

You can write your homework completely in HybLang! You can even put raw  $\text{\LaTeX}$  in the annotations in HybLang! Is it just me or is

$$\pi \approx 3!$$

We are tasked to show that

$$\begin{array}{c} \mathcal{L}_L \\ \hline \text{CTXT}(m \in \{\mathbf{0}, \mathbf{1}\}) : \\ k \leftarrow \{\mathbf{0}, \mathbf{1}\} \\ c := k \oplus m \\ \text{return } c \& m \end{array} \equiv \begin{array}{c} \mathcal{L}_R \\ \hline \text{CTXT}(m \in \{\mathbf{0}, \mathbf{1}\}) : \\ c \leftarrow \{\mathbf{0}, \mathbf{1}\} \\ \text{return } c \end{array}$$

are interchangeable. This obviously not the case, since the distinguishing program

$$\begin{array}{c} \mathcal{A} \\ m := \mathbf{0} \\ c := \text{CTXT}(m) \\ \text{return } m \stackrel{?}{=} \mathbf{0} \end{array}$$

always returns true when linked to library L. Since we have

$$\begin{array}{c} \mathcal{A} \\ m := \mathbf{0} \\ c := \text{CTXT}(m) \\ \text{return } m \stackrel{?}{=} \mathbf{0} \end{array} \diamond \begin{array}{c} \mathcal{L}_L \\ \hline \text{CTXT}(m \in \{\mathbf{0}, \mathbf{1}\}) : \\ k \leftarrow \{\mathbf{0}, \mathbf{1}\} \\ c := k \oplus m \\ \text{return } c \& m \end{array} \implies \text{true}$$

and

$$\begin{array}{c} \mathcal{A} \\ m := \mathbf{0} \\ c := \text{CTXT}(m) \\ \text{return } m \stackrel{?}{=} \mathbf{0} \end{array} \diamond \begin{array}{c} \mathcal{L}_R \\ \hline \text{CTXT}(m \in \{\mathbf{0}, \mathbf{1}\}) : \\ c \leftarrow \{\mathbf{0}, \mathbf{1}\} \\ \text{return } c \end{array} \implies \frac{1}{2}$$

so we know that

$$\begin{array}{c} \mathcal{A} \\ m := \mathbf{0} \\ c := \text{CTXT}(m) \\ \text{return } m \stackrel{?}{=} \mathbf{0} \end{array}$$

is a distinguishing program, so it is not the case that

$$\begin{array}{c} \mathcal{L}_L \\ \hline \text{CTXT}(m \in \{\mathbf{0}, \mathbf{1}\}) : \\ k \leftarrow \{\mathbf{0}, \mathbf{1}\} \\ c := k \oplus m \\ \text{return } c \& m \end{array} \text{ and } \begin{array}{c} \mathcal{L}_R \\ \hline \text{CTXT}(m \in \{\mathbf{0}, \mathbf{1}\}) : \\ c \leftarrow \{\mathbf{0}, \mathbf{1}\} \\ \text{return } c \end{array}$$

are interchangeable, thus proving a counterexample of the claim.