Name:	

This exam has 9 questions, for a total of 100 points.

1. 10 points Given the following grammar for language \mathcal{R} , indicate which of the following programs are in the language specified by the grammar. That is, which programs can be parsed as an exp non-terminal.

```
atm ::= int \mid var
exp ::= atm \mid (read) \mid (-atm) \mid (if exp exp exp) \mid (eq? atm atm)
      | (let ([var exp]) exp)
\mathcal{R} ::= exp
  1. (let ([x (read)])
       (let ([y (if (eq? x 0) 1 (- 2))])
         y))
  2. (let ([x 5])
       (let ([y (- (read))])
         y))
  3. (let ([x (read)])
       (let ([y (* 2 x)])
         y))
  4. (let ([x (read)])
       (let ([y (if (eq? x 5) (eq? 2 3)
                     (if (eq? x 0) (- x) (read)))])
         y))
  5. (let ([x (-5)])
       (let ([y (if (eq? (-x) 5) 0 1)])
         y))
```

Solution: (2 points each)

- 1. Yes
- 2. No, because (read) is not in atm but it is an argument of the negation operator.
- 3. No, because * is not in the grammar.
- 4. Yes
- 5. No, because (- x) is not in atm but it is an argument of the eq? operator.

2. 9 points Convert the following program to its Abstract Syntax Tree representation (see the grammar for \mathcal{L}_{While} in the Appendix of this exam) and draw the tree with one node per instance of a Racket struct.

```
(let ([sum 0])
  (begin
     (while (eq? (read) 0)
           (set! sum (+ sum 1)))
     sum))
```

3. 12 points Fill in the blanks to complete the following interpreter for \mathcal{L}_{Int} .

```
(define (interp_exp e)
 (match ___(a)___
    [(Int n) ___(b)___]
    [(Prim 'read '())
     (define r (read))
     (cond [(fixnum? r) r]
           [else (error 'interp_exp "read expected an integer: ~v" r)])]
    [(Prim '- (list e))
    (define v ___(c)___)
     (fx-0v)
    [(Prim '+ (list e1 e2))
    (define v1 (interp_exp e1))
    (define v2 (interp_exp e2))
   ___(d)___]
[(Prim '- ___(e)___)
     (define v1 (interp_exp e1))
     (define v2 (interp_exp e2))
    (fx- v1 v2)]))
(define (interp_Lint p)
 (match p
    [(Program '() e) ___(f)__]))
```

```
Solution: (2 points each)
    (a) e
    (b) n
    (c) (interp_exp e)
    (d) (fx+ v1 v2)
    (e) (list e1 e2)
    (f) (interp_exp e)
```

4. 10 points Fill in the labeled blanks in the following implementation of the Remove Complex Operands pass.

```
(define/public (rco-atom e)
 (match e
    [(Var x) (values (Var x) '())]
    [(Let x rhs body)
     (define new-rhs ___(a)___)
     (define-values (new-body body-ss) (rco-atom body))
     (values new-body ___(b)___)]
    [(Prim op es)
     (define-values (new-es sss)
       (for/lists (11 12) ([e es]) (rco-atom e)))
     (define ss (append* sss))
     (define tmp (gensym 'tmp))
     (values ___(c)___
             (append ss '((,tmp . ,(Prim op new-es)))))]
    ...))
(define/public (rco-exp e)
 (match e
    [(Var x) (Var x)]
    [(Prim op es)
     (define-values (new-es sss)
       (for/lists (11 12) ([e es]) ___(d)___))
     (make-lets (append* sss) (Prim op new-es))]
    ...))
(define/public (remove-complex-opera* p)
 (match p
    [(Program info e) (Program info ___(e)___)]))
```

Solution:

- (a) (rco-exp rhs)
- (b) (append '((,x . ,new-rhs)) body-ss)
- (c) (Var tmp)
- (d) (rco-atom e)
- (e) (rco-exp e)

