SimFL

January 30, 2024

Syntax

$$\alpha \in \textsc{TypeVar} \qquad T \in \textsc{TypeCon} \qquad C \in \textsc{DataCon}$$

$$\begin{aligned} \mathit{datadef} \in \textsc{DataDef} &::= \mathsf{data}\ T\ \overline{\alpha} = \delta\ \overline{\langle \mid\ \delta \rangle} \\ \delta \in \textsc{ConDef} &::= C\ \overline{\tau} \end{aligned}$$

$$\begin{aligned} e \in \textsc{Expr} ::= {} & x \\ \mid {} & n \\ \mid {} & C \\ \mid {} & [\,] \\ \mid {} & [\,e\ \overline{\langle , e \rangle}\,] \\ \mid {} & e \bullet e \\ \mid {} & (\bullet) \\ \mid {} & \mathsf{fun}\ x\ \mathsf{->}\ e \\ \mid {} & e\ e \\ \mid {} & \mathsf{let}\ x = e\ \mathsf{in}\ e \\ \mid {} & \mathsf{let\ rec}\ f\ x = e\ \overline{\langle \mathsf{and\ rec}\ f\ x = e \rangle}\ \mathsf{in}\ e \\ \mid {} & \mathsf{case}\ e\ \mathsf{of}\ \{\ p\ \mathsf{->}\ e\ \overline{\langle \mathsf{;}\ p\ \mathsf{->}\ e \rangle}\ \} \\ \mid {} & \mathsf{if}\ e\ \mathsf{then}\ e\ \mathsf{else}\ e \\ d \in \textsc{Decl} ::= {} & f = e \\ \mid {} & \mathsf{rec}\ f\ x = e \\ \mid {} & \mathsf{data}\ T = C\ \overline{\tau}\ \overline{\langle \mid\ C\ \overline{\tau} \rangle} \\ \mid {} & \mathsf{rec}\ f\ x : \tau = e \\ \mid {} & \mathsf{rec}\ f\ x\ \overline{x} = e \\ \mid {} & \mathsf{data}\ T\ \overline{\alpha} = \delta\ \overline{\langle \mid\ \delta \rangle} \\ \bullet \in \textsc{BinOp} ::= {} & s\overline{s} \end{aligned}$$

$$\begin{aligned} v \in \textsc{Value} ::= {} & C\ \overline{v} \\ \mid {} & (\textbf{closure}\ x \to e, \rho) \end{aligned}$$

$$\frac{}{\rho \vdash n \Rightarrow n}\ \textsc{Num} \qquad \frac{}{\rho \vdash C \Rightarrow C}\ \textsc{Con} \qquad \frac{(x, v) \in \rho}{\rho \vdash x \Rightarrow v}\ \textsc{Var}$$

$$\frac{}{\rho \vdash \mathsf{fun}\ x\ \texttt{->}\ e \Rightarrow (\textbf{closure}\ x \to e, \rho)}\ \textsc{Fun}$$

$$\frac{\rho \vdash e_1 \Rightarrow (\textbf{closure}\ x \to e_3, \sigma) \qquad \rho \vdash e_2 \Rightarrow v_2 \qquad \sigma[x \mapsto v_2] \vdash e_3 \Rightarrow v_3}{\rho \vdash e_1\ e_2 \Rightarrow v_3}\ \textsc{App}$$

$$\frac{\rho \vdash e_1 \Rightarrow C\ \hat{v} \qquad \rho \vdash e_2 \Rightarrow v}{\rho \vdash e_1\, e_2 \Rightarrow C\ \hat{v}, v}\ \textsc{AppCons}$$

$$\frac{\rho \vdash e_1 \Rightarrow v_1 \qquad \rho[x \mapsto v_1] \vdash e_2 \Rightarrow v_2}{\rho \vdash \mathsf{let}\ x = e_1\ \mathsf{in}\ e_2 \Rightarrow v_2}\ \textsc{Let}$$

$$\frac{\rho \vdash e \Rightarrow v \qquad v \triangleright p_i : \sigma_i \qquad \rho, \sigma_i \vdash e_i \Rightarrow v_i \qquad i \leq n}{\rho \vdash \mathsf{case}\ e\ \mathsf{of}\ \{\overline{\langle p_n\ \texttt{->}\ e_n \rangle}\} \Rightarrow v_2}\ \textsc{Case}$$

$$\frac{\rho \vdash e_1 \Rightarrow v_1 \qquad \rho \vdash e_2 \Rightarrow v_2 \qquad \mathsf{builtin}\ \bullet}{\rho \vdash e_1 \bullet e_2 \Rightarrow v_1 [\![\bullet]\!] v_2}\ \textsc{BuiltInOp} \qquad \frac{\rho \vdash \mathsf{fun\ a\ \texttt{->}\ (fun\ b\ \texttt{->}\ a\ \bullet\ b)} \Rightarrow v \qquad \mathsf{builtin}\ \bullet}{\rho \vdash (\bullet) \Rightarrow v}\ \textsc{BuiltInFun}$$

$$\frac{}{v \triangleright \_ : \varnothing}\ \textsc{MatchAny} \qquad \frac{}{v \triangleright x : \{x \mapsto v\}}\ \textsc{MatchVar}$$

$$\frac{\forall i \leq n,\ \ v_i \triangleright p_i : \sigma_i \qquad \bigcap_{j=1}^{n} \mathsf{free}(\sigma_j) = \varnothing \qquad \sigma = \bigcup_{j=1}^{n} \sigma_j}{C\ \hat{v} \triangleright C\ \hat{p} : \sigma}\ \textsc{MatchCons}$$