Artificial Intelligence -M4105C-

Constraint Programming: the user states the problem, the computer solve it

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Artificial Intelligence

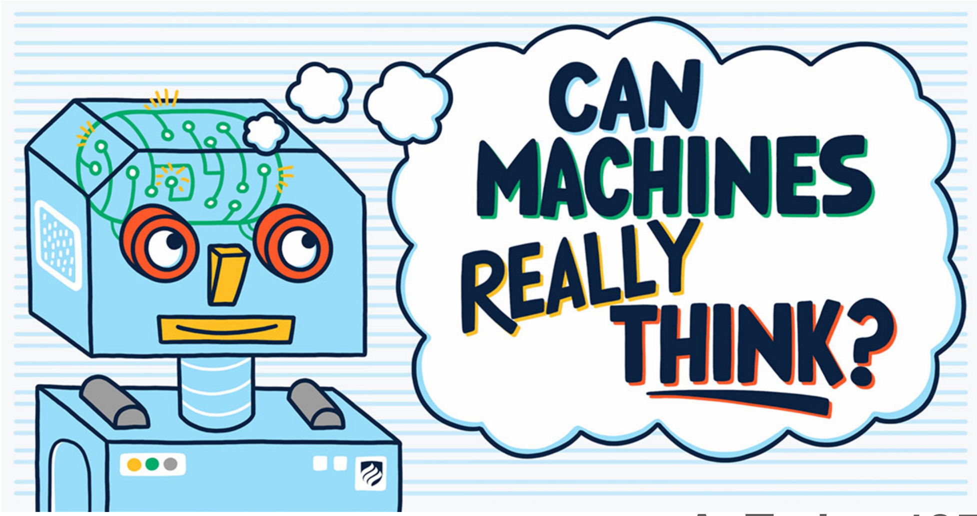
Received ideas

Blind men and an elephant "盲人摸

- ☑ AI is 100% artificial
  - AI needs our help
- ☑ AI would overall surpass human intelligence
  - Living being is far from a machine being
- ☑ AI is dangerous
  - Not about AI, but about data sovereignty
- ☑ An algorithm = an IA
  - 40 % of European AI start-ups are not using IA

Artificial Intelligence

Definition



A. Turing 1950

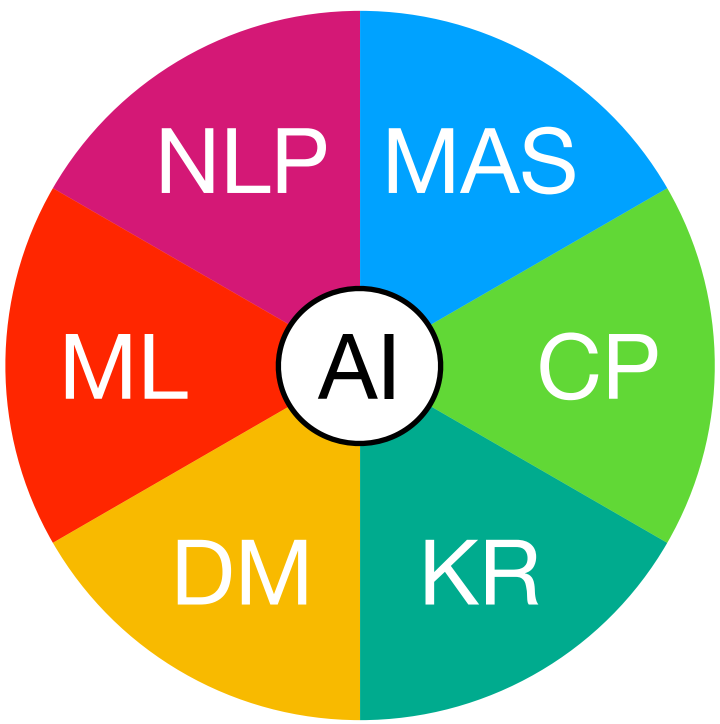
« The science of making machines do things that would require intelligence if done by men » Marvin Minsky

That is, be able to:

- use a language
- make abstractions and to express concepts
- solve different kind of human problems,
- improve themselves

