

PHYS 2310 Engineering Physics I Formula Sheets

Chapters 1-18

Chapter 1/Important Numbers

Units for SI Base Quantities

| Quantity | Unit Name | Unit Symbol |
|-------------------|-----------|-------------|
| Length | Meter | m |
| Time | Second | s |
| Mass (not weight) | Kilogram | kg |

Common Conversions

| | | | |
|-------------|-------------------|--------|-----------------------------|
| 1 kg or 1 m | 1000 g or m | 1 m | $1 \times 10^6 \mu\text{m}$ |
| 1 m | 100 cm | 1 inch | 2.54 cm |
| 1 m | 1000 mm | 1 day | 86400 seconds |
| 1 second | 1000 milliseconds | 1 hour | 3600 seconds |
| 1 m | 3.281 ft | 360° | 2π rad |

Important Constants/Measurements

| | |
|------------------------|---------------------------------------------|
| Mass of Earth | 5.98×10^{24} kg |
| Radius of Earth | 6.38×10^6 m |
| 1 u (Atomic Mass Unit) | 1.661×10^{-27} kg |
| Density of water | 1 g/cm^3 or 1000 kg/m^3 |
| g (on earth) | 9.8 m/s^2 |

Density

Common geometric Formulas

| | | | |
|----------------------------|---------------------------------------------------------------------|-----------------|--------------------------|
| Circumference | $C = 2\pi r$ | Area circle | $A = \pi r^2$ |
| Surface area (sphere) | $SA = 4\pi r^2$ | Volume (sphere) | $V = \frac{4}{3}\pi r^3$ |
| Volume (rectangular solid) | $V = l \cdot w \cdot h$ $V = \text{area} \cdot \text{thickness}$ | | |

Chapter 2

Velocity

| | | |
|------------------------|---------------------------------------------------------------------------------|-----|
| Average Velocity | $V_{avg} = \frac{\text{displacement}}{\text{time}} = \frac{\Delta x}{\Delta t}$ | 2.2 |
| Average Speed | $s_{avg} = \frac{\text{total distance}}{\text{time}}$ | 2.3 |
| Instantaneous Velocity | $v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$ | 2.4 |

Acceleration

| | | |
|----------------------------|-----------------------------------------|------------|
| Average Acceleration | $a_{avg} = \frac{\Delta v}{\Delta t}$ | 2.7 |
| Instantaneous Acceleration | $a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$ | 2.8 2.9 |

Motion of a particle with constant acceleration

| | |
|--------------------------------------|------|
| $v = v_0 + at$ | 2.11 |
| $\Delta x = \frac{1}{2}(v_0 + v)t$ | 2.17 |
| $\Delta x = v_0 t + \frac{1}{2}at^2$ | 2.15 |
| $v^2 = v_0^2 + 2a\Delta x$ | 2.16 |

Chapter 3

| | | |
|-----------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| Adding Vectors Geometrically | $\vec{a} + \vec{b} = \vec{b} + \vec{a}$ | 3.2 |
| Adding Vectors Geometrically (Associative Law) | $(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$ | 3.3 |
| Components of Vectors | $a_x = a \cos \theta$ $a_y = a \sin \theta$ | 3.5 |
| Magnitude of vector | $ \vec{a} = a = \sqrt{a_x^2 + a_y^2}$ | 3.6 |
| Angle between x axis and vector | $\tan \theta = \frac{a_y}{a_x}$ | 3.6 |
| Unit vector notation | $\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$ | 3.7 |
| Adding vectors in Component Form | $r_x = a_x + b_x$ | 3.10 |
| | $r_y = a_y + b_y$ | 3.11 |
| | $r_z = a_z + b_z$ | 3.12 |
| Scalar (dot product) | $\vec{a} \cdot \vec{b} = ab \cos \theta$ | 3.20 |
| Scalar (dot product) | $\vec{a} \cdot \vec{b} = (a_x \hat{i} + a_y \hat{j} + a_z \hat{k}) \cdot (b_x \hat{i} + b_y \hat{j} + b_z \hat{k})$ $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$ | 3.22 |
| Projection of \vec{a} on \vec{b} or component of \vec{a} on \vec{b} | $\frac{\vec{a} \cdot \vec{b}}{ \vec{b} }$ | |
| Vector (cross) product magnitude | $c = ab \sin \phi$ | 3.24 |
| Vector (cross product) | $\vec{a} \times \vec{b} = (a_x \hat{i} + a_y \hat{j} + a_z \hat{k}) \times (b_x \hat{i} + b_y \hat{j} + b_z \hat{k})$ $= (a_y b_z - b_y a_z) \hat{i} + (a_z b_x - b_z a_x) \hat{j} + (a_x b_y - b_x a_y) \hat{k}$ or $\vec{a} \times \vec{b} = \det \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$ | 3.26 |

