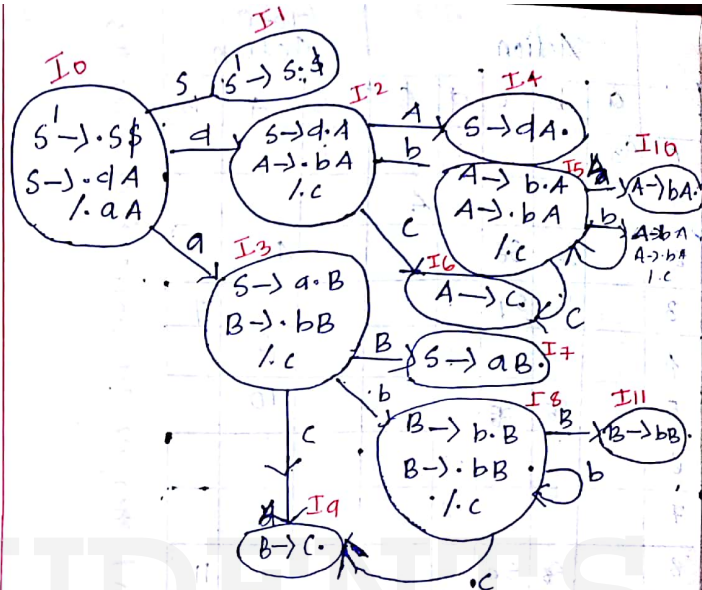
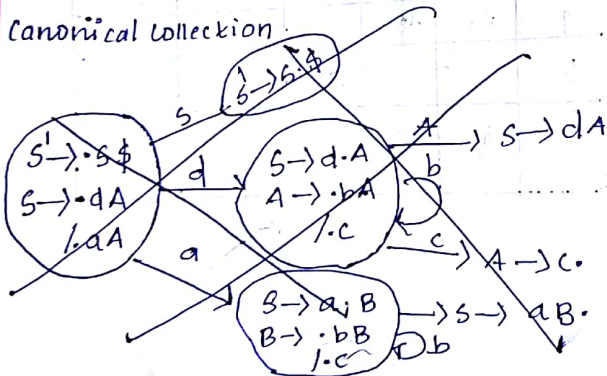
$S' \rightarrow s \$$

$S \rightarrow dA/aB$

$A \rightarrow bA/c$

$B \rightarrow bB/c$

Canonical collection



Follow ($A \$$) = { \$ }

Follow (A) = { \$ }

Follow (B) = { \$ }

	Action					Goto Action		
	a	b	c	d	\$	S	A	B
0	S ₃			S ₂		1		
1				A				
2		S ₅	S ₆			4		
3		S ₈	S ₉				7	
4				A			10	
5		S ₅	S ₆				10	
6				A				
7				A				
8		S ₈	S ₉				11	
9				A				
10				A				
11				A				

eg follow(a) → \$ then we can write item 10 like 9, 3

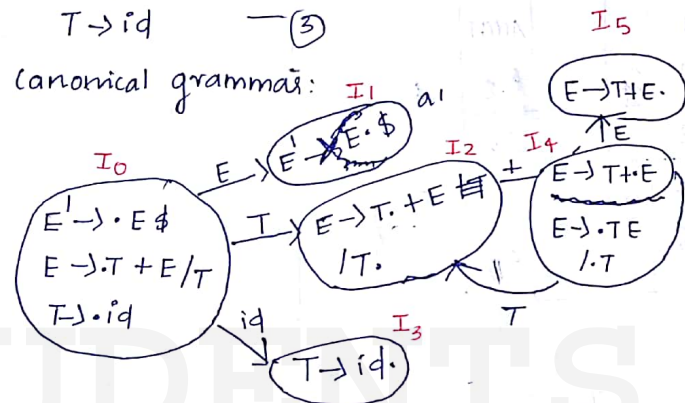
Q Construct SLR parsing table for below grammar.