Artificial Intelligence

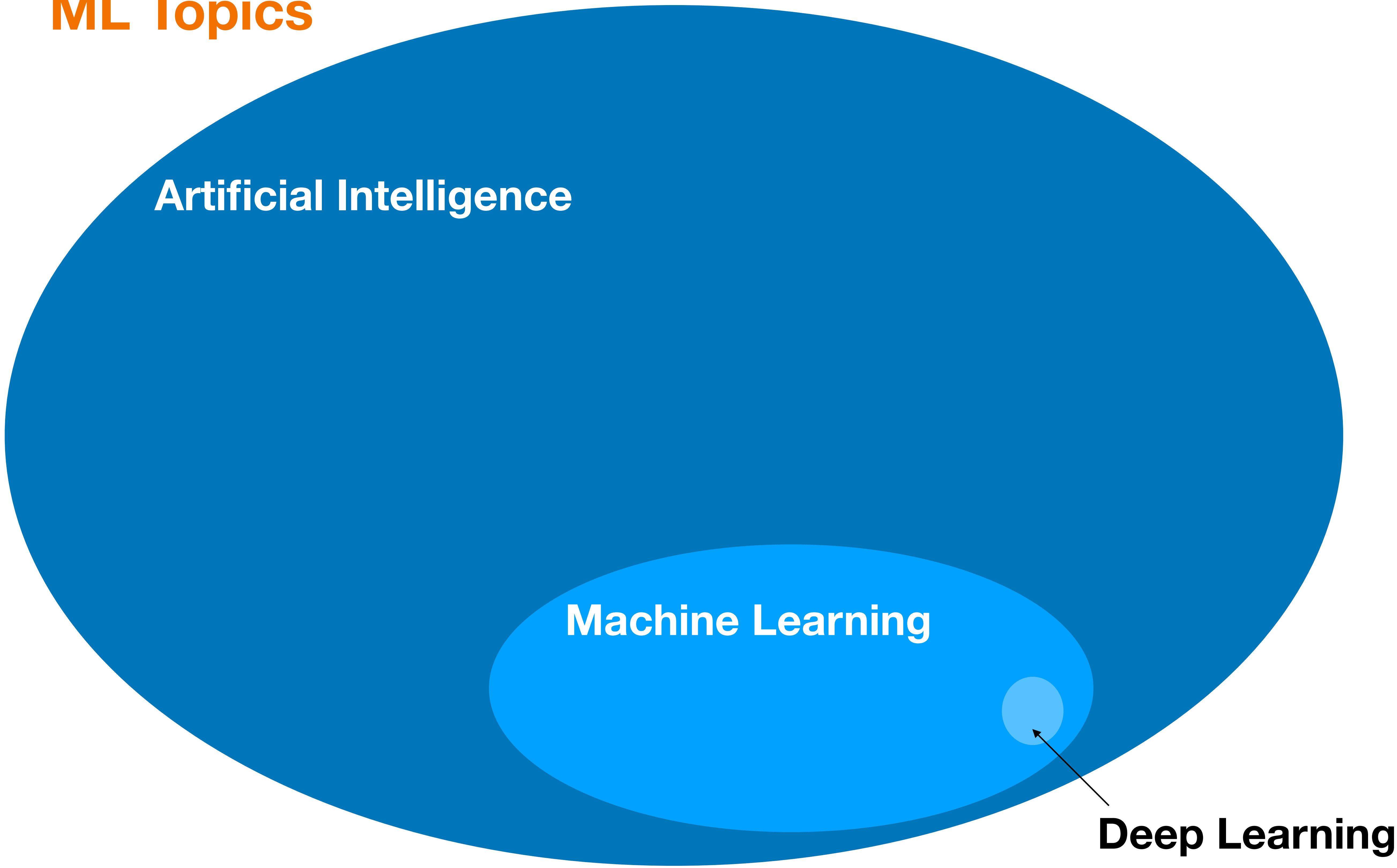
AI Topics



- NLP: Natural Language Processing
- MAS: Multi-Agent Systems
- KR: Knowledge Representation
- DM: Data Mining
- ML: Machine Learning
- CP: Constraint Programming

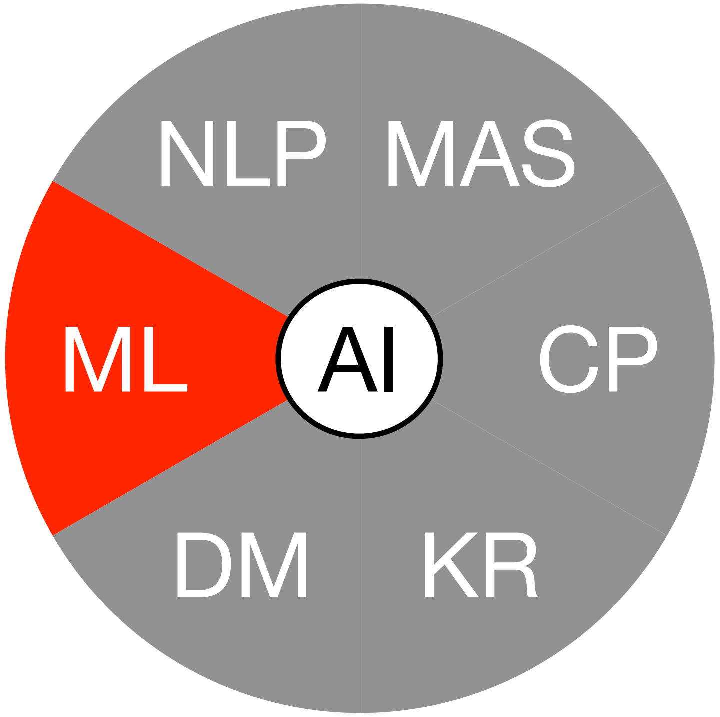
Artificial Intelligence

ML Topics



Artificial Intelligence

ML Topics



1. Active Learning
2. Adversarial Machine Learning
3. Bayesian Optimization
4. Classification
5. Clustering
6. Cost-Sensitive Learning
7. Deep Generative Models

8. Deep Learning

9. Developmental Learning
10. Dimensionality Reduction and Manifold Learning
11. Ensemble Methods
12. Explainable Machine Learning
13. Feature Selection
14. Learning Sparse Models
15. Federated Learning
16. Interpretability
17. Kernel Methods
18. Knowledge-based Learning
19. Learning Generative Models
20. Learning Graphical Models
21. Learning Preferences or Rankings
22. Learning Theory
23. Multi-instance;Multi-label;Multi-view learning
24. Neuro-Symbolic Methods
25. Online Learning
26. Probabilistic Machine Learning
27. Recommender Systems
28. Reinforcement Learning
29. Relational Learning
30. Semi-Supervised Learning
31. Structured Prediction
32. Tensor and Matrix Methods
33. Time-series;Data Streams
34. Transfer, Adaptation, Multi-task Learning
35. Trusted Machine Learning
36. Unsupervised Learning