Chapter 4

| | | |
|----------------------------|----------------------------------------------------------------------------------------|--------------|
| Position vector | $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ | 4.4 |
| displacement | $\Delta \vec{r} = \Delta x \hat{i} + \Delta y \hat{j} + \Delta z \hat{k}$ | 4.4 |
| Average Velocity | $\vec{V}_{avg} = \frac{\Delta \vec{r}}{\Delta t}$ | 4.8 |
| Instantaneous Velocity | $\vec{v} = \frac{d\vec{r}}{dt} = v_x \hat{i} + v_y \hat{j} + v_z \hat{k}$ | 4.10 4.11 |
| Average Acceleration | $\vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t}$ | 4.15 |
| Instantaneous Acceleration | $\vec{a} = \frac{d\vec{v}}{dt}$ $\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$ | 4.16 4.17 |

Projectile Motion

| | | |
|------------|------------------------------------------------------------------------------------------------------------|------|
| | $v_y = v_0 \sin \theta_0 - gt$ | 4.23 |
| | $\Delta x = v_0 \cos \theta_0 t + \frac{1}{2} a_x t^2$ or $\Delta x = v_0 \cos \theta_0 t$ if $a_x = 0$ | 4.21 |
| | $\Delta y = v_0 \sin \theta_0 t - \frac{1}{2} g t^2$ | 4.22 |
| | $v_y^2 = (v_0 \sin \theta_0)^2 - 2g \Delta y$ | 4.24 |
| | $v_y = v_0 \sin \theta_0 - gt$ | 4.23 |
| Trajectory | $y = (\tan \theta_0) x - \frac{g x^2}{2(v_0 \cos \theta_0)^2}$ | 4.25 |
| Range | $R = \frac{v_0^2 \sin(2\theta_0)}{g}$ | 4.26 |

| | | |
|-----------------|----------------------------------------------|------|
| Relative Motion | $\vec{v}_{AC} = \vec{v}_{AB} + \vec{v}_{BC}$ | 4.44 |
| | $\vec{a}_{AB} = \vec{a}_{BA}$ | 4.45 |

| | | |
|-------------------------|------------------------------------------------|--------------|
| Uniform Circular Motion | $a = \frac{v^2}{r} \quad T = \frac{2\pi r}{v}$ | 4.34 4.35 |
|-------------------------|------------------------------------------------|--------------|

Chapter 5

Newton's Second Law

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|----------------|----------------------------------------------------------------|-----|
| General | $\vec{F}_{net} = m\vec{a}$ | 5.1 |
| Component form | $F_{net,x} = ma_x$ $F_{net,y} = ma_y$ $F_{net,z} = ma_z$ | 5.2 |

Gravitational Force

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|---------------------|------------|------|
| Gravitational Force | $F_g = mg$ | 5.8 |
| Weight | $W = mg$ | 5.12 |

Chapter 6

Friction

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|---------------------------|--------------------------------------|------|
| Static Friction (maximum) | $\vec{f}_{s,max} = \mu_s F_N$ | 6.1 |
| Kinetic Frictional | $\vec{f}_k = \mu_k F_N$ | 6.2 |
| Drag Force | $D = \frac{1}{2} C \rho A v^2$ | 6.14 |
| Terminal velocity | $v_t = \sqrt{\frac{2F_g}{C \rho A}}$ | 6.16 |

| | | |
|--------------------------|----------------------|------|
| Centripetal acceleration | $a = \frac{v^2}{R}$ | 6.17 |
| Centripetal Force | $F = \frac{mv^2}{R}$ | 6.18 |