$E \rightarrow T + E$
 $T \rightarrow id$

augmented grammar

$E' \rightarrow E\$$ —
 $E \rightarrow T + E$ — (1)
 $T \rightarrow id$ — (2)

canonical grammar:



$\text{follow}(E) = \{ \$ \}$

$\text{follow}(T) = \{ \$, + \}$

	Action			goto	
	+	id	\$	E	T
0		S_3		1	2
1			ACCEPT		
2	S_4		R_2	4	
3			R_3		
4				5	2
5			R_6		

I_2
 $E \rightarrow T \cdot TE$
 $| T \cdot$

$+ \rightarrow S_4$

T is reduced in (2)

+
5 s/r

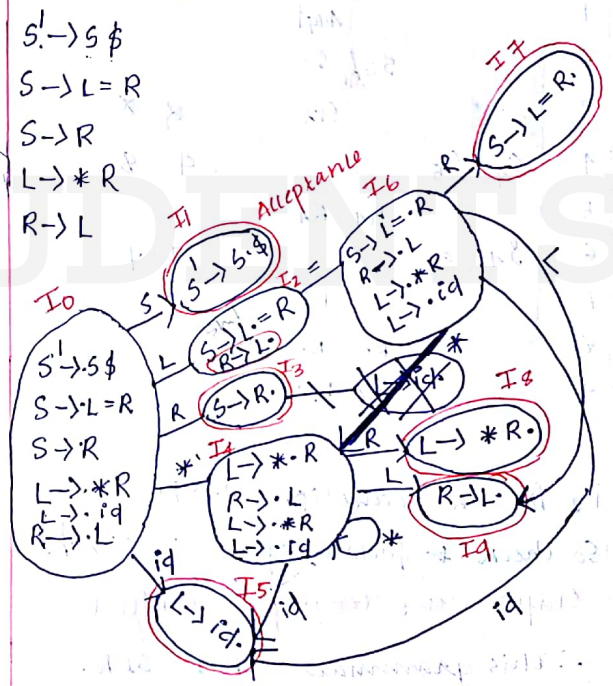
Shift Reduce Conflict
 Reduce Reduce Conflict

1/3/2018

Note
 Every SLR(1) grammar is unambiguous. But there are many unambiguous grammars that are not SLR(1)

eg:
 $S \rightarrow L = R$ - (1)
 $S \rightarrow R$ - (2)
 $L \rightarrow * R$ - (3)
 $L \rightarrow id$ - (4)
 $R \rightarrow L$ - (5)

Soln



$\text{follow}(S) = \{ \$ \}$

$\text{follow}(L) = \{ =, \$ \}$

$\text{follow}(R) = \{ =, \$ \}$

Parsing table.

	ACTION				Goto		
	*	id	=	\$	S	L	R
0	S ₄	S ₅			1	2	3
1			Accept				
2			S ₆ / R ₅				
3			R ₂				
4	S ₄	S ₅				9	8
5			R ₄	R ₄			
6	S ₄	S ₅				9	7
7			R ₁				
8			R ₃	R ₃			
9			R ₄	R ₄			

I_2 has a reduction $R \rightarrow L$.

So check follow of $R = \{ =, \$ \}$

Shift reduce conflict conflict

\therefore this grammar is not SLR.

• Reduce-Reduce Conflict

I_1

$A \rightarrow \alpha \cdot$

$B \rightarrow \beta \cdot$

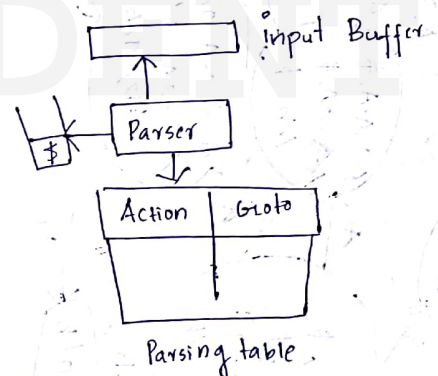
$\text{follow}(A) \cap \text{follow}(B) \neq \emptyset$

