

b) We have 17 lines: $\{A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, X, Y, P, Q, R\} \Rightarrow 40$ Faults

Let take the input vector (X, A, B) as $(1, 0, 1)$

The faults detected by:

$$(X, A, B) := (1, 0, 1) = \{X/0, A/1, B/0, C/0, D/0, H/0, I/0, J/1, K/1, L/0, M/0, O/0, Y/1\} \Rightarrow 13 \text{ Faults}$$

24 Faults left

$$\bullet \text{ Now let's try } (X, A, B) := (0, 1, 0) = \{X/1, A/0, B/1, C/1, D/0, F/1, G/0, H/0, I/0, J/0, M/1, L/1, N/1, O/1, Y/1\}$$

9 Faults remaining

$$\bullet \text{ Now let's try } (X, A, B) := (1, 1, 1) = \{X/0, A/0, B/0, D/1, E/1, H/1, I/0, J/1, K/0, L/0, M/1, N/1, O/1, Y/0\}$$

4 Faults remaining

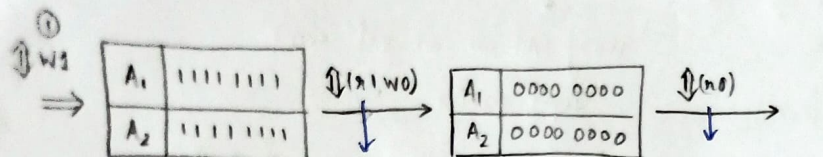
$$\bullet \text{ Now let's try } (X, A, B) := (0, 1, 1) \Rightarrow \text{This will cover them left}$$

$$\{E/0, F/0, G/1, N/0\}$$

Hence the test set is: $\{(1, 0, 1), (0, 1, 0), (1, 1, 1), (0, 1, 1)\}$

1. detect AND-decoder and stuck-at-all faults, we can use the following march sequence.

$\{\downarrow w1, \uparrow(r1, w0), \downarrow(r0), \uparrow(w1), \downarrow(r1, w0), \uparrow(r0)\}$

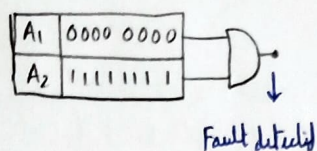


① If we don't read
then we have
a SA0 fault

① SA1 faults are
detected

② AND-Decoder fault
is also detected here

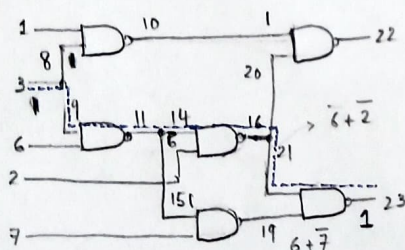
\uparrow : checks in ascending order
 \downarrow : checks in descending order



For the "10101010" and "01010101" fault we will add another element in the march test:

$\{\downarrow(w10101010), \downarrow(r10101010, w01010101), \downarrow(r01010101)\}$

The complete March test sequence is: $\{\downarrow w1, \uparrow(r1, w0), \downarrow(r0), \uparrow(w1), \downarrow(r1, w0), \uparrow(r0), \downarrow(w10101010), \downarrow(r10101010, w01010101), \downarrow(r01010101)\}$



$$11 = \overline{3} + \overline{6}$$

$$16 = \overline{2} + \overline{11} = \overline{2} + 3 \cdot 6$$

$$23 = \overline{16} + \overline{19} = \overline{2 \cdot (\overline{3} + \overline{6}) + \overline{19}} = \overline{2 \cdot (\overline{3} + \overline{6}) + 3 \cdot 6 + 7}$$

(or path)

The path is: $3 \uparrow, 9, 11, 14, 16, 21, 23 \downarrow$ \Rightarrow To detect fault - all signals should flip on change of input

So when $\Rightarrow 3 \equiv 0 \rightarrow 11 = 1$
 $\downarrow 16 = \overline{2} = 1$
 $23 = \overline{2} + \overline{7} = 1$

and

when $\Rightarrow 3 \equiv 1 \rightarrow 11 = \overline{6}$

$$16 = \overline{2} + \overline{6}$$

$$23 = \overline{2 \cdot \overline{6} + 6 + 7} = \overline{(2 + 7) \cdot \overline{6}} = 1$$

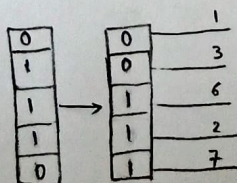
For signal toggle $\Rightarrow \overline{0} = 0 \Rightarrow 6 = 1$

$$\textcircled{2} \quad \overline{2} \oplus (\overline{2} + 6) = 1 \Rightarrow \overline{2} \oplus 6 = 1, 2 = 1$$

$$\textcircled{3} \quad 23 = 1 \rightarrow \overline{7} = 1$$

$$23 = 0 \rightarrow \text{already satisfied by } 6 = 1$$

Therefore to enable the path these two input sequences are required.



Bonus Parts

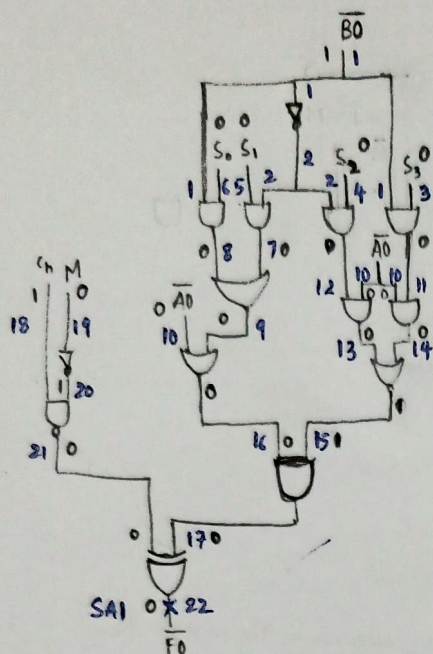
1. Since \overline{FO} is an output, it is observable already, we only need to excite it.
We don't need to consider the entire circuit \Rightarrow

Using SAT we can get some
Input vectors

$$T = (K_0, M, S_0, S_1, S_2, S_3, A_0, B_0, A_1, B_1, A_2, B_2, A_3, B_3)$$

$$\downarrow$$

$$(1, 0, 0, 1, 0, 0, 0, 0, X, X, X, X, X, X)$$



2. Like the last part we only need to excite both the faults:

Here we would have to consider the entire circuit so for brevity's sake, I am not drawing the circuit.

we use SAT to get our test input $\Rightarrow T = (1, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1)$