

# Project 2

## Part 1. introduction

Design a Turing machine  $M$ , which is used to determine whether the received string meets the following conditions

$$L = \{a^n b^m a^{(n+m)} \mid n, m \geq 1\}$$

## Part 2. Designation

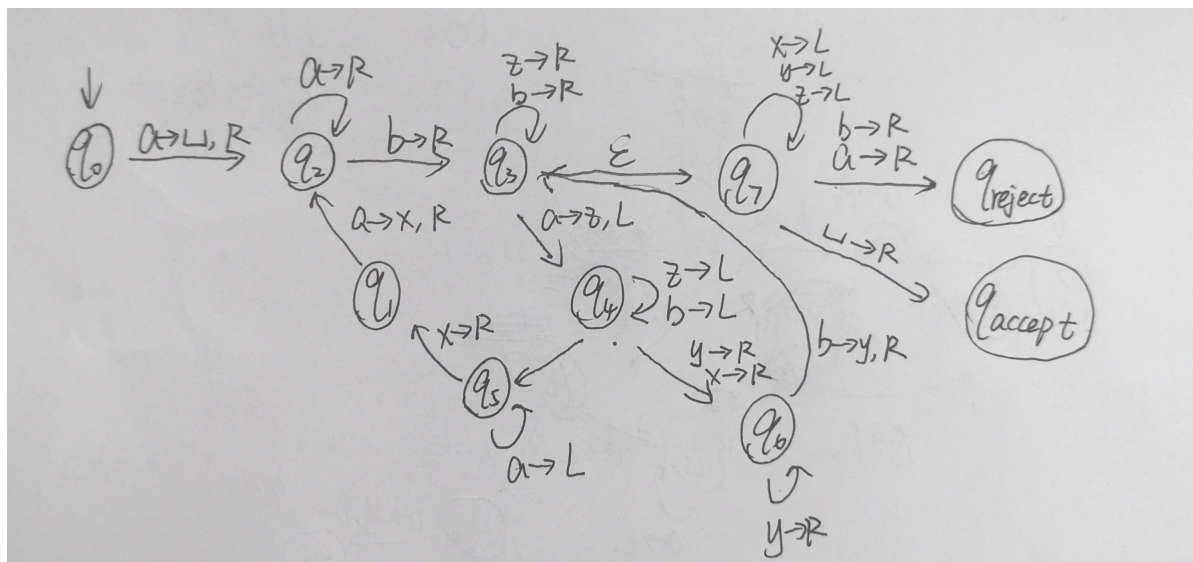
### 2.1 How to design state diagram

the procedure of the state diagram

```
while there exists  $a$  on the left
    1. when we accept one  $a$  on the  $b$ 's left , replace it by one  $x$ 
    2. the pointer move to right till the  $a$  on the  $b$ 's right, we
replace one  $a$  with one  $z$ 
    3. the pointer return to the right untill confronted with  $x$ 
while there exists  $b$  or  $a$  on the right
    4. replace one  $b$  by  $y$ 
    5. the pointer move right to one  $a$ , and replace it by  $z$ 
    6. the pointer return to the left till confronted with a  $y$ , move
right
    check all of the chars, if there still exist  $a, b, c$  , then reject, if not
exist, then accept
```

in a word, we firstly eliminate an  $a$  on the left or a  $b$ , then we eliminate an  $a$  on the right.

### 2.2 the picture of the state diagram



## 2.3 Design Turing machine

from part 2.2 we can describe the Turing machine as:

$$Q = \{q_0, q_1, \dots, q_9\}$$

$$\Sigma = \{a, b\}$$

$$\Gamma = \{a, b, @, x, y, z\}$$

$$\delta = \{f_0, f_1, \dots, f_{24}\}$$

$$q_{start} = q_0$$

$$q_{accept} = q_9$$

## Part 3. experiment result

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input a string to match: *aabaaa*

ACCEPTED!

input a string to match: *aabaa*

REJECTED!

input a string to match: *abaaa*

REJECTED!

input a string to match: *abaa*

ACCEPTED!