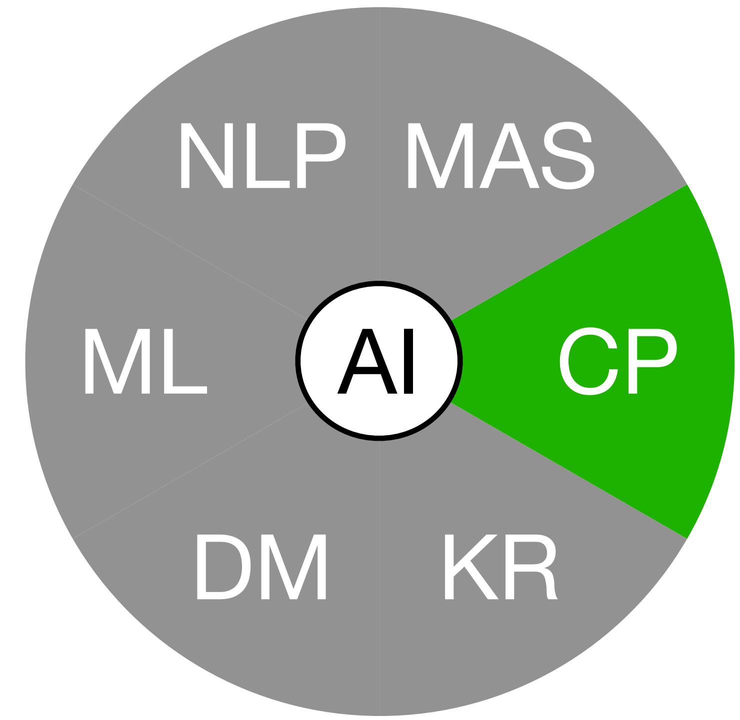
Constraint Programming (CP)

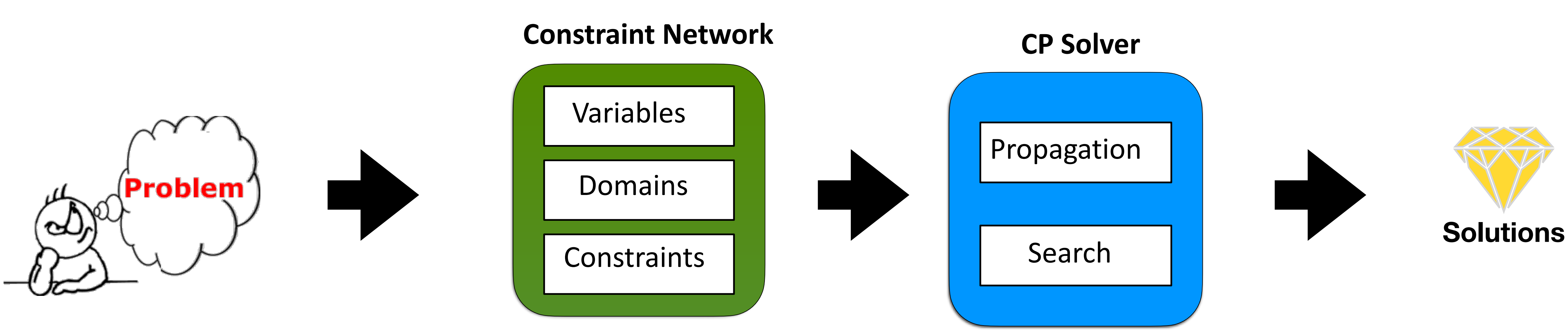
Definition

A formalism to model (**constraint network**) and to solve (**constraint solver**) combinatorial problems (scheduling, planning,…).

Examples of constraints :

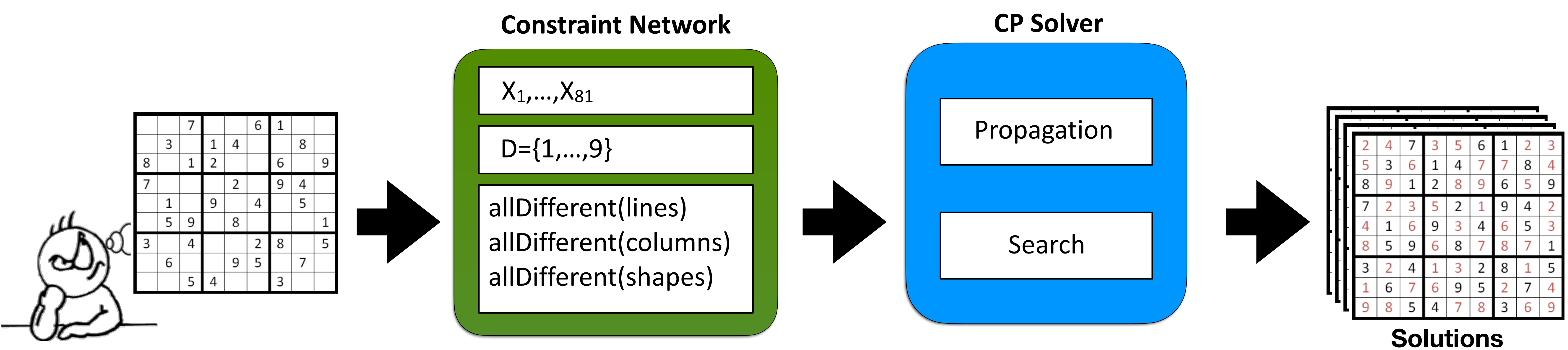
- $X_1+X_2=5$
- $\mathrm{allDifferent}(X_1,..X_n)$
- $c(X_i,X_j)= \{(1,1), (2,1),(2,3), (4,4)\}$





Constraint Programming (CP)

