

Multilayer Evolving Fuzzy Neural Networks

Xiaowei Gu , Plamen Angelov , *Fellow, IEEE*, Jungong Han, and Qiang Shen 

Abstract—It is widely recognized that learning systems have to go deeper to exchange for more powerful representational learning capabilities in order to precisely approximate nonlinear complex problems. However, the best-known computational intelligence approaches with such characteristics, namely, deep neural networks, are often criticized for lacking transparency. In this article, a novel multilayer evolving fuzzy neural network (MEFNN) with a transparent system structure is proposed. The proposed MEFNN is a metalevel stacking ensemble learning system composed of multiple cascading evolving neuro-fuzzy inference systems (ENFISs), processing input data layer-by-layer to automatically learn multilevel nonlinear distributed representations from data. Each ENFIS is an evolving fuzzy system capable of learning from new data sample by sample to self-organize a set of human-interpretable IF–THEN fuzzy rules that facilitate approximate reasoning. Adopting ENFIS as its ensemble component, the multilayer system structure of the MEFNN is flexible and transparent, and its internal reasoning and decision-making mechanism can be explained and interpreted to/by humans. To facilitate information exchange between different layers and attain stronger representation learning capability, the MEFNN utilizes error backpropagation to self-update the consequent parameters of the IF–THEN rules of each ensemble component based on the approximation error propagated backward. To enhance the capability of the MEFNN to handle complex problems, a nonlinear activation function is introduced to modeling the consequent parts of the IF–THEN rules of ENFISs, thereby empowering both the representation and the reflection of nonlinearity in the resulting fuzzy outputs. Numerical examples on a wide variety of challenging (benchmark and real-world) classification and regression problems demonstrate the superior practical performance of the MEFNN, revealing the effectiveness and validity of the proposed approach.

Index Terms—Evolving fuzzy system (EFS), fuzzy neural network, self-organized, stacking ensemble.

I. INTRODUCTION

DEEP neural networks (DNNs or artificial neural networks, ANNs), have demonstrated eye-catching successes on a range of practical problems concerning image, video, speech,

and text processing [1], [2]. Currently, DNNs are one of the most popular computational intelligence approaches, thanks to the state-of-the-art (SOTA) performances they have offered in terms of prediction accuracy, and have been implemented for many real-world applications such as autonomous driving [3], drug discovery [4], stock prediction [5], etc.

The success of DNNs is built upon their capability to automatically learn multiple levels of nonlinear distributed representations from raw data through a general-purpose learning procedure [6]. It is widely recognized that this powerful representation learning ability of DNNs comes from their huge amounts (millions or sometimes billions) of parameters that are arranged in multiple layers and tuned to preserve abstract information learned from training data [7], [8]. However, DNNs are the typical type of “black box” models lack of transparency. They are extremely complicated models, and their parameters do not carry clear physical meanings that can be linked to the practical problems directly. Consequently, their internal reasoning processes are not interpretable by humans and their decisions are not explainable [9]. Another critical issue of DNNs is their vulnerability to real-world uncertainties. DNNs are fragile to new samples of unfamiliar data patterns, and they cannot be fixed easily because the training process is computationally expensive and usually requires huge amount of training data. These deficiencies have limited the wider deployment of DNNs in real-world applications, particularly, these high-stake ones [9]. It has also been shown by recent studies that the huge increase in interest toward DNNs starts to saturate [8].

Realizing that the multilevel nonlinear distributed representations are the key to the success of DNNs, there have been a few works published in recent years attempting to build alternative multilayer stacking ensemble models that offer competitive performance to DNNs but with less deficiencies aforementioned [7], [10], [11]. Stacking is an ensemble learning scheme for minimizing the prediction error of individual base models by arranging them in multiple layers, such that the outputs of the base models at a lower layer are used as the inputs of the base models at the layer above [12]. In this way, base models at upper layers learn to improve the predictions made by base models at lower layers and achieve improved prediction accuracy [13]. Unlike the alternative better-known parallel ensemble schemes such as bagging [14], [15] and boosting [16], [17], which attempt to increase the diversity between base models to complement each other, stacking constructs a metalevel learning model to learn multilevel distributed representations from data, exploiting a more sophisticated decision-making strategy than (weighted) majority voting. Thanks to the outstanding performance on many

Manuscript received 13 February 2023; revised 18 April 2023; accepted 4 May 2023. Date of publication 16 May 2023; date of current version 1 December 2023. (Corresponding author: Xiaowei Gu.)

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This article has supplementary material provided by the authors and color versions of one or more figures available at <https://doi.org/10.1109/TFUZZ.2023.3276263>.

Digital Object Identifier 10.1109/TFUZZ.2023.3276263

learning tasks, stacking has received increasing popularity in recent years [18], [19].

On the other hand, existing ensemble learning approaches (including the stacking ones) mainly focus on employing mainstream learning models, such as decision tree (DT), random forest (RF), k-nearest neighbour (KNN), support vector machine (SVM), multilayer perceptron (MLP), long-short term memory (LSTM), convolutional neural networks (CNN), etc., as base models to construct ensemble predictors [20], [21], [22], [23]. Although such ensemble models have demonstrated great performance, these models are typically limited to offline scenarios and can only work with static data. In addition, many of these mainstream base models (e.g., SVM, MLP, LSTM, and CNN) are often being criticized for lacking transparency. As a result, there is a strong demand for utilizing alternative learning models in building ensemble models such that the created ensembles are capable of self-updating from new data while offering greater transparency and interpretability.

Evolving fuzzy systems (EFSs) are a special group of fuzzy systems and can be implemented in the form of fuzzy rule-based systems [24] or neuro-fuzzy systems [25]. EFSs are the prominent methodology for real-time nonstationary problem approximation [26]. They are capable of self-developing the transparent system structure and self-updating the parameters from data streams through a human-interpretable reasoning process to capture the changing data patterns. EFSs are well known for their strong capability to handle inherent uncertainties in data, and they have been widely implemented for many real-world applications concerning data stream processing [27], [28]. As a hot research topic, a variety of EFSs have been proposed in the literature since the underlying concepts being introduced around the beginning of this century [25], [29]. The most representative evolving fuzzy rule-based systems include, but are not limited to, evolving Takagi–Sugeno system (eTS) [29], sequential adaptive fuzzy inference system (SAFIS) [30], evolving fuzzy rule-based classifiers (eClass0 and eClass1) [24], extended sequential adaptive fuzzy inference system (ESAFIS) [31], generalized smart evolving fuzzy systems (Gen-Smart-EFS) [32], evolving fuzzy model (eFuMo) [33], self-evolving fuzzy system (SEFS) [34], autonomous learning multi-model system (ALMMo) [35], recursive maximum correntropy-based evolving fuzzy system (RMCEFS) [36], evolving fuzzy system with self-learning/adaptive thresholds (EFS-SLAT) [37], statistically evolving fuzzy inference system (SEFIS) [38], etc. The most popular examples of evolving neuro-fuzzy models include dynamic evolving neural-fuzzy inference system (DENFIS) [25], self-organising fuzzy neural network (SOFNN) [39], evolving granular neural network [40], generic evolving neuro-fuzzy inference system (GENEFIS) [41], parsimonious network based on fuzzy inference system (PANFIS) [42], correntropy-based evolving fuzzy neural system (CEFNS) [43], parsimonious learning machine (PALM) [44], etc.

