

Trabajo regresión lineal múltiple

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Asignatura

Analisis de Regresion



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Se realizará una análisis de regresión lineal múltiple(RLM):

$$y_i = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k + \varepsilon_i, \varepsilon_i \stackrel{iid}{\sim} N(0, \sigma^2)$$

Con la intencion de validar si dicho modelo es adecuado para

1. Base de datos

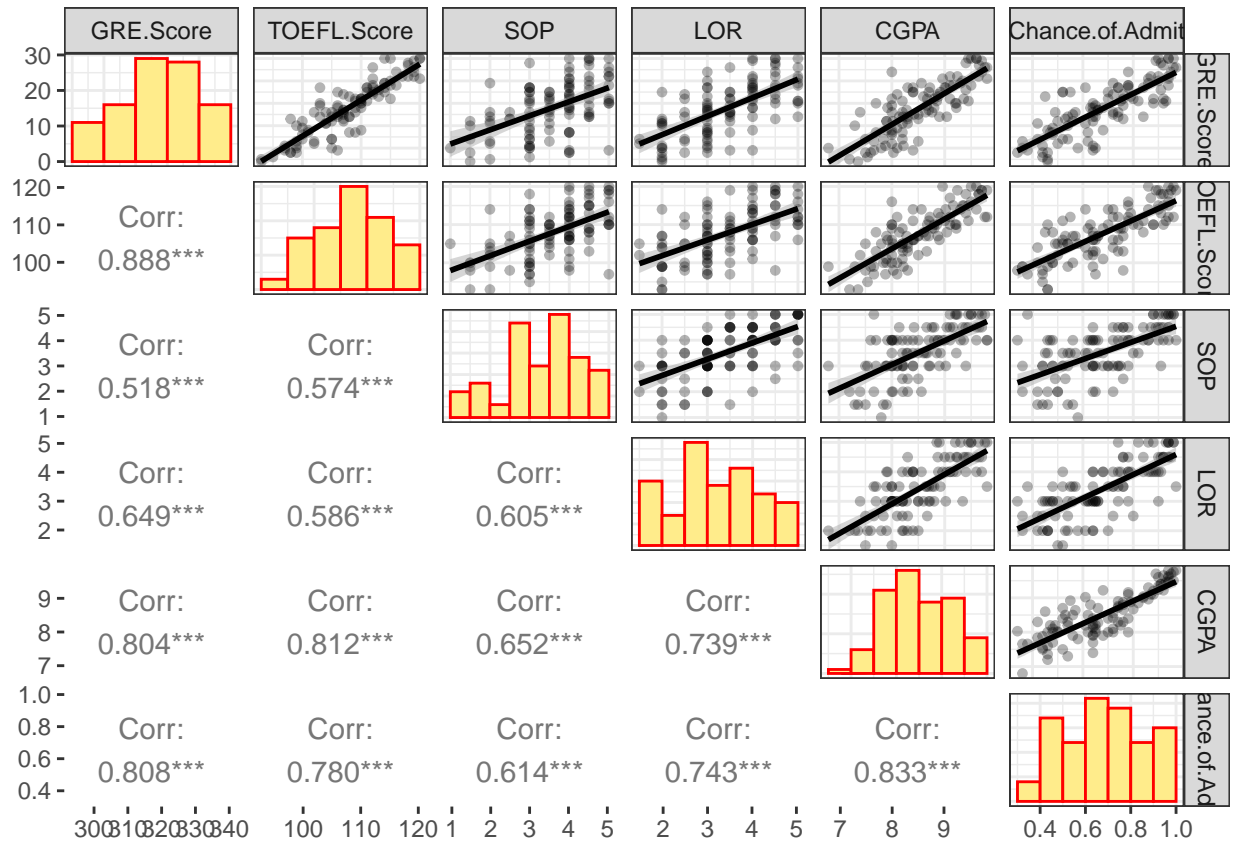
1.1. Breve Descripción de los Datos

La base de datos corresponden al puntaje de admision de estudiantes de posgrados pertenecientes a universidades de la India. Cuenta con 400 observaciones y 9 variables. De las cuales vamos a analizar un total de 100 estudiantes y 6 variables de interes.

| Variables | Descripción |
|-------------------------|--|
| Chance.of.Admit: | Posibilidad de ser admitido. |
| GRE Score: | Examen que tiene como finalidad medir la capacidad de razonamiento verbal, razonamiento cuantitativo, y habilidades para pensar y escribir de forma analítica. |
| TOEFL Score: | Prueba estandarizada de dominio del idioma inglés. |
| SOP: | Ensayo de admisión o solicitud de postgrado. |
| LOR: | Carta de recomendación. |
| CGPA: | Promedio general acumulado en el pregrado. |

2. Análisis descriptivo

2.1. Grafico de dispersión con Matriz de Correlaciones



Cuadro 3: Tabla ANOVA para el modelo

| | Df | Sum Sq | Mean Sq | F value | Pr(>F) |
|--|----|-----------|-----------|----------|--------|
| FO(GRE.Score, TOEFL.Score, SOP, LOR, CGPA) | 5 | 2.3674478 | 0.4734896 | 65.99381 | 0 |
| Residuals | 94 | 0.6744272 | 0.0071748 | NA | NA |

3. Modelo Ajustado de Regresion Lineal Multiple(MRLM)

3.1. Tabla de parámetros ajustados

Cuadro 2: Resumen de los coeficientes

| | Estimación | Error estándar | T_0 | Valor P |
|-----------|------------|----------------|---------|---------|
| β_0 | -1.7723 | 0.3007 | -5.8939 | 0.0000 |
| β_1 | 0.0041 | 0.0017 | 2.4400 | 0.0166 |
| β_2 | 0.0029 | 0.0031 | 0.9417 | 0.3488 |
| β_3 | 0.0120 | 0.0119 | 1.0098 | 0.3152 |
| β_4 | 0.0428 | 0.0143 | 3.0023 | 0.0034 |
| β_5 | 0.0757 | 0.0263 | 2.8756 | 0.0050 |