Chapter 7

| | | |
|--------------------------------------------------------------------|-----------------------------------------------------------------------------------|--------------|
| Kinetic Energy | $K = \frac{1}{2}mv^2$ | 7.1 |
| Work done by constant Force | $W = Fd\cos\theta = \vec{F} \cdot \vec{d}$ | 7.7 7.8 |
| Work- Kinetic Energy Theorem | $\Delta K = K_f - K_0 = W$ | 7.10 |
| Work done by gravity | $W_g = mgd\cos\phi$ | 7.12 |
| Work done by lifting/lowering object | $\Delta K = W_a + W_g$ $W_a = \text{applied Force}$ | 7.15 |
| Spring Force (Hooke's law) | $\vec{F}_s = -k\vec{d}$ $F_x = -kx$ (along x-axis) | 7.20 7.21 |
| Work done by spring | $W_s = \frac{1}{2}kx_i^2 - \frac{1}{2}kx_f^2$ | 7.25 |
| Work done by Variable Force | $W = \int_{x_i}^{x_f} F_x dx + \int_{y_i}^{y_f} F_y dy + \int_{z_i}^{z_f} F_z dz$ | 7.36 |
| Average Power (rate at which that force does work on an object) | $P_{avg} = \frac{W}{\Delta t}$ | 7.42 |
| Instantaneous Power | $P = \frac{dW}{dt} = FV\cos\theta = \vec{F} \cdot \vec{v}$ | 7.43 7.47 |

Chapter 8

| | | |
|------------------------------------------------------|------------------------------------------------------------------|--------------|
| Potential Energy | $\Delta U = -W = -\int_{x_i}^{x_f} F(x)dx$ | 8.1 8.6 |
| Gravitational Potential Energy | $\Delta U = mg\Delta y$ | 8.7 |
| Elastic Potential Energy | $U(x) = \frac{1}{2}kx^2$ | 8.11 |
| Mechanical Energy | $E_{mec} = K + U$ | 8.12 |
| Principle of conservation of mechanical energy | $K_1 + U_1 = K_2 + U_2$ $E_{mec} = \Delta K + \Delta U = 0$ | 8.18 8.17 |
| Force acting on particle | $F(x) = -\frac{dU(x)}{dx}$ | 8.22 |
| Work on System by external force With no friction | $W = \Delta E_{mec} = \Delta K + \Delta U$ | 8.25 8.26 |
| Work on System by external force With friction | $W = \Delta E_{mec} + \Delta E_{th}$ | 8.33 |
| Change in thermal energy | $\Delta E_{th} = f_k d\cos\theta$ | 8.31 |
| Conservation of Energy *if isolated W=0 | $W = \Delta E = \Delta E_{mec} + \Delta E_{th} + \Delta E_{int}$ | 8.35 |
| Average Power | $P_{avg} = \frac{\Delta E}{\Delta t}$ | 8.40 |
| Instantaneous Power | $P = \frac{dE}{dt}$ | 8.41 |

****In General Physics, Kinetic Energy is abbreviated to KE and Potential Energy is PE**

Chapter 9

Impulse and Momentum

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|------------------------------|----------------------------------------------------|------|
| Impulse | $\vec{J} = \int_{t_i}^{t_f} \vec{F}(t) dt$ | 9.30 |
| | $J = F_{net} \Delta t$ | 9.35 |
| Linear Momentum | $\vec{p} = m\vec{v}$ | 9.22 |
| Impulse-Momentum Theorem | $\vec{J} = \Delta \vec{p} = \vec{p}_f - \vec{p}_i$ | 9.31 |
| | | 9.32 |
| Newton's 2 nd law | $\vec{F}_{net} = \frac{d\vec{p}}{dt}$ | 9.22 |
| System of Particles | $\vec{F}_{net} = m\vec{a}_{com}$ | 9.14 |
| | $\vec{P} = M\vec{v}_{com}$ | 9.25 |
| | $\vec{F}_{net} = \frac{d\vec{P}}{dt}$ | 9.27 |

Collision

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|-----------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------|------|
| Final Velocity of 2 objects in a head-on collision where one object is initially at rest 1: moving object 2: object at rest | $v_{1f} = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) v_{1i}$ | 9.67 |
| | $v_{2f} = \left(\frac{2m_1}{m_1 + m_2} \right) v_{1i}$ | 9.68 |
| Conservation of Linear Momentum (in 1D) | $\vec{P} = \text{constant}$ | 9.42 |
| | $\vec{P}_i = \vec{P}_f$ | 9.43 |
| <i>Elastic Collision</i> | $\vec{p}_{1i} + \vec{p}_{2i} = \vec{p}_{1f} + \vec{p}_{2f}$ | 9.50 |
| | $m_1 v_{1i} + m_2 v_{12} = m_1 v_{f1} + m_2 v_{f2}$ | 9.51 |
| | $K_{1i} + K_{2i} = K_{1f} + K_{2f}$ | 9.78 |

Collision continued...