EFSs have demonstrated significant successes in a wide variety of time-critical applications in dynamical environment thanks to their simpler, highly flexible system structure and transparent internal reasoning mechanism [45]. However, it

is also recognized that **EFSs usually cannot reach the same level of performance as DNNs on large-scale, high-dimensional, complex problems** (e.g., image classification, image segmentation). Although there have been a number of EFS-based ensemble models proposed in the recent years reaching greater prediction performance on many challenging problems beyond individual single-model EFSs, the vast majority of existing works are focused on exploiting either parallel ensemble architectures to enhance the diversity between base models [14], [46], [47], [48], [49] or sequential ensemble architectures to enhance the adaptability of the ensemble system toward data pattern drifting in nonstationary environments by constructing a new base model from each newly arrived data chunk [50]. There only exist very few works on exploring the potential of building stacking ensemble models with EFSs to facilitate multi-level distributed representation learning [11], [51]. On the other hand, EFSs dominantly use the standard recursive least squares (RLS) algorithm or its variants for consequent parameter learning [25], [29], [40], [52], [53], which requires the error function to be explicitly defined. As a result, individual EFS models in a standard stacking ensemble framework have to learn from input data separately to minimize the differences between their predictions and the ground truth in order to avoid any ambiguity in defining the error functions for different layers. The lack of interaction between base models greatly restricts the capability of stacking ensemble models to learn more informative and descriptive representations from data.

To learn more descriptive multilevel distributed representations with high-level transparency and interpretability, a novel stacking ensemble fuzzy model named multilayer evolving fuzzy neural network (MEFNN) is introduced in this article. The proposed **MEFNN is a metalevel learning model consisted of a number of evolving neuro-fuzzy inference systems (ENFISs) cascading in multiple layers**. Each layer of the MEFNN is based on a single ENFIS that takes the outputs from the previous layer as its inputs, and passes its outputs to the next layer as inputs. In this way, the MEFNN processes input data layer-by-layer to learn multilevel distributed representations. **Each ENFIS is a multiple-input-multiple-output (MIMO) EFS that self-organizes and self-develops its system structure and parameters from data streams on a sample-by-sample basis**. To enhance the capability of **handling nonlinear** problems, a standard **sigmoid** function is introduced to the **consequent parts** of the IF–THEN fuzzy rules used by ENFISs to empower both the representation and the reflection of nonlinearity in the resulting fuzzy outputs, thereby enhancing the capability of the MEFNN to handle complex problems. **Unlike traditional EFSs, the MEFNN employs the error backpropagation algorithm** for updating the consequent parameters of its individual base models, which effectively avoids ambiguity in defining the error function for each individual layer by allowing the approximation error to be propagated backward from the last layer to the first layers. In this way, all the base models can interact and communicate with each other to learn more descriptive multilevel representations from data. Therefore, the **proposed MEFNN can also be viewed as a special type of the ANN with**

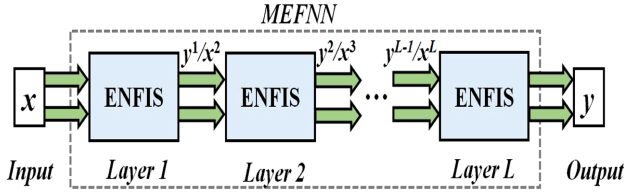


Fig. 1. General architecture of the MEFNN.

a highly flexible self-evolving multilayer structure (free from the requirement of specifying the numbers of nodes for each layer), human-interpretable internal reasoning mechanism, and meaningful parameters that can be directly linked to the practical problems.

To summarize, key features of the proposed MEFNN include the following.

- 1) A metalevel ensemble architecture composed of multiple cascading base models with self-evolving system structure and parameters to learn multilevel distributed representations from data on a sample-by-sample basis.
- 2) The use of error backpropagation to sequentially update the consequent parameters of the self-evolving base models based on the error of the existing approximation, facilitating information exchange between different layers to attain stronger representation learning capability.
- 3) The use of the sigmoid function in the consequent parts of IF-THEN fuzzy rules to empower both the representation and the reflection of nonlinearity in the fuzzy outputs of the base models, thereby enhancing the capability of the overall MEFNN to handle nonlinear, complex problems.

The remainder of this article is organized as follows. Technical details of the MEFNN are presented in Section II. Numerical examples on benchmark classification and regression problems are given in Section III as the proof of concept. Finally, Section IV concludes this article.

II. PROPOSED MEFNN

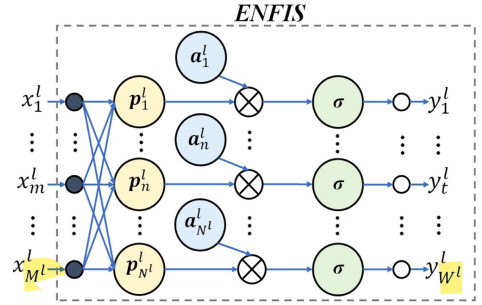
A. General Architecture

The general architecture of the MEFNN is depicted in Fig. 1. One can see from Fig. 1 that the proposed MEFNN is a stacking ensemble composed of multiple ENFISs arranged in layers (one ENFIS per layer). The inputs of the MEFNN are processed layer-by-layer until the final outputs are produced. Each ENFIS takes the outputs of the previous layer as its inputs (except for the first ENFIS) and uses its outputs as the inputs of the next layer (except for the last ENFIS). Hence, different layers are fully connected.

Assuming that the MEFNN is composed of L cascading ENFISs, the input-output relationship of the ENFIS at the l th layer can be defined as follows ($l = 1, 2, \dots, L$):

$$\mathbf{y}^l = f^l(\mathbf{x}^l) \quad (1)$$

where $\mathbf{x}^l = [x_1^l, x_2^l, \dots, x_{M^l}^l]^T$ is the $M^l \times 1$ dimensional input vector, and $\mathbf{y}^l = [y_1^l, y_2^l, \dots, y_{W^l}^l]^T$ is the $W^l \times 1$ dimensional output.

Fig. 2. Inner architecture of the l th ENFIS.

Since the l th layer takes the output of the $l - 1$ th layer as its input, namely, $\mathbf{x}^l = \mathbf{y}^{l-1}$ and $M^l = W^{l-1}$, the output of the l th layer can also be defined by the following composite function with respect to the input of the $l - 1$ th layer, \mathbf{x}^{l-1} :

$$\mathbf{y}^l = (f^l \circ f^{l-1})(\mathbf{x}^{l-1}) = f^l(f^{l-1}(\mathbf{x}^{l-1})). \quad (2)$$

Similarly, the overall ensemble system with a L -layer structure can be formulated by the following composite function:

$$\mathbf{y} = (f^L \circ f^{L-1} \circ \dots \circ f^2 \circ f^1)(\mathbf{x}) \quad (3)$$

where $\mathbf{x} = [x_1, x_2, \dots, x_M]^T$ and $\mathbf{y} = [y_1, y_2, \dots, y_W]^T$ are the respective input and output vectors of the MEFNN as depicted in Fig. 1. Note that the inputs to the MEFNN are normalized to the range of $[0, 1]$ in advance [54].

Different from conventional ANNs, the MEFNN does not require users to specify the numbers of nodes in each layer. Instead, users only need to set the output sizes of the cascading ENFISs (except for the final one) for the MEFNN, namely, W^1, W^2, \dots, W^{L-1} . The inner structure of each individual base model will automatically self-evolve from the input data to incorporate the observed data patterns without relying on any prior assumptions concerning data distribution and other properties. The output sizes control the amounts of information flowing between layers, and can be predefined based on users' preferences in the absence of specialized expertise and prior knowledge. In practice, the output size of a base model should be no greater than its input size to avoid overfitting and also, should be no less than the output size of the final layer to avoid losing too much information during the transmission between the layers. A detailed discussion on the parameter settings of the MEFNN, e.g., number of layers, output sizes of cascading base models, and their influence on the prediction performance of the system is presented in Section III-A. A recommended parameter setting is also given in Section III-A.