Example



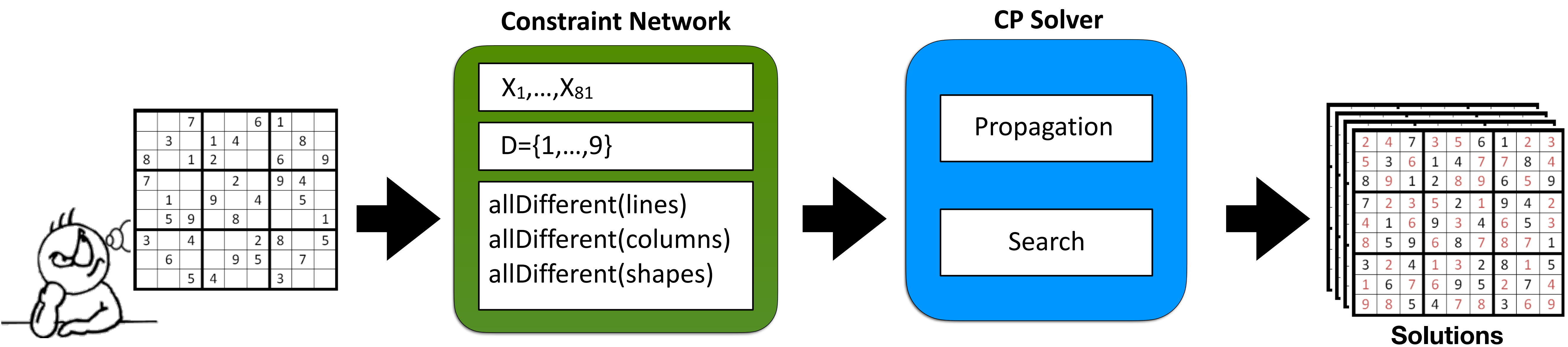
X1={1, 2, 3, 4, 5, 6, 7, 8, 9}

X2={1, 2, 3, 4, 5, 6, 7, 8, 9}

		7			6	1		
	3		1	4			8	
8		1	2			6		9
7				2		9	4	
	1		9		4		5	
	5	9		8				1
3		4			2	8		5
	6			9	5		7	
		5	4			3		

Constraint Programming (CP)

Example



Propagation!

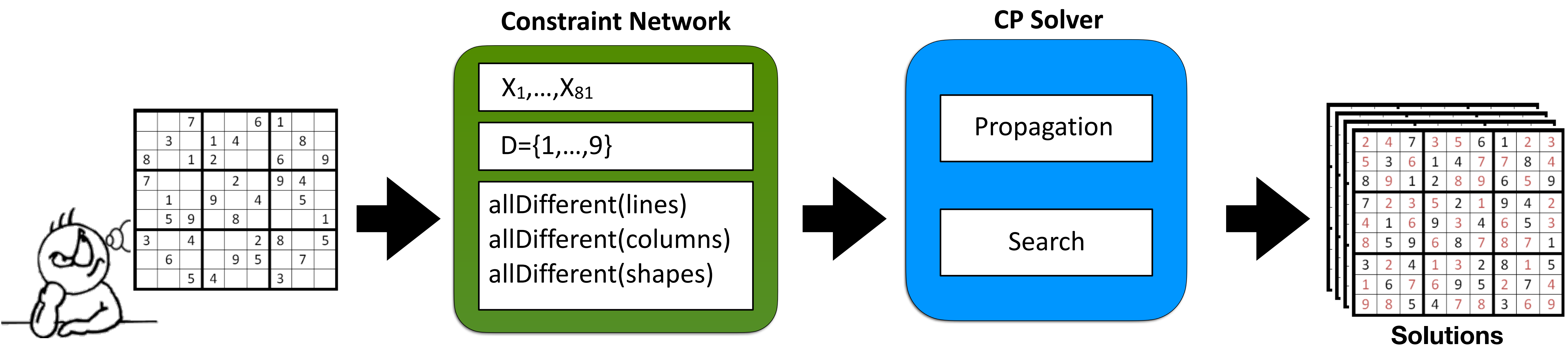
X1={~~1~~, 2, ~~3~~, 4, 5, ~~6~~, ~~7~~, ~~8~~, 9}

X2={1, 2, 3, 4, 5, 6, 7, 8, 9}

		7			6	1		
	3		1	4			8	
8		1	2			6		9
7				2		9	4	
	1		9		4		5	
	5	9		8				1
3		4			2	8		5
	6			9	5		7	
		5	4			3		

Constraint Programming (CP)

Example



Propagation!

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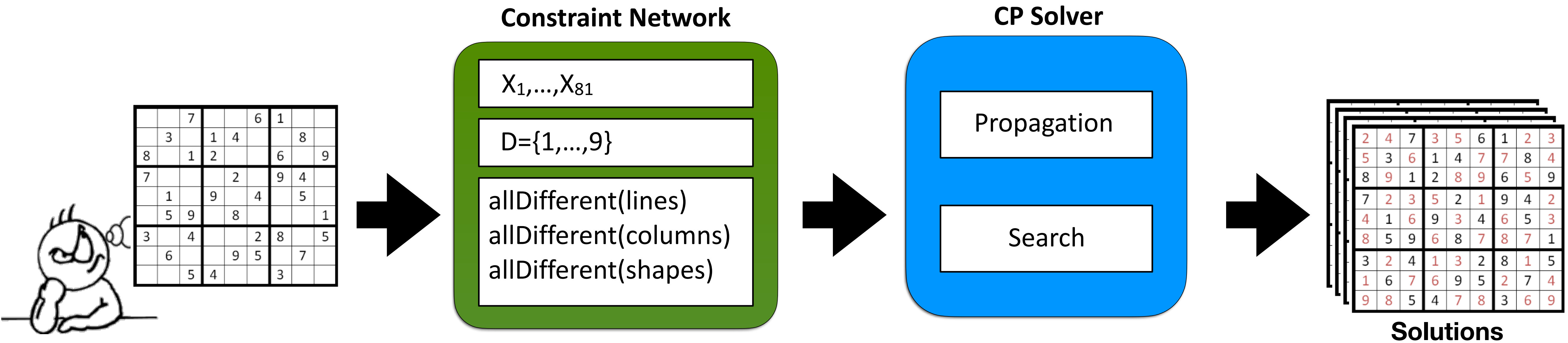
X2={~~1~~, 2, ~~3~~, ~~4~~, 5, 6, ~~7~~, ~~8~~, 9}

		7			6	1		
	3		1	4			8	
8		1	2			6		9
7				2		9	4	
	1		9		4		5	
	5	9		8				1
3		4			2	8		5
	6			9	5		7	
		5	4			3		

Constraint Programming (CP)

Example



search!