| | | |
|-----------------------------------------|---------------------------------------------------------------------------|------|
| <i>Inelastic Collision</i> | $m_1 v_{01} + m_2 v_{02} = (m_1 + m_2) v_f$ | |
| Conservation of Linear Momentum (in 2D) | $\vec{P}_{1i} + \vec{P}_{2i} = \vec{P}_{1f} + \vec{P}_{2f}$ | 9.77 |
| Average force | $F_{avg} = -\frac{n}{\Delta t} \Delta p = -\frac{n}{\Delta t} m \Delta v$ | 9.37 |
| | $F_{avg} = -\frac{\Delta m}{\Delta t} \Delta v$ | 9.40 |

Center of Mass

| | | |
|-------------------------|----------------------------------------------------------|-----|
| Center of mass location | $\vec{r}_{com} = \frac{1}{M} \sum_{i=1}^n m_i \vec{r}_i$ | 9.8 |
| Center of mass velocity | $\vec{v}_{com} = \frac{1}{M} \sum_{i=1}^n m_i \vec{v}_i$ | |

Rocket Equations

| | | |
|-----------------------|------------------------------------------|------|
| Thrust (Rv_{rel}) | $Rv_{rel} = Ma$ | 9.88 |
| Change in velocity | $\Delta v = v_{rel} \ln \frac{M_i}{M_f}$ | 9.88 |

Chapter 10

| | | |
|---------------------------------------|----------------------------------------------------------------|--------------|
| Angular displacement (in radians) | $\theta = \frac{s}{r}$ $\Delta\theta = \theta_2 - \theta_1$ | 10.1 10.4 |
| Average angular velocity | $\omega_{avg} = \frac{\Delta\theta}{\Delta t}$ | 10.5 |
| Instantaneous Velocity | $\omega = \frac{d\theta}{dt}$ | 10.6 |
| Average angular acceleration | $\alpha_{avg} = \frac{\Delta\omega}{\Delta t}$ | 10.7 |
| Instantaneous angular acceleration | $\alpha = \frac{d\omega}{dt}$ | 10.8 |

Rotational Kinematics

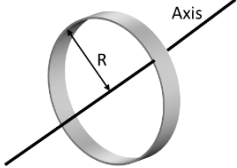
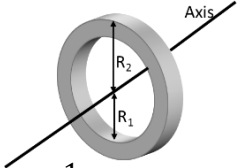
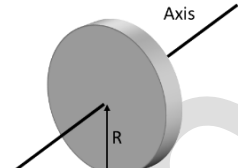
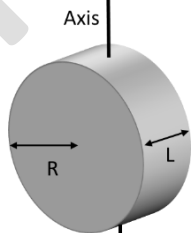
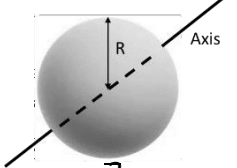
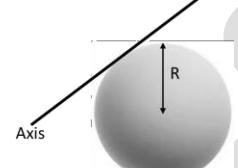
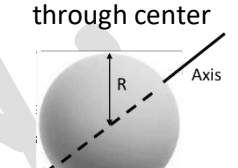

| | |
|-----------------------------------------------------|-------|
| $\omega = \omega_0 + \alpha t$ | 10.12 |
| $\Delta\theta = \omega_0 t + \frac{1}{2}\alpha t^2$ | 10.13 |
| $\omega^2 = \omega_0^2 + 2\alpha\Delta\theta$ | 10.14 |
| $\Delta\theta = \frac{1}{2}(\omega + \omega_0)t$ | 10.15 |
| $\Delta\theta = \omega t - \frac{1}{2}\alpha t^2$ | 10.16 |

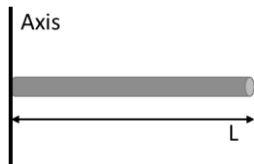
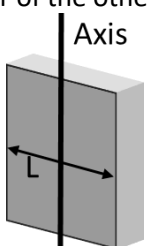
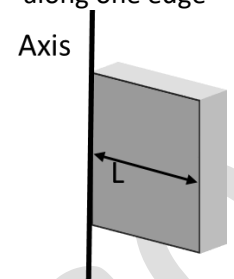
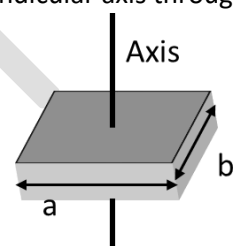
Relationship Between Angular and Linear Variables

| | | |
|--------------------------------|----------------------------------------------|----------------|
| Velocity | $v = \omega r$ | 10.18 |
| Tangential Acceleration | $a_t = \alpha r$ | 10.19 |
| Radical component of \vec{a} | $a_r = \frac{v^2}{r} = \omega^2 r$ | 10.23 |
| Period | $T = \frac{2\pi r}{v} = \frac{2\pi}{\omega}$ | 10.19 10.20 |