3.2. Ecuación Ajustada

Con base en la tabla de parámetros estimados se obtiene la ecuación de regresión ajustada:

$$\hat{Y}_i = \hat{\beta}_0 + \hat{\beta}_1 X_{i1} + \hat{\beta}_2 X_{i2} + \cdots + \hat{\beta}_5 X_{i5}, \quad i = 1, 2, \dots, 100$$

$$\hat{Y}_i = -1.7723 + 0.0041 X_{i1} + 0.0029 X_{i2} - 0.0120 X_{i3} + 0.0428 X_{i4} + 0.0757 X_{i5}, \quad i = 1, 2, \dots, 100$$

3.3. Tabla Anova

3.4. Prueba de significancia del Modelo

$$\begin{cases} H_0 : \beta_1 = \cdots = \beta_5 = 0 \\ H_1 : \text{Al menos un } \beta_j \neq 0 \end{cases}$$

3.5. Coeficiente de determinación

$$R^2 = \frac{SSR}{SST} = 1 - \frac{SSE}{SST}$$

$$R^2 = \frac{2.3674478}{2.3674478 + 0.6744272} = 0.7782857$$

4. Coeficientes de regresión estandarizados

Coeficientes estimados, sus I.C, Vifs y Coeficientes estimados estandarizados

| | Estimación | Limites.2.5.. | Limites.97.5.. | Vif | Coef.Std |
|-------------|------------|---------------|----------------|----------|-----------|
| (Intercept) | -1.7722651 | -2.3693009 | -1.1752294 | 0.000000 | 0.0000000 |
| GRE.Score | 0.0041091 | 0.0007654 | 0.0074528 | 5.691210 | 0.0495542 |
| TOEFL.Score | 0.0029116 | -0.0032277 | 0.0090508 | 5.858052 | 0.0194023 |
| SOP | 0.0120402 | -0.0116343 | 0.0357148 | 1.928844 | 0.0119389 |
| LOR | 0.0428307 | 0.0145058 | 0.0711556 | 2.519579 | 0.0405706 |
| CGPA | 0.0757081 | 0.0234330 | 0.1279833 | 4.615227 | 0.0525903 |

5. Significancia individual de los parámetros del modelo

5.1. Tabla de la significancia individual de los parámetros

Cuadro 4: Resumen de los coeficientes

| | Estimación | Error estándar | T_0 | Valor P |
|-----------|------------|----------------|---------|---------|
| β_0 | -1.7723 | 0.3007 | -5.8939 | 0.0000 |
| β_1 | 0.0041 | 0.0017 | 2.4400 | 0.0166 |
| β_2 | 0.0029 | 0.0031 | 0.9417 | 0.3488 |
| β_3 | 0.0120 | 0.0119 | 1.0098 | 0.3152 |
| β_4 | 0.0428 | 0.0143 | 3.0023 | 0.0034 |
| β_5 | 0.0757 | 0.0263 | 2.8756 | 0.0050 |

5.2. Pruebas de hipotesis

$$\begin{cases} H_0 : \beta_1 = 0 \\ H_1 : \beta_1 \neq 0 \end{cases}$$

$$\begin{cases} H_0 : \beta_2 = 0 \\ H_1 : \beta_2 \neq 0 \end{cases}$$

$$\begin{cases} H_0 : \beta_3 = 0 \\ H_1 : \beta_3 \neq 0 \end{cases}$$

$$\begin{cases} H_0 : \beta_4 = 0 \\ H_1 : \beta_4 \neq 0 \end{cases}$$

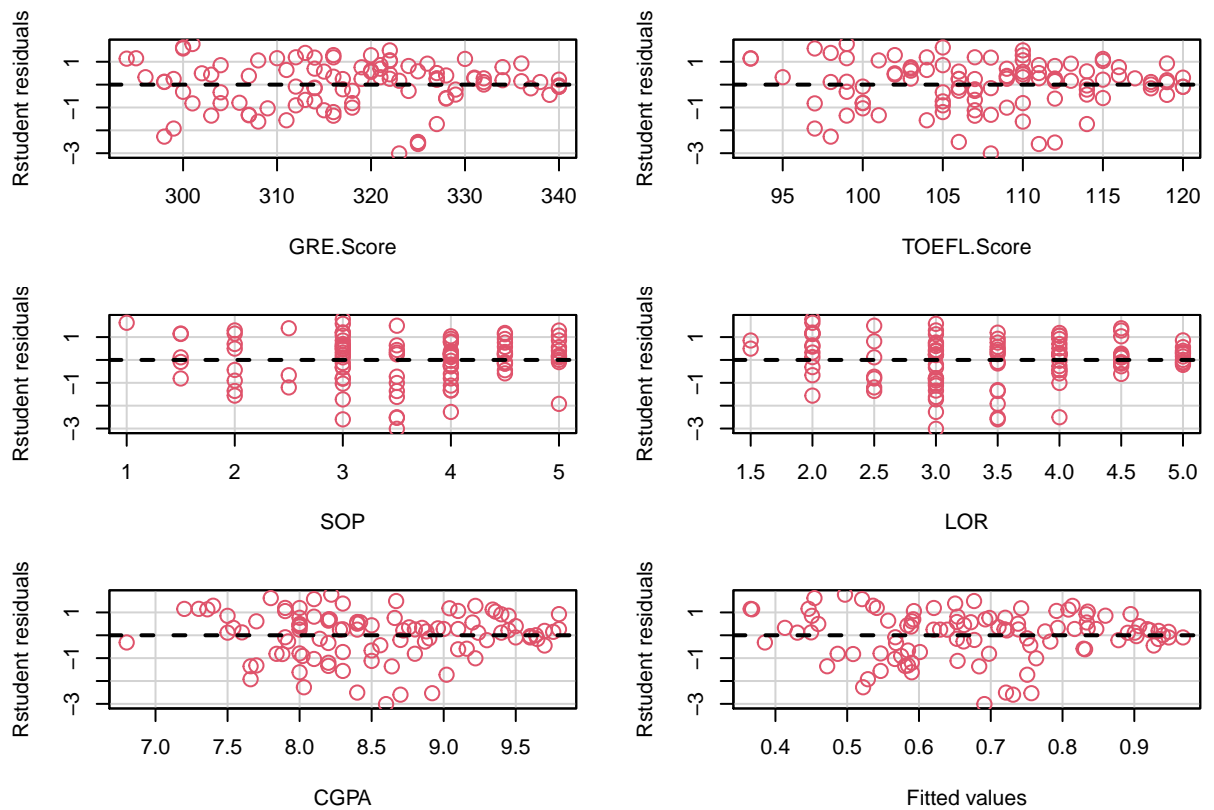
$$\begin{cases} H_0 : \beta_5 = 0 \\ H_1 : \beta_5 \neq 0 \end{cases}$$

