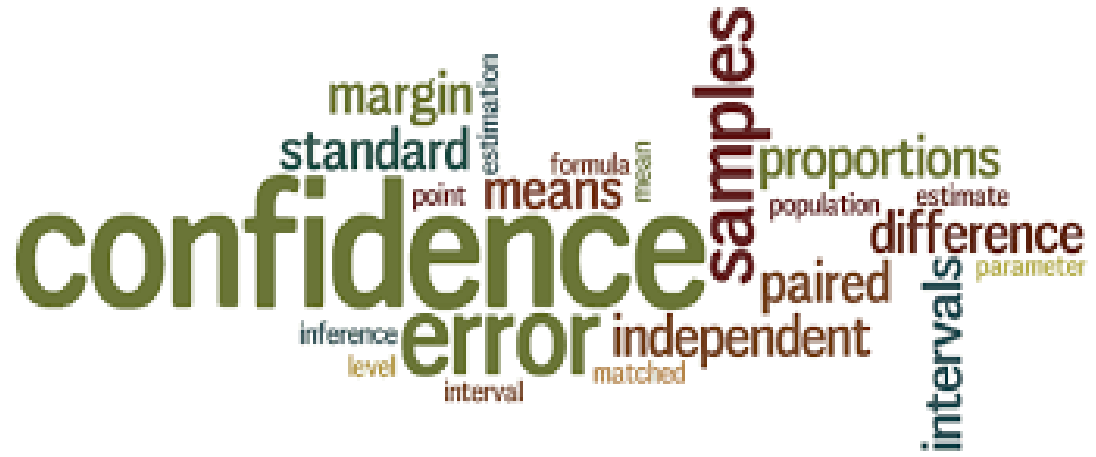


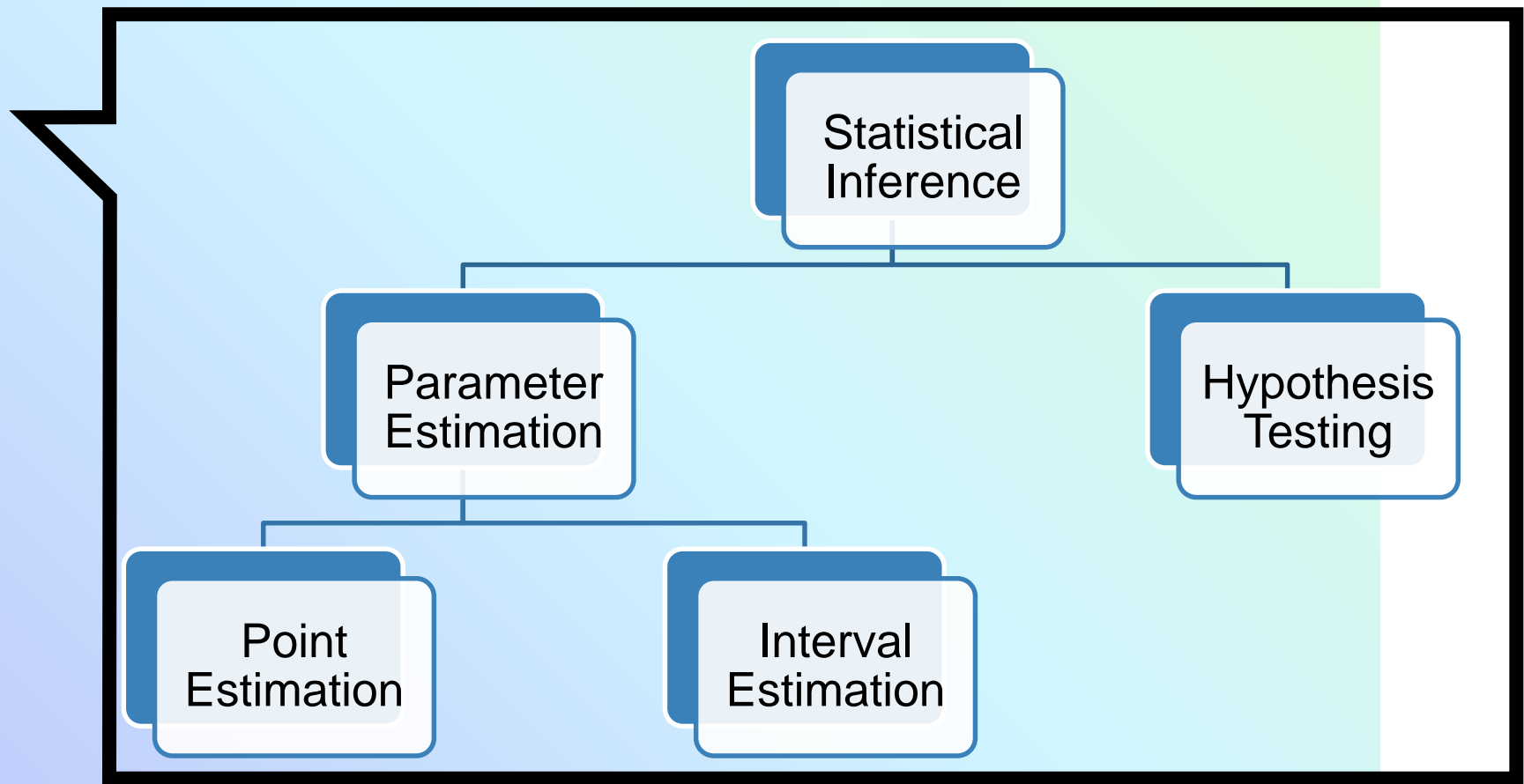
8. STATISTICAL INFERENCE (Part 2) [IT2110]

*By Department of Mathematics and Statistics
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8.2

CONFIDENCE INTERVALS







Introduction

- ▣ Estimates will differ from the true parameter values by varying amounts depending on the samples obtained.
- ▣ Point estimates do not convey any measure of reliability.

