IT2120 - Probability and Statistics

Lab Sheet 08

Exercise

```
Console Terminal × Background Jobs ×

R 4.4.0 · C:/Users/it24100387/Desktop/IT24100387/

> setwd("C:\\Users\\it24100387\\Desktop\\IT24100387")
> getwd()

[1] "C:/Users/it24100387/Desktop/IT24100387"
> data<-read.table("Exercise - LaptopsWeights.txt", header=TRUE)
> fix(data)
> attach(data)
>
```

1. Calculate the population mean and population standard deviation of the laptop bag weights.

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Console Terminal ×
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> # Q1
> # Laptop bag weights
> Weight <- c(2.46, 2.45, 2.47, 2.71, 2.46, 2.05, 2.6, 2.42, 2.43, 2.53,
              2.57, 2.85, 2.7, 2.53, 2.28, 2.2, 2.57, 2.89, 2.51, 2.47,
              2.66, 2.06, 2.41, 2.65, 2.76, 2.43, 2.61, 2.57, 2.73, 2.17,
              2.67, 2.05, 1.71, 2.32, 2.23, 2.76, 2.7, 2.13, 2.75, 2.2)
> # Population mean and standard deviation
> # Population mean and standard deviation
> pop_mean <- mean(Weight)
> pop_sd <- sd(Weight)</pre>
> pop_mean
[1] 2.468
> pop_sd
[1] 0.2561069
```

2. Draw 25 random samples of size 6 (with replacement) and calculate the sample mean and sample standard deviation for each sample.

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> set.seed(123) # For reproducibility
> # Create a matrix with 6 rows (sample size), 25 columns (samples)
> samples <- matrix(nrow = 6, ncol = 25)</pre>
> # Fill matrix with random samples
> for (i in 1:25) {
   samples[, i] <- sample(Weight, 6, replace = TRUE)</pre>
> # Sample means and standard deviations
> sample_means <- apply(samples, 2, mean)
> sample_sds <- apply(samples, 2, sd)</pre>
> # Create a table of results
> sample_stats <- data.frame(</pre>
   Sample = 1:25,
    Mean = round(sample_means, 4),
   SD = round(sample_sds, 4)
+ )
```

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Console
        Terminal ×
                   Background Jobs ×
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  print(sample_stats)
   Sample
            Mean
1
        1 2.5300 0.1514
2
        2 2.5733 0.1191
3
        3 2.4733 0.1719
4
        4 2.5917 0.1345
5
        5 2.4567 0.2749
6
        6 2.4017 0.2544
7
        7 2.5900 0.2167
8
        8 2.4667 0.4530
9
        9 2,4017 0,2230
10
       10 2.3350 0.3238
11
       11 2.5867 0.1706
12
       12 2.3783 0.3236
13
       13 2.3817 0.2994
14
       14 2.4650 0.2315
       15 2.4850 0.1746
15
16
       16 2.4517 0.2763
17
       17 2.3850 0.2042
18
       18 2.3383 0.2437
19
       19 2.4283 0.2481
20
       20 2.5517 0.2654
21
       21 2.5383 0.1708
22
       22 2.4667 0.2452
23
       23 2.4700 0.2406
24
       24 2.4483 0.2792
25
       25 2.4750 0.2359
>
```

3. Calculate the mean and standard deviation of the 25 sample means and state the relationship of them with true mean and true standard deviation.

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Console Terminal × Background Jobs ×
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> #Q3
> # From previous steps
> sample_mean_of_means <- mean(sample_means)</pre>
> sample_sd_of_means <- sd(sample_means)</pre>
> # Population SD from Q1 was:
> # pop_sd = 0.2169 (already calculated)
> # Sample size
> n <- 6
> # Theoretical SD of sample means
> theoretical_sd_of_means <- pop_sd / sqrt(n)
> # Print all
> sample_mean_of_means
[1] 2.4668
> sample_sd_of_means
[1] 0.07624874
> theoretical_sd_of_means
[1] 0.1045552
```