IT2120 - Probability and Statistics

Lab Sheet 08

IT24103555

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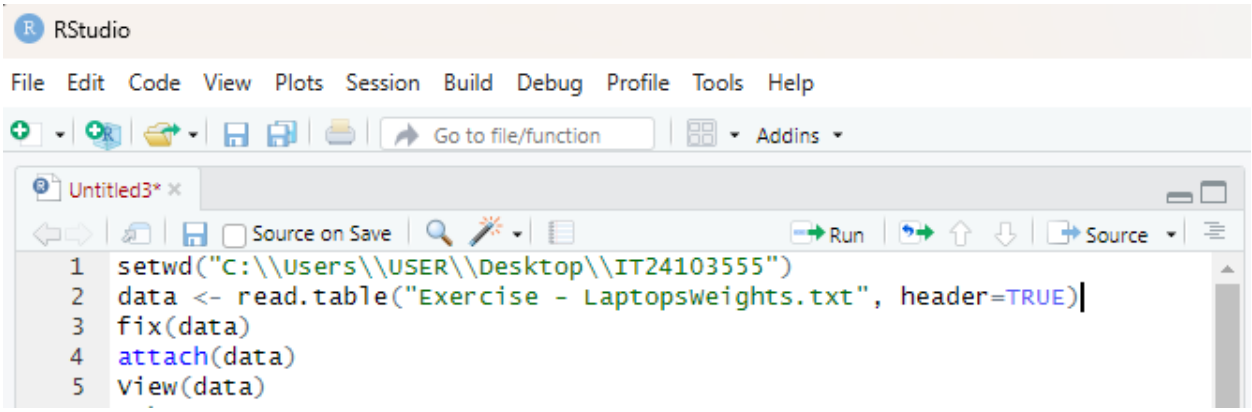
Exercise



1. Calculate the population mean and population standard deviation of the laptop bag weights.

```
6  #1)
7  pop.mean <- mean(weights)
8  pop.sd   <- sd(weights)
9
10 cat("Population mean =", pop.mean, "\n")
11 cat("Population SD =", pop.sd, "\n")
12
```

```
> pop.mean <- mean(weights)
> pop.sd   <- sd(weights)
>
> cat("Population mean =", pop.mean, "\n")
Population mean = 2.468
> cat("Population SD =", pop.sd, "\n")
Population SD = 0.2561069
```

2. Draw 25 random samples of size 6 (with replacement) and calculate the sample mean and sample standard deviation for each sample.

```
#2)
samples <- c()
n <- c()

for (i in 1:25){
  s <- sample(weights, 6, replace = TRUE)
  samples <- cbind(samples, s)
  n <- c(n, paste("s", i))
}

colnames(samples) <- n

s.means <- apply(samples, 2, mean)
s.sds   <- apply(samples, 2, sd)

cat("Sample Means:\n")
print(s.means)

cat("\nSample Standard Deviations:\n")
print(s.sds)
```

```
> samples <- c()
> n <- c()
>
> for (i in 1:25){
+   s <- sample(weights, 6, replace = TRUE)
+   samples <- cbind(samples, s)
+   n <- c(n, paste("s", i))
+ }
>
> colnames(samples) <- n
>
> s.means <- apply(samples, 2, mean)
> s.sds   <- apply(samples, 2, sd)
>
> cat("Sample Means:\n")
Sample Means:
> print(s.means)
     s 1      s 2      s 3      s 4      s 5      s 6
2.435000 2.243333 2.533333 2.465000 2.478333 2.401667
     s 7      s 8      s 9     s 10     s 11     s 12
2.503333 2.505000 2.413333 2.598333 2.480000 2.388333
    s 13     s 14     s 15     s 16     s 17     s 18
2.416667 2.510000 2.465000 2.601667 2.483333 2.531667
    s 19     s 20     s 21     s 22     s 23     s 24
2.380000 2.468333 2.426667 2.493333 2.446667 2.515000
    s 25
2.493333
>
```

```
> cat("\nSample Standard Deviations:\n")

Sample Standard Deviations:
> print(s.sds)
      s 1       s 2       s 3       s 4       s 5       s 6
0.1846889 0.3745753 0.2128536 0.1262933 0.3202759 0.2444927
      s 7       s 8       s 9      s 10      s 11      s 12
0.2004661 0.2049146 0.2991766 0.2821643 0.1425482 0.4067636
     s 13      s 14      s 15      s 16      s 17      s 18
0.2156540 0.2555778 0.2578953 0.2297317 0.1871541 0.3074031
     s 19      s 20      s 21      s 22      s 23      s 24
0.2515552 0.1824737 0.2324364 0.2768152 0.2370373 0.2449286
     s 25
0.1887503
```

3. Calculate the mean and standard deviation of the 25 sample means and state the relationship of them with true mean and true standard deviation.

```
34  #3)
35
36  mean.of.means <- mean(s.means)
37
38  sd.of.means <- sd(s.means)
39
40  cat("Mean of 25 sample means =", mean.of.means, "\n")
41  cat("SD of 25 sample means =", sd.of.means, "\n")
42
43  # Relationship with true mean and true SD
44  cat("Population mean =", pop.mean, "\n")
45  cat("Mean of sample means ≈ Population mean\n\n")
46
47  cat("Population SD =", pop.sd, "\n")
48  cat("SD of sample means =", sd.of.means, "\n")
49  cat("Population SD / sqrt(n) =", pop.sd/sqrt(6), "\n")
50  cat("SD of sample means ≈ Population SD / sqrt(n)\n")
51
```

```
> mean.of.means <- mean(s.means)
>
> sd.of.means <- sd(s.means)
>
> cat("Mean of 25 sample means =", mean.of.means, "\n")
Mean of 25 sample means = 2.467067
> cat("SD of 25 sample means =", sd.of.means, "\n")
SD of 25 sample means = 0.07342053
> # Relationship with true mean and true SD
> cat("Population mean =", pop.mean, "\n")
Population mean = 2.468
> cat("Mean of sample means ≈ Population mean\n\n")
Mean of sample means ≈ Population mean

>
> cat("Population SD =", pop.sd, "\n")
Population SD = 0.2561069
> cat("SD of sample means =", sd.of.means, "\n")
SD of sample means = 0.07342053
> cat("Population SD / sqrt(n) =", pop.sd/sqrt(6), "\n")
Population SD / sqrt(n) = 0.1045552
> cat("SD of sample means ≈ Population SD / sqrt(n)\n")
SD of sample means ≈ Population SD / sqrt(n)
```