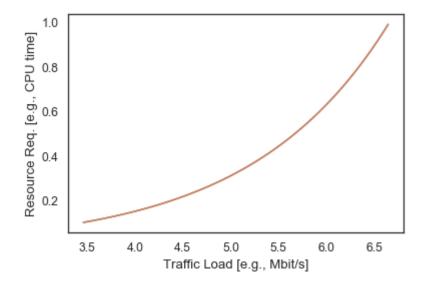
#### Script-1:

```
import math
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import joblib
from sklearn.model_selection import KFold
from sklearn.model selection import train test split
from sklearn.linear_model import LinearRegression
from sklearn.ensemble import GradientBoostingRegressor
from sklearn.preprocessing import MinMaxScaler
from sklearn.metrics import mean_squared_error
%matplotlib inline
sns.set(font_scale=1.1, style="white")
sns cmap = sns.color palette().as hex()
cpu_col = 'Resource Req. [e.g., CPU time]'
thr_col = 'Traffic Load [e.g., Mbit/s]'
def gen_benchmark(cpu, coeff1=1, coeff2=1):
    return coeff1 * math.log2(1 + coeff2 * cpu)
def synthetic_benchmark():
    cpu_list = np.arange(0.1, 1, .01)
    data = []
    for cpu in cpu list:
        data.append([cpu, gen_benchmark(cpu, coeff2=100)])
    return pd.DataFrame(data, columns=[cpu_col, thr_col])
def inverse(thru, coeff2=1):
   return (1/coeff2) * (2**thru - 1)
df = synthetic_benchmark()
# sns.lineplot(df[cpu_col], df[thr_col])
sns.lineplot(df[thr_col], df[cpu_col])
cpu = [inverse(thr, coeff2=100) for thr in df[thr_col]]
sns.lineplot(df[thr col], cpu)
```

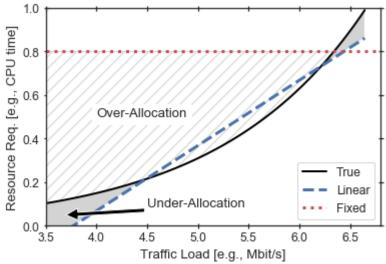


```
X = df[[thr_col]]
y = df[cpu_col]
lin_reg = LinearRegression()
lin_reg.fit(X, y)
lin_col = 'Linear'
df[lin_col] = lin_reg.predict(X)
joblib.dump(lin_reg, 'ml_models/synth_data/linear.joblib')
boost = GradientBoostingRegressor()
boost.fit(X, y)
boost_col = 'Boosting'
df[boost_col] = boost.predict(X)
joblib.dump(boost, 'ml_models/synth_data/boosting.joblib')
# nice fit
mean_squared_error(df[cpu_col], df[boost_col])
boost.predict([[10.0]])
inverse(10, coeff2=100)
# plotting for cpu 0-100
def plot_cpu_0_100():
    fig, ax = plt.subplots()
    fixed = 80
    # lines
    plt.plot(df[thr_col], df[cpu_col], label='True', color='black',
linewidth=2)
    plt.plot(df[thr_col], df[lin_col], color='blue', linewidth=2)
    plt.axhline(y=fixed, label='Fixed', color='green', linewidth=2)
    # fill in between
```

```
ax.fill_between(df[thr_col], df[cpu_col], fixed, where=df[cpu_col]<fixed,</pre>
facecolor='white', edgecolor='grey', hatch='//')
    ax.fill between(df[thr col], df[lin col], df[cpu col],
where=df[lin_col]<df[cpu_col], facecolor='lightgrey', edgecolor='grey',</pre>
hatch='\\')
    ax.text(10.5, 60, 'Over-allocation', bbox={'facecolor': 'white'})
    ax.annotate('Under-allocation', xy=(10.2, 5), xytext=(11, 5),
arrowprops={'facecolor': 'black'}, verticalalignment='center')
    plt.xlabel(thr col)
    plt.ylabel(cpu_col)
    plt.xlim(10)
    plt.legend()
    fig.savefig('plots/example_alloc.pdf', bbox_inches='tight')
# plot cpu 0 100()
# plotting for cpu 0-1
fig, ax = plt.subplots()
fixed = 0.8
# lines
plt.plot(df[thr_col], df[cpu_col], label='True', color='black', linewidth=2)
plt.plot(df[thr_col], df[lin_col], color=sns_cmap[0], linewidth=3,
linestyle="dashed")
# plt.plot(df[thr_col], df[boost_col], color='red', linewidth=2)
plt.axhline(y=fixed, label='Fixed', color=sns_cmap[3], linewidth=3,
linestyle="dotted")
# fill in between
ax.fill_between(df[thr_col], df[cpu_col], fixed, where=df[cpu_col]<fixed,</pre>
facecolor='white', edgecolor='lightgrey', hatch='//')
ax.fill_between(df[thr_col], df[lin_col], df[cpu_col],
where=df[lin_col]<df[cpu_col], facecolor='lightgrey')</pre>
# # text
ax.text(4, 0.5, 'Over-Allocation', bbox={'facecolor': 'white'})
ax.annotate('Under-Allocation', xy=(3.7, 0.05), xytext=(4.5, 0.1),
arrowprops={'facecolor': 'black'}, verticalalignment='center')
plt.xlabel(thr col)
plt.ylabel(cpu_col)
plt.xlim(3.5)
plt.ylim(0, 1)
```

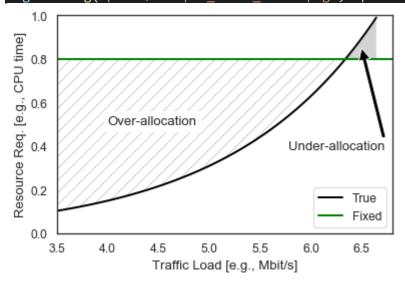
```
plt.tick_params(axis='both', direction='inout', length=5, bottom=True,
left=True, right=True, top=True)
plt.legend()

fig.savefig('plots/example_alloc.pdf', bbox_inches='tight')
# for presentation as png
fig.savefig('plots/example_alloc_lin.png', dpi=150, bbox_inches='tight')
```



```
# 2nd: plot fixed resource alloc at 80%
fig, ax = plt.subplots()
fixed=0.8
# lines
plt.plot(df[thr_col], df[cpu_col], label='True', color='black', linewidth=2)
plt.axhline(y=fixed, label='Fixed', color='green', linewidth=2)
# fill in between
ax.fill_between(df[thr_col], df[cpu_col], fixed, where=df[cpu_col]<fixed,</pre>
facecolor='white', edgecolor='lightgrey', hatch='//')
ax.fill_between(df[thr_col], df[cpu_col], fixed, where=df[cpu_col]>fixed,
facecolor='lightgrey')
ax.text(4, 0.5, 'Over-allocation', bbox={'facecolor': 'white'})
ax.annotate('Under-allocation', xy=(6.5, 0.85), xytext=(6.25, 0.4),
arrowprops={'facecolor': 'black'}, verticalalignment='center',
horizontalalignment='center')
plt.xlabel(thr_col)
plt.ylabel(cpu_col)
plt.xlim(3.5)
plt.ylim(0, 1)
plt.legend()
```