5. 12 points Translate the following $\mathcal{L}_{\mathsf{While}}^{\mathit{mon}}$ program into an equivalent $\mathcal{C}_{\circlearrowleft}$ program. The grammars for $\mathcal{L}_{\mathsf{While}}^{\mathit{mon}}$ and $\mathcal{C}_{\circlearrowleft}$ are in the Appendix of this exam. You may write your answer in either abstract syntax or concrete syntax.

```
Solution:
  start:
      n69 = (read);
      goto loop71;
  loop71:
      tmp70 = (read);
      if (< tmp70 n69)
         goto block73;
      else
         goto block74;
  block74:
      if (> n69 100)
         goto loop71;
      else
         goto block72;
  block73:
      if (> n69 0)
         goto loop71;
      else
         goto block72;
  block72:
      return (read);
```

6. 12 points Annotate each of the following instructions with the set of variables that are live immediately after the instruction. Annotate each label with the set of variables that are live before the first instruction in the label's block.

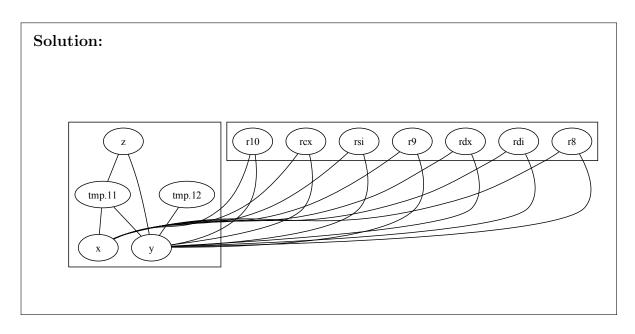
block79:

```
start:
                                              movq y, tmp3
    callq read_int
                                              movq y, tmp4
   movq %rax, x
                                              movq tmp3, y
   movq $1, y
                                              addq tmp4, y
    callq read_int
                                              movq i, tmp5
    movq %rax, i
                                              movq tmp5, i
    jmp loop77
                                              subq $1, i
loop77:
                                              jmp loop77
    movq i, tmp2
                                          block78:
    cmpq $0, tmp2
                                              movq y, tmp6
    jg block79
                                              movq x, %rax
    jmp block78
                                              addq tmp6, %rax
                                              jmp conclusion
```

```
Solution: It's OK to ignore rax and rsp.
                                                block78:
                                                                      { x y rsp }
  start:
                                                   movq y, tmp6
                         { rax rsp }
                                                                      { x tmp6 rsp }
      callq read_int
                         { rax rsp }
                                                   movq x, %rax
                                                                      { rax tmp6 rsp }
      movq %rax, x movq $1, y
                         { rax x rsp }
                                                    addq tmp6, %rax
                                                                      { rax rsp }
                         { rax x y rsp }
                                                    jmp conclusion
                                                                      { rax rsp }
      callq read_int
                        { rax x y rsp }
      movq %rax, i
                                               block79:
                         {xyirsp}
                                                                      { x y i rsp }
      jmp loop77
                         {xyirsp}
                                                   movq y, tmp3
                                                                      { x y i tmp3 rsp }
                                                   movq y, tmp4
                                                                      { x i tmp3 tmp4 rsp }
                                                   movq tmp3, y
                         {xyirsp}
                                                                      { x y i tmp4 rsp }
      movq i, tmp2
cmpq $0, tmp2
                         { x y i tmp2 rsp }
                                                                      { x y i rsp }
                                                   addq tmp4, y
                         {xyirsp}
                                                   movq i, tmp5
                                                                      { x y tmp5 rsp }
      jg block79
                         { x y i rsp }
                                                   movq tmp5, i
                                                                      {xyirsp}
      jmp block78
                         {xyirsp}
                                                    subq $1, i
                                                                      {xyirsp}
                                                    jmp loop77
                                                                      {xyirsp}
```

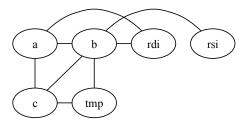
7. 12 points Given the following results from liveness analysis, draw the interference graph. (The callee and caller saved registers are listed in the Appendix of this exam. The liveness results ignore rsp and rax to simplify the graph and because they are not used in register allocation.)

```
start:
 callq read_int
                {}
 movq %rax, x
                {x}
 movq x, y
                \{y, x\}
 callq read_int
                {y, x}
 movq %rax, tmp.11
                {y, tmp.11, x}
 movq x, z
                {y, tmp.11, z}
 addq tmp.11, z
                 {y, z}
 movq z, tmp.12
                {y, tmp.12}
 addq y, tmp.12
                {tmp.12}
 movq tmp.12, %rdi
                {%rdi}
 callq print_int
 movq $0, %rax
  jmp conclusion
                {}
```