6. Ejercicio6

7. Ejercicio7

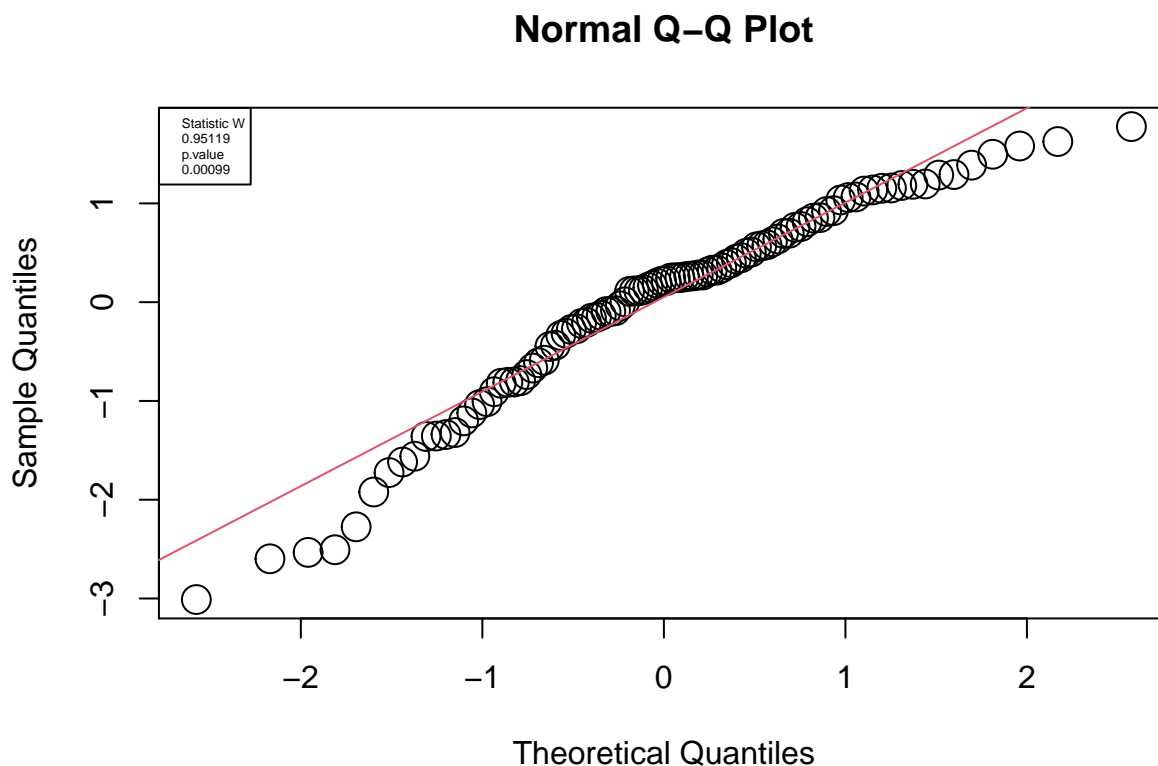
8. Residuales estudentizados vs. Valores ajustados

8.1. Gráfico de los residuales estudentizados vs. Valores ajustados



9. Prueba de normalidad para los residuales estudentizados

9.1. Gráfico q-norm residuales estudentizados



10. Diagnostico sobre la presencia de observaciones atipicas, de balanceo y/o inflenciales

```
## Influence measures of
## lm(formula = data$Chance.of.Admit ~ ., data = data) :
##
##      dfb.1_  dfb.GRE.  dfb.TOEFL  dfb.SOP  dfb.LOR  dfb.CGPA      dffit cov.r
## 1  0.015973 -0.005271 -0.000885  1.31e-03  0.002340 -8.90e-03 -0.032882 1.108
## 2  0.010661 -0.024639  0.034326 -4.49e-03 -0.022518 -1.79e-03 -0.056504 1.105
## 3 -0.024402  0.089374 -0.049594 -2.27e-02  0.092619 -1.18e-01  0.213646 1.005
## 4 -0.146856  0.086964 -0.039096  3.90e-02 -0.271542  1.05e-01  0.319520 0.966
## 5 -0.021116  0.031828 -0.043631 -1.08e-01  0.005196  3.90e-02  0.150002 1.081
## 6 -0.141724  0.061166 -0.037386  9.77e-02 -0.252847  1.41e-01  0.313284 1.060
```