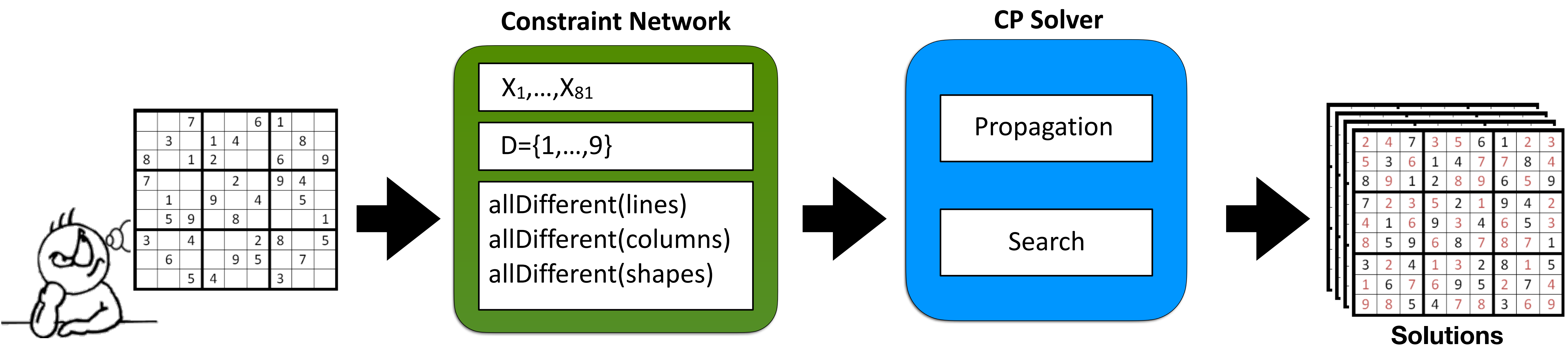
X1={~~1~~, 2, ~~3~~, 4, 5, ~~6~~, ~~7~~, ~~8~~, 9}

X2={2}

		7			6	1		
	3		1	4			8	
8		1	2			6		9
7				2		9	4	
	1		9		4		5	
	5	9		8				1
3		4			2	8		5
	6			9	5		7	
		5	4			3		

Constraint Programming (CP)

Example




```
search <=> propagation
```

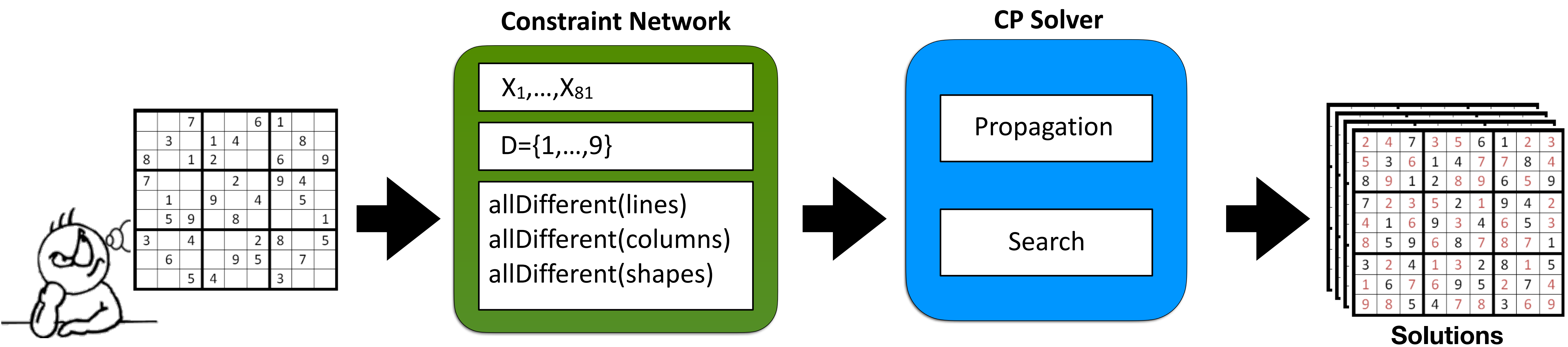
$X1=\{\cancel{1}, \cancel{2}, \cancel{3}, 4, 5, \cancel{6}, \cancel{7}, \cancel{8}, 9\}$

$X2=\{2\}$

		7			6	1		
	3		1	4			8	
8		1	2			6		9
7				2		9	4	
	1		9		4		5	
	5	9		8				1
3		4			2	8		5
	6			9	5		7	
		5	4			3		

Constraint Programming (CP)

Example



`search <=> propagation`

X1={~~1~~, ~~2~~, ~~3~~, 4, 5, ~~6~~, ~~7~~, ~~8~~, 9}

X2={2}

		7			6	1		
	3		1	4			8	
8		1	2			6		9
7				2		9	4	
	1		9		4		5	
	5	9		8				1
3		4			2	8		5
	6			9	5		7	
		5	4			3		

