

Sri Lanka Institute of Information Technology



Lab Submission

Lab Sheet 09

IT24102699
Mummullage B.U.T

Probability and Statistics| IT2120

B.Sc. (Hons) in Information Technology

Self-Try Codes

1. Let's suppose that a student is interested in estimating how many memes their professors know and love. So they go to class, and every time a professor uses a new meme, they write it down. After a year of classes, the student has recorded the following meme counts, where each count corresponds to a single class they took:

3, 7, 11, 0, 7, 0, 4, 5, 6, 2

Test whether on average, professors know 3 memes at 5% level of significance.

```
IT24102699_Self_Try_Codes.R* x IT24102699.R x
Source on Save Run
1
2 # IT24102699
3
4 # Mummullage B.U.T
5
6 # IT2120 - Probability and Statistics - Lab 08
7
8 getwd()
9 setwd("F:\\SLIIT\\_Year_02\\Semester 01\\PS - Probability and Statistics\\Lab Practicals\\Lab 09\\IT24102699")
10 getwd()
11
12
13 ## Question 01
14
15 # Since the true variance is unknown and sample size is less than 30,
16 # we can apply one sample t-test.
17 # Hypothesis: H0: u = 3 Vs H1: u = 3
18 # Consider 5% level of significance
19 # To run the one-sample t test, "t.test" command can be used as follows.
20 x<-c(3, 7, 11, 0, 7, 0, 4, 5, 6, 2)
21 t.test(x, mu = 3)
22
23 # P value approach will be used to get the conclusion of hypothesis testing.
24 # Conclusion: Since p value (0.2012) is greater than 0.05, do not reject H0 at 5% level of significance.
25 # Therefore, we can conclude that the true average number of memes that professors know is not
26 # significantly different from 3 (exactly equal to 3).
27
28:1 (Top Level) :
Console Terminal Background Jobs x
R 4.5.1 · F:\\SLIIT\\_Year_02\\Semester 01\\PS - Probability and Statistics\\Lab Practicals\\Lab 09\\IT24102699/
> x<-c(3, 7, 11, 0, 7, 0, 4, 5, 6, 2)
> t.test(x, mu = 3)

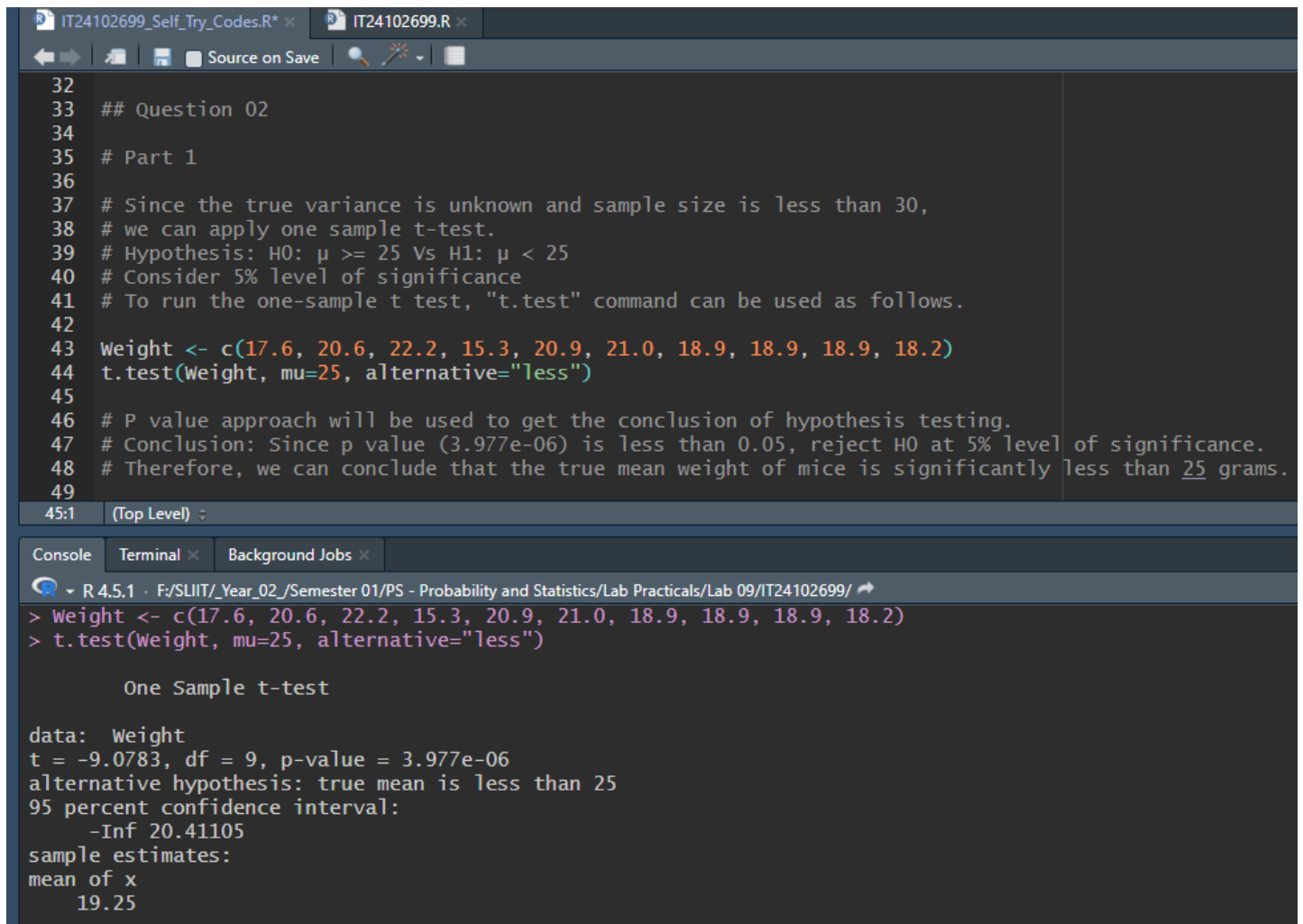
One Sample t-test

data: x
t = 1.3789, df = 9, p-value = 0.2012
alternative hypothesis: true mean is not equal to 3
95 percent confidence interval:
 2.0392 6.9608
sample estimates:
mean of x
 4.5
```