The inner architecture of the l th ENFIS is presented in Fig. 2. ENFIS is a MIMO neuro-fuzzy system composed of N^l first-order IF-THEN fuzzy production rules in the following form ($l = 1, 2, \dots, L$):

$$\mathbf{R}_n^l : \text{IF } (\mathbf{x}^l \sim \mathbf{p}_n^l) \text{ THEN } (\mathbf{y}_n^l = \sigma(\mathbf{A}_n^l \bar{\mathbf{x}}^l)) \quad (4)$$

where \mathbf{R}_n^l denotes the n th IF-THEN rule of l th ENFIS in MEFNN; $n = 1, 2, \dots, N^l$; N^l is the number of rules; \mathbf{x}^l is the $M^l \times 1$ dimensional input vector; $\bar{\mathbf{x}}^l = [1, (\mathbf{x}^l)^T]^T$;

“ \sim ” denotes similarity; $\mathbf{p}_n^l = [p_{n,1}^l, p_{n,2}^l, \dots, p_{n,M^l}^l]^T$ is the $M^l \times 1$ dimensional prototype (antecedent parameters) of \mathbf{R}_n^l ; $\mathbf{A}_n^l = [a_{n,1}^l, a_{n,2}^l, \dots, a_{n,W^l}^l]^T$ is the $W^l \times (M^l + 1)$ dimensional consequent parameter matrix and there is $\mathbf{a}_{n,w}^l = [a_{n,w,0}^l, a_{n,w,1}^l, \dots, a_{n,w,M^l}^l]^T$ ($w = 1, 2, \dots, W^l$); $\mathbf{y}_n^l = [y_{n,1}^l, y_{n,2}^l, \dots, y_{n,W^l}^l]^T$ is the $W^l \times 1$ dimensional output of \mathbf{R}_n^l ; and $\sigma(\cdot)$ denotes the standard activation function used by ANNs [55]. The activation function is utilized in the consequent part of the IF–THEN rules to add extra nonlinearity to ENFIS. Compared with the first-order IF–THEN rules used by conventional EFSs [24], [56], such modification (the utilization of activation function) greatly enhances the capability of ENFIS to handle nonlinear, complex problems. In this study, the classic sigmoid function, namely, $\sigma(x) = \frac{1}{1+e^{-x}}$ is employed. However, one may consider other types of activation functions, such as hyperbolic tangent, rectified linear unit.

Due to the utilization of sigmoid function, each IF–THEN rule of ENFIS becomes a nonlinear model, and the output \mathbf{y}^l of ENFIS in response to a particular input vector \mathbf{x}^l is produced as a weighted sum of the outputs generated by its individual IF–THEN rules as

$$\mathbf{y}^l = f^l(\mathbf{x}^l) = \sum_{n=1}^{N^l} \lambda_n^l \mathbf{y}_n^l = \sum_{n=1}^{N^l} \lambda_n^l \sigma(\mathbf{A}_n^l \bar{\mathbf{x}}^l) \quad (5)$$

where λ_n^l is the firing strength of \mathbf{x}^l to \mathbf{R}_n^l , defined as follows [26]:

$$\lambda_n^l = \frac{D_n(\mathbf{x}^l)}{\sum_{j=1}^{N^l} D_j(\mathbf{x}^l)} \quad (6)$$

and there is $D_n(\mathbf{x}^l) = e^{-\frac{\|\mathbf{x}^l - \mathbf{p}_n^l\|^2}{(\tau_n^l)^2}}$; $\|\mathbf{x}^l - \mathbf{p}_n^l\| = \sqrt{(\mathbf{x}^l - \mathbf{p}_n^l)^T (\mathbf{x}^l - \mathbf{p}_n^l)}$; τ_n^l is the width of the exponential kernel associated with \mathbf{R}_n^l , and its value is derived directly based on the mutual distances of data [as to be specified later in (11)].

In the next subsection, the identification process of the MEFNN, which include structure evolving and parameter learning, is presented. It is worth noting that all the cascading ENFISs follow the exactly same identification and decision-making procedures.

B. Identification Process

As aforementioned, MEFNN self-organizes its multilayer structure and parameters from the scratch by learning from data on a sample-by-sample basis. The identification process of the MEFNN is composed of the following three stages repeated for every input.

Stage 0. System Initialization: Given a particular input \mathbf{x}_k , the system structures and parameters of the cascading ENFISs in the MEFNN will be initialized one-by-one from the first ($l = 1$) layer to the last ($l = L$) layer if \mathbf{x}_k is the very first input, namely, $k = 1$. Otherwise, the identification process enters Stage 1 instead.

Once the l th ($l = 1, 2, \dots, L$) ENFIS receives its first input, \mathbf{x}_k^l ($\mathbf{x}_k^l = \mathbf{x}_k$ if $l = 1$ or $\mathbf{x}_k^l = \mathbf{y}_k^{l-1}$ if $l > 1$), its global

parameters are set as [26]

$$\boldsymbol{\mu}^l \leftarrow \mathbf{x}_k^l; \quad X^l \leftarrow \|\mathbf{x}_k^l\|^2 \quad (7)$$

where $\boldsymbol{\mu}^l$ is the global mean of all the input samples to the l th ENFIS, and X^l is the global mean of the squared Euclidean norms of all these input samples.

The first IF–THEN rule, $\mathbf{R}_{N^l}^l$ ($N^l \leftarrow 1$) is initialized in the form of (4) with its antecedent (prototype) and consequent parameters set by

$$\mathbf{p}_{N^l}^l \leftarrow \mathbf{x}_k^l; \quad \mathbf{A}_{N^l}^l \leftarrow \frac{1}{M^l + 1} \boldsymbol{\epsilon}_o \quad (8)$$

where $\boldsymbol{\epsilon}_o = [\epsilon_{o,j,k}]_{k=1:(M^l+1)}^{j=1:W^l}$ is a randomly generated $W^l \times (M^l + 1)$ dimensional matrix, whose elements equal to either 0 or 1, namely, $\epsilon_{o,j,k} \in \{0, 1\} \forall j, k$, following the symmetrical binomial distribution. This simple initialisation strategy prevents the derivatives from always being zeros.

Parameters of the shape-free cluster formed around the prototype $\mathbf{p}_{N^l}^l$ denoted by $\mathbf{C}_{N^l}^l$ are initialized as follows [26]:

$$\mathbf{c}_{N^l}^l \leftarrow \mathbf{x}_k^l; \quad \chi_{N^l}^l \leftarrow \|\mathbf{x}_k^l\|^2; \quad S_{N^l}^l \leftarrow 1 \quad (9)$$

where $\mathbf{c}_{N^l}^l$ is the mean of data samples associated with $\mathbf{C}_{N^l}^l$; $\chi_{N^l}^l$ is the mean of the squared Euclidean norms of these samples; and $S_{N^l}^l$ is the support (number of members) of $\mathbf{C}_{N^l}^l$.

After this, the l th ENFIS produces the output \mathbf{y}_k^l using (5). The output \mathbf{y}_k^l is then used as the input of the ENFIS at the next layer ($\mathbf{x}_k^{l+1} \leftarrow \mathbf{y}_k^l$). The same process repeats for every individual ENFIS in the stacking ensemble until the last (L th) ENFIS is initialized and the final output of the MEFNN is produced ($\mathbf{y}_k \leftarrow \mathbf{y}_k^L$). Then, the identification process enters Stage 2 for consequent parameter learning.

Stage 1. Structure Evolving and Output Generation: If $k > 1$, namely, \mathbf{x}_k is not the first input sample, the system structure and parameters of the MEFNN will be updated by adjusting the cascading ENFISs layer-by-layer with respect to the input.