## fig.savefig('plots/example\_alloc\_fixed.png', dpi=150, bbox\_inches='tight')



### Script-2:

```
import warnings
warnings.simplefilter(action='ignore', category=FutureWarning)
import os
import math
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import joblib
from sklearn.base import BaseEstimator
from sklearn.model_selection import KFold, train_test_split, cross_val_score,
GridSearchCV
from sklearn.linear model import LinearRegression, Ridge
from sklearn.ensemble import RandomForestRegressor, GradientBoostingRegressor
from sklearn.svm import SVR
from sklearn.neural network import MLPRegressor
from sklearn.preprocessing import LabelEncoder, StandardScaler,
PolynomialFeatures
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import MinMaxScaler
from sklearn.metrics import mean_squared_error
%matplotlib inline
sns.set(font_scale=3, style="white")
class FixedModel(BaseEstimator):
```

```
def __init__(self, fixed_value):
        self.fixed value = fixed value
    def fit(self, X, y):
        return self
   def predict(self, X):
        n_samples = X.shape[0]
        return [self.fixed_value for _ in range(n_samples)]
# define column names
cpu_col = 'Resource req. [e.g., CPU]'
thr_col = 'Traffic load [e.g., Mbit/s]'
# generate synthetic data
def gen_benchmark(cpu, coeff1=1, coeff2=1):
    return coeff1 * math.log2(1 + coeff2 * cpu)
def synthetic_benchmark():
    cpu_list = np.arange(0.1, 1, .01)
    data = []
    for cpu in cpu_list:
        data.append([cpu, gen_benchmark(cpu, coeff2=100)])
    return pd.DataFrame(data, columns=[cpu_col, thr_col])
# inverse function to calculate cpu given a throughput
def inverse(thru, coeff2=1):
    return (1/coeff2) * (2**thru - 1)
# prepare data
df = synthetic_benchmark()
X = df[[thr_col]]
y = df[cpu_col]
def cross_validation_rmse(model, X, y, k=5, save_model=False):
    scores = cross_val_score(model, X, y, scoring="neg_mean_squared_error",
cv=k)
    rmse = np.sqrt(-scores)
    name = type(model).__name__
    print(f"CV RMSE of {name}: {rmse.mean()} (+/-{rmse.std()})")
    if save_model:
        model.fit(X, y)
        joblib.dump(model, f'ml_models/synth_data/{name}.joblib')
    return rmse
def barplot_rmse(scores, labels, data_name):
    assert len(scores) == len(labels)
   rmse_mean = [s.mean() for s in scores]
    rmse_std = [s.std() for s in scores]
    x = np.arange(len(labels))
   fig, ax = plt.subplots(figsize = (8, 6))
```

```
plt.barh(x, rmse_mean, color='grey', xerr=rmse_std, capsize=5)
    ax.set xlabel('RMSE')
    ax.set_yticks(x)
    ax.set yticklabels(labels)
    fig.savefig(f'plots/{data_name}_rmse.pdf', bbox_inches='tight')
models = [LinearRegression(), Ridge(), SVR(), RandomForestRegressor(),
          GradientBoostingRegressor(), MLPRegressor(max_iter=1500),
          FixedModel(fixed_value=0.8)]
labels = ['Linear', 'Ridge', 'SVR', 'Forest', 'Boosting', 'MLP', 'Fixed']
rmse = [cross_validation_rmse(model, X, y) for model in models]
barplot_rmse(rmse, labels, 'synth_default')
 CV RMSE of LinearRegression: 0.12121162713679334 (+/-0.0834142420571489)
 CV RMSE of Ridge: 0.1157083036553567 (+/-0.07204672163128789)
  CV RMSE of SVR: 0.15772899390054107 (+/-0.08774146778153001)
  CV RMSE of RandomForestRegressor: 0.079016930017029 (+/-0.02892004867091995)
  CV RMSE of GradientBoostingRegressor: 0.07805364007331642 (+/-0.025433426403506574)
  CV RMSE of MLPRegressor: 0.1884970322400931 (+/-0.19317890469508217)
  CV RMSE of FixedModel: 0.30476112171679437 (+/-0.19909124881970067)
        Fixed
         MLP
   Boosting
       Forest
         SVR
       Ridge
       Linear
                                     0.2
                                                       0.4
                  0.0
                                      RMSE
```

```
scaler = MinMaxScaler()
X_scaled = scaler.fit_transform(X)
os.makedirs(f'ml_models/synth_data', exist_ok=True)
joblib.dump(scaler, f'ml_models/synth_data/scaler.joblib')
rmse = [cross_validation_rmse(model, X_scaled, y) for model in models]
```

```
barplot_rmse(rmse, labels, 'synth_scaled')
CV RMSE of LinearRegression: 0.12121162713679334 (+/-0.0834142420571489)
CV RMSE of Ridge: 0.09668457215749979 (+/-0.060822156542014665)
CV RMSE of SVR: 0.10148672105555254 (+/-0.04273273250016648)
CV RMSE of RandomForestRegressor: 0.07883837751219168 (+/-0.026953441506102894)
CV RMSE of GradientBoostingRegressor: 0.07805364007331642 (+/-0.025433426403506574)
CV RMSE of MLPRegressor: 0.1386704339625999 (+/-0.05389148824940066)
CV RMSE of FixedModel: 0.30476112171679437 (+/-0.19909124881970067)
       Fixed
         MLP
 Boosting
      Forest
         SVR
      Ridge
      Linear
                                   0.2
                                                       0.4
               0.0
                                      RMSE
```

```
def tune_hyperparams(model, X, y, params):
    grid_search = GridSearchCV(model, params, cv=5,
scoring="neg_mean_squared_error")
    grid_search.fit(X, y)
    return grid search.best estimator
# hyperparam tuning
params_ridge = {'alpha': [0.1, 1, 10]}
params_svr = {'kernel': ['linear', 'poly', 'rbf'], 'C': [1, 10, 100],
              'epsilon': [0.001, 0.01, 0.1]}
params_forest = {'n_estimators': [10, 100, 200]}
params_boosting = {'learning_rate': [0.01, 0.1, 0.3], 'n_estimators': [10,
100, 200]}
params_mlp = {'hidden_layer_sizes': [(64,), (128,), (256)], 'alpha': [0.001,
0.0001, 0.00001],
              'learning rate init': [0.01, 0.001, 0.0001]}
params = [{}, params_ridge, params_svr, params_forest, params_boosting,
params mlp, {}]
```

```
models_tuned = [tune_hyperparams(models[i], X_scaled, y, params[i]) for i in
range(len(models))]
rmse_tuned = [cross_validation_rmse(model, X_scaled, y, save_model=True) for
model in models tuned]
barplot_rmse(rmse_tuned, labels, 'synth_tuned')
 CV RMSE of LinearRegression: 0.12121162713679334 (+/-0.0834142420571489)
 CV RMSE of Ridge: 0.09668457215749979 (+/-0.060822156542014665)
 CV RMSE of SVR: 0.005448995192915848 (+/-0.005411929454877605)
 CV RMSE of RandomForestRegressor: 0.07856988066678042 (+/-0.026776989848397992)
 CV RMSE of GradientBoostingRegressor: 0.07755613024304038 (+/-0.025150165128635854)
 CV RMSE of MLPRegressor: 0.09011693060882102 (+/-0.04934555264115149)
 CV RMSE of FixedModel: 0.30476112171679437 (+/-0.19909124881970067)
        Fixed
         MLP
  Boosting
      Forest
         SVR |
       Ridge
      Linear
               0.0
                                  0.2
                                                      0.4
                                     RMSE
```

```
# plot
sns.set(font_scale=1, style="white")

def plot_predictions(models, labels, X, y):
    assert len(models) == len(labels)

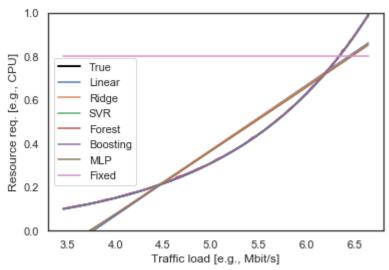
fig, ax = plt.subplots()
    plt.plot(X[thr_col], y, label='True', color='black', linewidth=2)

for i in range(len(models)):
    models[i].fit(X, y)
    plt.plot(X[thr_col], models[i].predict(X), label=labels[i])

plt.xlabel(thr_col)
    plt.ylabel(cpu_col)
```

```
plt.ylim(0, 1)
plt.legend()
```

