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Variante: 2

Q7, ans:

$$9x^2 - 4y^2 + 18x + 16y - 43 = 0$$

$$(9x^2 + 18x) - 4(y^2 + 4y) = 43$$

$$9(x^2 + 2x) - 4(y^2 + 4y) = 43$$

$$9(x^2 + 2x + 1 - 1) - 4(y^2 + 4y + 4 - 4) = 43$$

$$9(x+1)^2 - 4(y+2)^2 = 46$$

$$\frac{9(x+1)^2}{46} - \frac{4(y+2)^2}{46} = 1$$

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$$\frac{9(x+1)^2}{46} - \frac{4(y+2)^2}{46} = 1$$

$$\frac{(x+1)^2}{\frac{46}{9}} - \frac{(y+2)^2}{\frac{46}{4}} = 1$$

$$\text{Center} = (-1, -2)$$

$$a^2 = 4 \quad a = 2 \quad b^2 = 9 \quad b = 3$$

$$e \text{ eccentricity} = \sqrt{1 + \frac{b^2}{a^2}} = \sqrt{1 + \frac{9}{4}} = \sqrt{3.25}$$

$$c^2 = a^2 + b^2 = 4 + 9 = 13 \quad c = \sqrt{13}$$

$$\text{foci} = (-1 \pm c, -2) \quad F_1 = (-1 - \sqrt{13}, -2) \quad F_2 = (-1 + \sqrt{13}, -2)$$