| | | |
|--------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|-----------------|
| Rotation inertia | $I = \sum m_i r_i^2$ | 10.34 |
| Rotation inertia (discrete particle system) | $I = \int r^2 dm$ | 10.35 |
| Parallel Axis Theorem h=perpendicular distance between two axes | $I = I_{com} + Mh^2$ | 10.36 |
| Torque | $\tau = rF_t = r_{\perp}F = rF\sin\theta$ | 10.39- 10.41 |
| Newton's Second Law | $\tau_{net} = I\alpha$ | 10.45 |
| Rotational work done by a torque | $W = \int_{\theta_i}^{\theta_f} \tau d\theta$ $W = \tau\Delta\theta$ (τ constant) | 10.53 10.54 |
| Power in rotational motion | $P = \frac{dW}{dt} = \tau\omega$ | 10.55 |
| Rotational Kinetic Energy | $K = \frac{1}{2}I\omega^2$ | 10.34 |
| Work-kinetic energy theorem | $\Delta K = K_f - K_i = \frac{1}{2}I\omega_f^2 - \frac{1}{2}I\omega_i^2 = W$ | 10.52 |

Moments of Inertia I for various rigid objects of Mass M

| | | | |
|------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Thin walled hollow cylinder or hoop about central axis</p>  $I = MR^2$ | <p>Annular cylinder (or ring) about central axis</p>  $I = \frac{1}{2} M(R_1^2 + R_2^2)$ | <p>Solid cylinder or disk about central axis</p>  $I = \frac{1}{2} MR^2$ | <p>Solid cylinder or disk about central diameter</p>  $I = \frac{1}{4} MR^2 + \frac{1}{12} ML^2$ |
| <p>Solid Sphere, axis through center</p>  $I = \frac{2}{5} MR^2$ | <p>Solid Sphere, axis tangent to surface</p>  $I = \frac{7}{5} MR^2$ | <p>Thin Walled spherical shell, axis through center</p>  $I = \frac{2}{3} MR^2$ | <p>Thin rod, axis perpendicular to rod and passing through center</p>  $I = \frac{1}{12} ML^2$ |

| | | | |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Thin rod, axis perpendicular to rod and passing through end</p>  <p>$I = \frac{1}{3}ML^2$</p> | <p>Thin Rectangular sheet (slab), axis parallel to sheet and passing through center of the other edge</p>  <p>$I = \frac{1}{12}ML^2$</p> | <p>Thin Rectangular sheet (slab), axis along one edge</p>  <p>$I = \frac{1}{3}ML^2$</p> | <p>Thin rectangular sheet (slab) about perpendicular axis through center</p>  <p>$I = \frac{1}{12}M(a^2 + b^2)$</p> |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Chapter 11

Rolling Bodies (wheel)

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|-------------------------------------------------|---------------------------------------------------------------|-------|
| Speed of rolling wheel | $v_{com} = \omega R$ | 11.2 |
| Kinetic Energy of Rolling Wheel | $K = \frac{1}{2} I_{com} \omega^2 + \frac{1}{2} M v_{com}^2$ | 11.5 |
| Acceleration of rolling wheel | $a_{com} = \alpha R$ | 11.6 |
| Acceleration along x-axis extending up the ramp | $a_{com,x} = -\frac{g \sin \theta}{1 + \frac{I_{com}}{MR^2}}$ | 11.10 |

Torque as a vector

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|------------------------------|----------------------------------------------------|-----------------|
| Torque | $\vec{\tau} = \vec{r} \times \vec{F}$ | 11.14 |
| Magnitude of torque | $\tau = r F_{\perp} = r_{\perp} F = r F \sin \phi$ | 11.15- 11.17 |
| Newton's 2 nd Law | $\vec{\tau}_{net} = \frac{d\vec{L}}{dt}$ | 11.23 |

Angular Momentum

| | | |
|-------------------------------------------|-----------------------------------------------------------------------------|-----------------|
| Angular Momentum | $\vec{L} = \vec{r} \times \vec{p} = m(\vec{r} \times \vec{v})$ | 11.18 |
| Magnitude of Angular Momentum | $P = rmv \sin \phi$ $P = r p_{\perp} = r m v_{\perp}$ | 11.19- 11.21 |
| Angular momentum of a system of particles | $\vec{L} = \sum_{i=1}^n \vec{p}_i$ $\vec{r}_{net} = \frac{d\vec{L}}{dt}$ | 11.26 11.29 |