## plot\_predictions(models\_tuned, labels, X, y)



#### Script-3:

```
import warnings
warnings.simplefilter(action='ignore', category=FutureWarning)
import os
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import joblib
import time
from sklearn.base import BaseEstimator
from sklearn.model_selection import KFold, train_test_split, cross_val_score,
GridSearchCV
from sklearn.linear_model import LinearRegression, Ridge
from sklearn.ensemble import RandomForestRegressor, GradientBoostingRegressor
from sklearn.svm import SVR
from sklearn.neural_network import MLPRegressor
from sklearn.preprocessing import LabelEncoder, StandardScaler,
PolynomialFeatures
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import MinMaxScaler
from sklearn.metrics import mean_squared_error
sns.set(font_scale=1.1, style='white')
class FixedModel(BaseEstimator):
```

```
def init (self, fixed value):
        self.fixed value = fixed value
    def fit(self, X, y):
        return self
    def predict(self, X):
        n samples = X.shape[0]
        return [self.fixed_value for _ in range(n_samples)]
def select_and_rename(df, mapping):
    dff = df[list(mapping.keys())]
    # rename
    for k, v in mapping.items():
        dff.rename(columns={k: v}, inplace=True)
    return dff
def replaceSize(df):
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench_share/ab_dist.csv -s 60 -k -i http://20.0.0.254:8888/", "small")
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench_share/ab_dist.csv -s 60 -k http://20.0.0.254:8888/bunny.mp4", "big")
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench_share/ab_dist.csv -s 60 -k -i -X 20.0.0.254:3128
http://40.0.0.254:80/", "small")
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench_share/ab_dist.csv -s 60 -k -X 20.0.0.254:3128
http://40.0.0.254:80/bunny.mp4", "big")
    return df
# Load data from path
web1 = pd.read_csv("vnf_data/csv_experiments_WEB1.csv")
web2 = pd.read_csv("vnf_data/csv_experiments_WEB2.csv")
web3 = pd.read_csv("vnf_data/csv_experiments_WEB3.csv")
# do processing, renaming and selection
mapping = {
    "param__func__mp.input__cmd_start": "size",
    "metric_mp.input.vdu01.0_ab_transfer_rate_kbyte_per_second": "Max.
throughput [kB/s]",
mapping01 = mapping.copy()
mapping01["param_func_de.upb.lb-nginx.0.1_cpu_bw"] = "CPU"
mapping01["param_func_de.upb.lb-nginx.0.1_mem_max"] = "Memory"
mapping02 = mapping.copy()
mapping02["param func de.upb.lb-haproxy.0.1 cpu bw"] = "CPU"
```

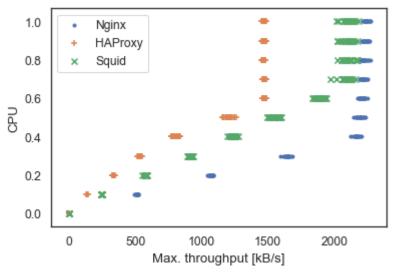
```
mapping02["param__func__de.upb.lb-haproxy.0.1__mem_max"] = "Memory"
mapping03 = mapping.copy()
mapping03["param__func__de.upb.px-squid.0.1 cpu bw"] = "CPU"
mapping03["param func de.upb.px-squid.0.1 mem max"] = "Memory"
web1 = select and rename(web1, mapping01)
web2 = select_and_rename(web2, mapping02)
web3 = select_and_rename(web3, mapping03)
web1 = replaceSize(web1)
web2 = replaceSize(web2)
web3 = replaceSize(web3)
mem = 128
web1_small = web1.loc[(web1["size"] == "small") & (web1["Memory"] == mem)]
web1_small = web1_small[["Max. throughput [kB/s]", "CPU"]]
web1_big = web1.loc[(web1["size"] == "big") & (web1["Memory"] == mem)]
web1 big = web1 big[["Max. throughput [kB/s]", "CPU"]]
web2_small = web2.loc[(web2["size"] == "small") & (web2["Memory"] == mem)]
web2_small = web2_small[["Max. throughput [kB/s]", "CPU"]]
web2_big = web2.loc[(web2["size"] == "big") & (web2["Memory"] == mem)]
web2_big = web2_big[["Max. throughput [kB/s]", "CPU"]]
web3_small = web3.loc[(web3["size"] == "small") & (web3["Memory"] == mem)]
web3_small = web3_small[["Max. throughput [kB/s]", "CPU"]]
web3_big = web3.loc[(web3["size"] == "big") & (web3["Memory"] == mem)]
web3_big = web3_big[["Max. throughput [kB/s]", "CPU"]]
num_measures = 20
measures = [0 for _ in range(num_measures)]
web1_small = web1_small.append(pd.DataFrame({'Max. throughput [kB/s]':
measures, 'CPU': measures}), ignore_index=True)
web1_big = web1_big.append(pd.DataFrame({'Max. throughput [kB/s]': measures,
'CPU': measures}), ignore_index=True)
web2 small = web2 small.append(pd.DataFrame({'Max. throughput [kB/s]':
measures, 'CPU': measures}), ignore_index=True)
web2_big = web2_big.append(pd.DataFrame({'Max. throughput [kB/s]': measures,
'CPU': measures}), ignore_index=True)
web3 small = web3 small.append(pd.DataFrame({'Max. throughput [kB/s]':
measures, 'CPU': measures}), ignore_index=True)
web3_big = web3_big.append(pd.DataFrame({'Max. throughput [kB/s]': measures,
'CPU': measures}), ignore_index=True)
nginx = web1_small
haproxy = web2_small
squid = web3 small
```

```
def plot_vnf_data():
    sns.set(font_scale=1.1, style='white')
    fig, ax = plt.subplots()
    plt.scatter(nginx['Max. throughput [kB/s]'], nginx['CPU'], label='Nginx',
marker='.')
    plt.scatter(haproxy['Max. throughput [kB/s]'], haproxy['CPU'],
label='HAProxy', marker='+')
    plt.scatter(squid['Max. throughput [kB/s]'], squid['CPU'], label='Squid',
marker='x')

# labels
    ax.set_xlabel('Max. throughput [kB/s]')
    ax.set_ylabel('CPU')
    plt.legend()

fig.savefig(f'plots/web_vnf_data.pdf', bbox_inches='tight')

plot_vnf_data()
```



```
def cross_validation_rmse(model, X, y, vnf_name, k=5, save_model=False):
    scores = cross_val_score(model, X, y, scoring="neg_mean_squared_error",

cv=k)
    rmse = np.sqrt(-scores)
    name = type(model).__name__
    print(f"CV RMSE of {name}: {rmse.mean()} (+/-{rmse.std()})")
    if save_model:
        model.fit(X, y)
        joblib.dump(model, f'ml_models/{vnf_name}/{name}.joblib')
    return rmse

def tune_hyperparams(model, X, y, params):
    grid_search = GridSearchCV(model, params, cv=5,
scoring="neg_mean_squared_error")
```