CLR(1) Parsing

• LR parsing technique

CLR - Canonical LR

Require canonical collection of LR(1) items

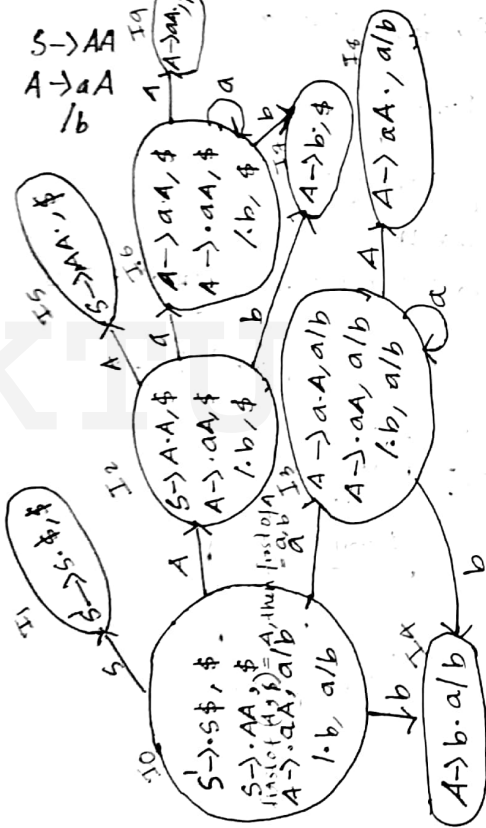


LR(0) SLR(1) CLR LALR
 need LR(0) items LR(1) items

LR(1) items = LR(0) items + look ahead

eg:

$S \rightarrow AA$
 $A \rightarrow aA$
 $A \rightarrow b$



Go to move don't have lookahead changes

	Action			GoTo	
	a	b	\$	S	A
0	S3	S4		1	2
1			A6		
2	S6	S4			5
3	S3	S4			8
4	r3	r3			
5			r1		
6	S6	S4			9
7			r3		
8	r2	r2			
9			r2		

$S \rightarrow AA$ - ①
 $A \rightarrow aA$ - ②
 $A \rightarrow b$ - ③

3/3/18

LALR(1) parsing table for above grammar

Identify same items with different look ahead
 if any such item sets are present form a new
 state by merging similar items.

$I_3, I_6 \rightarrow I_{36}$

$I_8, I_9 \rightarrow I_{89}$

$I_4, I_7 \rightarrow I_{47}$

	ACTION			GOTO	
	a	b	\$	S	A
0	S ₃₆	S ₄₇		1	2
1			Accept		
2	S ₃₆	S ₄₇			5
36	3	S ₃₆	S ₄₇		89
47	4	A ₃	A ₃		
	5		A ₁		
89	8	A ₂	A ₂		

11/10/16

LALR

- look ahead LR parser
- size of the CLR parsing table is large compared to other parsing technique
- LALR reduces the size of CLR parsing
- CLR is merged with δ

Q Construct SLR parsing table for below grammar.

$S \rightarrow L = R / R$

$L \rightarrow * R / id$

$R \rightarrow L$

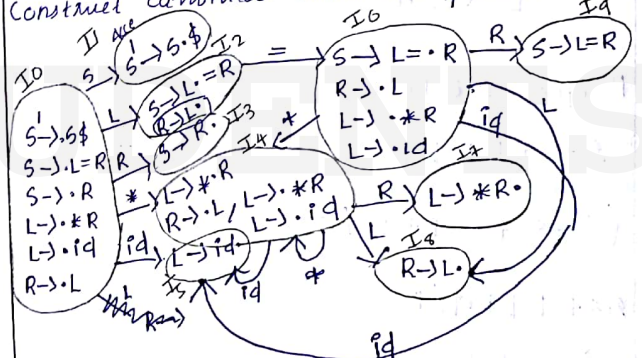
Solⁿ Construct augmented grammar.

$S' \rightarrow S \$$

$S \rightarrow * R / id$

$R \rightarrow L$

Construct canonical collection of LR(0) items



$Follow(S) = \{ \$ \}$

$Follow(L) = \{ =, \$ \}$

$Follow(R) = \{ =, \$ \}$