DAA HOTS BUESTION RAZSIIO26010909 AE-2 CINTEL

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1) Gives a weighted directed graph containing both positive and negative edge weights, but without any negative cycles, is Dykstra's algorithm appropriate for finding the single - source shortest path.

No, Dijkstra's algorithm is not appropriate for finding the single-source shortest path in a group with negative tentative distance and relaxing its edges. It assumes that once a vertex is visited and its distance is finalized, that distance is the Shortest possible path to the vertex. This assumption holds true for graph with non-negative edges weights because adding a non negative edge weight will not hamper the path's length.

For graphs with negative edge weights but no negative cycles, the Boltzman-Forod algorithm is the appropriate choice for finding the single source shortest path. It can handle negative edge weights and can also handle negative cycles.

2) Given two souted average, each combining n elements, devise an algorithm to efficiently compute the median of their combined 2n elements with a time complexity of O(logn).

To compute the median of two souted avoiays of size of in O(logn) time, we can stay that we can use the Binary Search algorithm. The median of the combined In elements will be the average of the nth and (n+1)th smallest element.

Algorithm: We can find the K-th smallest element in the combined array using a necursion function. To find the median, we need to fixed the nth element and also the (771)th smallest element Let's define a function finakth (and, and 2, K) that finds the kth smallest element in the combined souted array and and arra ?

- If avoil is empty, network K-th element of avoil. (1) Best case: · If are is empty, network the element of ares
- · If K=1, gretum the minimum of the first
- elements of arms and arms

2> Remosive Step

- · Find the middle indices in both avoisys relative to the avoident search space.
 - Let, mid 1 = min(n/2, size(avoi1)) and mid 2 = min(n/2, size(avoi2))
- · Compare the elements and [mid 1-1] and avois [mid 2-1]
- If any 1 [mid 1-1] < any 2 [mid 2-1]: This element in any 1 are upto mid-1 are smaller them any 2 [mid 2-1]. We succursively search for the (K-mid 1)-th smallest element in the sumaining part of any 1 (from index mid 1) and the whole are 2.
- off and [mid 1-1] = = and 2 [mid 2-1]; We have found the (mid 1 + mid 2) the smallest element if K = mid 1 + mid 2, this is an element
- (3) Given a weighted undirected graph, design am efficient adjoroithm to determine the existence of a second-best Minimum Spanning True and Calculate its total weight.

First, find a minimum Spanning True (MST) ming a standard Algorithm like Komskal's on Prints a standard Algorithm like Komskal's on Prints A second-best MST can be found by considering each edge (U,V) from the oxiginal graph that

is not in the initial MST. Adding such an edge (H,V) to the MST croeates a lonique cycle. To find a potential second best MST, someone the edge with the max weight from this cycle. The second best MST is one among all three resulting spanning tree that has minimum total weight. The algorithm iterates through all edges not in the initial MST, calculates the weight of the resulting tree after adding the edge and gremoving the max weight edge on the cycle and keeps track of the minimum weight found.

You are given that subset sum < p Problem X. What can you conclude about problem X. Provide a brief justification.

The notation subset sum & p Poroblem X means that there is a polynomial—time reduction from the subset problem to Poroblem X.

Subset sum is a well known NP-complete problem, which implies it is also NP-hard.

A polynomial time oreduction means that an instance of student sum can be toransformed into instance of problem X in polynomial time.

Such that solving the instance of Poroblem X gues the solution to the subset sum instance.

Because subset sum as NP hard. Solving Peroblem X in polynomial time (via Heduction). We can conclude that Peroblem X is NP-hard

Explain the seasoning.

This problem belongs to the complexity class NP. The property that a proposed solution can be verified in O(n²) time means the verification perocess takes a polynomial amount of time with supert to the input size n(o(n2)) is a polynomial) This is the defining characteristic of psublems in the class NP-solutions can be easily and efficiently verified. The fact that there is no polynomial time algorithm Known coverently to solve the problem suggest that it might not be in class p (powblems solvable in polynomial time) and is consistent with NP-complete problems that are NP hard on NP-complete However solely based on the croîteria property directly places provided, the revision property directly places it within the class NP.

SRM