2. Let's consider the weight of 10 mice in gram:

17.6, 20.6, 22.2, 15.3, 20.9, 21.0, 18.9, 18.9, 18.9, 18.2.

- i. Test whether the true mean weight of mice is less than 25g at 5% level of significance.



```
IT24102699_Self_Try_Codes.R* x IT24102699.R x
Source on Save
32
33 ## Question 02
34
35 # Part 1
36
37 # Since the true variance is unknown and sample size is less than 30,
38 # we can apply one sample t-test.
39 # Hypothesis: H0:  $\mu \geq 25$  Vs H1:  $\mu < 25$ 
40 # Consider 5% level of significance
41 # To run the one-sample t test, "t.test" command can be used as follows.
42
43 Weight <- c(17.6, 20.6, 22.2, 15.3, 20.9, 21.0, 18.9, 18.9, 18.9, 18.2)
44 t.test(Weight, mu=25, alternative="less")
45
46 # P value approach will be used to get the conclusion of hypothesis testing.
47 # Conclusion: Since p value (3.977e-06) is less than 0.05, reject H0 at 5% level of significance.
48 # Therefore, we can conclude that the true mean weight of mice is significantly less than 25 grams.
49
45:1 (Top Level)
Console Terminal x Background Jobs x
R 4.5.1 · F:/SLIIT/Year_02/Semester 01/PS - Probability and Statistics/Lab Practicals/Lab 09/IT24102699/
> Weight <- c(17.6, 20.6, 22.2, 15.3, 20.9, 21.0, 18.9, 18.9, 18.9, 18.2)
> t.test(Weight, mu=25, alternative="less")

One Sample t-test

data: Weight
t = -9.0783, df = 9, p-value = 3.977e-06
alternative hypothesis: true mean is less than 25
95 percent confidence interval:
 -Inf 20.41105
sample estimates:
mean of x
19.25
```

- ii. Obtain the value of test statistic, p-value and confidence interval out of the test results separately using suitable R codes.

```
51
52 # Part 2
53 # To obtain each value separately, we need to store the results of the hypothesis testing into a variable.
54 # Accordingly, results were stored into "res" variable.
55 res <- t.test(weight, mu=25, alternative="less")
56
57 # To extract test statistic, use "res$statistic" command as follows.
58 res$statistic
59
60 # To extract p value for the test, use "res$p.value" command as follows.
61 res$p.value
62
63 # To extract confidence interval for the test, use "res$conf.int" command as follows.
64 res$conf.int
65
```

```
Console Terminal Background Jobs
R 4.5.1 · F:/SLIIT/Year_02/Semester 01/PS - Probability and Statistics/Lab Practicals/Lab 09/IT24102699/
> # Part 2
> # To obtain each value separately, we need to store the results of the hypothesis testing into a variable.
> # Accordingly, results were stored into "res" variable.
> res <- t.test(weight, mu=25, alternative="less")
>
> # To extract test statistic, use "res$statistic" command as follows.
> res$statistic
      t
-9.078319
>
> # To extract p value for the test, use "res$p.value" command as follows.
> res$p.value
[1] 3.976692e-06
>
> # To extract confidence interval for the test, use "res$conf.int" command as follows.
> res$conf.int
[1] -Inf 20.41105
attr(,"conf.level")
[1] 0.95
>
```

3. The Sugar level of a Cookie follows a normal distribution with mean 9.8 and the standard deviation 0.05. Let's take a sample of size 30.