| | | | | | | | | |
|-------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-------|
| ## 7 | -0.000457 | 0.008477 | 0.050364 | -5.48e-02 | 0.107665 | -1.05e-01 | 0.157786 | 1.087 |
| ## 8 | 0.114484 | -0.026751 | -0.010652 | -4.42e-02 | 0.206779 | -1.07e-01 | 0.260972 | 1.052 |
| ## 9 | 0.030175 | -0.047175 | 0.017687 | -5.13e-02 | -0.085702 | 7.61e-02 | 0.149108 | 1.145 |
| ## 10 | 0.331213 | -0.336547 | 0.264130 | -7.77e-02 | 0.323458 | -1.01e-01 | -0.519954 | 0.629 |
| ## 11 | 0.274899 | -0.435231 | 0.332579 | -3.85e-02 | -0.156837 | 2.08e-01 | -0.582385 | 0.759 |
| ## 12 | -0.008881 | 0.010344 | -0.008548 | -3.61e-03 | 0.022573 | -3.28e-03 | 0.044150 | 1.088 |
| ## 13 | 0.020921 | -0.015918 | 0.011308 | 1.51e-02 | -0.044372 | -2.35e-03 | -0.096725 | 1.067 |
| ## 14 | 0.066481 | -0.074405 | 0.087449 | 3.07e-02 | 0.015934 | -4.92e-02 | 0.114265 | 1.151 |
| ## 15 | -0.020685 | 0.026567 | -0.041123 | 5.93e-02 | -0.128505 | 4.48e-02 | 0.151365 | 1.097 |
| ## 16 | 0.025571 | -0.034946 | 0.043923 | -4.62e-02 | 0.097394 | -3.15e-02 | -0.128213 | 1.062 |
| ## 17 | 0.004144 | -0.004799 | 0.013229 | -1.55e-02 | 0.024002 | -1.68e-02 | -0.035468 | 1.095 |
| ## 18 | -0.019400 | 0.032642 | -0.014545 | 3.59e-02 | -0.011729 | -3.35e-02 | 0.057146 | 1.119 |
| ## 19 | -0.004595 | 0.032455 | -0.017848 | -3.99e-02 | 0.089071 | -5.98e-02 | -0.139737 | 1.053 |
| ## 20 | 0.064999 | -0.057361 | -0.007345 | 3.40e-03 | -0.017908 | 6.56e-02 | 0.103144 | 1.112 |
| ## 21 | -0.013257 | -0.014360 | 0.095139 | 2.85e-02 | -0.145174 | -5.83e-02 | 0.260675 | 1.019 |
| ## 22 | -0.077504 | 0.023602 | 0.061565 | -1.24e-02 | -0.115764 | -1.39e-02 | 0.179340 | 1.143 |
| ## 23 | 0.023989 | -0.039710 | 0.031889 | 1.38e-02 | 0.040631 | 5.31e-03 | 0.092445 | 1.112 |
| ## 24 | -0.006252 | -0.008693 | 0.012712 | 8.08e-03 | -0.003257 | 1.02e-02 | 0.042630 | 1.116 |
| ## 25 | -0.124820 | 0.008542 | 0.016489 | -5.15e-02 | -0.163031 | 1.71e-01 | 0.282553 | 1.103 |
| ## 26 | 0.011731 | -0.004207 | -0.004059 | 8.36e-04 | 0.000665 | -3.30e-04 | -0.021018 | 1.117 |
| ## 27 | -0.011184 | 0.014573 | -0.017092 | 3.03e-02 | -0.018890 | 5.01e-03 | 0.043659 | 1.093 |
| ## 28 | 0.015479 | -0.011365 | 0.005564 | -1.95e-02 | 0.008679 | 3.29e-04 | 0.030514 | 1.140 |
| ## 29 | 0.089603 | 0.028826 | -0.115292 | -2.49e-02 | -0.022679 | -3.50e-03 | 0.295331 | 1.043 |
| ## 30 | -0.113045 | 0.181667 | -0.099887 | -1.10e-01 | -0.047718 | -9.79e-02 | 0.340113 | 1.063 |
| ## 31 | 0.198657 | -0.079822 | -0.166260 | -1.05e-02 | 0.006879 | 1.78e-01 | 0.375503 | 0.961 |
| ## 32 | -0.051491 | 0.085395 | -0.076129 | 3.43e-02 | 0.005311 | -2.82e-02 | 0.100998 | 1.219 |
| ## 33 | -0.013715 | 0.003431 | 0.007064 | -2.34e-02 | 0.008446 | 2.70e-03 | 0.033081 | 1.155 |
| ## 34 | 0.009161 | -0.008044 | 0.007108 | 4.24e-04 | 0.004706 | -4.90e-03 | -0.011655 | 1.171 |
| ## 35 | -0.011816 | 0.006516 | -0.031057 | -2.48e-02 | 0.014565 | 4.89e-02 | 0.076932 | 1.150 |
| ## 36 | 0.061927 | -0.049089 | 0.000340 | 4.18e-02 | 0.074195 | 1.17e-02 | 0.140805 | 1.111 |
| ## 37 | 0.088374 | -0.089525 | 0.058479 | -1.43e-03 | 0.046613 | -6.19e-04 | 0.099095 | 1.232 |
| ## 38 | 0.289491 | -0.429309 | 0.423333 | -4.91e-01 | 0.031771 | 9.97e-02 | 0.694648 | 1.066 |
| ## 39 | 0.052161 | -0.066482 | 0.122254 | 5.63e-02 | -0.113521 | -7.53e-02 | 0.251884 | 1.107 |
| ## 40 | -0.255487 | 0.232718 | -0.326200 | -1.17e-01 | -0.215678 | 3.35e-01 | -0.477976 | 1.079 |
| ## 41 | -0.277706 | 0.346912 | -0.434158 | -4.85e-03 | -0.106308 | 2.07e-01 | -0.497296 | 0.988 |
| ## 42 | 0.084137 | -0.082768 | 0.058895 | 7.84e-02 | 0.108972 | -4.59e-02 | -0.218716 | 1.004 |
| ## 43 | 0.013603 | 0.026640 | -0.011987 | 6.10e-02 | 0.123882 | -1.05e-01 | -0.180700 | 1.112 |
| ## 44 | -0.018278 | 0.003128 | 0.021003 | 1.30e-02 | -0.003311 | -1.48e-02 | 0.051596 | 1.099 |
| ## 45 | -0.014287 | -0.021290 | -0.016245 | 3.08e-02 | -0.048117 | 1.02e-01 | 0.167914 | 1.044 |
| ## 46 | 0.007463 | 0.004356 | -0.059844 | 1.46e-01 | -0.041006 | 5.42e-02 | 0.213723 | 1.031 |
| ## 47 | -0.002662 | 0.008571 | -0.008722 | 1.63e-02 | -0.031293 | -9.99e-04 | -0.046295 | 1.112 |
| ## 48 | 0.068405 | -0.029890 | 0.004641 | -5.31e-03 | 0.049188 | -3.87e-02 | -0.108445 | 1.114 |
| ## 49 | 0.029021 | -0.027530 | 0.021785 | -3.67e-02 | 0.075908 | -1.40e-02 | 0.086286 | 1.134 |
| ## 50 | -0.037297 | 0.035597 | 0.020621 | -4.45e-02 | 0.057919 | -6.79e-02 | 0.115376 | 1.103 |
| ## 51 | 0.026081 | 0.140218 | -0.290453 | -1.84e-01 | 0.285638 | 3.97e-02 | 0.516553 | 1.074 |