Given the corresponding input, \mathbf{x}_k^l ($\mathbf{x}_k^l = \mathbf{x}_k$ if $l = 1$ or $\mathbf{x}_k^l = \mathbf{y}_k^{l-1}$ if $l > 1$), the global parameters of the l th ENFIS are updated as follows [26]:

$$\begin{aligned} \boldsymbol{\mu}^l &\leftarrow \boldsymbol{\mu}^l + \frac{\mathbf{x}_k^l - \boldsymbol{\mu}^l}{k} \\ X^l &\leftarrow X^l + \frac{\|\mathbf{x}_k^l\|^2 - X^l}{k}. \end{aligned} \quad (10)$$

Then, the local density of \mathbf{x}_k^l at each cluster, denoted as $D_n(\mathbf{x}_k^l)$, is calculated as follows ($n = 1, 2, \dots, N^l$) [26]:

$$D_n(\mathbf{x}_k^l) = e^{-\frac{\|\mathbf{x}_k^l - \mathbf{p}_n^l\|^2}{(\tau_n^l)^2}} \quad (11)$$

where $\tau_n^l = \sqrt{\frac{X^l - \|\boldsymbol{\mu}^l\|^2 + \chi_{N^l}^l - \|\mathbf{c}_n^l\|^2}{2}}$.

Condition 1 is checked to see if \mathbf{x}_k^l represents a novel data pattern unseen from the historical inputs [26]

$$\begin{aligned} \text{Cond. 1 : if } &\left(\max_{n=1,2,\dots,N^l} (D_n(\mathbf{x}_k^l)) < \delta_o \right) \\ &\text{then } (\mathbf{x}_k^l \text{ becomes a new prototype}) \end{aligned} \quad (12)$$

where δ_o is a threshold to determine whether \mathbf{x}_k^l is sufficiently different from the data patterns represented by existing prototypes, and there is $0 < \delta_o < 1$. In this study, $\delta_o = e^{-3}$ is used. According to the Chebyshev rule, the chance for the Euclidean distance between \mathbf{x}_k^l and \mathbf{p}_n^l to be greater than $\sqrt{3}\tau_n^l$ is less than 33.3%.

If Condition 1 is satisfied, it suggests that \mathbf{x}_k^l falls out of the areas of influence of existing prototypes, showing a significant departure from the existing local models in the l th ENFIS. In other words, \mathbf{x}_k^l is distinctive from existing prototypes and more likely to represent an unseen data pattern. Hence, a new IF-THEN rule ($N^l \leftarrow N^l + 1$) is introduced to the l th ENFIS to incorporate this new data pattern represented by \mathbf{x}_k^l . The antecedent and consequent parameters of the new rule $\mathbf{R}_n^{N^l}$ are set by (8) and the parameters of the associated shape-free cluster are initialized by (9).

However, if \mathbf{x}_k^l fails to meet Condition 1, \mathbf{x}_k^l is used for updating the parameters of the cluster associated with the nearest prototype, denoted by $\mathbf{p}_{n^*}^l$, as follows [26]:

$$\begin{aligned} c_{n^*}^l &\leftarrow c_{n^*}^l + \frac{\mathbf{x}_k^l - c_{n^*}^l}{S_{n^*}^l + 1} \\ \chi_{n^*}^l &\leftarrow \chi_{n^*}^l + \frac{\|\mathbf{x}_k^l\|^2 - \chi_{n^*}^l}{S_{n^*}^l + 1} \\ S_{n^*}^l &\leftarrow S_{n^*}^l + 1 \end{aligned} \quad (13)$$

where $n^* = \arg \max_{n=1,2,\dots,n^*} (D_n(\mathbf{x}_k^l))$, and $c_{n^*}^l$, $\chi_{n^*}^l$, and $S_{n^*}^l$ are the parameters of $\mathbf{C}_{n^*}^l$ associated with $\mathbf{p}_{n^*}^l$.

After the parameter updating and possible structure evolving, the l th ENFIS produces the output \mathbf{y}_k^l using (5). The output \mathbf{y}_k^l is then used as the input of ENFIS at the next layer ($\mathbf{x}_k^{l+1} \leftarrow \mathbf{y}_k^l$). The same updating process repeats for each individual ENFIS until the last one (namely, the L th one) has been updated. The identification process enters Stage 2 for consequent parameter learning once the final output, \mathbf{y}_k of the MEFNN in response to \mathbf{x}_k has been produced ($\mathbf{y}_k \leftarrow \mathbf{y}_k^L$). Note that different from conventional EFSs, the outputs of individual base models in the MEFNN are produced after structural evolving and antecedent parameter updating. In so doing, the derivative of the measured prediction errors with respect to the consequent parameters gives a better idea regarding how to adjust the consequent parameters, in order to minimize prediction errors given the current model structure and antecedent parameters.

Stage 2. Consequent Parameter Updating: As aforementioned, the MEFNN utilizes error backpropagation for updating the consequent parameters of its individual ensemble components unlike conventional first-order EFSs. Backpropagation is commonly used by ANNs and neuro-fuzzy systems with prefixed system structure [57], [58], [59]. The main reason for choosing backpropagation rather than standard algorithms used by EFSs such as RLS and its variants or least squares [25], [60] is because only the last ENFIS in the stacking ensemble has the target output. This makes it practically impossible to define an error function for any layer except the final one. Backpropagation, however, allows the error to be propagated backwards from the final layer to the first layer by the use

of chain rule, greatly facilitating the information exchanging between different layers. Due to the use of backpropagation, the MEFNN also removes the need of co-variance matrices by conventional RLS-based algorithms for consequent parameter updating, which greatly reduces the computational complexity especially when the data dimensionality is high.

Once the MEFNN generates the final output, \mathbf{y}_k in response to the current input, \mathbf{x}_k , the corresponding loss function is defined as

$$\mathbf{e}_k = \frac{1}{2}(\mathbf{y}_k - \mathbf{r}_k)^T(\mathbf{y}_k - \mathbf{r}_k) \quad (14)$$

where $\mathbf{r}_k = [r_{k,1}, r_{k,2}, \dots, r_{k,W}]^T$ is the corresponding target output. Note that for classification problems, \mathbf{r}_k is the vectorized class label of \mathbf{x}_k via dummy coding.

The derivative of the prediction error with respect to \mathbf{y}_k is obtained as follows:

$$\frac{\partial \mathbf{e}_k}{\partial \mathbf{y}_k} = \mathbf{y}_k - \mathbf{r}_k. \quad (15)$$

Then, the consequent parameter matrices of the cascading ENFISs are updated one-by-one backwards from the L th layer to the first layer utilizing the chain rule.

The derivative of the consequent parameter matrix of the l th ENFIS is derived as follows ($n = 1, 2, \dots, N^l$):

$$\frac{\partial \mathbf{e}_k}{\partial \mathbf{A}_n^l} = \frac{\partial \mathbf{e}_k}{\partial \mathbf{y}_k^L} \cdot \frac{\partial \mathbf{y}_k^L}{\partial \mathbf{y}_k^{L-1}} \cdot \dots \cdot \frac{\partial \mathbf{y}_k^{l+1}}{\partial \mathbf{y}_k^l} \cdot \frac{\partial \mathbf{y}_k^l}{\partial \mathbf{A}_n^l} \quad (16)$$

where $l = 1, 2, \dots, L$; $\mathbf{y}_k^L = \mathbf{y}_k$. Given $\mathbf{y}_k^j = \mathbf{x}_k^{j+1} \quad \forall j = 1, 2, \dots, L-1$. Equation (16) can be reformulated as (17) ($l = 1, 2, \dots, L$). The detailed derivations are presented in Section A of the Supplementary Material.