- i. Generate 30 random numbers (sugar levels) from the above distribution.

```
69
70 ## Question 03
71
72 # Part 1
73
74 # To generate random numbers from a Normal distribution, we can use "rnorm" command as follows.
75 y <- rnorm(30, mean = 9.8, sd = 0.05)
76
```

```
Console Terminal Background Jobs
R 4.5.1 · F:/SLIIT/Year_02/Semester 01/PS - Probability and Statistics/Lab Practicals/Lab 09/IT24102699/
> ## Question 03
>
> # Part 1
>
> # To generate random numbers from a Normal distribution, we can use "rnorm" command as follows.
> y <- rnorm(30, mean = 9.8, sd = 0.05)
>
```

- ii. Test whether the mean sugar level of the Cookies is greater than 10 at 5% level of significance.

```
IT24102699_Self_Try_Codes.R* x IT24102699.R x
Source on Save
77
78 # Part 2
79
80 # Since the true variance is known we can apply one sample z-test.
81 # Hypothesis: H0:  $\mu \leq 10$  Vs H1:  $\mu > 10$ 
82 # Consider 5% level of significance
83 # To run the one-sample z test, "t.test" command can be used as follows.
84 # When samples are large enough, t distribution can be approximated into Normal distribution.
85 # So that same command ("t.test") can be used for one sample z test.
86
87 t.test(y, mu=10, alternative="greater")
88
89 # P value approach will be used to get the conclusion of hypothesis testing.
90 # Conclusion: Since p value (1) is greater than 0.05, do not reject H0 at 5% level of significance.
91 # Therefore, we can conclude that the true mean sugar level of a cookie is less than or equal to 10.
92 # Note that based on the random numbers you got as the sample, results of the test will be different.
93
94
87:40 (Top Level) :

Console Terminal x Background Jobs x
R 4.5.1 · F:/SLIIT/Year_02/Semester 01/PS - Probability and Statistics/Lab Practicals/Lab 09/IT24102699/ ➔
> t.test(y, mu=10, alternative="greater")

One Sample t-test

data: y
t = -23.043, df = 29, p-value = 1
alternative hypothesis: true mean is greater than 10
95 percent confidence interval:
 9.791583      Inf
sample estimates:
mean of x
 9.805895

> |
```

Exercise

Instructions: Create a folder in your desktop with your registration number (Eg: "IT....."). You need to save the R script file and take screenshots of the command prompt with answers and save it in a word document inside the folder. Save both R script file and word document with your registration number (Eg: "IT....."). After you finish the exercise, zip the folder and upload the zip file to the submission link.

1. Assume that the time taken to bake a batch of cookies is normally distributed with mean 45 minutes and standard deviation 2 minutes.
 - i. Generate a random sample of size 25 for the baking time.
 - ii. Test whether the average baking time is less than 46 minutes at a 5% level of significance.

```
8 setwd("F:\\SLIIT\\_Year_02\\Semester 01\\PS - Probability and Statistics\\Lab Practicals\\Lab 09\\IT24102699")
9 getwd()
10
11
12 # Exercise
13
14 # Part i
15
16 baking_times <- rnorm(25, mean = 45, sd = 2)
17 print(baking_times)
18
19
20 # Part ii
21
22 t.test(baking_times, mu = 46, alternative = "less")
23
```

23:1 (Top Level) ▾

Console Terminal Background Jobs

R 4.5.1 · F:/SLIIT/_Year_02/Semester 01/PS - Probability and Statistics/Lab Practicals/Lab 09/IT24102699/ ↗

```
>
> # Exercise
>
> # Part i
>
> baking_times <- rnorm(25, mean = 45, sd = 2)
> print(baking_times)
[1] 44.97996 45.34064 43.44288 43.97647 43.67674 45.93679 40.96677 46.16282 45.00349 45.81906 41.83532 47.62596 43.42704 42.02320
[15] 42.98409 43.95436 45.33096 43.56644 45.17716 45.68700 43.58766 42.25269 44.77530 41.84349 42.33064
>
>
> # Part ii
>
> t.test(baking_times, mu = 46, alternative = "less")

One Sample t-test

data:  baking_times
t = -5.844, df = 24, p-value = 2.503e-06
alternative hypothesis: true mean is less than 46
95 percent confidence interval:
 -Inf 44.63381
sample estimates:
mean of x
 44.06828
```