

2.9 let $G = \{V, \Sigma, R, S\}$, we know that $\Sigma = \{a, b, c\}$, R is following rules:

$$S \rightarrow U/V$$

$$U \rightarrow Uc/A$$

$$A \rightarrow \cancel{aA} aAb/\epsilon$$

$$V \rightarrow aV/B$$

$$B \rightarrow bBc/\epsilon$$

G is ambiguity, for $\cancel{A}abc$, we have

$$S \Rightarrow U \Rightarrow Uc \Rightarrow Ac \Rightarrow aAbc \Rightarrow a\epsilon bc \Rightarrow abc$$

or

$$S \Rightarrow V \Rightarrow aV \Rightarrow aB \Rightarrow abBc \Rightarrow ab\epsilon c \Rightarrow abc$$

2.13 a. $L_1 = 0^i \# 0^j$ where $i \geq 0$ and $j \geq 0$

$$L_2 = \cancel{0} 0^i \# 0^{2i} \quad i \geq 0$$

$$L(G) = L_1 \cup L_2$$

b. assume $L(G)$ is regular, let $\cancel{L_1} S = 0^p \# 0^{2p} \in L$,
let $xy = 0^p$ $|xy| \leq p$, so y must be all 0,

$$xyz = 0^p \# 0^{2p}$$

$$xy^0z = 0^{p-k} \# 0^{2p}$$

xy^0z is doesn't belongs to L , so L is not regular

4.3 we construct the following TM:

$M =$ "On input $\langle A \rangle$ where $A = (Q, \Sigma, \delta, q, F)$ is a DFA

1. Construct a new DFA $B = (Q, \Sigma, \delta, q, Q - F)$

2. ~~Run~~ run TM T in theory 4.4 to see if $L(B) = \emptyset$

3. ~~is $L(B)$~~ if T accept, ~~$L(B)$~~ accept

4. if T reject, then reject "

because $L(A) \cup L(B) = \Sigma^*$, so if $L(B) = \emptyset$, then $L(A) = \Sigma^*$

Q5.1 ALLCFG is undecidable, Define ~~CFG~~ CFG G_0 to make $L(G_0) = \Sigma^*$

Let M be a TM that decide EQCFG and construct TMS to decide ALLCFG,

$S =$ "on input $\langle G \rangle$, where G is a CFG;

1. Run M on input $\langle G, G_0 \rangle$

2. if M accept, accept, if M reject, reject "

because ALLCFG is undecidable, so ~~we can~~ M ~~can not~~ ~~will not~~ can not decide if G is equal to G_0 , therefore EQCFG is undecidable.