Angular Momentum continued

| | | |
|-------------------------------------------|--------------------------------------------------------|----------------|
| Angular Momentum of a rotating rigid body | $L = I \omega$ | 11.31 |
| Conservation of angular momentum | $\vec{L} = \text{constant}$ $\vec{L}_i = \vec{L}_f$ | 11.32 11.33 |

Precession of a Gyroscope

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|-----------------|---------------------------------|-------|
| Precession rate | $\Omega = \frac{Mgr}{I \omega}$ | 11.31 |
|-----------------|---------------------------------|-------|

Chapter 12

Static Equilibrium

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|-------------------------------|--------------------------------------------|--------------|
| | $\vec{F}_{net} = 0$ | 12.3 |
| | $\vec{r}_{net} = 0$ | 12.5 |
| If forces lie on the xy-plane | $\vec{F}_{net,x} = 0, \vec{F}_{net,y} = 0$ | 12.7 12.8 |
| | $\vec{r}_{net,z} = 0$ | 12.9 |

| | | |
|----------------------------------------------------------------------|--------------------------------------|-------|
| Stress (force per unit area) Strain (fractional change in length) | $stress = modulus \times strain$ | 12.22 |
| Stress (pressure) | $P = \frac{F}{A}$ | |
| Tension/Compression E: Young's modulus | $\frac{F}{A} = E \frac{\Delta L}{L}$ | 12.23 |
| Shearing Stress G: Shear modulus | $\frac{F}{A} = G \frac{\Delta x}{L}$ | 12.24 |
| Hydraulic Stress B: Bulk modulus | $p = B \frac{\Delta V}{V}$ | |

Chapter 13

| | | |
|----------------------------------------------------------------|-------------------------------------------------------------------------------------------------|----------------|
| Gravitational Force (Newton's law of gravitation) | $F = G \frac{m_1 m_2}{r^2}$ | 13.1 |
| Principle of Superposition | $\vec{F}_{1,net} = \sum_{i=2}^n \vec{F}_{1i}$ | 13.5 |
| Gravitational Force acting on a particle from an extended body | $\vec{F}_1 = \int d\vec{F}$ | 13.6 |
| Gravitational acceleration | $a_g = \frac{GM}{r^2}$ | 13.11 |
| Gravitation within a spherical Shell | $F = \frac{GmM}{R^3} r$ | 13.19 |
| Gravitational Potential Energy | $U = -\frac{GMm}{r}$ | 13.21 |
| Potential energy on a system (3 particles) | $U = -\left(\frac{Gm_1 m_2}{r_{12}} + \frac{Gm_1 m_3}{r_{13}} + \frac{Gm_2 m_3}{r_{23}}\right)$ | 13.22 |
| Escape Speed | $v = \sqrt{\frac{2GM}{R}}$ | 13.28 |
| Kepler's 3 rd Law (law of periods) | $T^2 = \left(\frac{4\pi^2}{GM}\right) r^3$ | 13.34 |
| Energy for bject in circular orbit | $U = -\frac{GMm}{r} \quad K = \frac{GMm}{2r}$ | 13.21 13.38 |
| Mechanical Energy (circular orbit) | $E = -\frac{GMm}{2r}$ | 13.40 |
| Mechanical Energy (elliptical orbit) | $E = -\frac{GMm}{2a}$ | 13.42 |

*Note: $G = 6.6704 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$

Chapter 14

| | | |
|--------------------------------------------------------------|-------------------------------------------------------|-------|
| Density | $\rho = \frac{\Delta m}{\Delta V}$ | 14.1 |
| | $\rho = \frac{m}{V}$ | 14.2 |
| Pressure | $p = \frac{\Delta F}{\Delta A}$ | 14.3 |
| | $p = \frac{F}{A}$ | 14.4 |
| | | |
| Pressure and depth in a static Fluid P1 is higher than P2 | $p_2 = p_1 + \rho g(y_1 - y_2)$ | 14.7 |
| | $p = p_0 + \rho gh$ | 14.8 |
| Gauge Pressure | ρgh | |
| Archimedes' principle | $F_b = m_f g$ | 14.16 |
| Mass Flow Rate | $R_m = \rho R_V = \rho Av$ | 14.25 |
| Volume flow rate | $R_V = Av$ | 14.24 |
| Bernoulli's Equation | $p + \frac{1}{2}\rho v^2 + \rho gy = \text{constant}$ | 14.29 |
| Equation of continuity | $R_m = \rho R_V = \rho Av = \text{constant}$ | 14.25 |
| Equation of continuity when | $R_V = Av = \text{constant}$ | 14.24 |