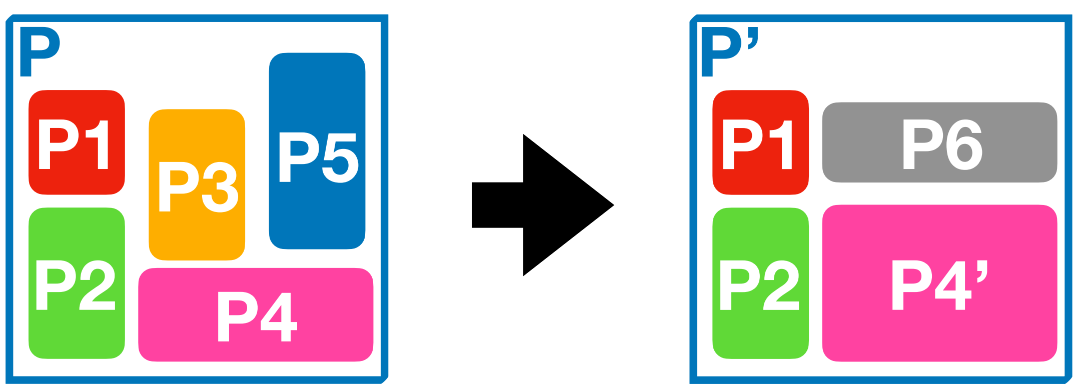
2	4	7	3	5	6	1	2	3
5	3	6	1	4	7	7	8	4
8	9	1	2	8	9	6	5	9
7	2	3	5	2	1	9	4	2
4	1	6	9	3	4	6	5	3
8	5	9	6	8	7	8	7	1
3	2	4	1	3	2	8	1	5
1	6	7	6	9	5	2	7	4
9	8	5	4	7	8	3	6	9

solution!

Constraint Programming

Why CP?

- Combinatorial problems can be solved by Integer Linear Programming (ILP) or by propositional satisfiability (SAT)
- Advantages of CP :
  - Compactness
  - Expressiveness
  - And (often) efficiency



Constraint Programming

Why CP?

- Sudoku 9x9:
  - CP: `sudoku.mod` with n=9

```
Variables X= {X1,1, …Xn,n}

Domaine des variables : {1,…,n}

Contraintes :
allDifferent(Xi,1,..,Xi,n), ∀i (rows)
allDifferent(Xi,1,..,Xi,n), ∀i (columns)
allDifferent(Xi,j), ∀i,j (squares)
```

`sudoku.mod`

Sudoku 36x36

17		5				16		24										2		19				27		13									
	22			18					32		9	4		21	3		12		10			28					8		15	6		23	25		31
2		19				27		13										17		5				16		24									
						4		21				16	32	24		9								6		23				27	8	13		15	
	10			28					8		15	6		23	25		31		22			18					32		9	4		21	3		12
						6		23				27	8	13		15								4		21				16	32	24		9	
32		9							16		24				17		5	8		15							27		13				2		19
			17		5							3		12							2		19							25		31			
8		15							27		13				2		19	32		9							16		24				17		5
7		20				1		11							16		24	26		34				29		35							27		13
			2		19							25		31							17		5							3		12			
26		34				29		35							27		13	7		20				1		11							16		24
	17		22	5	18				36		14								2		10	19	28				30		33						
1		11	16		24	32		9					36			14		29		35	27		13	8		15					30			33	
	2		10	19	28				30		33								17		22	5	18				36		14						
									4		21				1		11										6		23				29		35
29		35	27		13	8		15					30			33		1		11	16		24	32		9					36			14	
									6		23				29		35										4		21				1		11
5		17				24		16										19		2				13		27									
	18			22					9		32	21		4	12		3		28			10					15		8	23		6	31		25
19		2				13		27										5		17				24		16									
						21		4				24	9	16		32								23		6				13	15	27		8	
	28			10					15		8	23		6	31		25		18			22					9		32	21		4	12		3
						23		6				13	15	27		8								21		4				24	9	16		32	
9		32							24		16				5		17	15		8							13		27				19		2
			5		17							12		3							19		2							31		25			
15		8							13		27				19		2	9		32							24		16				5		17
20		7				11		1							24		16	34		26				35		29							13		27
			19		2							31		25							5		17							12		3			
34		26				35		29							13		27	20		7				11		1							24		16
	5		18	17	22				14		36								19		28	2	10				33		30						
11		1	24		16	9		32					14			36		35		29	13		27	15		8					33			30	
	19		28	2	10				33		30								5		18	17	22				14		36						
									21		4				11		1										23		6				35		29
35		29	13		27	15		8					33			30		11		1	24		16	9		32					14			36	
									23		6				35		29										4		21				11		1

Constraint Programming

Why CP?