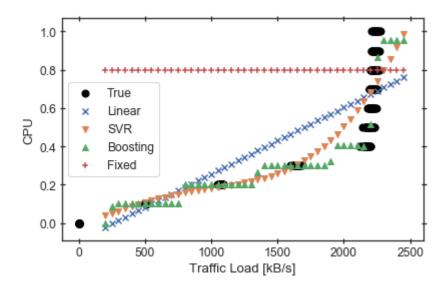
```
grid_search.fit(X, y)
    return grid search.best estimator
def barplot_rmse(scores, labels, data_name):
    sns.set(font scale=1.1, style='white')
    assert len(scores) == len(labels)
    # preparation
    rmse_mean = [s.mean() for s in scores]
    rmse_std = [s.std() for s in scores]
    x = np.arange(len(labels))
   # plot
    fig, ax = plt.subplots() #figsize = (8, 6))
    plt.barh(x, rmse_mean, color='grey', xerr=rmse_std, capsize=5)
    ax.set_xlabel('RMSE')
    ax.set_yticks(x)
    ax.set yticklabels(labels)
    fig.savefig(f'plots/{data_name}_rmse.pdf', bbox_inches='tight')
def train_eval_models(X, y, vnf_name, tune_params=False):
    # prepare models
    labels = ['Linear', 'Ridge', 'SVR', 'Forest', 'Boosting', 'MLP', 'Fixed']
    models = [LinearRegression(), Ridge(), SVR(), RandomForestRegressor(),
              GradientBoostingRegressor(), MLPRegressor(max_iter=1500),
              FixedModel(fixed_value=0.8)]
    # params for tuning
    params_ridge = {'alpha': [0.1, 1, 10]}
    params_svr = {'kernel': ['linear', 'poly', 'rbf'], 'C': [1, 10, 100],
                  'epsilon': [0.001, 0.01, 0.1]}
    params_forest = {'n_estimators': [10, 100, 200]}
    params_boosting = {'learning_rate': [0.01, 0.1, 0.3], 'n_estimators': [10,
100, 200]}
    params_mlp = {'hidden_layer_sizes': [(64,), (128,), (256)], 'alpha':
[0.001, 0.0001, 0.00001],
                  'learning_rate_init': [0.01, 0.001, 0.0001]}
    params = [{}, params_ridge, params_svr, params_forest, params_boosting,
params_mlp, {}]
    if tune_params:
        models = [tune_hyperparams(models[i], X, y, params[i]) for i in
range(len(models))]
    rmse = [cross_validation_rmse(model, X, y, vnf_name, save_model=True) for
model in models]
```

```
# plot
    if tune params:
        barplot_rmse(rmse, labels, f'{vnf_name}_tuned')
        barplot rmse(rmse, labels, f'{vnf name} default')
    return models
def prepare_data(data, vnf_name):
    X = data[['Max. throughput [kB/s]']]
    y = data['CPU']
    X = X.fillna(X.median())
    scaler = MinMaxScaler()
    scaler.fit(X)
    os.makedirs(f'ml models/{vnf name}', exist ok=True)
    joblib.dump(scaler, f'ml_models/{vnf_name}/scaler.joblib')
    return X, y, scaler
def predict_plot_all(models, scaler, X, y, vnf_name):
    sns.set(font_scale=1.1, style='white')
    models = [models[0], models[2], models[3], models[6]]
    labels = ['Linear', 'SVR', 'Boosting', 'Fixed']
    markers = ['x', 'v', '^', '+']
    colors = ['blue', 'orange', 'red', 'green']
    fig, ax = plt.subplots()
   plt.scatter(X, y, label='True', marker='o', color='black', s=50)
   X = scaler.transform(X)
    times = []
    for i, model in enumerate(models):
        name = type(model).__name__
        model.fit(X, y)
        os.makedirs(f'ml_models/{vnf_name}', exist_ok=True)
        X_plot = pd.DataFrame({'Max. Throughput [kB/s]': np.arange(200, 2500,
50)})
        X_plot_scaled = scaler.transform(X_plot)
        start = time.time()
        y_pred = model.predict(X_plot_scaled)
        times.append(start - time.time())
        plt.scatter(X_plot, y_pred, label=labels[i], marker=markers[i])
    plt.xlabel('Traffic Load [kB/s]')
    plt.ylabel('CPU')
    plt.tick_params(axis='both', direction='inout', length=5, bottom=True,
left=True, right=True, top=True)
   plt.legend()
```

```
# save, avoid cutting off labels
    plt.tight layout()
    fig.savefig(f'plots/{vnf name} model comparison.pdf')
    return times
def barplot compare rmse(scores default, scores tuned, labels, data name):
    sns.set(font_scale=1.1, style='white')
    assert len(scores default) == len(scores tuned) == len(labels)
    x = np.arange(len(labels))
   width = 0.35
   # plot
   fig, ax = plt.subplots() # prev: figsize = (8, 5))
    # default
    rmse_mean = [s.mean() for s in scores_default]
    rmse_std = [s.std() for s in scores_default]
    ci95 = [1.96 * std / np.sqrt(len(rmse_std)) for std in rmse_std]
    ax.bar(x - width/2, rmse_mean, width, yerr=ci95, capsize=5, color='gray',
label='Default')
    # same for tuned version
    rmse_mean = [s.mean() for s in scores tuned]
    rmse_std = [s.std() for s in scores_tuned]
    ci95 = [1.96 * std / np.sqrt(len(rmse_std)) for std in rmse_std]
    ax.bar(x + width/2, rmse_mean, width, yerr=ci95, capsize=5,
color='lightgray', label='Tuned')
   # labels
    ax.set_ylabel('RMSE')
    ax.set_xticks(x)
    ax.set_xticklabels(labels)
    ax.tick_params(axis='both', direction='inout', length=5, bottom=False,
left=True, right=True, top=False)
    ax.legend()
    fig.savefig(f'plots/{data_name}_rmse.pdf', bbox_inches='tight')
def train tune eval_models(X, y, vnf_name):
    # prepare models and rmse without tuning
    labels = ['Linear', 'Ridge', 'SVR', 'Forest', 'Boosting', 'MLP', 'Fixed']
    models_default = [LinearRegression(), Ridge(), SVR(),
RandomForestRegressor(),
              GradientBoostingRegressor(), MLPRegressor(max_iter=1500),
              FixedModel(fixed_value=0.8)]
    rmse_default = [cross_validation_rmse(model, X, y, vnf_name,
save model=False) for model in models default]
```

```
# hyperparam tuning
    params_ridge = {'alpha': [0.1, 1, 10]}
    params_svr = {'kernel': ['poly', 'rbf'], 'C': [1, 10, 100],
                  'epsilon': [0.001, 0.01, 0.1]}
    params_forest = {'n_estimators': [10, 100, 200]}
    params_boosting = {'learning_rate': [0.01, 0.1, 0.3], 'n_estimators': [10,
100, 200]}
    params_mlp = {'hidden_layer_sizes': [(64,), (128,), (256)], 'alpha':
[0.001, 0.0001, 0.00001],
                  'learning_rate_init': [0.01, 0.001, 0.0001]}
    params = [{}, params_ridge, params_svr, params_forest, params_boosting,
params_mlp, {}]
    models_tuned = [tune_hyperparams(models_default[i], X, y, params[i]) for i
in range(len(labels))]
    rmse_tuned = [cross_validation_rmse(model, X, y, vnf_name,
save_model=True) for model in models_tuned]
    barplot_compare_rmse(rmse_default, rmse_tuned, labels,
f'{vnf_name}_default-tuned')
    return models_tuned
vnf_name = 'nginx'
X, y, scaler = prepare_data(nginx, vnf_name)
X_scaled = scaler.transform(X)
models = train_tune_eval_models(X_scaled, y, vnf_name)
predict plot all(models, scaler, X, y, vnf name)
```

```
CV RMSE of LinearRegression: 0.19651294327683955 (+/-0.0770302015503735)
CV RMSE of Ridge: 0.19747963738692514 (+/-0.07374557483743582)
CV RMSE of SVR: 0.23843849102511663 (+/-0.03133600651863603)
CV RMSE of RandomForestRegressor: 0.1544186506720129 (+/-0.04566173409977426)
CV RMSE of GradientBoostingRegressor: 0.15532875692425963 (+/-0.04397880798814986)
CV RMSE of MLPRegressor: 0.20690428180788495 (+/-0.07598079094190109)
CV RMSE of FixedModel: 0.38153965300099446 (+/-0.21077830340877302)
CV RMSE of LinearRegression: 0.19651294327683955 (+/-0.0770302015503735)
CV RMSE of Ridge: 0.19747963738692514 (+/-0.07374557483743582)
CV RMSE of SVR: 0.1829420132476261 (+/-0.08049356087609329)
CV RMSE of RandomForestRegressor: 0.1523560777807378 (+/-0.04203026966747045)
CV RMSE of GradientBoostingRegressor: 0.14334186263227305 (+/-0.0379499323771591)
CV RMSE of MLPRegressor: 0.17355377473628966 (+/-0.06294255153363573)
CV RMSE of FixedModel: 0.38153965300099446 (+/-0.21077830340877302)
[0.0, 0.0, -0.015516519546508789, 0.0]
            Default
            Tuned
   0.4
RMSE
0.3
   0.2
   0.1
   0.0
        Linear
              Ridge
                    SVR
                          Forest Boosting MLP
                                            Fixed
```