| | | | | | | | | |
|-------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-------|
| ## 52 | 0.000729 | -0.005882 | 0.007035 | 1.86e-02 | -0.012222 | 1.43e-03 | -0.026790 | 1.169 |
| ## 53 | -0.160106 | 0.142206 | 0.082089 | 9.95e-02 | -0.034187 | -2.55e-01 | 0.327963 | 1.215 |
| ## 54 | -0.093182 | 0.076644 | 0.053409 | 1.11e-01 | -0.101269 | -1.33e-01 | 0.237963 | 1.109 |
| ## 55 | -0.018067 | 0.018214 | 0.043723 | -1.96e-02 | 0.043928 | -8.83e-02 | 0.109819 | 1.115 |
| ## 56 | -0.087691 | 0.138606 | -0.077528 | 3.09e-02 | 0.000688 | -1.02e-01 | 0.177323 | 1.129 |
| ## 57 | -0.118490 | 0.211814 | -0.059031 | -1.04e-01 | 0.122542 | -2.61e-01 | 0.407980 | 1.054 |
| ## 58 | 0.014636 | -0.005705 | -0.002282 | 2.59e-02 | -0.015036 | -3.71e-03 | 0.037494 | 1.159 |
| ## 59 | -0.022431 | -0.005830 | -0.021343 | -4.07e-02 | -0.005099 | 8.32e-02 | -0.107246 | 1.183 |
| ## 60 | 0.047541 | 0.003836 | 0.048042 | 2.08e-01 | 0.240416 | -2.42e-01 | -0.420743 | 0.980 |
| ## 61 | -0.012294 | -0.055765 | 0.124552 | -2.84e-03 | 0.018216 | -4.29e-02 | -0.182073 | 1.026 |
| ## 62 | -0.081901 | -0.008995 | 0.126685 | -1.66e-01 | 0.069436 | -4.59e-02 | -0.272327 | 0.990 |
| ## 63 | -0.057222 | 0.062205 | -0.042738 | 2.05e-02 | -0.012725 | -1.06e-02 | -0.073869 | 1.109 |
| ## 64 | -0.012667 | 0.005902 | 0.017642 | -9.38e-02 | 0.090919 | -2.98e-02 | -0.167268 | 1.006 |
| ## 65 | 0.175776 | -0.087560 | -0.048097 | 2.40e-01 | 0.000367 | -1.04e-02 | -0.407973 | 0.718 |
| ## 66 | 0.129238 | -0.019008 | -0.046649 | 1.14e-01 | 0.100351 | -1.12e-01 | -0.353366 | 0.728 |
| ## 67 | 0.155795 | 0.000649 | -0.086083 | 1.89e-01 | 0.195107 | -1.67e-01 | -0.403104 | 0.931 |
| ## 68 | -0.039722 | 0.037537 | 0.014270 | 2.48e-02 | -0.001391 | -6.70e-02 | -0.157145 | 0.960 |
| ## 69 | -0.064875 | 0.096831 | 0.005195 | 9.56e-02 | -0.019210 | -1.69e-01 | -0.224471 | 1.049 |
| ## 70 | 0.014708 | 0.012221 | -0.030933 | -2.56e-02 | 0.009103 | -2.35e-03 | -0.093566 | 1.069 |
| ## 71 | 0.000075 | -0.000283 | 0.000299 | 8.24e-05 | 0.000287 | 6.69e-05 | 0.000828 | 1.122 |
| ## 72 | -0.020166 | 0.023640 | -0.032527 | 1.13e-02 | -0.001191 | 1.77e-02 | 0.046797 | 1.167 |
| ## 73 | 0.094859 | -0.092866 | -0.001896 | 4.41e-02 | 0.088543 | 7.29e-02 | 0.222919 | 1.086 |
| ## 74 | 0.137421 | -0.136186 | 0.004666 | 6.64e-02 | 0.017041 | 1.22e-01 | 0.252313 | 1.020 |
| ## 75 | -0.021091 | 0.018772 | -0.003615 | 2.49e-02 | -0.034008 | -8.94e-03 | -0.045077 | 1.188 |
| ## 76 | 0.028506 | 0.001118 | -0.061666 | 1.17e-01 | -0.066943 | 4.16e-02 | -0.151314 | 1.180 |
| ## 77 | -0.025741 | 0.014689 | 0.001279 | -1.50e-02 | -0.019196 | 5.39e-03 | 0.041335 | 1.104 |
| ## 78 | 0.127688 | -0.081097 | -0.172463 | 3.78e-02 | -0.310500 | 3.46e-01 | 0.509345 | 0.944 |
| ## 79 | 0.030019 | -0.000635 | -0.033715 | 2.78e-02 | -0.030049 | 1.39e-02 | 0.082230 | 1.127 |
| ## 80 | 0.111463 | -0.020275 | -0.100074 | -1.26e-01 | -0.016872 | 7.94e-02 | 0.320202 | 1.060 |
| ## 81 | -0.026938 | 0.032904 | -0.054656 | 1.47e-01 | -0.053523 | 1.93e-02 | -0.188881 | 1.055 |
| ## 82 | 0.008637 | -0.003825 | -0.005465 | -4.43e-03 | -0.006818 | 7.62e-03 | -0.023089 | 1.130 |
| ## 83 | 0.098485 | -0.084766 | -0.026844 | 1.24e-01 | 0.054883 | 7.97e-02 | 0.281096 | 1.005 |
| ## 84 | 0.119641 | -0.198210 | 0.158992 | -9.28e-02 | 0.100847 | 7.59e-02 | 0.269832 | 1.063 |
| ## 85 | -0.042854 | 0.040413 | -0.028288 | 8.92e-03 | -0.006532 | 3.63e-03 | 0.055436 | 1.132 |
| ## 86 | -0.060438 | 0.124849 | -0.180635 | 1.27e-01 | -0.070342 | 4.58e-02 | 0.218606 | 1.113 |
| ## 87 | 0.016725 | 0.009047 | -0.022808 | 8.29e-02 | -0.008040 | -2.18e-02 | 0.103772 | 1.079 |
| ## 88 | -0.006190 | 0.008571 | -0.001700 | 8.79e-03 | -0.010627 | -8.03e-03 | 0.030202 | 1.078 |
| ## 89 | -0.011000 | 0.006249 | -0.012024 | -2.30e-02 | -0.006780 | 2.29e-02 | -0.035760 | 1.122 |
| ## 90 | 0.020258 | -0.021429 | 0.007697 | 3.48e-02 | -0.013044 | 1.02e-02 | 0.059259 | 1.089 |
| ## 91 | -0.001317 | -0.019541 | -0.000741 | -2.70e-02 | -0.038467 | 6.19e-02 | -0.074524 | 1.142 |
| ## 92 | -0.342180 | 0.033477 | 0.170196 | -5.82e-01 | -0.145039 | 2.59e-01 | -0.776410 | 0.982 |
| ## 93 | -0.396022 | 0.201905 | 0.139874 | -2.95e-01 | 0.018618 | -1.16e-01 | -0.605135 | 0.825 |
| ## 94 | -0.086032 | 0.013961 | 0.078864 | -1.12e-02 | -0.022405 | -3.13e-02 | -0.172054 | 1.066 |
| ## 95 | -0.084618 | 0.025508 | 0.023474 | 1.32e-01 | -0.021645 | -7.56e-03 | -0.267881 | 0.985 |
| ## 96 | -0.050721 | 0.039164 | -0.001385 | 1.53e-01 | -0.013264 | -5.24e-02 | -0.203312 | 1.086 |

```

## 97 -0.049015  0.000753  0.053381  2.65e-04 -0.008551 -1.66e-02 -0.126933 1.050
## 98 -0.002882 -0.028471  0.071999 -1.24e-02  0.017486 -3.54e-02  0.087095 1.146
## 99 -0.000438 -0.006485  0.015672  7.69e-03  0.005817 -9.51e-03  0.026547 1.128
## 100 0.004924 -0.011130  0.015630 -1.58e-03  0.008346 -4.14e-03  0.025468 1.088
##      cook.d      hat inf
## 1  1.82e-04 0.0393
## 2  5.37e-04 0.0401
## 3  7.57e-03 0.0310
## 4  1.68e-02 0.0435
## 5  3.77e-03 0.0441
## 6  1.63e-02 0.0720
## 7  4.17e-03 0.0489
## 8  1.13e-02 0.0572
## 9  3.74e-03 0.0831
## 10 4.15e-02 0.0290  *
## 11 5.35e-02 0.0512  *
## 12 3.28e-04 0.0251
## 13 1.57e-03 0.0243
## 14 2.20e-03 0.0823
## 15 3.84e-03 0.0530
## 16 2.75e-03 0.0297
## 17 2.12e-04 0.0292
## 18 5.50e-04 0.0507
## 19 3.27e-03 0.0290
## 20 1.79e-03 0.0530
## 21 1.13e-02 0.0453
## 22 5.40e-03 0.0871
## 23 1.44e-03 0.0507
## 24 3.06e-04 0.0465
## 25 1.33e-02 0.0851
## 26 7.44e-05 0.0463
## 27 3.21e-04 0.0283
## 28 1.57e-04 0.0657
## 29 1.45e-02 0.0615
## 30 1.92e-02 0.0796
## 31 2.31e-02 0.0534
## 32 1.72e-03 0.1291  *
## 33 1.84e-04 0.0778
## 34 2.29e-05 0.0892
## 35 9.96e-04 0.0769
## 36 3.33e-03 0.0594
## 37 1.65e-03 0.1379  *
## 38 7.90e-02 0.1543
## 39 1.06e-02 0.0806
## 40 3.78e-02 0.1160

