

SimFL

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Syntax

$T \in \text{TYPECON} \quad C \in \text{DATA CON}$

$e \in \text{EXPR} ::= x$
| n
| C
| $[]$
| $[e \overline{\langle, e \rangle}]$
| $e \bullet e$
| (\bullet)
| $\text{fun } x \rightarrow e$
| $e e$
| $\text{let } x = e \text{ in } e$
| $\text{let rec } f x = e \overline{\langle \text{and rec } f x = e \rangle} \text{ in } e$
| $\text{case } e \text{ of } \{ p \rightarrow e \overline{\langle; p \rightarrow e \rangle} \}$
| $\text{if } e \text{ then } e \text{ else } e$

$\bullet \in \text{BINOP} ::= s\bar{s}$
 $v \in \text{VALUE} ::= C \bar{v}$
| $(\text{closure } x \rightarrow e, \rho)$

Natural Semantics

$$\begin{array}{c}
\frac{}{\rho \vdash n \Rightarrow n} \text{NUM} \quad \frac{}{\rho \vdash C \Rightarrow C} \text{CON} \quad \frac{(x, v) \in \rho}{\rho \vdash x \Rightarrow v} \text{VAR} \\
\\
\frac{}{\rho \vdash \text{fun } x \rightarrow e \Rightarrow (\text{closure } x \rightarrow e, \rho)} \text{FUN} \\
\\
\frac{\rho \vdash e_1 \Rightarrow (\text{closure } x \rightarrow e_3, \sigma) \quad \rho \vdash e_2 \Rightarrow v_2 \quad \sigma[x \mapsto v_2] \vdash e_3 \Rightarrow v_3}{\rho \vdash e_1 e_2 \Rightarrow v_3} \text{APP} \\
\\
\frac{\rho \vdash e_1 \Rightarrow C \hat{v} \quad \rho \vdash e_2 \Rightarrow v}{\rho \vdash e_1 e_2 \Rightarrow C \hat{v}, v} \text{APPCONS} \\
\\
\frac{\rho \vdash e_1 \Rightarrow v_1 \quad \rho[x \mapsto v_1] \vdash e_2 \Rightarrow v_2}{\rho \vdash \text{let } x = e_1 \text{ in } e_2 \Rightarrow v_2} \text{LET} \\
\\
\frac{\rho[f \mapsto (\text{closure } x \rightarrow \text{let rec } f \text{ } x = e_1 \text{ in } e_1, \rho)] \vdash e_2 \Rightarrow v}{\rho \vdash \text{let rec } f \text{ } x = e_1 \text{ in } e_2 \Rightarrow v} \text{LETREC} \\
\\
\frac{\rho \vdash e \Rightarrow v \quad v \triangleright p_i : \sigma_i \quad \rho, \sigma_i \vdash e_i \Rightarrow v_i \quad i \leq n}{\rho \vdash \text{case } e \text{ of } \{\overline{p_n \rightarrow e_n}\} \Rightarrow v_2} \text{CASE} \\
\\
\frac{\rho \vdash e_1 \Rightarrow \text{True} \quad \rho \vdash e_2 \Rightarrow v_2}{\rho \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \Rightarrow v_2} \text{IFTRUE} \quad \frac{\rho \vdash e_1 \Rightarrow \text{False} \quad \rho \vdash e_3 \Rightarrow v_3}{\rho \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \Rightarrow v_3} \text{IFFALSE} \\
\\
\frac{\rho \vdash e_1 \Rightarrow v_1 \quad \rho \vdash e_2 \Rightarrow v_2 \quad \text{builtin } \bullet}{\rho \vdash e_1 \bullet e_2 \Rightarrow v_1 \llbracket \bullet \rrbracket v_2} \text{BUILTINOP} \\
\\
\frac{\rho \vdash \text{fun } a \rightarrow (\text{fun } b \rightarrow a \bullet b) \Rightarrow v \quad \text{builtin } \bullet}{\rho \vdash (\bullet) \Rightarrow v} \text{BUILTINFUN} \\
\\
\frac{[] \Downarrow e \quad \rho \vdash e \Rightarrow v}{\rho \vdash [] \Rightarrow v} \text{LIST}_1 \quad \frac{1 \leq n \quad [e_1, \dots, e_n] \Downarrow e \quad \rho \vdash e \Rightarrow v}{\rho \vdash [e_1, \dots, e_n] \Rightarrow v} \text{LIST}_2 \\
\\
\frac{}{v \triangleright _ : \emptyset} \text{MATCHANY} \quad \frac{}{v \triangleright x : \{x \mapsto v\}} \text{MATCHVAR} \\
\\
\frac{\forall i \leq n, \ v_i \triangleright p_i : \sigma_i \quad \bigcap_{j=1}^n \text{free}(p_j) = \emptyset \quad \sigma = \bigcup_{j=1}^n \sigma_j}{C \hat{v} \triangleright C \hat{p} : \sigma} \text{MATCHCONS} \\
\\
\frac{}{[] \Downarrow []} \text{NIL} \quad \frac{}{[e_1, \dots, e_n] \Downarrow []} \text{NIL}
\end{array}$$