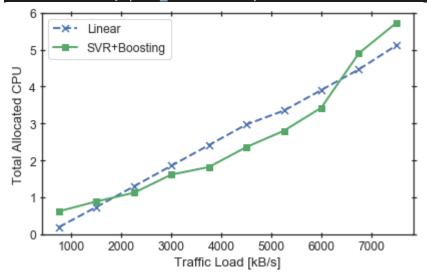
## Script-4:

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```

```
import matplotlib as mpl
import seaborn as sns
import sklearn
import yaml
import sys
import glob
import os
%matplotlib inline
sns.set(font_scale=1.1, style='white')
sns_cmap = sns.color_palette().as_hex()
def sum_cpu(node_res):
    cpu = sum([v['cpu'] for v in node_res])
    return cpu
def read placement(placement, df data, flow dr=250):
    df_data['num_flows'].append(placement['input']['num_flows'])
    df_data['num_sources'].append(placement['input']['num_sources'])
    df_data['source_dr'].append(placement['input']['num_flows'] * flow_dr)
    df_data['num_instances'].append(placement['metrics']['num_instances'])
    df_data['max_e2e_delay'].append(placement['metrics']['max_endToEnd_delay']
    df_data['total_delay'].append(placement['metrics']['total_delay'])
    df_data['runtime'].append(placement['metrics']['runtime'])
    df_data['total_cpu'].append(sum_cpu(placement['placement']['alloc_node_res
']))
   return df_data
def read_results(results):
    data = {'num_sources' : [], 'num_flows': [], 'source_dr': [],
 num_instances': [],
            'max_e2e_delay': [], 'total_delay': [], 'runtime': [],
 total_cpu': []}
    # iterate through result files
    for res in glob.glob(results):
        # open and save metrics of interest
        with open(res, 'r') as f:
            placement = yaml.load(f, Loader=yaml.SafeLoader)
            data = read_placement(placement, data)
    return pd.DataFrame(data).sort_values(by=['num_flows'])
# read results
dataset = 'web_data'
sources = 'three_source_dr250'
results = f'placement_data/{dataset}/{sources}/'
df_true = read_results(results + 'true/*.yaml')
df fixed = read results(results + 'fixed/*.yaml')
```

```
df_linear = read_results(results + 'linear/*.yaml')
df boost = read results(results + 'boosting/*.yaml')
df svr = read results(results + 'svr/*.yaml')
df ml = read results(results + 'ml/*.yaml')
def plot(x col, x label, y col, y label, save plot=True, plot fixed=True):
    sns.set(font_scale=1.1, style='white')
    fig, ax = plt.subplots()
    if plot fixed:
        plt.plot(df_fixed[x_col], df_fixed[y_col], label='Fixed',
color=sns_cmap[3], marker='+',
                  linewidth=3, linestyle="dotted", markersize=10,
markeredgewidth=1.5)
    plt.plot(df_linear[x_col], df_linear[y_col], label='Linear',
color=sns cmap[0], marker='x',
             linewidth=2, linestyle="dashed", markersize=7,
markeredgewidth=1.5)
    plt.plot(df_ml[x_col], df_ml[y_col], label='SVR+Boosting',
color=sns_cmap[2], marker='s',
             linewidth=2)
    plt.xlabel(x_label)
    plt.ylabel(y_label)
    plt.ylim(bottom=0)
    plt.tick_params(axis='both', direction='inout', length=5, bottom=True,
left=True, right=True, top=True)
    plt.legend()
    plt.tight_layout()
    if save_plot:
        fig.savefig(f'plots/{dataset}_{y_col}.pdf')
    return fig, ax
                                          'total_cpu', 'Total Allocated CPU')
plot('source_dr', 'Traffic Load [kB/s]',
   16
   14
Total Allocated CPU
   12
                                          Fixed
   10
                                          Linear
    8
                                          SVR+Boosting
    6
    4
    2
        1000
              2000
                     3000
                           4000
                                  5000
                                        6000
                                               7000
                       Traffic Load [kB/s]
```