$$\frac{\partial \mathbf{e}_k}{\partial \mathbf{A}_n^l} = \lambda_{n,k}^l \cdot (\mathbf{d}_k^l \otimes \sigma'(\mathbf{A}_n^l \bar{\mathbf{x}}_k^l)) \cdot (\bar{\mathbf{x}}_k^l)^T \quad (17)$$

where “ \otimes ” denotes element-wise multiplication; $\sigma'(\mathbf{A}_n^l \bar{\mathbf{x}}_k^l) = \sigma(\mathbf{A}_n^l \bar{\mathbf{x}}_k^l) \otimes (1 - \sigma(\mathbf{A}_n^l \bar{\mathbf{x}}_k^l))$; \mathbf{d}_k^l is the derivate of the loss with respect to \mathbf{y}_k^l ($l = 1, 2, \dots, L-1$)

$$\begin{aligned} \mathbf{d}_k^l &= \frac{\partial \mathbf{e}_k}{\partial \mathbf{y}_k^L} \cdot \frac{\partial \mathbf{y}_k^L}{\partial \mathbf{y}_k^{L-1}} \cdot \dots \cdot \frac{\partial \mathbf{y}_k^{l+1}}{\partial \mathbf{y}_k^l} \\ &= \sum_{n=1}^{N^{l+1}} \left(\frac{\partial \lambda_{n,k}^{l+1}}{\partial \mathbf{x}_k^{l+1}} \cdot \sigma^T(\mathbf{A}_n^{l+1} \bar{\mathbf{x}}_k^{l+1}) \cdot \mathbf{d}_k^{l+1} \right. \\ &\quad \left. + \lambda_{n,k}^{l+1} \cdot (\tilde{\mathbf{A}}_n^{l+1})^T \cdot (\mathbf{d}_k^{l+1} \otimes \sigma'(\mathbf{A}_n^{l+1} \bar{\mathbf{x}}_k^{l+1})) \right). \end{aligned} \quad (18)$$

Here, $\mathbf{d}_k^L = \frac{\partial \mathbf{e}_k}{\partial \mathbf{y}_k^L} = \mathbf{y}_k^L - \mathbf{r}_k$; $\tilde{\mathbf{A}}_n^l = [\mathbf{a}_{n,w,m}^l]_{m=1:W^l}^{w=1:W^l}$ is the $W^l \times M^l$ dimensional consequent parameter matrix obtained by removing the first column of \mathbf{A}_n^l ; and there is

$$\frac{\partial \lambda_{n,k}^l}{\partial \mathbf{x}_k^l} = \lambda_{n,k}^l \cdot \left(\frac{2(\mathbf{p}_n^l - \mathbf{x}_k^l)}{(\tau_n^l)^2} - \sum_{i=1}^{N^l} \left(\lambda_{i,k}^l \cdot \frac{2(\mathbf{p}_i^l - \mathbf{x}_k^l)}{(\tau_i^l)^2} \right) \right). \quad (19)$$

Based on the derivative $\frac{\partial e_k}{\partial \mathbf{A}_n^l}$, the consequent parameter matrix, \mathbf{A}_n^l can be updated as follows:

$$\mathbf{A}_n^l \leftarrow \mathbf{A}_n^l - \gamma_o \cdot \frac{\partial e_k}{\partial \mathbf{A}_n^l} \quad (20)$$

where γ_o is the learning rate. In this study, $\gamma_o = 1$ is used by default. However, the learning rate of the MEFNN can be adjusted in the same way as the learning rate used in ANNs. Experienced users may further specify a particular learning rate for each layer of the MEFNN.

Once the consequent parameter matrices of all the ENFISs in the stacking ensemble have been updated based on the loss calculated with the current output [namely, (14)], the MEFNN can proceed to process the next input ($k \leftarrow k + 1$) and a new learning cycle starts. The system identification process of the proposed MEFNN is summarized by Algorithm S1 in the Supplementary Material for clarity.

It has to be stressed that the main purpose of this study is to demonstrate the proposed concept and general principles. Therefore, the operation mechanism of ENFIS is kept simple with only the essential rule adding scheme being used. However, the proposed MEFNN and its base model, ENFIS are, in fact, highly flexible. Alternative schemes such as rule merging, pruning and splitting can be added to ENFIS to help the model construct and maintain a more compact rule base [37], thereby enabling the MEFNN to achieve greater prediction performance. More advanced MIMO EFSs may be employed by the MEFNN as base models as well.

C. Computational Complexity Analysis

A detailed analysis on the computational complexity of the MEFNN is presented as follows. Since the MEFNN processes the data on a sample-by-sample basis, it is assumed that the analysis is performed at the k th time instance at which \mathbf{x}_k is given as the input of the MEFNN.

Stage 0 is for system initialization and will not be repeated again after the system has been initialized. Hence, the computational complexity of Stage 0 is negligible within the overall learning process.

Stage 1 is for updating the system structure and producing the output. For the l th ENFIS ($l = 1, 2, \dots, L$), the computational complexity of updating global parameters $\boldsymbol{\mu}^l$ and X^l in response to \mathbf{x}_k^l is $O(M^l)$, and that of calculating the local density value of \mathbf{x}_k^l at each cluster is $O(N^l M^l)$. The complexity of adding or updating a cluster is $O(N^l M^l)$, and that of output generation is $O(N^l M^l W^l)$. Therefore, the computational complexity of the l th ENFIS at Stage 1 is $O(N^l M^l W^l)$ and the overall computational complexity of Stage 1 of the MEFNN given the input \mathbf{x}_k is $O(\sum_{l=1}^L N^l M^l W^l)$.

The consequent parameters of the individual ensemble components are updated in response to \mathbf{x}_k at Stage 2. The complexity of calculating $\frac{\partial e_k}{\partial \mathbf{A}_n^l}$ for the l th ENFIS ($l = 1, 2, \dots, L$) is $O(N^l M^l W^l)$ and that of deriving \mathbf{d}_k^l is $O(N^{l+1} M^{l+1} W^{l+1})$ for the l th ENFIS ($l = 1, 2, \dots, L-1$). Thus, the overall computational complexity of Stage 2 of the MEFNN is $O(\sum_{l=1}^L N^l M^l W^l)$ as well.

Together, the computational complexity of the overall system identification process of the MEFNN given K input samples is $O(K \sum_{l=1}^L N^l M^l W^l)$.

In contrast, for a representative, conventional M -input W -output EFS that uses the RLS-based algorithm for consequent parameter learning, the overall computational complexity of its system identification process given K input samples is typically $O(K N M^2 W)$ if the local learning approach is used and $O(K N^2 M^2 W)$ if the global learning approach is used [24], where N denotes the number of rules in the model.

III. EXPERIMENTAL INVESTIGATION

In this section, numerical examples based on a variety of benchmark problems are presented for demonstrating the performance of the proposed MEFNN. The algorithms were developed on MATLAB2021b platform and the performance was evaluated on a desktop with dual core i7 processor 3.80 GHz $\times 2$ and 32.0-GB RAM. Unless specifically declared otherwise, the reported numerical results were obtained as the average of ten Monte Carlo experiments to allow a certain degree of randomness, and hence, a fair comparison.

A. Configuration

1) *Data Description*: In this study, a total of 24 popular numerical benchmark datasets for classification from UCI machine learning repository¹ and KEEL-dataset repository² are involved in performance evaluation, which include the following: cardiocography (CA); wall-following robot navigation (WF); gesture phase segmentation (GP); optical recognition of handwritten digits (OR); Australia (AU); balance (BA); liver (LI); magic (MG); monk (MO); pageblocks (PB); pima (PI); seismic (SE); sonar (SO); spectfheart (SH); occupancy detection (OD); multiple features (MF); pen-based recognition of handwritten digits (PR); abalone (AB); image segmentation (IS); phishing websites (PW); spambase (SP); mammography (MA); texture (TE); and steel plates faults (SPF).

To evaluate the performance of the MEFNN on high-dimensional classification problems, the following four remote sensing image sets for land-use classification are used, namely, OPTIMAL-31 (OPT),³ WHU-RS19 (WHU),⁴ UCMerced (UCM),⁵ and RSSCN7 (RSS).⁶ Following the same procedure as described in [61], in this study, three mainstream DCNN models, namely, ResNet50 [62], DenseNet121 [63], and InceptionV3 [64], are employed for feature extraction after being fine tuned on the NWPU45 dataset.⁷ In running the experiments, each fine-tuned DCNN model will extract a 1024×1 dimensional feature vector from each image. The arithmetic mean of the three feature vectors will be used as the representation of the image for model training and testing.

