

## Armstrong Axioms. (functional dependencies)

- Can be used to identify all functional dependencies that exist.

- Armstrong Axiom has 3 rules and 4 Secondary rules.

3 primary rules

- Reflexivity
- Augmentation
- Transitivity.

o Reflexivity.

if AB is a relationship also a subset of ABC, in that case it can say ABC functionally determines AB.

$$AB \subseteq ABC = ABC \rightarrow AB$$

↑  
Subset

o Augmentation.

if we have a functional dependency called  $A \rightarrow B$   
We can add an same attribute to both side.

$$A \rightarrow B = AC \rightarrow CB$$

attribute C added to both side.

o Transitivity

if  $A \rightarrow B$  and  $B \rightarrow C$ , in that case we can

Say  $A \rightarrow C$ .

$$A \rightarrow B, B \rightarrow C = A \rightarrow C$$

#### 4 Secondary rules.

o Union

o Composition

o Decomposition

o Pseudo Transitivity

o Union.

if  $x \rightarrow y$  and  $x \rightarrow z$ , then we can say

$$x \rightarrow y, x \rightarrow z = x \rightarrow yz$$

o Composition.

if  $x \rightarrow Y$  and  $A \rightarrow B$  then the combination of  $X_A$  determine  $Y_B$

o Decomposition.

Simply the opposite of union.

$$x \rightarrow yz = x \rightarrow y, x \rightarrow z$$

only separate L.H.S.

### o Pseudo Transitivity.

if  $x \rightarrow Y$  and  $YZ \rightarrow W$ . then we can say  
 $xz \rightarrow W$ .

$$x \rightarrow \overline{Y}, \overline{YZ} \rightarrow W = xz \rightarrow W$$

transitivity

define or replace with  $x$

### Attribute closure. $[x]^+$

Set of attributes that could be determined.  
 notation  $[x]^+$ .

if  $R(A, B, C, D, E)$  and FD  $\{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow E\}$ .  
 find  $A$  and  $AB$ .

$A \rightarrow$

$A \rightarrow A$  (reflexivity)

$A \rightarrow B$  (given)

$A \rightarrow C$  (Transitivity)

$A \rightarrow D$  (Transitivity)

$A \rightarrow E$  (Trans)

$$\therefore A^+ = \{A, B, C, D, E\}$$

BC  $\rightarrow$

$B \rightarrow C$  therefore  $BC \rightarrow C$  (reflexivity)

$BC \rightarrow D$  (union)

$BC \rightarrow E$  (transitivity)

$$\therefore BC^+ = \{C, D, E\}$$

Activity 1 2.1

$R(A, B, C, D)$

$$F = \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$$

$A \rightarrow A$  (ref)

$B \rightarrow B$  (ref)

$C \rightarrow C$  (ref)

$D \rightarrow D$  (ref)

$A \rightarrow B$  (given)

$B \rightarrow C$  (given)

$C \rightarrow D$  (given)

$A \rightarrow C$  (trans)

$A \rightarrow D$  (trans)

$A \rightarrow BC$  (union)

$A \rightarrow AB$  (union)

### Activity 2.1

$$R(A, B, C, D) \quad f = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D \}$$

$A \rightarrow A$  (union)

$B \rightarrow B$  (union)

$C \rightarrow C$  (union)

$D \rightarrow D$  (ref)

$A \rightarrow B$  (giv)

$B \rightarrow C$  (giv)

$B \rightarrow D$  (giv)

$A \rightarrow C$  (trans)

$A \rightarrow D$  (trans)

$A \rightarrow ABCD$  (union)  $\rightarrow Pk$

$B \rightarrow BCD$  (union)

$\leftarrow C$

### Activity 2.2.

$$R(A, B, C, D, E) \quad f = \{ A \rightarrow B, A \rightarrow C, CD \rightarrow E, B \rightarrow D, E \rightarrow A \}$$

$A \rightarrow A$

$A \rightarrow ABCDE$  (union)  $\leftarrow R.L$

$B \rightarrow B$

$E \rightarrow ABCDE$  (union)  $\rightarrow R.R$

$C \rightarrow C$

$CD \rightarrow ABCDE$  (union)  $\rightarrow L$

$D \rightarrow D$

$BC \rightarrow CD = ABCDE$

$E \rightarrow E$

$BC = ABCDE$  (trans)  $\rightarrow h$

$A \rightarrow D$  (trans)

$A \rightarrow C$  (trans)

$A \rightarrow CD$  (union)

$A \rightarrow E$  (trans)

## Lecture 03

### Normalization

refining the schema.

might have,

- Data redundancy
- Data Anomalies. (Insert / Delete / Update)

to solve these we can do Decompose the relation.

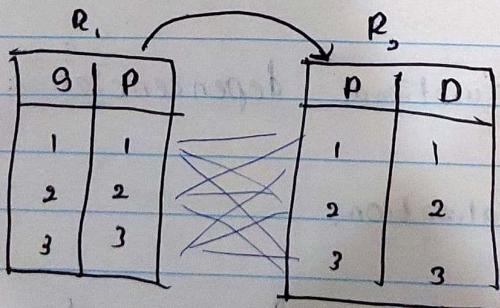
Decompose - Separating to Smaller relations.