```

```
## 41 4.05e-02 0.0863
## 42 7.94e-03 0.0321
## 43 5.47e-03 0.0684
## 44 4.48e-04 0.0342
## 45 4.71e-03 0.0324
## 46 7.60e-03 0.0387
## 47 3.61e-04 0.0441
## 48 1.98e-03 0.0553
## 49 1.25e-03 0.0662
## 50 2.24e-03 0.0493
## 51 4.40e-02 0.1218
## 52 1.21e-04 0.0885
## 53 1.80e-02 0.1550 *
## 54 9.47e-03 0.0786
## 55 2.03e-03 0.0563
## 56 5.28e-03 0.0776
## 57 2.75e-02 0.0907
## 58 2.37e-04 0.0810
## 59 1.94e-03 0.1044
## 60 2.91e-02 0.0678
## 61 5.52e-03 0.0299
## 62 1.23e-02 0.0397
## 63 9.18e-04 0.0458
## 64 4.65e-03 0.0218
## 65 2.61e-02 0.0241 *
## 66 1.97e-02 0.0191 *
## 67 2.65e-02 0.0518
## 68 4.08e-03 0.0132
## 69 8.40e-03 0.0473
## 70 1.47e-03 0.0247
## 71 1.15e-07 0.0499
## 72 3.69e-04 0.0880
## 73 8.31e-03 0.0635
## 74 1.06e-02 0.0436
## 75 3.42e-04 0.1035
## 76 3.85e-03 0.1076
## 77 2.88e-04 0.0367
## 78 4.23e-02 0.0759
## 79 1.14e-03 0.0604
## 80 1.70e-02 0.0736
## 81 5.96e-03 0.0416
## 82 8.98e-05 0.0566
## 83 1.31e-02 0.0455
## 84 1.21e-02 0.0637
## 85 5.17e-04 0.0608
```



```

## 74  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 75  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 76  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 77  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 78  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 79  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 80  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 81  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 82  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 83  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 84  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 85  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 86  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 87  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 88  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 89  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 90  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 91  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 92  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  TRUE  FALSE  FALSE  FALSE
## 93  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 94  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 95  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 96  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 97  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 98  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 99  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE
## 100 FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE  FALSE