¹ Available at: <https://archive.ics.uci.edu/ml/index.php>

² Available at: <https://sci2s.ugr.es/keel/datasets.php>

³ Available at: <https://1drv.ms/u/s!Ags4cxbCq3lUguxW3bq0D0wbm1zCDQ>

⁴ Available at: <https://captain-whu.github.io/BED4RS/>

⁵ Available at: <http://weegeee.vision.ucmerced.edu/datasets/landuse.html>

⁶ Available at: <https://github.com/palewithout/RSSCN7>

⁷ Available at: <https://www.tensorflow.org/datasets/catalog/resisc45>

To demonstrate the performance of the MEFNN on large-scale, nonstationary, complex problems, the following two popular benchmark datasets for network intrusion detection, namely, NSLKDD [65] and UNSWNB15 [66] are also involved in experimental investigation. As a common practice, the categorical attributes of the two datasets have been converted to numerical ones by one-hot mapping in advance.

Furthermore, six widely used benchmark datasets are employed to test the performance of the MEFNN on regression problems, which include four real-world regression problems, one Mackey–Glass time-series prediction problem and one S&P500 closing price prediction problem. The four real-world problems are: autos; autmpg; delta ailerons; and california housing.

Key information of the 24 benchmark numerical classification datasets, four image classification datasets, two network intrusion detection datasets and six regression problems used in the numerical examples presented in this study is summarized in Section C of the Supplementary Material

2) *Parameter Setting for the MEFNN*: A key feature of the MEFNN is that its multilayered system structure is highly flexible and is self-evolving with data. Users are required to predetermine the number of base models/layers in the stacking ensemble, L , the output size for each individual base model (except for the final one), namely, W^1, W^2, \dots, W^{L-1} and the threshold δ_o that enables the base models to identify data patterns different from previously observed ones. However, it has to be stressed that these externally controlled parameters can be determined based on the users' preferences without any prior knowledge of the problem. In this study, the output sizes of the 1th to $L - 1$ th base models are set uniformly the same as $W^1 = W^2 = \dots = W^{L-1} = W_o$ for simplicity.

To demonstrate the proposed concept and general principles, in running the experiments, the number of layers, L of the MEFNN is set as 2 unless specifically declared otherwise, and the other two externally controlled parameters, W_o and δ_o are fixed as $3W$ and e^{-3} , respectively. Due to its multilayer structure, MEFNN has stronger multilevel representation learning ability and more trainable parameters. To ensure that the stacking ensemble model is trained sufficiently, the MEFNN is trained on the same training sets with shuffling for 200 epochs during the experiments.

It is worth noting that the parameter setting of the MEFNN in this study only serves as a feasible option for users' consideration. However, it will be demonstrated through numerical examples presented in the rest of this section that the MEFNN can achieve superior prediction performance on a wide range of benchmark classification and regression problems using this set of parameters, outperforming the SOTA alternatives. In practice, one can adjust the three externally controlled parameters (namely, L , W_o , and δ_o) to maximize the prediction performance of the MEFNN according to the nature of data. More experienced users may further consider using different output sizes for individual base models at different layers. To understand the impacts of the three parameters on the performance of the MEFNN, a sensitivity analysis is carried out on the following four benchmark datasets, namely, CA, WF, GP, and OR. The

detailed analysis results are presented in Section D of the Supplementary Material. In addition, an ablation analysis is performed and presented in Section E of the Supplementary Material to demonstrate the performance improvement brought forward by the sigmoid function used in the consequent part of IF–THEN rules of the MEFNN. Note that, the four datasets will not be used for performance demonstration presented in the rest of this section.

3) *SOTA Methods for Comparison*: In this study, the following 17 single-model SOTA algorithms are used for performance comparison: SVM [67]; KNN [68]; sequential classifier (SEQ) [69]; sequence-dictionary-based KNN classifier (SDKNN) [69]; extreme learning machine (ELM) [70]; MLP; LSTM [71]; probabilistic neural network (PNN) [72]; eigenvalue classifier (EIG) [73]; spherical approximation classifier (SPA) [74]; self-adaptive fuzzy learning system (SALF) [26]; multiobjective optimized self-organizing fuzzy inference system (MOOSOFIS) [75]; SEFIS [38]; ESAFIS [31]; PALM [44]; eClass0 classifier [24]; and eClass1 classifier [24].

In addition, the following five ensemble learning approaches are involved for performance comparison, which include: random forest (RF) [21]; stagewise additive modeling using a multiclass exponential loss function (SAMME) [17]; fuzzily weighted adaptive boosting (FWAdaBoost) [49]; XGBoost [76]; and eEnsemble [46]. In this study, XGBoost uses decision tree (DT) as its base classifiers; two ensemble models are created with SAMME by using DT and KNN as the base classifiers, denoted as SAMMED and SAMMEK, respectively. Hence, a total of six ensemble models are involved in this study.

The parameter settings of the 17 single-model predictors and six ensemble models used for numerical experiments are given in Section F of the Supplementary Material.

B. Performance Demonstration on Numerical Classification Problems

First, the performance of the MEFNN is evaluated on ten benchmark classification datasets from KEEL, which include AU; BA; LI; MG; MO; PB; PI; SE; SO; and SH. Following the common practice [77], [78], the **maximum accuracy, mean accuracy, and standard deviation** obtained by the MEFNN from tenfold cross validation on each dataset are tabulated in **Table S8** in the Supplementary Material. The following **six algorithms**: EIG; SPA; SAFL; MOOSOFIS; SEFIS; and PALM, are involved in performance comparison under the same experimental protocol and the results are given in **Table S8** of the Supplementary Material. For better comparison, the results obtained by the **three state-of-the-art classification** approaches in the literature, namely, Chebyshev polynomial broad learning system (CPBLS) [77], compact fuzzy broad learning system (CFBLS) [78], and highly interpretable deep fuzzy classifier (HIDFC) [79], are also reported in the **same table**. In addition, the performances of the MEFNN with a **three-layer structure** ($L = 3$), denoted as MEFNN₃, on the ten benchmark datasets are reported in **Table S8** of the Supplementary Material to better demonstrate the proposed concept. The best results per datasets in terms of maximum accuracy and mean accuracy are

highlighted in Table S8 in the Supplementary Material for visual clarity.

It can be observed from Table S8 in the Supplementary Material that the MEFNN outperforms the nine alternative classification approaches in terms of maximum accuracy on five out of the ten benchmark problems (namely, BA, MG, MO, PI, and SO) and its mean accuracy surpasses others on two out of the ten problems (namely, MG and MO). The average classification accuracy of the MEFNN over the ten problems is 0.8684, which is ranked the first place among the ten classification approaches involved in this numerical example. With a three-layer structure, MEFNN₃ achieves greater mean accuracy than the MEFNN on three benchmark problems (namely, BA, MG, and MO) and its maximum accuracy surpasses the MEFNN on SH dataset. Its average classification accuracy over the ten problems is 0.8596, which is slightly lower than the two-layer MEFNN but greater than the nine competitors. In contrast, CPBLS and CFBLs are the two best performing ones among the nine competitors, respectively, with the average classification accuracies of 0.8558 and 0.8544.

Next, the classification performance of the MEFNN is evaluated on the following ten benchmark problems from UCI: OD; MF; PR; AB; IS; PW; SP; MA; TE; and SPF, and compared with the 21 single-model and multimodel classification approaches mentioned in Section III-A (SPA is not involved in this example due to its extremely low computational efficiency on high-dimensional problems). In running the experiments, for OD, PR, and IS datasets, their original training–testing splits are used. For the other seven datasets, 50% of data samples are randomly selected to construct the training sets and the remaining 50% are used as the validation sets [75]. The detailed classification results in terms of accuracy (Acc) and balanced accuracy (BAcc) are given in Tables S9 and S10 in the Supplementary Material, respectively. Similarly, the results obtained by the MEFNN₃ are also reported in Tables S9 and S10 in the Supplementary Material. The mean accuracies and mean balanced accuracies of the 23 classification approaches (including MEFNN and MEFNN₃) and their respective ranks from the best to the worst over the ten benchmark problems are given by Table I.