Interval Estimation

- Interval estimation states that a ***population parameter*** is ***within two values*** (an interval) with a ***certain probability (Confidence Level)***.
- Interval Estimation is also known as ***Confidence Interval***.
- For a good interval estimate,
 - *The probability that the parameter is within the interval should be high.*
 - *The length of the interval should be small.*

- A confidence level for the interval should be defined first.

$$\textit{Confidence Level} = 1 - \alpha$$

where α is the significance level discussed in hypothesis testing.

- Let L and U be the lower and upper confidence limits for a parameter θ based on a random sample X_1, \dots, X_n . Both L and U are functions of the sample. We can write the interval estimate of θ as,

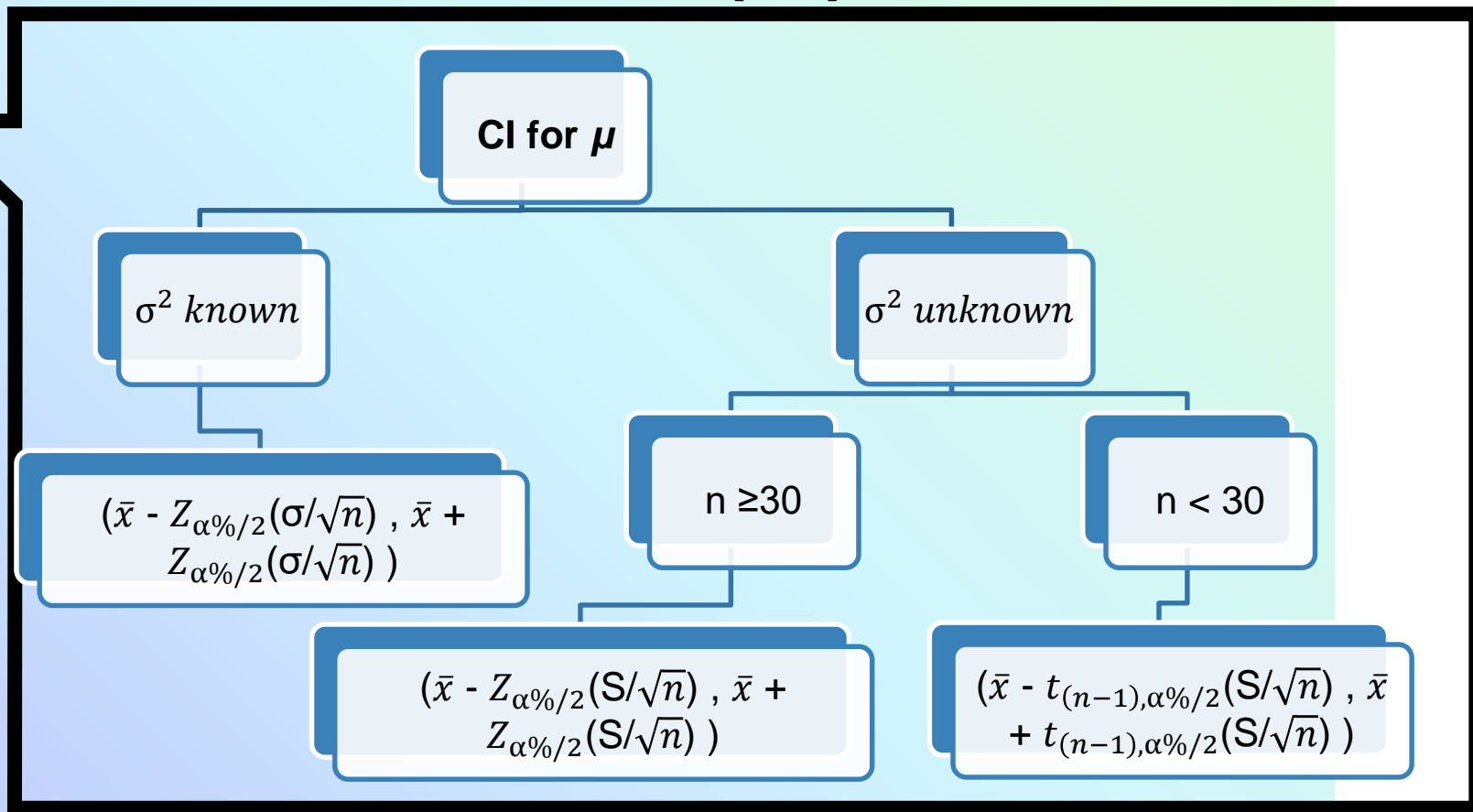
$$Pr (L \leq \theta \leq U) = 1-\alpha$$

- ***Interpretation:***

We are $(1 - \alpha)$ % confident that the true parameter θ is located in the interval (L, U) .

- In this session, we will discuss confidence intervals for population mean (μ) only.

Confidence Intervals (CI)



Example:

A company that manufactures cars claims that the gas mileage for its new line of hybrid cars, has a standard deviation of 4 mpg. It was also found out that the mpg was normally distributed. A random sample of 16 cars yielded a mean of 57 miles per gallon. What is the interval estimation for the population mean at a 95% confidence level?

Thanks!

Any questions?