```

11. Ejercicio11

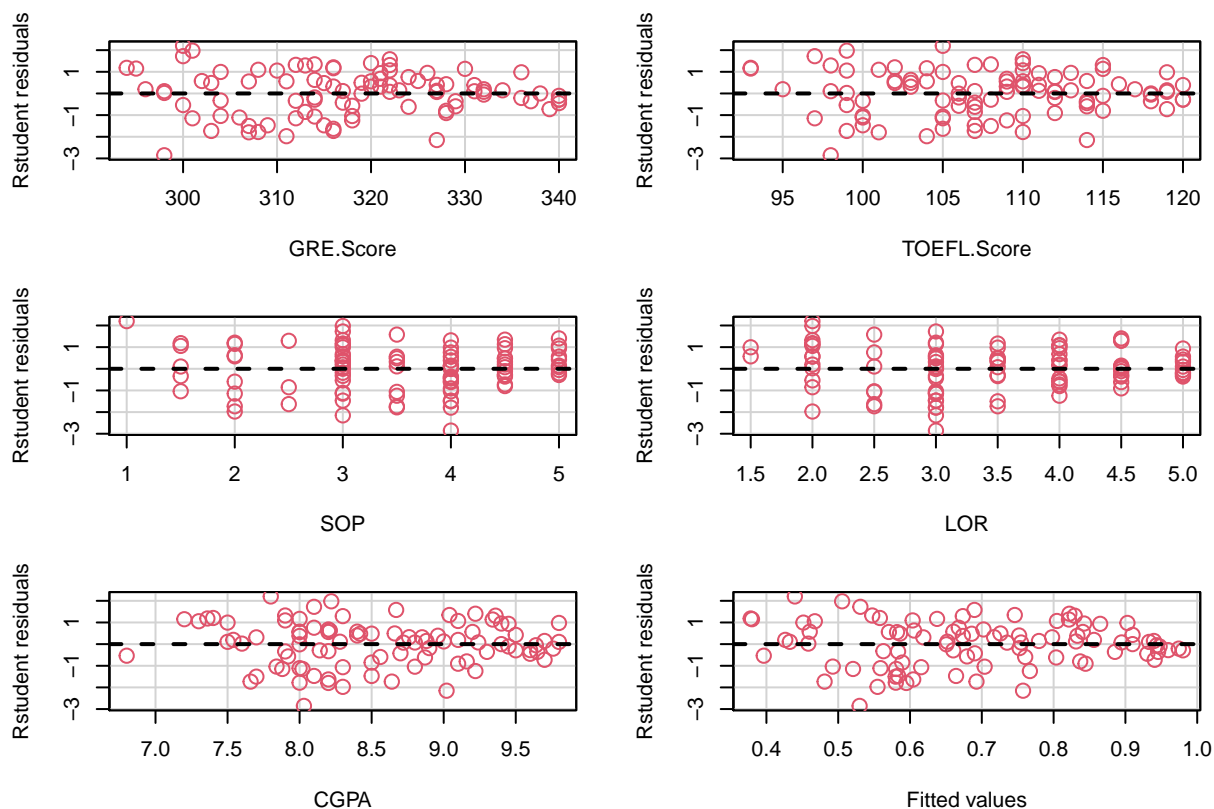
```

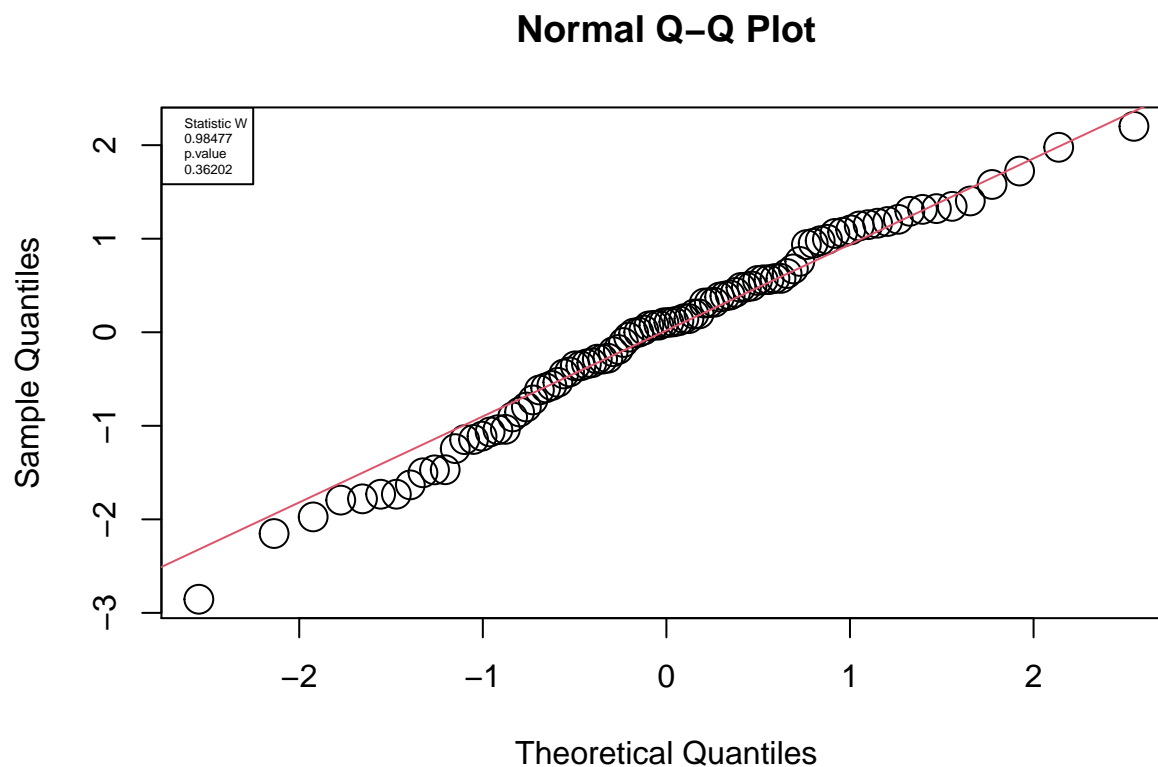
## Analysis of Variance Table
##
## Response: Chance.of.Admit
##
##              Df Sum Sq Mean Sq F value    Pr(>F)
## FO(GRE.Score, TOEFL.Score, SOP, LOR, CGPA)  5 2.35558 0.47112  90.573 < 2.2e-16
## Residuals                                86 0.44733 0.00520
##
## FO(GRE.Score, TOEFL.Score, SOP, LOR, CGPA) ***
## Residuals
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##