One can see from Table I that the MEFNN outperforms 20 single-model and multimodel classification approaches on the ten benchmark problems in terms of average accuracy and average balanced accuracy, and is only outperformed by XGBoost. Meanwhile, the MEFNN is ranked the top place on both accuracy measures, suggesting that the predicted labels produced by the MEFNN are more accurate than other approaches in the majority of cases. On the other hand, despite that MEFNN₃ outperforms the MEFNN on a number of benchmark problems in terms of mean (balanced) accuracy and maximum accuracy, it can be seen from this numerical example that its average classification accuracy over the 20 benchmark problems is slightly lower than the MEFNN. This suggests that, with the recommended parameter setting, the two-level distributed representations learned by the MEFNN from data are sufficiently discriminative for accurately classifying the unlabeled testing data of the 20 benchmark datasets used for performance demonstration. However, it has to be stressed that the optimal parameter setting for the MEFNN

TABLE I
OVERALL CLASSIFICATION PERFORMANCES AND THE RESPECTIVE RANKS OF
THE 23 CLASSIFICATION APPROACHES ON TEN BENCHMARK CLASSIFICATION
PROBLEMS FROM UCI

Algorithm	Acc		Bacc	
	Mean	Rank	Mean	Rank
MEFNN	0.8928	5.00	0.8686	5.30
MEFNN ₃	0.8861	7.80	0.8543	8.90
SVM	0.8874	7.10	0.8525	9.40
KNN	0.8773	10.45	0.8570	9.65
SEQ	0.7902	14.40	0.8033	12.60
SDKNN	0.7930	16.60	0.8081	15.00
ELM	0.7170	15.40	0.7008	14.40
MLP	0.8554	13.80	0.8197	14.60
LSTM	0.8832	7.80	0.8559	8.60
PNN	0.8477	14.15	0.8616	10.00
EIG	0.8413	15.70	0.8150	16.00
SAFL	0.8882	6.50	0.8561	7.65
MOOSOFIS	0.8731	12.70	0.8526	11.00
SEFIS	0.6711	21.70	0.6223	22.00
ESAFIS	0.8828	9.10	0.8501	9.75
PALM	0.8580	12.50	0.8053	13.90
eClass0	0.7350	20.90	0.7604	18.80
eClass1	0.8620	12.60	0.8111	13.90
RF	0.8679	9.00	0.8299	11.10
FWAdaBoost	0.8783	10.40	0.8312	11.00
SAMMED	0.8401	14.50	0.8070	14.90
SAMMEK	0.8754	11.25	0.8550	10.45
XGBoost	0.9001	6.65	0.8773	7.10

The bold values indicate the best performance.

always varies from problem to problem depending on the nature of data.

To examine the statistical significance of the superior performance achieved by the MEFNN, over the 21 comparative approaches involved in this example (excluding MEFNN₃), pairwise Wilcoxon rank tests [80] are conducted, and the outcomes in terms of p -value are reported in Table S11 in the Supplementary Material, where the cascaded classification results by each classification approach across the ten Monte-Carlo experiments are used. One can see from Table S8 in the Supplementary Material that 86.19% of the p -values returned by the pairwise Wilcoxon tests are below the level of significance specified by $\alpha = 0.05$. The statistical analysis demonstrates that the performance of the MEFNN is, indeed, significantly better than the 21 alternative classification approaches.

C. Performance Demonstration on Image Classification Problems

Then, the performance of the MEFNN on high-dimensional problems are tested on the four image classification problems. In running the experiments, the training–testing split ratio of OPT is set to 8:2; and for WHU, UCM, and RSS datasets, two different split ratios are considered for each, namely, 4:6 and 6:6, 5:5 and 8:2, and 2:8 and 5:5, respectively, by following the common practice in the literature [81]. The classification accuracies of the MEFNN on the four visual benchmark problems under different split ratios are reported in Table II. The results obtained by the MEFNN (in terms of average classification accuracy and standard deviation) and a selected group of the SOTA approaches from the literature are given in Table II for comparison. Note that the results by comparative approaches are obtained from [75]

TABLE II
PERFORMANCE COMPARISON ON FOUR VISUAL CLASSIFICATION PROBLEMS

Algorithm	OPT	WHU		UCM		RSS	
		4:6	6:4	5:5	8:2	2:8	5:5
MEFNN	1.0000	0.9713	0.9791	0.9650	0.9743	0.9169	0.9287
MOOSOFIS [75]	0.9989	0.9630	0.9749	0.9598	0.9693	0.8908	0.9157
CaffeNet [81]	-	0.9511	0.9624	0.9398	0.9502	0.8557	0.8826
VGG-VD-16 [81]	-	0.9544	0.9605	0.9414	0.9521	0.8398	0.8718
GoogLeNet [81]	-	0.9312	0.9471	0.9370	0.9431	0.8255	0.8584
SalM ³ LBP-CLM [83]	-	0.9421	0.9575	0.9535	0.9638	-	-
ARCNet-VGG16 [84]	0.9270	0.9750	0.9975	0.9681	0.9912	-	-
GBNet [85]	0.9328	0.9705	0.9857	0.9732	0.9925	-	-
EfficientNet-B3-Basic [86]	0.9476	0.9728	0.9768	0.9763	0.9873	0.9206	0.9439
EfficientNet-B3-Attn-2 [86]	0.9586	0.9860	0.9868	0.9790	0.9921	0.9330	0.9617
MSDS [87]	-	-	0.9761	-	0.9696	-	-
MLDS [87]	-	-	0.9829	-	0.9788	-	-
RANet [82]	0.9461	0.9798	0.9897	0.9780	0.9927	-	-

TABLE III
PERFORMANCE COMPARISON ON TWO BENCHMARK PROBLEMS FOR NETWORK INTRUSION DETECTION

Algorithm	NSLKDD		UNSWNB15	
	Acc	B _{Acc}	Acc	B _{Acc}
MEFNN	0.7861	0.8029	0.8334	0.8163
SAFL	0.7737	0.7918	0.8139	0.7932
SEFIS	0.7721	0.7874	0.7430	0.7234
ESAFIS	0.7421	0.7704	0.7714	0.7456
PALM	0.7644	0.7842	0.8068	0.7847
eClass0	0.7177	0.7470	0.7250	0.7129
eClass1	0.5668	0.5000	0.5511	0.5000
eEnsemble	0.7018	0.7321	0.7223	0.7090
FWAdaBoost	0.7741	0.7924	0.8301	0.8136

The bold values indicate the best performance.

and [82] directly. It can be seen from Table II that the MEFNN is able to achieve great classification performance on these visual classification problems, outperforming many DNN-based approaches.

D. Performance Demonstration on Network Intrusion Detection Problems

Furthermore, the performance of the MEFNN on large-scale, nonstationary, and complex problems is evaluated on the two aforementioned network instruction detection datasets and compared with six single-model EFS models and two ensemble EFS models aforementioned. In running the experiments, the original training–testing splits of the two datasets are kept. To facilitate simulation, 10% of the training and testing samples are randomly selected and used in each experiment. The numerical results obtained by the MEFNN and the eight competitors on the two datasets are reported in Table III in terms of Acc and B_{Acc}. One can see from Table III that the MEFNN outperforms all its EFS competitors by offering the greatest Acc and B_{Acc} on both datasets, showing its stronger capability to handle highly challenging problems.

E. Performance Demonstration on Regression Problems

In this section, the regression performance of the MEFNN is examined on widely used benchmark problems and compared with a variety of mainstream EFSs.