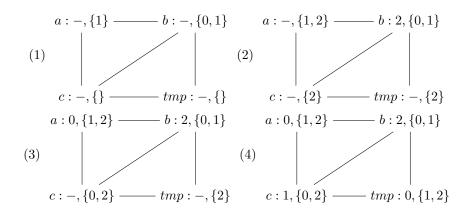
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8. 14 points Given the following interference graph, use the saturation-based graph coloring algorithm to assign the variables a, b, c, and tmp to registers and stack locations. You may only use the registers rdi and rsi. Show each step of the algorithm, include the saturation sets for each variable. To break ties regarding which variables to color first, use alphabetical order.



Solution: Here's a register to color mapping: {rsi:0,rdi:1}.

- 1. We pre-color the variables with the colors of the registers that they interfere with. Variable a interferes with rdi (color 1) and b interferes with both rdi (color 1) and rsi (color 0) (2 points).
- 2. b is the most saturated, so we color b to 2 (2 points).
- 3. Now a is the most saturated, se we color a to 0. (2 points)
- 4. Of the two remaining variables, c is the most saturated, so we color it 1. (2 points)
- 5. Finally, we color tmp with 0. (2 points)



The assignment of variables to registers and stack locations is: (4 points)

 $\{a: rsi, b: -8(\%rbp), c: rdi, tmp: rsi\}$

9. 9 points Given the following code as the result of Patch Instructions, generate a prelude and conclusion to produce a complete x86 program.

```
movq $5, -16(%rbp)
movq $6, %rbx
callq read_int
movq %rax, %rdi
movq -16(%rbp), %rcx
addq %rbx, %rcx
addq %rdi, %rcx
movq %rcx, %rdi
callq print_int
movq $0, %rax
jmp conclusion
```

```
Solution: (1 point per correct instruction)

.globl main

main:
    pushq %rbp
    movq %rsp, %rbp
    pushq %rbx
    subq $8, %rsp
    jmp start

conclusion:
    addq $8, %rsp
    popq %rbx
    popq %rbp
    retq
```

Appendix

```
The caller-saved registers are:
rax rcx rdx rsi rdi r8 r9 r10 r11
and the callee-saved registers are:
rsp rbp rbx r12 r13 r14 r15
```

Grammar for $\mathcal{L}_{\mathsf{While}}$

```
type ::= Integer
 op ::= read | + | -
exp ::= (Int int)
                     | (Prim op (exp...))
                       (Let var exp exp)
exp ::= (Var var)
     ::= Boolean
type
     ::= #t | #f
bool
cmp ::= eq? | < | <= | > | >=
op
      ::= cmp \mid and \mid or \mid not
      ::= (Bool bool) | (If exp \ exp \ exp)
exp
type ::= Void
     ::= (SetBang var \ exp) | (Begin exp^* \ exp) | (WhileLoop exp \ exp) | (Void)
\mathcal{L}_{\mathsf{While}} ::= (Program '() exp)
```

Grammar for $\mathcal{L}_{\mathsf{While}}^{\mathit{mon}}$

Grammar for $\mathcal{C}_{\circlearrowleft}$

```
::= (Int int) | (Var var)
      ::= atm | (Prim 'read ()) | (Prim '- (atm))
           (Prim '+ (atm atm)) | (Prim '- (atm atm))
stmt ::= (Assign (Var var) exp)
tail
      ::= (Return exp) | (Seq stmt \ tail)
     ::= (Bool bool)
atm
cmp ::= eq? | < | <= | > | >=
     ::= (Prim 'not (atm)) | (Prim 'cmp (atm atm))
exp
tail
     ::= (Goto label)
           (IfStmt (Prim cmp (atm atm)) (Goto label) (Goto label))
     ::= (Void)
atm
stmt ::= (Prim 'read ())
\mathcal{C}_{\circlearrowleft} ::= (CProgram info ((label . tail) ...))
```