- Sudoku 36x36:
    - CP: `sudoku.mod` with n=36

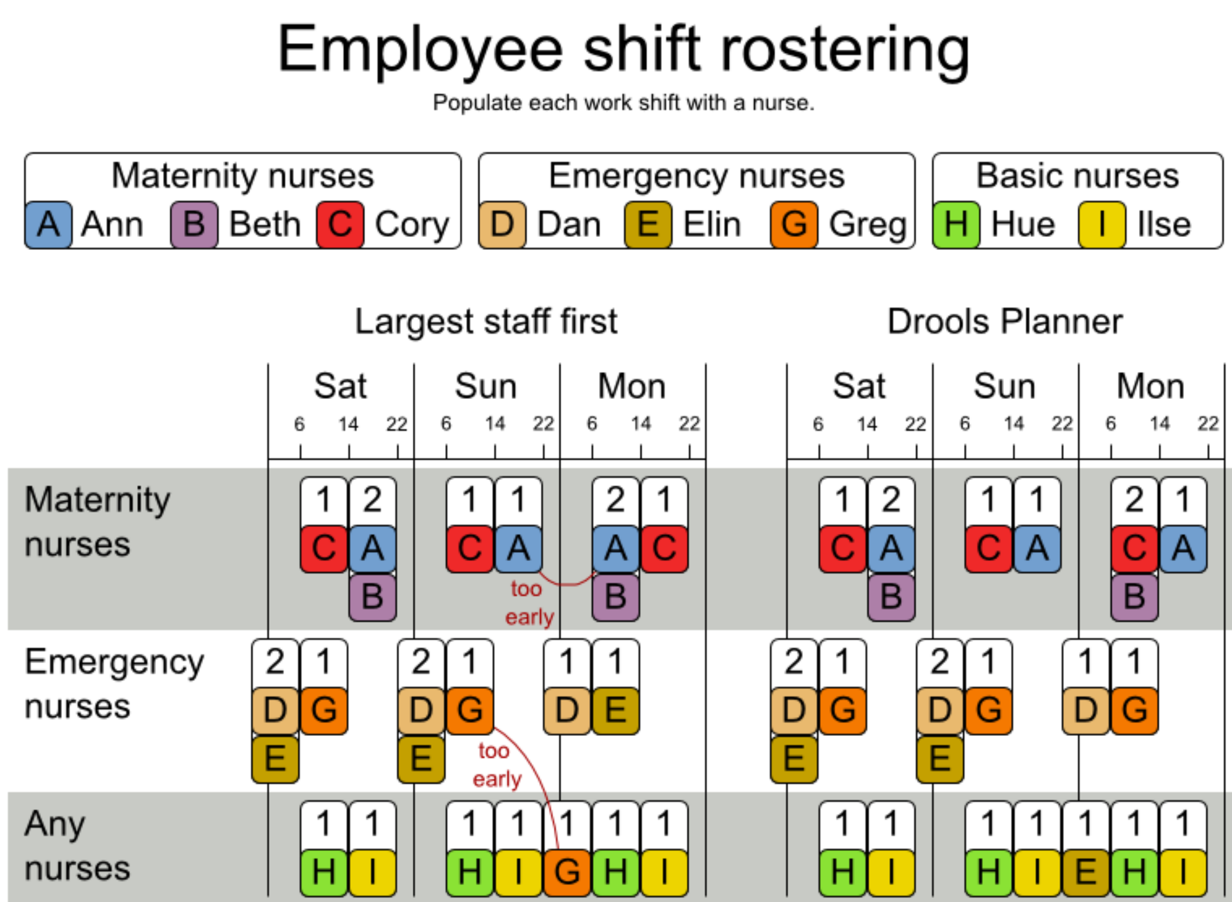
```
Variables X= {X1,1, …Xn,n}

Domaine des variables : {1,…,n}

Contraintes :
allDifferent(Xi,1,..,Xi,n), ∀i (rows)
allDifferent(Xi,1,..,Xi,n), ∀i (columns)
allDifferent(Xi,j), ∀i,j (squares)
```

sudoku.mod

Constraint Programming

Why CP?

- Nurse Rostering Problem
  - Best Linear Program: more than 10 000 lines



Constraint Programming

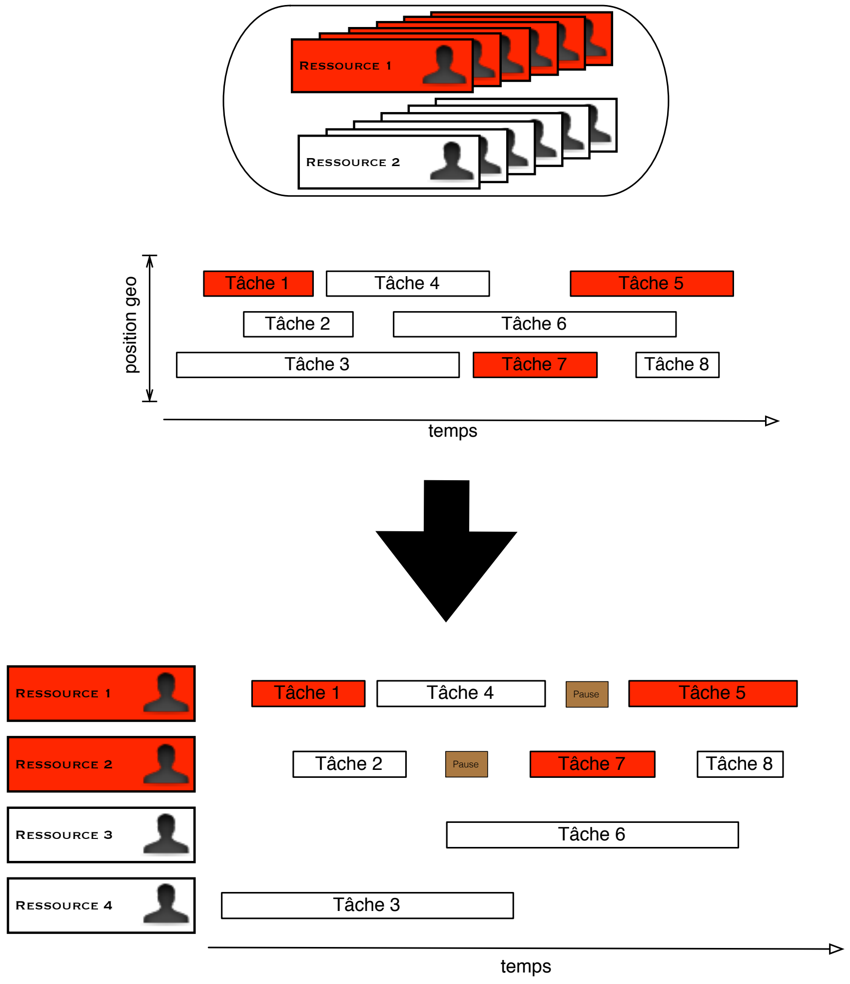
Solvers and CP plateforms

IBM ILOG CP Optimizer (Java, C++, Python, .NET)	IBM
Google OR-Tools (C++, Java, C#, Python)	Google OR-Tools
Artelys Kalis (Java, C++, Python)	ARTELYS KALIS™ Constraint Programming Library
SICStus Prolog (CLPFD bib in prolog)	SICStus 4
Gecode (C++)	G
Choco (Java)	CHOCO
Minizinc (high-level, solver-independent)	Mini Zn