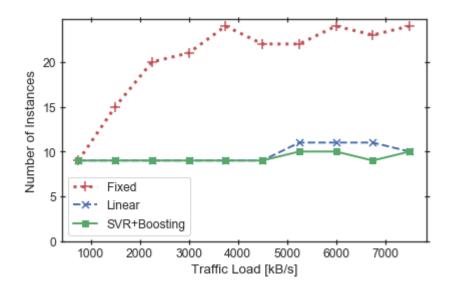
# fig, ax = plot('source\_dr', 'Traffic Load [kB/s]', 'total\_cpu', 'Total Allocated CPU', plot fixed=False)

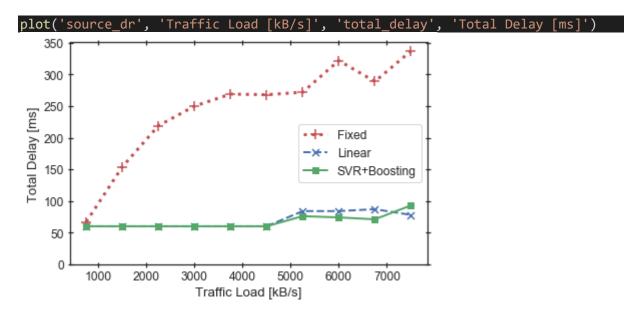


```
# plot both
def plot_both(x_col, x_label, y_col, y_label):
    sns.set(font_scale=1.1, style='white')
    fig, ax = plt.subplots(nrows=1, ncols=2, figsize=(8, 4))
    ax[0].plot(df_fixed[x_col], df_fixed[y_col], label='Fixed',
color=sns_cmap[3], marker='+',
               linewidth=3, linestyle="dotted", markersize=10,
markeredgewidth=1.5)
    ax[0].plot(df_linear[x_col], df_linear[y_col], label='Linear',
color=sns_cmap[0], marker='x',
               linewidth=2, linestyle="dashed", markersize=7,
markeredgewidth=1.5)
    ax[0].plot(df_ml[x_col], df_ml[y_col], label='SVR+Boosting',
color=sns_cmap[2], marker='s',
               linewidth=2)
    ax[0].set(xlabel=x_label, ylabel=y_label)
    ax[0].set_ylim(bottom=0)
    ax[0].tick_params(axis='both', direction='inout', length=5, bottom=True,
left=True, right=True, top=True)
      ax[0].legend()
    ax[1].plot([], [], label='Fixed', color=sns_cmap[3], marker='+',
linewidth=3,
               linestyle="dotted", markersize=10, markeredgewidth=1.5)
    ax[1].plot(df_linear[x_col], df_linear[y_col], label='Linear',
color=sns_cmap[0], marker='x',
               linewidth=2, linestyle="dashed", markersize=7,
markeredgewidth=1.5)
```

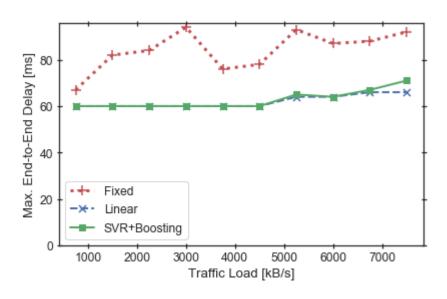
```
ax[1].plot(df_ml[x_col], df_ml[y_col], label='SVR+Boosting',
color=sns_cmap[2], marker='s',
                linewidth=2)
    ax[1].set(xlabel=x_label)
    ax[1].set ylim(bottom=0)
    ax[1].tick_params(axis='both', direction='inout', length=5, bottom=True,
left=True, right=True, top=True)
    ax[1].legend()
    # avoid cutting off figure labels
    plt.tight_layout()
    fig.savefig(f'plots/{dataset}_{y_col}_both.pdf')
plot_both('source_dr', 'Traffic Load [kB/s]', 'total_cpu', 'Total Allocated
                                                   Fixed
   16
                                                   Linear
   14
                                                   SVR+Boosting
Total Allocated CPU
   12
                                           4
   10
                                           3
    8
    6
                                          2
    4
    2
                    4000
           2000
                             6000
                                                 2000
                                                           4000
                                                                    6000
               Traffic Load [kB/s]
                                                     Traffic Load [kB/s]
```

plot('source\_dr', 'Traffic Load [kB/s]', 'num\_instances', 'Number of
Instances')





plot('source\_dr', 'Traffic Load [kB/s]', 'max\_e2e\_delay', 'Max. End-to-End
Delay [ms]')



Script-5:

```
import warnings
warnings.simplefilter(action='ignore', category=FutureWarning)

import os
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import joblib
```

