

IT24104178-JAYASURIYA J.A.Y.N-LAB6

1. An IT company claims that their newly developed learning platform improves student performance in online tests. According to previous data, 85% of students who used the platform passed their online tests. A batch of 50 students is selected at random who have completed the course using this platform. Let X denote the number of students who passed the test out of 50 students.

i. What is the distribution of X ?

ii. What is the probability that at least 47 students passed the test?

```
> setwd("C:\\Users\\ASUS\\Downloads\\IT24100500")
> getwd()
[1] "C:/Users/ASUS/Downloads/IT24100500"
> #PART 1
> # i) Distribution:
> #  $X \sim \text{Binomial}(n = 50, p = 0.85)$ 
>
> # ii)  $P(X \geq 47) = 1 - P(X \leq 46) = 1 - \text{pbinom}(46, \text{size}=50, \text{prob}=0.85)$ 
> n <- 50
> p <- 0.85
>
> prob_at_least_47 <- 1 - pbinom(46, size = n, prob = p)
> prob_at_least_47
[1] 0.04604658
```

2. A call center receives an average of 12 customer calls per hour.

i. What is the random variable (X) for the problem?

ii. What is the distribution of X ?

iii. What is the probability that exactly 15 calls are received in an hour?

```
> #PART 2
> # i) Random variable  $X$  = number of calls in an hour
> # ii) Distribution:  $X \sim \text{Poisson}(\lambda = 12)$ 
>
> # iii) Probability exactly 15 calls in an hour:
> lambda <- 12
> prob_exactly_15 <- dpois(15, lambda)
> prob_exactly_15
[1] 0.07239112
>
> cat(sprintf("P(X >= 47) for Binomial(50,0.85) = %.12f\n", prob_at_least_47))
P(X >= 47) for Binomial(50,0.85) = 0.046046578892
> cat(sprintf("P(X = 15) for Poisson(12) = %.12f\n", prob_exactly_15))
P(X = 15) for Poisson(12) = 0.072391120147
```

| Values | |
|------------------|--------------------|
| lambda | 12 |
| n | 50 |
| p | 0.85 |
| prob_at_least_47 | 0.0460465788923019 |
| prob_exactly_15 | 0.0723911201466387 |