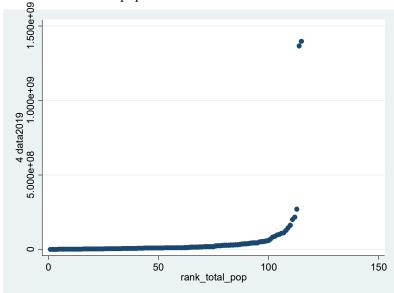
Use data eviews - simp.dta. Perform structural break tests in Eviews 9.

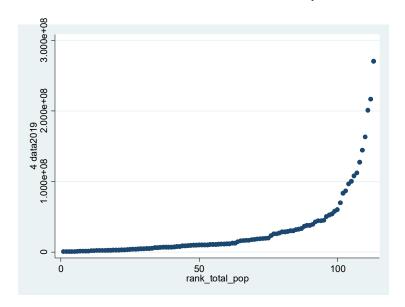
# (1) Choosing cutoffs

115 countries in total in the original WBES. We focus on total population in a country which is ranked in an ascending order. Rank\_total\_pop =1 for the country with the smallest population (Malta). Rank total pop =115 for the country with the largest population (China).

Distribution of total population size is as follows. X-axis is the rank and y-axis is the total population:



Rank = 114 and 115 are India and China, obviously outliers. If we remove China and India, we get:



The distribution looks exponential. Running the following regression and conduct structural break tests on the slope and the intercept:

Log(total pop) = a\*Rank total pop + constant

Use Bai-Perron test to identify the structural breaks in the distribution of country population size. Bai-Perron testidentifies multiple unknown break points in the whole sample. H0: no break points. H1: N break points. Set maximal N to be 5. Significance level = 10%.

### Eviews code:

 $import(link) \ D: \ Research \ WEBS \ Geo\_data \ city\_category \ WBdata \ data\_eviews - simp. dta \ @freq \ U \ 1 \ @smpl \ @all series \ ln\_pop = log(total\_pop)$ 

{%equation}.ls ln pop c rank total pop

{%equation}.multibreak(method=glob, trim=5, size=10, heterr) c rank total pop

#### Results:

Multiple breakpoint tests

Bai-Perron tests of 1 to M globally determined breaks

Date: 03/13/21 Time: 23:36

Sample: 1 115

Included observations: 115

Breaking variables: C RANK TOTAL POP

Break test options: Trimming 0.05, Max. breaks 5, Sig. level 0.10

Allow heterogeneous error distributions across breaks

Sequential F-statistic determined breaks:	5
Significant F-statistic largest breaks:	5
UDmax determined breaks:	1
WDmax determined breaks:	5

Breaks	F-statistic	Scaled F-statistic	Weighted F-statistic	Critical Value	
1 * 2 * 3 * 4 * 5 *	6.753357 6.614795 4.879671 5.309670 5.658020	13.50671 13.22959 9.759342 10.61934 11.31604	13.50671 13.91127 11.19125 13.01726 14.67091	11.02 10.48 9.61 8.99 8.50	
UDMax statistic* WDMax statistic*		13.50671 14.67091	UDMax critical value** WDMax critical value**		11.69 12.33

<sup>\*</sup> Significant at the 0.10 level.

## Estimated break dates:

1: 90

2: 91, 96

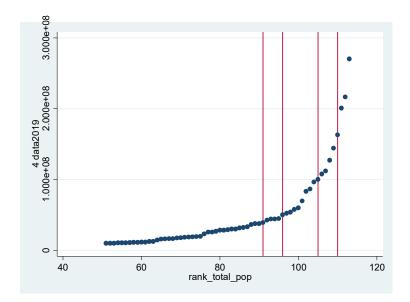
3: 91, 96, 107

4: 91, 96, 105, 110

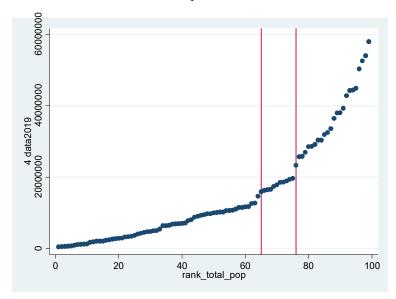
5: 34, 91, 96, 105, 110

Bai-Perron robustly identifies breaks at rank = 91 (just reaching 40 million population), 96 (just reaching 50 million population), 105 (just reaching 100 million population), 110 (about to reach 200 million population), as follows. 96 seems to be a better cutoff than 91 based on the following graph. So we keep rank = 96, 105, 110 as structural breaks.

<sup>\*\*</sup> Bai-Perron (Econometric Journal, 2003) critical values.



It is hard to identify robust structural breaks below rank =95 in the whole sample. Take the subsample of rank 1-95. Judging from the graph, the break can be rank =65 (15 million) or rank =76 (20 million). Chow tests on these two known breaks show that rank =76 gives more significant statistics than rank =65. Choose rank =76 as the break point.



## Eviews code:

```
{%equation}.ls ln_pop c rank_total_pop (note: for rank = 1-95 only) {%equation}.chow 76 {%equation}.chow 65
```

Combining the above structural break tests and the distribution of country population, we get:

- -Class 1: Rank 1-75, country population <20 million
- -Class 2: Rank 76-95, country population 20-50 million
- -Class 3: Rank 96-104, country population 50-100 million

- -Class 4: Rank 105-110: country population 100-200 million
- -Class 5: Rank 111-113: country population > 200 million
- -Class 6: Rank 114 and 115, China and India, country population >1 billion

We include more cities in the sample in larger countries. How to determine the number of cities? Think about the modal country populations for each category:

- 1.<20 million: modal = 10 million
- 2. 20-50 million: modal = 25 million (X2.5)
- 3. 50-100 million: modal = 75 million (X3)
- 4. 100-200 million: modal = 150 million (X2)
- 5. 200-1000 million: modal = 600 million (X4)
- 6. > 1000 million: modal = 1200 million (X2)

The modal population goes up by 120 across the six categories. If in the base category we choose 1 city, category 6 will have 12 cities. This implies:

- 1. country population <20 million: include top 1 city
- 2. country population 20-50 million: include top 2 cities
- 3. country population 50-100 million: include top 3 cities
- 4. country population 100-200 million: include top 5 cities
- 5. country population 200-1000 million: include top 6 cities
- 6. country population > 1 billion: include top 12 cities