Constraint Programming

SNCF train driver planning using CP

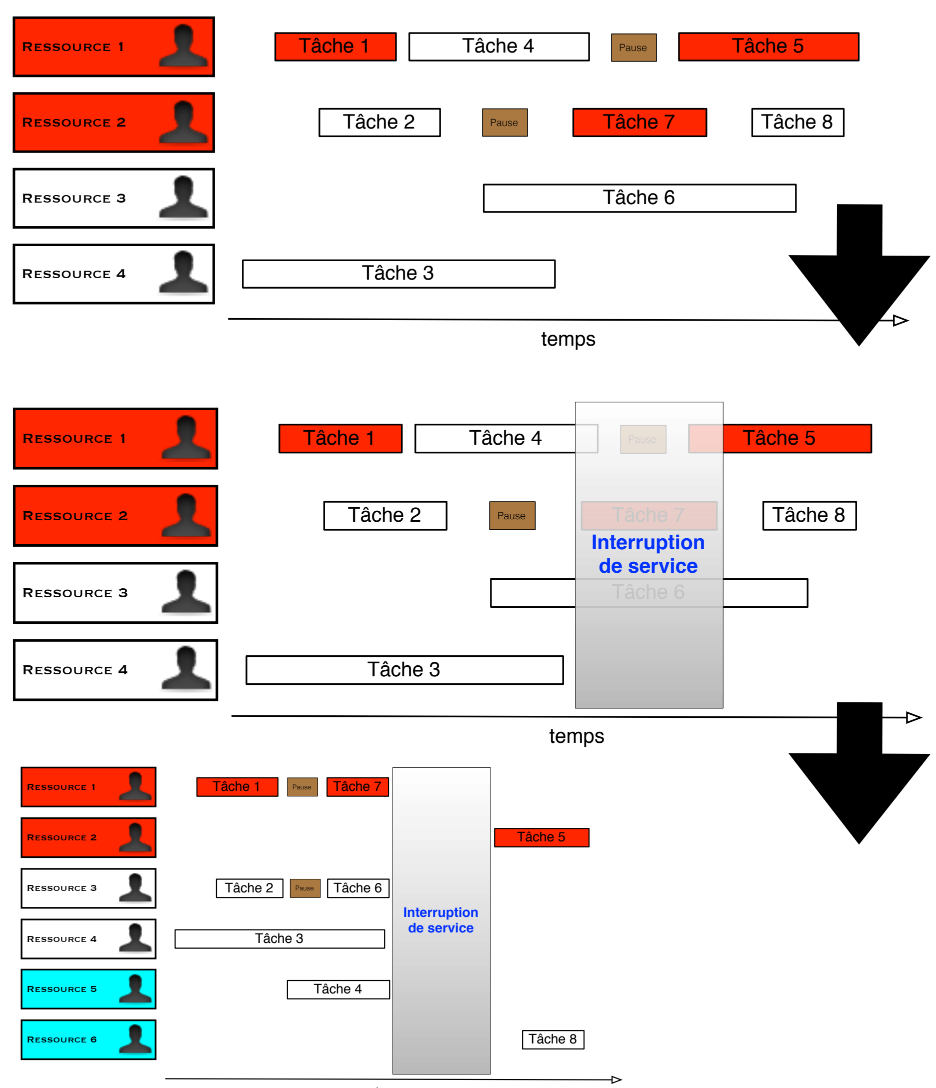
- Legal rules constraints:
  - daily working time
  - daily rest periods
  - …
- Preferences:
  - Type of lines
  - Day of rest
  - Place of rest
  - …
- Solution:
  - Best in terms of ressources
  - Robust one
  - Cheapest one
  - …



Constraint Programming

SNCF train driver planning using CP

- Maintaining an existing planning



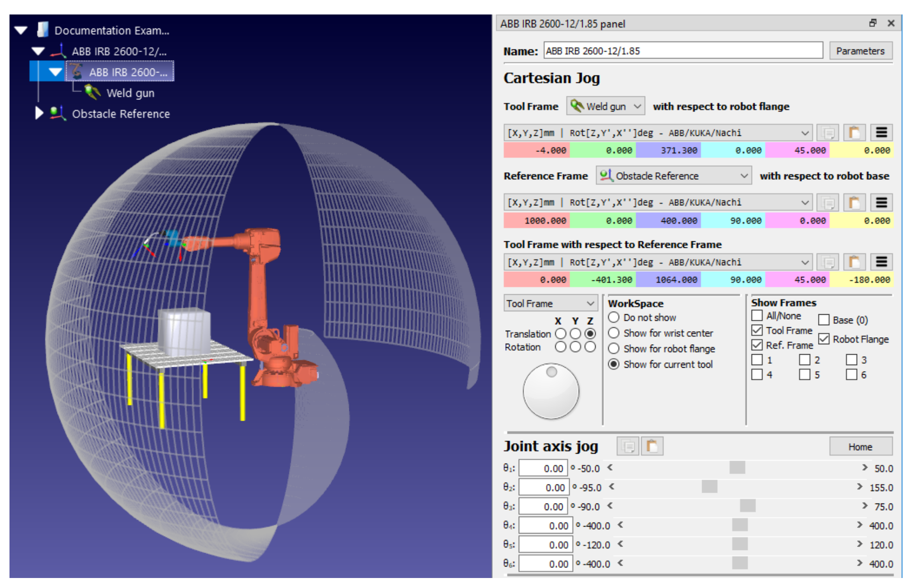
Constraint Programming

ABB Robotics Partner Projects

- SWMOD: Test Case Execution Scheduling with CP

"SWMOD deployed at ABB Robotics and used every day to schedule tests throughout several ABB centers in the world (Norway, Sweden, India, China)"

- Robtest: Optimal Stress Test Trajectories for Robots with CP



https://github.com/Makouno44/Robtest

Constraint Programming

Aircraft Industry - Dassault Aviation

Aircraft Industry - Dassault Aviation

Assembly of Mirage aircraft