Chapter 15

| | | |
|------------------------------|--------------------------------------------------------|-------|
| Frequency cycles per time | $f = \frac{1}{T}$ | 15.2 |
| displacement | $x = x_m \cos(\omega t + \phi)$ | 15.3 |
| Angular frequency | $\omega = \frac{2\pi}{T} = 2\pi f$ | 15.5 |
| Velocity | $v = -\omega x_m \sin(\omega t + \phi)$ | 15.6 |
| Acceleration | $a = -\omega^2 x_m \cos(\omega t + \phi)$ | 15.7 |
| Kinetic and Potential Energy | $K = \frac{1}{2}mv^2 \quad U = \frac{1}{2}kx^2$ | |
| Angular frequency | $\omega = \sqrt{\frac{k}{m}}$ | 15.12 |
| Period | $T = 2\pi\sqrt{\frac{m}{k}}$ | 15.13 |
| Torsion pendulum | $T = 2\pi\sqrt{\frac{I}{\kappa}}$ | 15.23 |
| Simple Pendulum | $T = 2\pi\sqrt{\frac{L}{g}}$ | 15.28 |
| Physical Pendulum | $T = 2\pi\sqrt{\frac{I}{mgL}}$ | 15.29 |
| Damping force | $\vec{F}_d = -b\vec{v}$ | |
| displacement | $x(t) = x_m e^{-\frac{bt}{2m}} \cos(\omega' t + \phi)$ | 15.42 |
| Angular frequency | $\omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$ | 15.43 |
| Mechanical Energy | $E(t) \approx \frac{1}{2}kx_m^2 e^{-\frac{bt}{m}}$ | 15.44 |

Chapter 16

Sinusoidal Waves

| | | |
|----------------------------------------|--------------------------------------------------------|-------|
| Mathematical form (positive direction) | $y(x, t) = y_m \sin(kx - \omega t)$ | 16.2 |
| Angular wave number | $k = \frac{2\pi}{\lambda}$ | 16.5 |
| Angular frequency | $\omega = \frac{2\pi}{T} = 2\pi f$ | 16.9 |
| Wave speed | $v = \frac{\omega}{k} = \frac{\lambda}{T} = \lambda f$ | 16.13 |
| Average Power | $P_{avg} = \frac{1}{2} \mu v \omega^2 y_m^2$ | 16.33 |

| | | |
|-----------------------------------------------------------|---------------------------------------------------------------------------------|-------|
| Traveling Wave Form | $y(x, t) = h(kx \pm \omega t)$ | 16.17 |
| Wave speed on stretched string | $v = \sqrt{\frac{T}{\mu}}$ | 16.26 |
| Resulting wave when 2 waves only differ by phase constant | $y'(x, t) = [2y_m \cos(\frac{1}{2}\phi)] \sin(kx - \omega t + \frac{1}{2}\phi)$ | 16.51 |
| Standing wave | $y'(x, t) = [2y_m \sin(kx)] \cos(\omega t)$ | 16.60 |
| Resonant frequency | $f = \frac{v}{\lambda} = n \frac{v}{2L}$ for $n=1, 2, \dots$ | 16.66 |

Chapter 17

Sound Waves

| | | |
|---------------------|---------------------------------------------|-------|
| Speed of sound wave | $v = \sqrt{\frac{B}{\rho}}$ | 17.3 |
| displacement | $s = s_m \cos(kx - \omega t)$ | 17.12 |
| Change in pressure | $\Delta p = \Delta p_m \sin(kx - \omega t)$ | 17.13 |
| Pressure amplitude | $\Delta p_m = (v\rho\omega)s_m$ | 17.14 |

Interference

| | | |
|---------------------------------|------------------------------------------------------|-------|
| Phase difference | $\phi = \frac{\Delta L}{\lambda} 2\pi$ | 17.21 |
| Fully Constructive Interference | $\phi = m(2\pi)$ for $m=0,1,2,\dots$ | 17.22 |
| | $\frac{\Delta L}{\lambda} = 0,1,2$ | 17.23 |
| Full Destructive interference | $\phi = (2m+1)\pi$ for $m=0,1,2,\dots$ | 17.24 |
| | $\frac{\Delta L}{\lambda} = .5, 1.5, 2.5, \dots$ | 17.25 |
| Mechanical Energy | $E(t) \approx \frac{1}{2} k x_m^2 e^{-\frac{bt}{m}}$ | 15.44 |