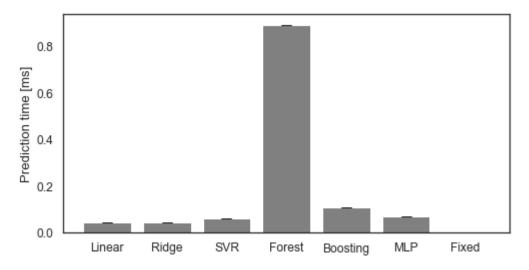
```
import random
import glob
import yaml
import timeit
import math
from sklearn.base import BaseEstimator
from sklearn.model_selection import KFold, train_test_split, cross_val_score,
GridSearchCV
from sklearn.linear_model import LinearRegression, Ridge
from sklearn.ensemble import RandomForestRegressor, GradientBoostingRegressor
from sklearn.svm import SVR
from sklearn.neural network import MLPRegressor
from sklearn.preprocessing import LabelEncoder, StandardScaler,
PolynomialFeatures
from sklearn.model selection import train test split
from sklearn.preprocessing import MinMaxScaler
from sklearn.metrics import mean_squared_error
sns.set(font scale=1.1, style='white')
```

```
class FixedModel(BaseEstimator):
    def __init__(self, fixed_value):
        self.fixed_value = fixed_value
    def fit(self, X, y):
        return self
    def predict(self, X):
        n_samples = X.shape[0]
        return [self.fixed_value for _ in range(n_samples)]
# function for processing and simplifying the dataset
def select_and_rename(df, mapping):
    # select subset of columns
    dff = df[list(mapping.keys())]
    # rename
    for k, v in mapping.items():
        dff.rename(columns={k: v}, inplace=True)
    return dff
def replaceSize(df):
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench_share/ab_dist.csv -s 60 -k -i http://20.0.0.254:8888/", "small")
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench share/ab dist.csv -s 60 -k http://20.0.0.254:8888/bunny.mp4", "big"
```

```
df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench share/ab dist.csv -s 60 -k -i -X 20.0.0.254:3128
http://40.0.0.254:80/", "small")
    df["size"] = df["size"].str.replace("ab -c 1 -t 60 -n 99999999 -e
/tngbench share/ab dist.csv -s 60 -k -X 20.0.0.254:3128
http://40.0.0.254:80/bunny.mp4", "big")
    return df
web1 = pd.read csv("vnf data/csv experiments WEB1.csv")
web3 = pd.read_csv("vnf_data/csv_experiments_WEB3.csv")
mapping = {
    "param func mp.input cmd start": "size",
    "metric mp.input.vdu01.0 ab transfer rate kbyte per second": "Max.
throughput [kB/s]",
mapping01 = mapping.copy()
mapping01["param__func__de.upb.lb-nginx.0.1 cpu_bw"] = "CPU"
mapping01["param__func__de.upb.lb-nginx.0.1__mem_max"] = "Memory"
mapping03 = mapping.copy()
mapping03["param__func__de.upb.px-squid.0.1__cpu_bw"] = "CPU"
mapping03["param func de.upb.px-squid.0.1 mem max"] = "Memory"
web1 = select_and_rename(web1, mapping01)
web3 = select_and_rename(web3, mapping03)
web1 = replaceSize(web1)
web3 = replaceSize(web3)
# select sub-datasets with small and large flows
# and with specific memory
mem = 128
web1 small = web1.loc[(web1["size"] == "small") & (web1["Memory"] == mem)]
web1_small = web1_small[["Max. throughput [kB/s]", "CPU"]]
web3_small = web3.loc[(web3["size"] == "small") & (web3["Memory"] == mem)]
web3_small = web3_small[["Max. throughput [kB/s]", "CPU"]]
# add 20 "measurements" at 0 CPU and throuhgput
num_measures = 20
measures = [0 for in range(num measures)]
web1_small = web1_small.append(pd.DataFrame({'Max. throughput [kB/s]':
measures, 'CPU': measures}), ignore_index=True)
web3_small = web3_small.append(pd.DataFrame({'Max. throughput [kB/s]':
measures, 'CPU': measures}), ignore_index=True)
def prepare_data(data):
   X = data[['Max. throughput [kB/s]']]
```