TABLE IV
PERFORMANCE COMPARISON ON MACKEY–GLASS TIME-SERIES PROBLEM

Algorithm	NDEI	#(Rules)	t_{exe}
MEFNN	0.0914	(4.4, 13.1)	164.2392
PSO-ALMMo	0.1910	8	314.3214
SAFL	0.1048	20	0.1868
CEFNS	0.2635	5	0.4368
eTS	0.2141	4	21.9745
ESAFIS	0.2487	6	2.7656
SAFIS	0.2925	4	0.4375
RMCEFS	0.1172	5	0.3432
OS-Fuzzy-ELM	0.2991	5	0.9253
PANFIS	0.2847	33	4.8679
GENEFIS	0.1198	42	4.9694
PALM	0.1380	18	0.7771
eFuMo	0.1388	41	-
EFS-SLAT	0.1140	8	-
SEFS	0.1287	4	0.3510
LEOA [90]	0.2480	42	144.7818
eGAUSS+ [91]	0.2728	25	~5
HiPCA [92]	0.2495	25	~14
InFuR [93]	0.1545	22	-

The bold values indicate the best performance.

The performances of the MEFNN on the four real-world benchmark problems, namely, autos; autmpg; delta ailerons; and california housing, in terms of root mean squared error (RMSE) and number of rules in the rule base (#(Rules)) are reported in Table S12 in the Supplementary Material, where the results by comparative approaches, including PSO-ALMMo [35]; SB-ALMMo [88]; CEFNS [43]; DENFIS [25]; eTS [29]; ESAFIS [31]; SAFIS [30]; RMCEFS [36]; and OS-Fuzzy-ELM [89], are obtained from the literature.

One can see from Table S12 in the Supplementary Material that the MEFNN outperforms all nine mainstream EFSs on the autmpg and california housing problems by producing the most accurate predictions (with lowest RMSE), and its performance on the other two datasets are also well above the average. This example demonstrates the great potential of the MEFNN on real-world regression problems.

Next, the performance of the MEFNN is evaluated on the widely used Mackey–Glass chaotic time series problem following the standard experimental protocol [34], [36], [90]. The result obtained by the MEFNN is reported in Table IV in terms of nondimensional error index (NDEI), number of rules in the

rule base ($\#(\text{Rules})$), and execution time (t_{exe}). The results by the mainstream EFSs are obtained directly from [26], [34], [36], [91], [92], and [93] and reported in the same table. It is shown by Table IV that the MEFNN surpasses the SOTA competitors on the Mackey–Glass problem with the lowest NDEI (0.0914), which further demonstrates its superior performance on regression tasks.

Finally, the MEFNN is tested on the S&P500 problem. The prediction performance of the MEFNN on the testing data following the standard test-then-train protocol is reported in Table S13 in the Supplementary Material (in terms of NDEI and $\#(\text{Rules})$). The prediction performance of the MEFNN without online training (following the same setting used in other examples presented in this section) is also reported in the same table for comparison. To differentiate between the two results, the MEFNN that follows the test-then-train protocol is redented as MEFNN*. The prediction results by the MEFNN and MEFNN* are depicted in Fig. S2 in the Supplementary Material for better comparison. In addition, results by selected SOTA approaches on this problem following the commonly used test-then-train protocol are tabulated in Table S13 in the Supplementary Material for comparison.

Table S13 in the Supplementary Material shows that MEFNN* demonstrates greater prediction performance on the S&P500 problem with a lower NDEI value of 0.0162, which is ranked the third place among the regression approaches involved in this example. In addition, it can be seen from Table S13 and Fig. S2 in the Supplementary Material that the MEFNN can effectively utilize new streaming data samples to self-update its knowledge base and self-improve its predictions with the NDEI value improved from 0.0200 to 0.0162. This example demonstrates the potential of the MEFNN as a powerful tool for handling data streams. The IF–THEN rules learned by the MEFNN from S&P500 problem during one particular experiment are presented in Table S14 in the Supplementary Material, where one can see that the learned metalevel knowledge base of the MEFNN can be visualized in a meaningful, human-interpretable form thanks to the use of ENFISs as its base components. This is useful for developing transparent inference tools.

To summarize, the systematic experimental studies over a wide variety of benchmark classification and regression problems presented in this section collectively and consistently demonstrate the superior performance of the MEFNN in comparison to the SOTA approaches in terms of prediction accuracy. Numerical examples based on 20 popular numerical problems presented in Section III-B demonstrate that the MEFNN with the default parameter setting can achieve a great classification accuracy surpassing, or at least on par with the SOTA competitors. Numerical examples on four visual classification problems and two network intrusion detection problems presented in Sections III-C and III-D show the strong capability of the MEFNN to handle high-dimensional, large-scale, complex problems. Thanks to the multilevel distributed representation learned from data, the MEFNN achieves a greater classification accuracy on these challenging benchmark problems than alternative EFS-based comparative models involved in experimental comparison. Last,

the MEFNN is tested on six benchmark regression problems, and numerical results show the great potential of the MEFNN in solving real-world regression problems while offering high-level transparency and interpretability. On the other hand, as the main purpose of this article is to demonstrate the concept and general principles of the proposed stacking ensemble model, all the numerical results of the MEFNN are obtained with the same parameter setting, thereby ensuring a fair comparison. The structure of the MEFNN is, in fact, highly flexible, one can easily increase the depth by adding more base models in the stacking ensemble, control the size of each layer by changing the threshold, δ_o and increase/reduce the amount of information exchanged between successive layers by adjusting W_o . Therefore, there is still a large space for performance improvement by adjusting the externally controlled parameters according to the nature of data.

IV. CONCLUSION

This article has presented a new metalevel ensemble learning model, composed of multiple cascading simpler EFSs to learn multilevel nonlinear distributed representation from data. The resultant MEFNN learns from data on a sample-by-sample basis to self-organize the underlying multilayer system structure and self-update the network parameters. Systematic comparative investigations have demonstrated the superior performance of the MEFNN on various challenging classification and regression problems, outperforming the SOTA approaches.

A number of open issues remain that require further considerations. First, theoretical analysis on the stability and convergence of the proposed MEFNN is not conducted in this study. Although there have been a number of works analyzing the convergence of backpropagation and the stability of EFSs, the use of backpropagation in EFS-based metalevel ensemble models has not been explored before. Thus, this will be an important direction for future research. Second, compared with single-model EFSs, the MEFNN requires larger amounts of training data (or being trained repeatedly with the same data) to reach practically excellent performance. This is fundamentally due to the use of the error backpropagation algorithm for consequent parameter updating, a limitation shared with many SOTA methods. As the ambiguity in defining the error functions for individual layers poses a challenge to the use of RLS-based algorithms in the MEFNN, it would be worth exploring different options to address this aspect, better facilitating the consequent parameter training. Third, numerical examples presented in this study demonstrate that the MEFNN with the same fixed parameter setting outperforms the SOTA approaches on many classification and regression problems in terms of prediction accuracy. However, predetermining the externally controlled parameters for the MEFNN may still be a challenging task, especially for these less experienced users. Therefore, it would be helpful to explore the possibilities of deriving some of the parameters directly from data, for example, the MEFNN may self-determine to increase or decrease the number of layers based on the nature of data. Fourth, this study only explores the use of the sigmoid function in the consequent part of IF–THEN rules of the MEFNN and compared

it with the classical linear function. It would be interesting to see how the MEFNN might perform with other types of nonlinear activation function, particularly, rectified linear unit, which is computationally cheaper and converges faster than sigmoid. Fifth, the base model ENFIS employed in this research only possesses the essential rule adding scheme. It would be helpful to introduce other potentially useful schemes such as pruning, merging, and splitting in an effort to learn a more compact, meaningful rule base from data, thereby improving the overall prediction performance of the MEFNN. Last, the numerical results presented in this article are focused on classification and regression problems. The MEFNN, in fact, is a generic, flexible approach for multilevel representation learning and has great potential for solving more complex problems concerning visual and audio information. The utilization of the MEFNN in other types of applications, such as dimensionality reduction, image feature extraction, etc., will be further explored in future works.

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