Decompose Methods (2)

- Loss-less join property.
- Dependency preserving property.

Decomposed relation should have loss-less and dependency preserving properties.

| T <sub>1</sub> | S | P | D |
|----------------|---|---|---|
| 1              | 1 | 1 | 1 |
| 2              | 2 | 2 | 2 |
| 3              | 3 | 3 | 3 |

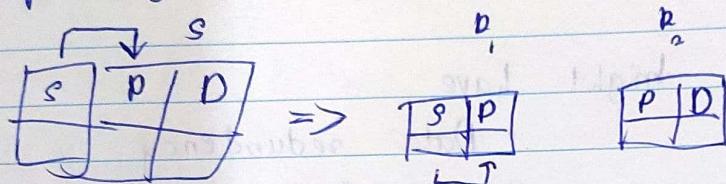


- T<sub>1</sub> table divided into R<sub>1</sub> and R<sub>2</sub>, by joining R<sub>1</sub> and R<sub>2</sub> you should able to restore T<sub>1</sub>.

~~s p p~~

## Dependency Preserving.

After decompose you should able to find  
dependency on relational  $a'$  well.



## functional dependency

$$x \rightarrow y$$

- $x$  functionally determines  $y$
- $y$  functionally dependent on  $x$ .

if you know ' $x$ ' you can retrieve  $y$ .

## Normalization.

- Way of guide to show how to decompose a relation.
- functional dependencies causes redundancy.

## Step of Normalization.

- identify functional dependencies } given to us.
- identify all keys in relation
- Normaliz. the relation.

## Stages of Normalization

you have to add each and every table to Normalization

### ① Unnormalized

(UoF)

↓ Remove a repeating group (multivalue, composite attributes)

### ② First Normal Form

(1NF)

↓ Remove Partial dependencies

### ③ Second Normal form

(2NF)

↓ Remove transitive dependencies.

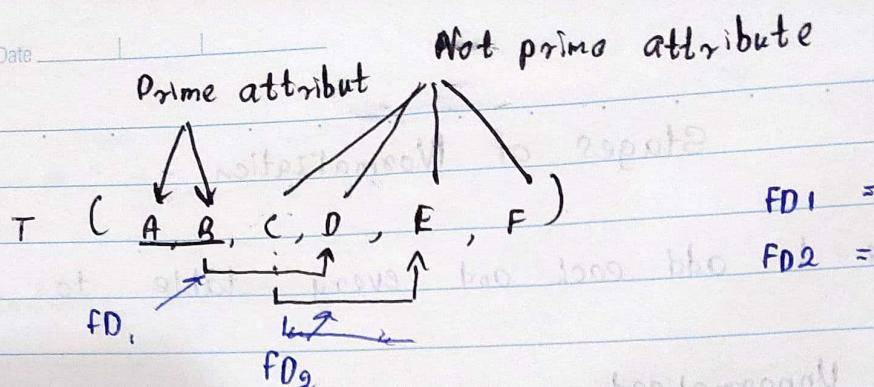
### ④ Third normal form → Need to do Uniti. 3NF

(3NF)

↓ Remove a remaining functional dependency anomalies.

### ⑤ Boyce - codd normal form

(BCNF)



$$FD_1 = A \rightarrow B \rightarrow 0$$

$$FD_2 = A \rightarrow C \rightarrow E$$

### ① Partial functional dependency

Non prime attribute depend on part of the primary key.

ex :  $FD_1$  is a partial dependant.

### ② Default functional dependency

occurs from the primary key, this not cause redundancy by pk.

ex :  $\{A, B\} \rightarrow C, D, E, F$

### ③ Transitive functional dependency

$$FD_2 = C \rightarrow E$$

$$\begin{array}{l} A, B \rightarrow C \\ \hline A, B \rightarrow E \end{array}$$

Non prime attribute transitively depends on the  $A, B$  prime key

## ① 1<sup>st</sup> Normalization form

- remove all repeating, multivalues.

ex: user (Tp-no, ID, name)

- Separate multivalu. to another table.

user (ID, name)

user-Tp (ID, Tp-no)

## ② 2<sup>nd</sup> Normalization form

- Remove all partial functional dependencies.

ex: R2 (x, y, z, m, f)  
      |  
      ↑

Separate prime attribut and non prim attribut that  
having Partial dependency

R2 (x, y, z, m, f)  
      |  
      ↑

R2A (y, m)

R2B (x, ~~y~~, z, f)

Date \_\_\_\_\_

### ③ 3<sup>rd</sup> normalization form

To achieve this Remove all transitive functional dependency

ex:  $R_3A(x, y, z, m)$

~~$x \rightarrow z$~~

Bring ~~pk~~ and non pk Attributes to

Separate table. make appointer pk.

$R_{3A}(z, m)$

$R_{3B}(x, y, z)$

Books are in the library being stored

Author is present in the library

$(x, y, z, m) \rightarrow z$

$(m, z) \rightarrow m$

$(x, y, z) \rightarrow x$