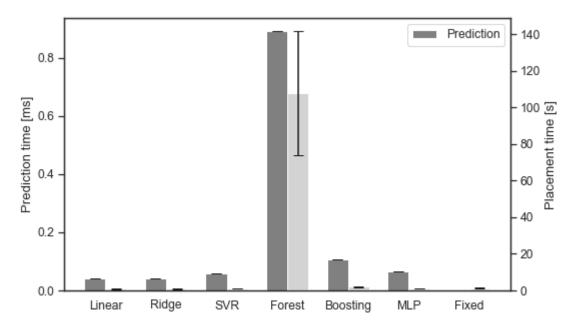
```
y = data['CPU']
   X = X.fillna(X.median())
    scaler = MinMaxScaler()
    scaler.fit transform(X)
    return X, y
def barplot(times, labels, ylabel='Time [s]', filename=None):
    assert len(times) == len(labels)
    times_mean = [np.array(t).mean() for t in times]
    print(times mean)
    times_std = [np.array(t).std() for t in times]
    x = np.arange(len(labels))
    sns.set(font scale=1.1, style='white')
    fig, ax = plt.subplots(figsize=(8, 4))
    plt.bar(x, times_mean, yerr=times_std, capsize=5, color='gray')
    ax.set xticks(x)
    ax.set_xticklabels(labels)
    ax.set_ylabel(ylabel)
    if filename is not None:
        fig.savefig(f'plots/{filename}.pdf', bbox_inches='tight')
# prepare data
X_nginx, y_nginx = prepare_data(web1_small)
X_squid, y_squid = prepare_data(web3_small)
X = X_nginx
y = y_nginx
vnf_name = 'nginx'
# generate synthetic data
def gen_benchmark(cpu, coeff1=1, coeff2=1):
    return coeff1 * math.log2(1 + coeff2 * cpu)
def synthetic_benchmark(n):
    cpu_list = [random.random() for _ in range(n)]
    thr_list = [gen_benchmark(cpu, coeff2=100) for cpu in cpu_list]
   X = pd.DataFrame(data={'Throughput': thr_list})
   y = np.array(cpu_list)
    return X, y
def training_times(models, X, y, scaler):
    # measure training times
    times = []
    for model in models:
        print(type(model).__name__)
        X scaled = scaler.transform(X)
```

```
t = %timeit -o model.fit(X, y)
         times.append(t)
    return times
labels = ['Linear', 'Ridge', 'SVR', 'Forest', 'Boosting', 'MLP', 'Fixed']
models = [LinearRegression(), Ridge(), SVR(verbose=True),
RandomForestRegressor(n estimators=10),
           GradientBoostingRegressor(), MLPRegressor(max_iter=1500),
           FixedModel(fixed_value=0.8)]
model_names = [type(model).__name__ for model in models]
models = [joblib.load(f'ml_models/{vnf_name}/{name}.joblib') for name in
model_names]
scaler = joblib.load(f'ml models/{vnf name}/scaler.joblib')
models = [joblib.load(f'ml_models/{vnf_name}/{name}.joblib') for name in
model names]
scaler = joblib.load(f'ml models/{vnf name}/scaler.joblib')
X_rand = pd.DataFrame(data={'Rand max. throughput': [random.randrange(0, 3000)
for _ in range(1)]})
times = []
for model in models:
    print(type(model).__name__)
    X scaled = scaler.transform(X rand)
    t = %timeit -o model.predict(X_scaled)
    times.append(t)
LinearRegression
The slowest run took 4.49 times longer than the fastest. This could mean that an intermediate result is being cached.
83.2 \mus \pm 63.5 \mus per loop (mean \pm std. dev. of 7 runs, 10000 loops each)
64.5 \mus \pm 17.2 \mus per loop (mean \pm std. dev. of 7 runs, 10000 loops each)
86.2 \mu s \pm 19 \mu s per loop (mean \pm std. dev. of 7 runs, 10000 loops each)
{\tt RandomForestRegressor}
7.29 ms ± 170 μs per loop (mean ± std. dev. of 7 runs, 100 loops each)
GradientBoostingRegressor
123 μs ± 1.98 μs per loop (mean ± std. dev. of 7 runs, 10000 loops each)
MLPRegressor
115 \mus \pm 5.04 \mus per loop (mean \pm std. dev. of 7 runs, 10000 loops each)
FixedModel
1.13 \mu s \pm 135 ns per loop (mean \pm std. dev. of 7 runs, 1000000 loops each)
all_times_ms = [[i * 1000.0 / t.loops for i in t.all_runs] for t in times]
all_times_ms = [0.041868121428571416, 0.04201067571428731,
0.059522719999998634, 0.8912386999999821, 0.10723779999999741,
                  0.06644656000000201, 0.0009462411285714519]
labels = ['Linear', 'Ridge', 'SVR', 'Forest', 'Boosting', 'MLP', 'Fixed']
barplot(all times ms, labels, ylabel="Prediction time [ms]",
filename='prediction times')
```



```
def sum_cpu(node_res):
    cpu = sum([v['cpu'] for v in node_res])
    return cpu
def read_placement(placement, df_data, flow_dr=250):
    df_data['num_flows'].append(placement['input']['num_flows'])
    df_data['num_sources'].append(placement['input']['num_sources'])
    df_data['source_dr'].append(placement['input']['num_flows'] * flow_dr)
    df_data['num_instances'].append(placement['metrics']['num_instances'])
    df_data['max_e2e_delay'].append(placement['metrics']['max_endToEnd_delay']
    df_data['total_delay'].append(placement['metrics']['total_delay'])
    df_data['runtime'].append(placement['metrics']['runtime'])
    df_data['total_cpu'].append(sum_cpu(placement['placement']['alloc_node_res
']))
    return df_data
def read_results(results):
    data = {'num_sources' : [], 'num_flows': [], 'source_dr': [],
num_instances': [],
            'max_e2e_delay': [], 'total_delay': [], 'runtime': [],
'total_cpu': []}
    # iterate through result files
    for res in glob.glob(results):
        # open and save metrics of interest
        with open(res, 'r') as f:
            placement = yaml.load(f, Loader=yaml.SafeLoader)
            data = read_placement(placement, data)
    return pd.DataFrame(data).sort_values(by=['num_flows'])
dataset = 'web_data'
sources = 'runtime'
```

```
results = f'placement_data/{dataset}/{sources}/'
df results = []
df results.append(read_results(results + 'linear/*.yaml'))
df results.append(read results(results + 'ridge/*.yaml'))
df results.append(read results(results + 'svr/*.yaml'))
df results.append(read results(results + 'forest/*.yaml'))
df_results.append(read_results(results + 'boosting/*.yaml'))
df results.append(read results(results + 'mlp/*.yaml'))
df results.append(read results(results + 'fixed/*.yaml'))
# df_results.append(read_results(results + 'ml/*.yaml'))
labels = ['Linear', 'Ridge', 'SVR', 'Forest', 'Boosting', 'MLP', 'Fixed']
placement_times = [df['runtime'] for df in df_results]
barplot(placement times, labels)
def comparison_barplot_one(pred_times, place_times, labels, filename=None):
    sns.set(font_scale=1.1, style='white')
    assert len(pred_times) == len(place_times) == len(labels)
    # prepare data
    pred_times_mean = [np.array(t).mean() for t in pred_times]
    pred_times_std = [np.array(t).std() for t in pred_times]
    place_times_mean = [np.array(t).mean() for t in place_times]
    place_times_std = [np.array(t).std() for t in place_times]
    x = np.arange(len(labels))
   width = 0.35
    # plot: separate axes
    fig, ax1 = plt.subplots(figsize = (8, 5))
    ax1.bar(x - width/2, pred_times_mean, width, yerr=pred_times_std,
capsize=5, color='gray', label='Prediction')
    ax1.set_ylabel("Prediction time [ms]")
    ax1.set_xticks(x)
    ax1.set_xticklabels(labels)
    ax2 = ax1.twinx()
    ax2.bar(x + width/2, place_times_mean, width, yerr=place_times_std,
capsize=5, color='lightgray', label='Placement')
    ax2.set_ylabel("Placement time [s]")
    # labels
    ax1.legend()
    if filename is not None:
        fig.savefig(f'plots/{filename}.pdf', bbox inches='tight')
```



```
from matplotlib.ticker import ScalarFormatter
def comparison_barplot_two(pred_times, place_times, labels):
    sns.set(font_scale=1.1, style='white')
    assert len(pred_times) == len(place_times) == len(labels)
    fig, (ax1, ax2) = plt.subplots(nrows=1, ncols=2, sharey='all', figsize=(8,
4))
    # prepare data
    pred_times_mean = [np.array(t).mean() for t in pred_times]
    pred_times_std = [np.array(t).std() for t in pred_times]
    # 95% CI (not bootstrapped like seaborn does):
https://en.wikipedia.org/wiki/Confidence_interval#Basic_steps
    pred_times_ci95 = [1.96 * std / np.sqrt(len(pred_times_std)) for std in
pred_times_std]
    place_times_mean = [np.array(t).mean() for t in place_times]
    place_times_std = [np.array(t).std() for t in place_times]
    place_times_ci95 = [1.96 * std / np.sqrt(len(place_times_std)) for std in
place_times_std]
    x = np.arange(len(labels))
    # plot: separate axes
    ax1.barh(x, pred_times_mean, xerr=pred_times_ci95, capsize=5,
color='gray', label='Prediction')
    ax1.set_xlabel("Prediction Time [ms]")
    ax1.set_yticks(x)
    ax1.set yticklabels(labels)
```

```
ax1.tick_params(axis='both', direction='inout', length=5, bottom=True,
top=True)

ax2.barh(x, place_times_mean, xerr=place_times_ci95, capsize=5,
color='lightgray', label='Placement')
   ax2.set_xlabel("Total Time [s]")
   # log scale; avoid "power 10" labels
   ax2.set_xscale('log')
   ax2.tick_params(axis='both', direction='inout', length=5, bottom=True,
top=True)
   ax2.xaxis.set_major_formatter(ScalarFormatter())

plt.tight_layout()
   fig.savefig(f'plots/runtimes.pdf', bbox_inches='tight')
comparison_barplot_two(list(reversed(all_times_ms)),
list(reversed(placement_times)), list(reversed(labels)))
```