Sound Intensity

| | | |
|--------------------------------------|--------------------------------------------------------|-------|
| Intensity | $I = \frac{P}{A}$ | 17.26 |
| | $I = \frac{1}{2} \rho v \omega^2 s_m^2$ | 17.27 |
| Intensity -uniform in all directions | $I = \frac{P_s}{4\pi r^2}$ | 17.29 |
| Intensity level in decibels | $\beta = (10\text{dB}) \log\left(\frac{I}{I_o}\right)$ | 17.29 |
| Mechanical Energy | $E(t) \approx \frac{1}{2} k x_m^2 e^{-\frac{bt}{m}}$ | 15.44 |

Standing Waves Patterns in Pipes

| | | |
|---------------------------------------------|-------------------------------------------------------|-------|
| Standing wave frequency (open at both ends) | $f = \frac{v}{\lambda} = \frac{nv}{2L}$ for $n=1,2,3$ | 17.39 |
| Standing wave frequency (open at one end) | $f = \frac{v}{\lambda} = \frac{nv}{4L}$ for $n=1,3,5$ | 17.41 |

| | | |
|-------|-------------------------------|-------|
| beats | $f_{\text{beat}} = f_1 - f_2$ | 17.46 |
|-------|-------------------------------|-------|

Doppler Effect

| | | |
|----------------------------------------------------|----------------------------|-------|
| Source Moving <i>toward</i> stationary observer | $f' = f \frac{v}{v - v_s}$ | 17.53 |
| Source Moving <i>away</i> from stationary observer | $f' = f \frac{v}{v + v_s}$ | 17.54 |
| Observer moving <i>toward</i> stationary source | $f' = f \frac{v + v_D}{v}$ | 17.49 |
| Observer moving <i>away</i> from stationary source | $f' = f \frac{v - v_D}{v}$ | 17.51 |

Shockwave

| | | |
|----------------------------------|------------------------------|-------|
| Half-angle θ of Mach cone | $\sin\theta = \frac{v}{v_s}$ | 17.57 |
|----------------------------------|------------------------------|-------|

Chapter 18

Temperature Scales

| | | |
|-----------------------|-------------------------------|------|
| Fahrenheit to Celsius | $T_C = \frac{5}{9}(T_F - 32)$ | 18.8 |
| Celsius to Fahrenheit | $T_F = \frac{9}{5}T_C + 32$ | 18.8 |
| Celsius to Kelvin | $T = T_C + 273.15$ | 18.7 |

Thermal Expansion

| | | |
|--------------------------|------------------------------|-------|
| Linear Thermal Expansion | $\Delta L = L\alpha\Delta T$ | 18.9 |
| Volume Thermal Expansion | $\Delta V = V\beta\Delta T$ | 18.10 |

Heat

| | | |
|-----------------------------|---------------------------------------------------|-------|
| Heat and temperature change | $Q = C(T_f - T_i)$ | 18.13 |
| | $Q = cm(T_f - T_i)$ | 18.14 |
| Heat and phase change | $Q = Lm$ | 18.16 |
| Power | $P = Q/t$ | |
| Power (Conducted) | $P_{cond} = \frac{Q}{t} = kA \frac{T_H - T_C}{L}$ | 18.32 |
| Rate objects absorbs energy | $P_{abs} = \sigma\epsilon AT_{env}^4$ | 18.39 |
| Power from radiation | $P_{rad} = \sigma\epsilon AT^4$ | 18.38 |

$$\sigma = 5.6704 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$$

First Law of Thermodynamics

| | | |
|-----------------------------|--------------------------------------------------|-------|
| First Law of Thermodynamics | $\Delta E_{int} = E_{int,f} - E_{int,i} = Q - W$ | 18.26 |
| | $dE_{int} = dQ - dW$ | 18.27 |

Note:

ΔE_{int} Change in Internal Energy

Q (heat) is positive when the system absorbs heat and negative when it loses heat. **W** (work) is work done by system. W is positive when expanding and negative contracts because of an external force

Applications of First Law

| | |
|-----------------------------|--------------------------------|
| Adiabatic (no heat flow) | $Q=0$ $\Delta E_{int} = -W$ |
| (constant volume) | $W=0$ $\Delta E_{int} = Q$ |
| Cyclical process | $\Delta E_{int} = 0$ $Q=W$ |
| Free expansions | $Q = W = \Delta E_{int} = 0$ |

Misc.

| | | |
|------------------------------------|----------------------------------------------------------|-------|
| Work Associated with Volume Change | $W = \int dW = \int_{V_i}^{V_f} p dV$ $W = p\Delta v$ | 18.25 |
|------------------------------------|----------------------------------------------------------|-------|

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