```



```
## Call:
## lm(formula = Chance.of.Admit ~ ., data = AdmissionPredict_sin_influencias)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.189817 -0.041224  0.007218  0.045167  0.140378
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.9798608  0.2948862  -6.714 1.93e-09 ***
## GRE.Score     0.0057790  0.0016903   3.419 0.000963 ***
## TOEFL.Score   0.0002077  0.0028940   0.072 0.942945
## SOP           0.0153807  0.0108883   1.413 0.161385
## LOR           0.0403174  0.0125305   3.218 0.001823 **
## CGPA          0.0728150  0.0241848   3.011 0.003420 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.07212 on 86 degrees of freedom
## Multiple R-squared:  0.8404, Adjusted R-squared:  0.8311
## F-statistic: 90.57 on 5 and 86 DF,  p-value: < 2.2e-16
```





12. Ejercicio 12

```
##          GRE.Score TOEFL.Score      SOP      LOR      CGPA
## GRE.Score      1.0000000  0.8883788 0.5183744 0.6493865 0.8040898
## TOEFL.Score    0.8883788  1.0000000 0.5739543 0.5855924 0.8117425
## SOP            0.5183744  0.5739543 1.0000000 0.6050348 0.6515129
## LOR            0.6493865  0.5855924 0.6050348 1.0000000 0.7393324
## CGPA           0.8040898  0.8117425 0.6515129 0.7393324 1.0000000
## Chance.of.Admit 0.8078850  0.7800010 0.6136879 0.7428750 0.8326816
##
##          Chance.of.Admit
## GRE.Score      0.8078850
## TOEFL.Score    0.7800010
## SOP            0.6136879
## LOR            0.7428750
## CGPA           0.8326816
## Chance.of.Admit 1.0000000
```

```
##  GRE.Score TOEFL.Score      SOP      LOR      CGPA
##  5.691210  5.858051    1.928844  2.519579  4.615227
```

```

##          GRE.Score TOEFL.Score          SOP          LOR          CGPA
## GRE.Score      1.0000000  0.9061621 0.5769656 0.6945897 0.8381136
## TOEFL.Score    0.9061621  1.0000000 0.6269824 0.6213013 0.8266527
## SOP            0.5769656  0.6269824 1.0000000 0.6153549 0.6986389
## LOR            0.6945897  0.6213013 0.6153549 1.0000000 0.7571056
## CGPA           0.8381136  0.8266527 0.6986389 0.7571056 1.0000000
## Chance.of.Admit 0.8595873  0.8077359 0.6683703 0.7845642 0.8677695
##          Chance.of.Admit
## GRE.Score      0.8595873
## TOEFL.Score    0.8077359
## SOP            0.6683703
## LOR            0.7845642
## CGPA           0.8677695
## Chance.of.Admit 1.0000000

##  GRE.Score TOEFL.Score          SOP          LOR          CGPA
##   7.229071   6.690216   2.147637   2.640310   5.224542

```

13. Ejercicio13

14. Selección del modelo